

Department of Computer Science and Engineering
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Data Structures Quiz, Chapter 1, Sept. 23, 2024

1. What are printed by each of the following C programs? (30%)

- (a) `char d=172;`
`printf("%d \n",d);`
- (b) `char a= 'C'; // 'A'=65`
`char b= 'G';`
`printf("%d %c %d \n", a, a, b-a);`

2. Ackermann's function $A(m,n)$ is defined as follows:

$$\begin{aligned} A(m,n) &= n+1, & \text{if } m=0 \\ A(m,n) &= A(m-1,1), & \text{if } n=0 \\ A(m,n) &= A(m-1, A(m,n-1)), & \text{otherwise.} \end{aligned}$$

Calculate the value of $A(2,2)$. (30%)

3. Write a recursive C/C++ function to print out all permutations of given elements. (40%)

```
void Permu(char a[ ], int k, int m)
//Generate all the permutations of  $a[k], \dots, a[m]$ 
{
```

Please write the body of Permu ().

```
} // end of Permu ( )
int main( )
{   char a[ ]={ 'a','b','c','d'};
    Permu(a,0,3);
};
```

Answers:

參考解答

1. (a) -84

解釋: 172 儲存於 char 時，其二進位之值為 10101100。列印時，以 %d 印出，將其視為 signed char (integer)，其 8 bits 中，最左方的 bit 作為判斷正負使用，若為 1 則為負數，若為 0 則為正數。本題最左方為 1，故為負數。10101100 之 2 補數 (2's complement) 為 **01010100**₍₂₎ = 84₍₁₀₎，故答案為 84₍₁₀₎ 的負數 -84。

註：10101100 之 2 補數：先將全部的 bit，0 轉換成 1，1 轉換成 0 (亦即為 1's complement)，得到 01010011，最後再加 1，得到 01010100。另一種簡單算法，計算 172 的 256 補數，亦即 256-172=84。

(b) 67 C 4

解釋: 'C' = 67，以 %d 十進制印出，答案為 67。

'G' = 71，故 'G' - 'C' = 4，以 %d 十進制印出為 4。

2. $A(2, 2) = A(1, A(2, 1))$

$$A(2, 1) = A(1, A(2, 0))$$

$$A(2, 0) = A(1, 1)$$

$$A(1, 1) = A(0, A(1, 0))$$

$$A(1, 0) = A(0, 1)$$

$$A(0, 1) = 2$$

$$A(1, 0) = 2$$

$$\textcolor{red}{A(1, 1)} = A(0, 2) = 3$$

$$A(2, 0) = 3$$

$$A(2, 1) = A(1, 3)$$

$$A(1, 3) = A(0, A(1, 2))$$

$$A(1, 2) = A(0, \textcolor{red}{A(1, 1)}) = A(0, 3) = 4$$

$$\textcolor{blue}{A(1, 3)} = A(0, 4) = 5$$

$$A(2, 1) = 5$$

$$A(2, 2) = A(1, 5)$$

$$A(1, 5) = A(0, A(1, 4))$$

$$A(1, 4) = A(0, \textcolor{blue}{A(1, 3)}) = A(0, 5) = 6$$

$$A(1, 5) = A(0, 6) = 7$$

$$\textcolor{red}{A(2, 2)} = 7$$

3.

```
void Permu(char a[ ], int k, int m)
//Generate all the permutations of  $a[k]$ , ...,  $a[m]$ 
{
    if (k == m) { //Output permutation
        for (int i = 0; i <= m; i++) cout << a[i] << " ";
        cout << endl;
    }
    else { //a[k], ..., a[m] has more than one permutation
        for (int i = k; i <= m; i++)
        {
            swap(a[k], a[i]); // exchange
            Permu(a, k+1, m);
            swap(a[k], a[i]);
        }
    } // end of else
} // end of Permu ( )

int main( )
{
    char a[ ] = { 'a','b','c','d' };
    Permu(a,0,3);
};
```