

CSC 135 Section 5 (Friday)

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Context free Grammar assignment:

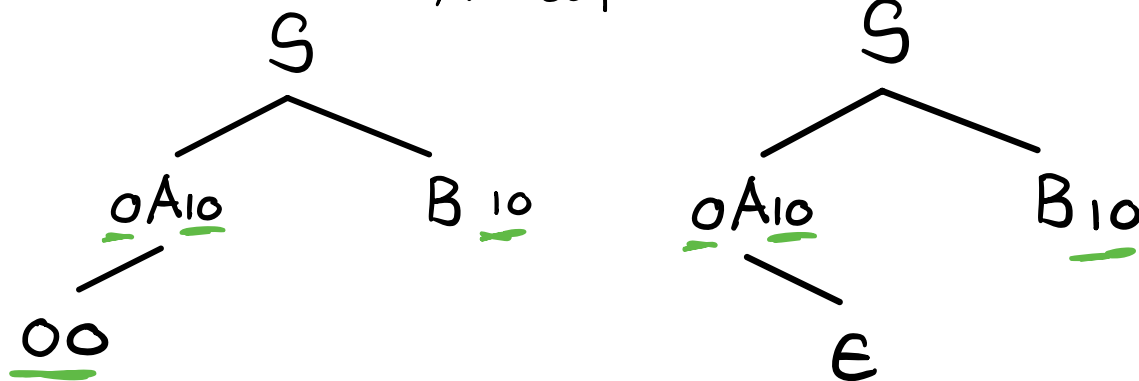
1. Show that the following CFG is ambiguous by finding an example of a string having two different leftmost derivation: $S \rightarrow 0A10 \mid B10$, $B \rightarrow A0 \mid B1$, $A \rightarrow 00 \mid \epsilon$.
2. Create a PDA for the language $L = \{a^i b^j c^k \mid i, j, k \geq 0 \text{ and } i=j \text{ or } i=k\}$
3. Create the context free grammar for all the strings over $\{a,b\}$ with at most two a's anywhere in the string.
4. Consider the grammar $E \rightarrow E + T \mid T$, $T \rightarrow T * F \mid F$, $F \rightarrow \epsilon \mid a$. give the parse tree (left most or right most) for the expressions:
 - a. $a + a + a$
 - b. $((a))$
5. Create the context free grammar for the following languages over $\{a,b\}$
 - a. $\{W \mid w \text{ contains at least 3 ones anywhere in the string}\}$
 - b. $\{W \mid \text{The set of all the strings with the number of a's more than the number of b's.}\}$
6. Convert the following CFG to its CNF: $A \rightarrow BAB \mid B \mid \epsilon$, $B \rightarrow 00 \mid \epsilon$
7. Create the PDA for the following languages
 - a. $A = \{a^m b^n c^n \mid m, n \geq 0\}$
 - b. $\{a^n b^n c^m \mid m, n \geq 0\}$

- ✓ 1. Show that the following CFG is ambiguous by finding an example of a string having two different leftmost derivation: $S \rightarrow 0A10 \mid B10$, $B \rightarrow A0 \mid B1$, $A \rightarrow 00 \mid \epsilon$.

