

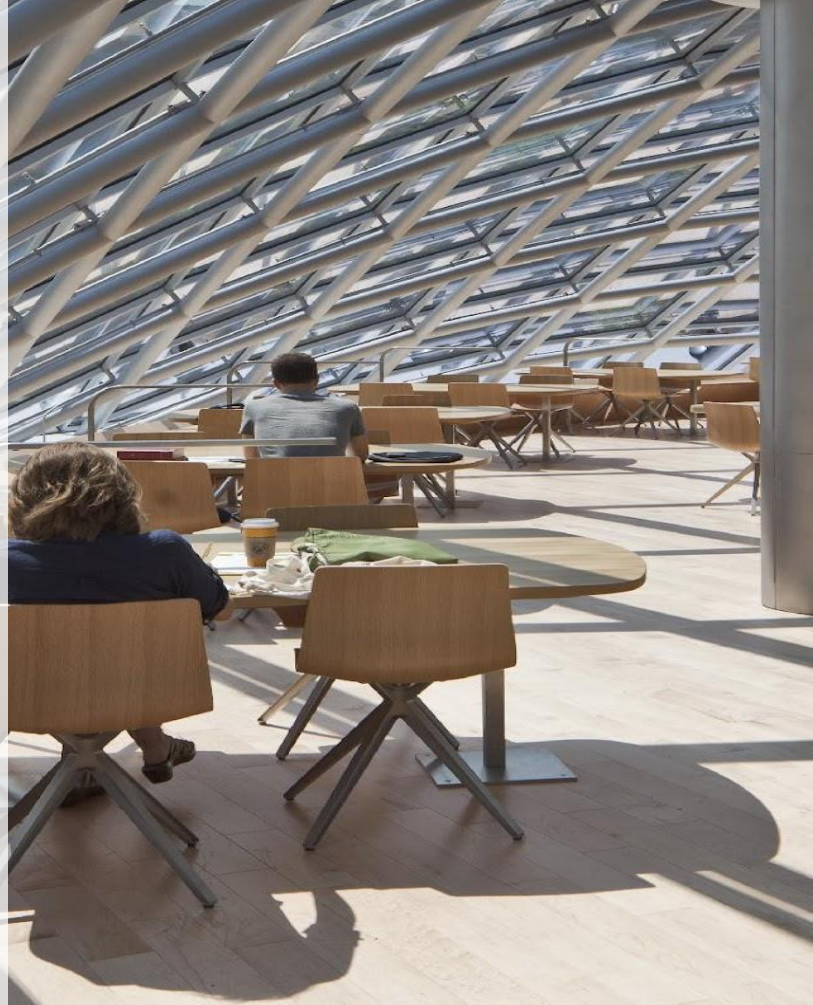
# Prime Trading

**Project Lab - The University of Chicago**  
**May 16th meeting**

Futures Basis Model

**Presented by**

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# 1. Theoretical value for basis



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# Data Cleaning

- BTIC , Dividend Futures, ES front month parsing
- Code Snippets

```
.with_columns([\n    pl.when(pl.col("month_code")== "F").then(1)\n    .when(pl.col("month_code")== "G").then(2)\n    .when(pl.col("month_code")== "H").then(3)\n    .when(pl.col("month_code")== "J").then(4)\n    .when(pl.col("month_code")== "K").then(5)\n    .when(pl.col("month_code")== "M").then(6)\n    .when(pl.col("month_code")== "N").then(7)\n    .when(pl.col("month_code")== "Q").then(8)\n    .when(pl.col("month_code")== "U").then(9)\n    .when(pl.col("month_code")== "V").then(10)\n    .when(pl.col("month_code")== "X").then(11)\n    .when(pl.col("month_code")== "Z").then(12)\n    .otherwise(None)\n    .alias("contract_month")\n])
```

# Implied Financing Cost

- **Recall**
- In D.E Shaw Publication, it highlights the surge in additional financing cost
- Also, previously our theoretical price was constantly below the market price
- Thus we need to take into consideration, the financing cost
- **Practical Considerations**
  - What financing rate should we use ? Repo ? Proprietary model?
  - We can use implied financing spot rate in practice
  - Brief Paper review ( **Implied Futures Financing Rate, Gunther, 2021**)

## The Implied Futures Financing Rate\*

Nicholas L. Gunther<sup>†</sup> Robert M. Anderson<sup>‡</sup> Lisa R. Goldberg<sup>§</sup>  
Alex Papanicolau<sup>¶</sup>

February 20, 2021

# Implied Financing Cost

- **Brief Paper Review**
- Data we would need to implement,
  1. Front, Near Month Trade data
  2. SPX Option implied dividend yield
- Use option around ATM,  $\sim T_2$

$$E_t[M(t, T_1)] = \frac{K_{div}(t) \times IFFR}{C_X t}$$

$$K_{div}(t) = 1 - r_{div}(t) \Delta T$$

$$\textcircled{1} IFFR (\text{Inverse forward futures rate}) \\ = \frac{F(t, T_1)}{F(t, T_2)}$$

$\textcircled{2} \Delta T$ : time between  $T_1, T_2$  maturity  $\approx 3\text{mos.}$

