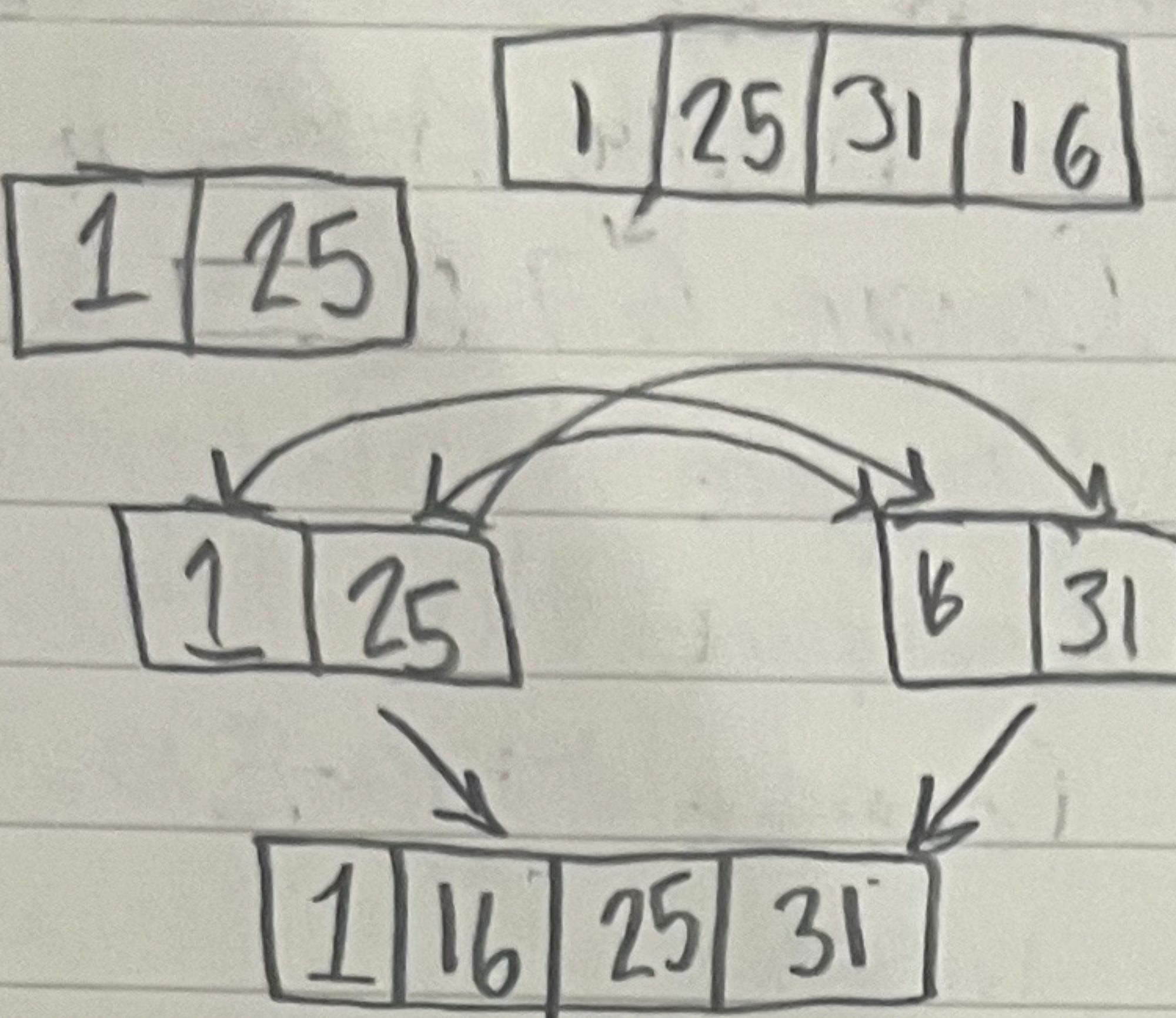


Assignment 2

Kevin Gonzalez

1. Merge Sort - Assuming both of our lists are sorted.
Unless this is a typo, list 1 is not sorted

1 25



1. Split list

31 16

31 16

2. Swap 31 & 16, then merge.

3. Compare elements.

$$1 < 16 = 1$$

$$25 > 16 = 16$$

$$25 < 31 = 25$$

Finally add 31.

Now we can merge the two lists (conquer part of algorithm)

1 16 25 31

-3 0 16 27

1. Compare 1 and -3 = -3

-3

1 16 25 31

0 16 27

2. Compare 1 and 0 = 0

-3 0

1 16 25 31

16 27

3. Compare 1 and 16 = 1

-3 0 1

16 25 31

4. Compare 16 and 16 = 16 (from list 1)

-3 0 1 16

25 31

5. Compare 25 and 16 = 25

-3 0 1 16 16

25 31

6. Compare 25 and 27 = 25

-3 0 1 16 16 25

31 27

7. Compare 31 and 27 = 27

-3 0 1 16 16 25 27 31

8. Add last 31.

Assignment 2 cont...

date / /

2. Insertion Sort: $[-1, -5, 67, -10, 21, 8, 4, 1]$

Assume sorted

$[-1, -5, 67, -10, 21, 8, 4, 1]$

Iteration: 1. $-5 < -1 \Rightarrow$ move -1 to right

insert -5 (the rest follow this, so I simplify)