$$S \rightarrow 0A10 \mid B10$$

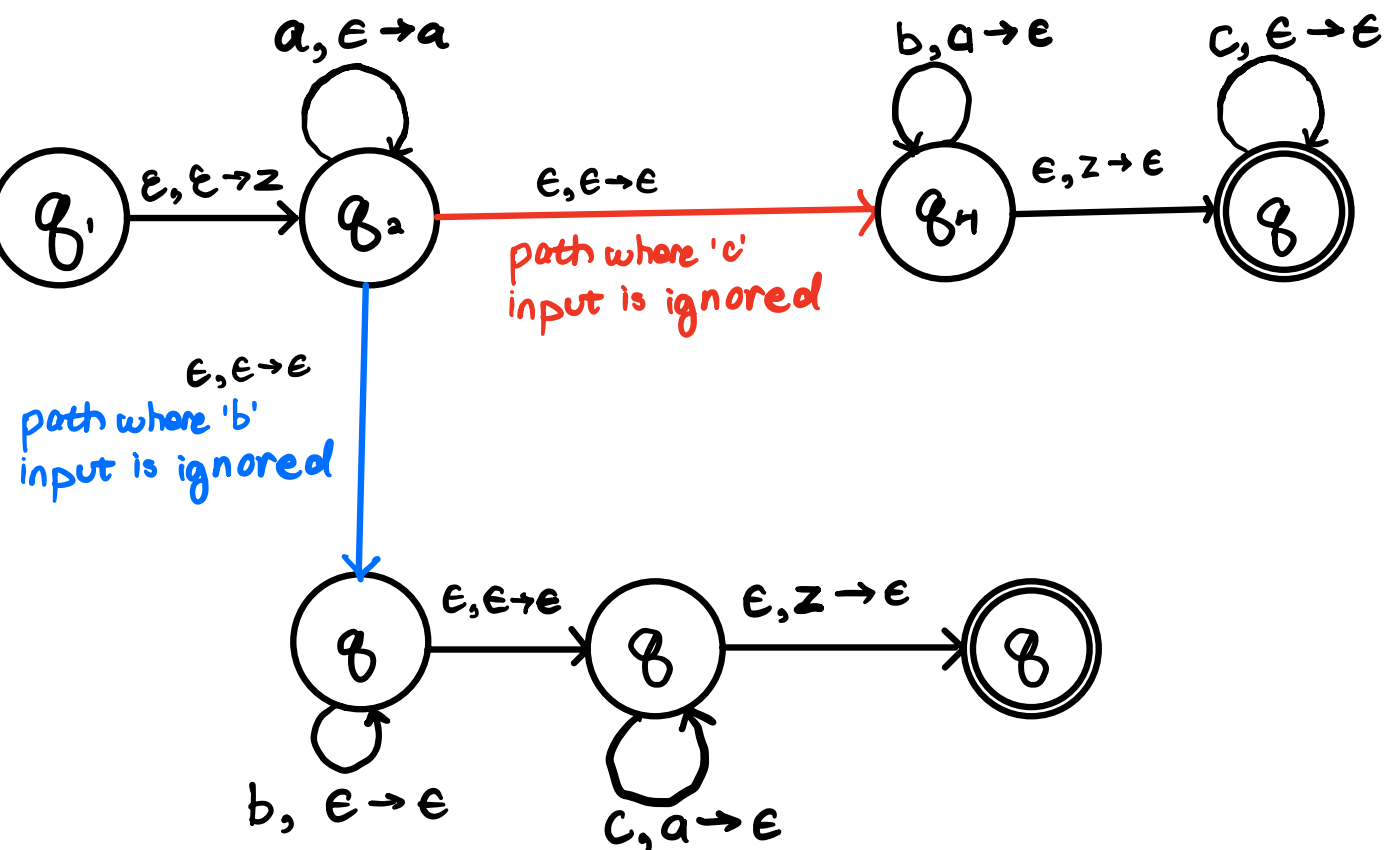
$$B \rightarrow A0 \mid B1$$

$$A \rightarrow 00 \mid \epsilon$$



$$00001010 \neq 01010$$

2. Create a PDA for the language $L = \{a^i b^j c^k \mid i, j, k \geq 0 \text{ and } i=j \text{ or } i=k\}$



3. Create the context free grammar for all the strings over $\{a, b\}$ with at most two a's anywhere in the string.

$$S = BABAB$$

$$B = bB \mid \epsilon$$

$$A = a \mid \epsilon$$

✓ 5. Create the context free grammar for the following languages over $\{a, b\}$

a. $\{W \mid w \text{ contains at least 3 ones anywhere in the string}\}$

b. $\{W \mid \text{The set of all the strings with the number of a's more than the number of b's.}\}$

$$a) S = BaBaBaBA$$

$$B = bB \mid \epsilon$$

$$A = aA \mid \epsilon$$

$$b) S = \epsilon \mid XaX$$

$$X = \epsilon \mid aX \mid Xa \mid aXb \mid bXa$$

✓ 6. Convert the following CFG to its CNF: $A \rightarrow BAB \mid B \mid \epsilon$, $B \rightarrow 00 \mid \epsilon$

$$A \rightarrow BAB \mid B \mid \epsilon$$

$$B \rightarrow 00 \mid \epsilon$$

Remove ϵ from $A \rightarrow \epsilon$!

$$A \rightarrow BAB \mid BA \mid AB \mid A \mid B$$

Repeat for $B \rightarrow \epsilon$

$$B \rightarrow 00$$

New production: $C \in N$

$$C \rightarrow BA$$

$$A \rightarrow CB \mid BA \mid AB$$

$$B \rightarrow 00$$

$$B \rightarrow RB$$

7. Create the PDA for the following languages

a. $A = \{a^m b^n \underline{c^n} \mid m, n \geq 0\}$

b. $\{a^n b^n \underline{c^m} \mid m, n \geq 0\}$