$\textcircled{3} r_{div}$ : Implied dividend yield from SPX option from P-C Parity relation.  
 - provided by OPTIMATICS on WARD

$$C - P = e^{-rT} (S_0 e^{(r-g)T} - K) = S_0 e^{-gT} - K e^{-rT} \\ = F_t - K e^{-rT}$$

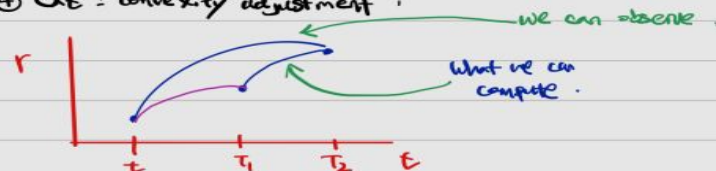
$$\text{Let, } Y_i = \ln\left(\frac{F_i}{S_i}\right) \quad X_i = T_i$$

Run regression on

$$Y_i = \beta X_i \quad \text{for different strike.}$$

$$g(t) = -\hat{\beta}$$

$\textcircled{4} C_X t$ : convexity adjustment



$$\text{Thus, } (1 + r(t, T_1))(1 + f(t, T_2)) - 1 = r(t, T_2) \\ \text{we can extract implied spot rate.}$$

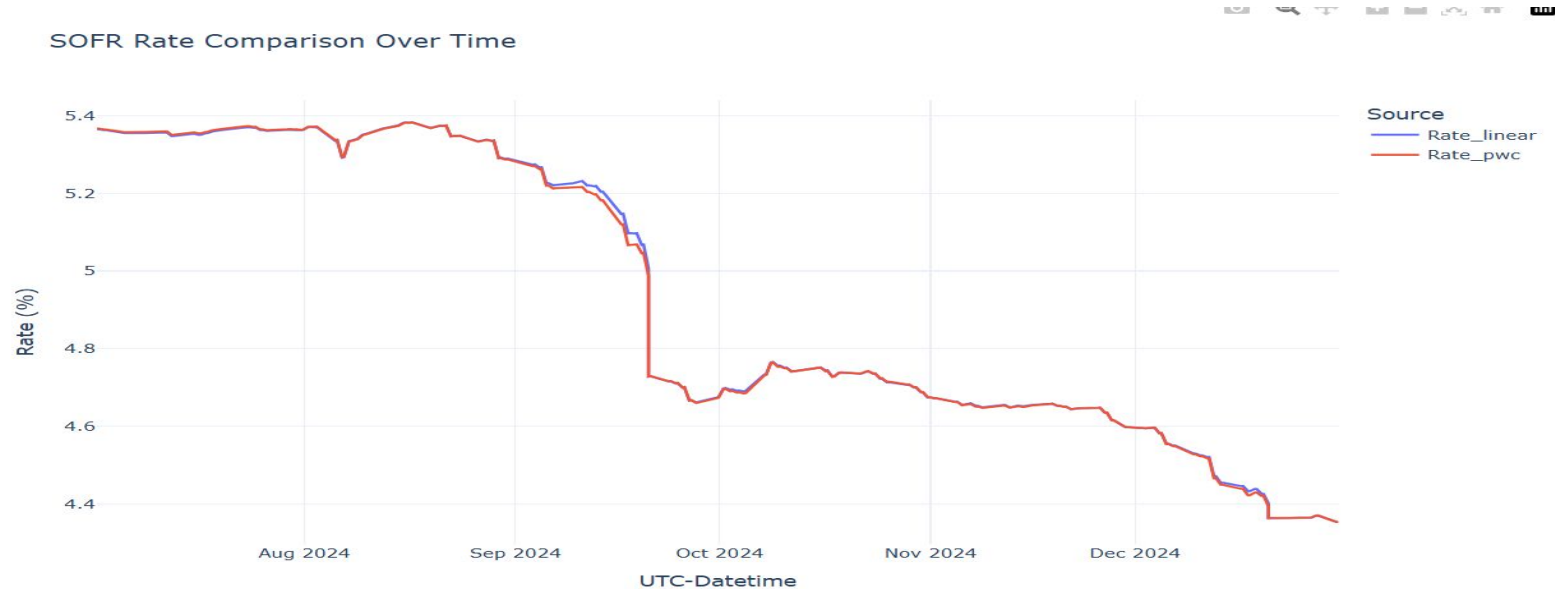
# Implied Financing Cost

- **What we did**
- We fed the D.E Shaw paper's plot and asked GPT to produce approximate values for each date
- Shortcomings : the plot was 20day rolling average thus has some errors
- GPT produced the best approximate values but not exact values
- Going back to basic used simple discrete carry model without considering tax which we mentioned the last time



# Interpolation methods

- **PWC vs Linear**





# Visualization

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- Spreads / percentage change / twinx / twinx for specific date  
( for two different interpolation methods; pwc & linear )
- See html file

# Next Steps

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- Wrap up and write a readme file on how to run the code
- Give a summary of what we did for previous weeks
- **Worth researching on Prime Trading's side:**
  - Use implied futures forward rate to calculate the implied spot rate
  - Doesn't even need complex interpolation methods
  - Consistent with no arbitrage argument

**Thank you!**