$[-5, -1, 67, -10, 21, 8, 4, 1]$

2. Compare $67 > 1 \Rightarrow$ No change

$[-5, -1, 67, -10, 21, 8, 4, 1]$

3. Compare $-10 < 67 \Rightarrow 67$ right

Compare $-10 < -1 \Rightarrow -1$ right

Compare $-10 < -5 \Rightarrow -5$ right

insert -10

$[-10, -5, -1, 67, 21, 8, 4, 1]$

4. Compare $21 < 67 \Rightarrow 67$ right

Compare $21 > -1 \Rightarrow$ insert 21

$[-10, -5, -1, 21, 67, 8, 4, 1]$

5. Compare $8 < 67 \Rightarrow 67$ right

Compare $8 < 21 \Rightarrow 21$ right

Compare $8 > -1 \Rightarrow$ insert 8

$[-10, -5, -1, 8, 21, 67, 4, 1]$

6. Compare $4 < 67 \Rightarrow 67$ right

Compare $4 < 21 \Rightarrow 21$ right

Compare $4 < 8 \Rightarrow 8$ right

Compare $4 > -1 \Rightarrow$ insert 4

$[-10, -5, -1, 4, 8, 21, 67, 1]$

7. Compare $1 < 67 \Rightarrow 67$ right

Compare $1 < 21 \Rightarrow 21$ right

Compare $1 < 8 \Rightarrow 8$ right

Compare $1 < 4 \Rightarrow 4$ right

Compare $1 > -1 \Rightarrow 1$ insert

$[-10, -5, -1, 1, 4, 8, 21, 67]$

Assignment 2 cont...

date

3. Quicksort: $[5, 42, 6, 19, 11, 25, 26, -3]$

Step 1: Choose last element as pivot.

$[5, 42, 6, 19, 11, 25, 26, -3]$

Compare all elements to -3

$-5 < -3 \Rightarrow -5$ left

$42 > -3 \Rightarrow 42$ right

$6 > -3 \Rightarrow 6$ right

$19 > -3 \Rightarrow 19$ right

$11 > -3 \Rightarrow 11$ right

$25 > -3 \Rightarrow 25$ right

$26 > -3 \Rightarrow 26$ right

Step 2: Choose last element 26

$[5, -3, 6, 26]$

$42 > 26 \Rightarrow 42$ right

$[-5, -3, 6, 19, 26]$

$6 < 26 \Rightarrow 6$ left

$[-5, -3, 6, 19, 11, 26]$

$19 < 26 \Rightarrow 19$ left

$[-5, -3, 6, 19, 11, 25]$

$11 < 26 \Rightarrow 11$ left

$[-5, -3, 6, 19, 11, 25, 26]$

$25 < 26 \Rightarrow 25$ left

$[-5, -3, 6, 19, 11, 25, 26]$

$26 < 26 \Rightarrow 26$ left

\downarrow

remains same

$[-5, -3, 6, 11]$

Step 3: choose last element 25

$26 < 25 \Rightarrow 6$ stay left

$19 < 25 \Rightarrow 19$ stay left

$11 < 25 \Rightarrow 11$ stay left

Step 4: choose last element 11

$19 > 11 \Rightarrow 19$ right

$6 < 11 \Rightarrow 6$ left

Assignment 2 cont..

Shell Sort:

$[15, 14, -6, 10, 1, 15, -6, 0]$

5 | i |

Step 1: Initial gap: $\frac{8}{2} = 4$
length
Compare and swap elements 4 positions apart

$15 \nmid 1 \Rightarrow 1 < 15 \rightarrow \text{swap}$
 $14 \nmid 15 \Rightarrow 14 > 15 \rightarrow \text{no swap}$
 $-6 \nmid -6 \Rightarrow -6 = -6 \rightarrow \text{no swap}$
 $10 \nmid 0 \Rightarrow 0 < 10 \rightarrow \text{swap}$

$[1, 14, -6, 0, 15, 15, -6, 10]$

1 | 6 | 1 |
 $14 \nmid 0 \Rightarrow 0 < 14 \rightarrow \text{swap}$
 $11 \nmid 15 \Rightarrow 11 > 15 \rightarrow \text{no swap}$
 $14 \nmid -6 \Rightarrow -6 < 14 \rightarrow \text{swap}$
 $15 \nmid 10 \Rightarrow 10 < 15 \rightarrow \text{swap}$

Step 2: Repeat $\frac{4}{2} = 2$
Compare and swap elements 2 positions apart.

$[-6, 0, 1, -6, 15, 10, 14, 15]$

$-6 \nmid 0 \Rightarrow \text{no swap}$
 $0 \nmid 1 \Rightarrow \text{no swap}$
 $1 \nmid -6 \Rightarrow -6 < 1 \rightarrow \text{swap}$
 $1 \nmid 15 \Rightarrow \text{no swap}$
 $15 \nmid 10 \Rightarrow 10 < 15 \rightarrow \text{swap}$
 $15 \nmid 14 \Rightarrow 14 < 15 \rightarrow \text{swap}$

Step 3: Insertion sort $2/2 = 1$

$[-6, -6, 0, 1, 10, 14, 15, 15]$

Assignment 2 Cont...

date / /

5.1. Merge sort

Shell sort

Quicksort

selection sort

insertion sort

Bubble sort

I put Merge sort on top due to its $\Theta(n \log n)$ complexity that could help with large lists. Shell sort a close second only due to its $O(n^2)$ worst scenario. Otherwise, I would put it first because it could help with random lists.

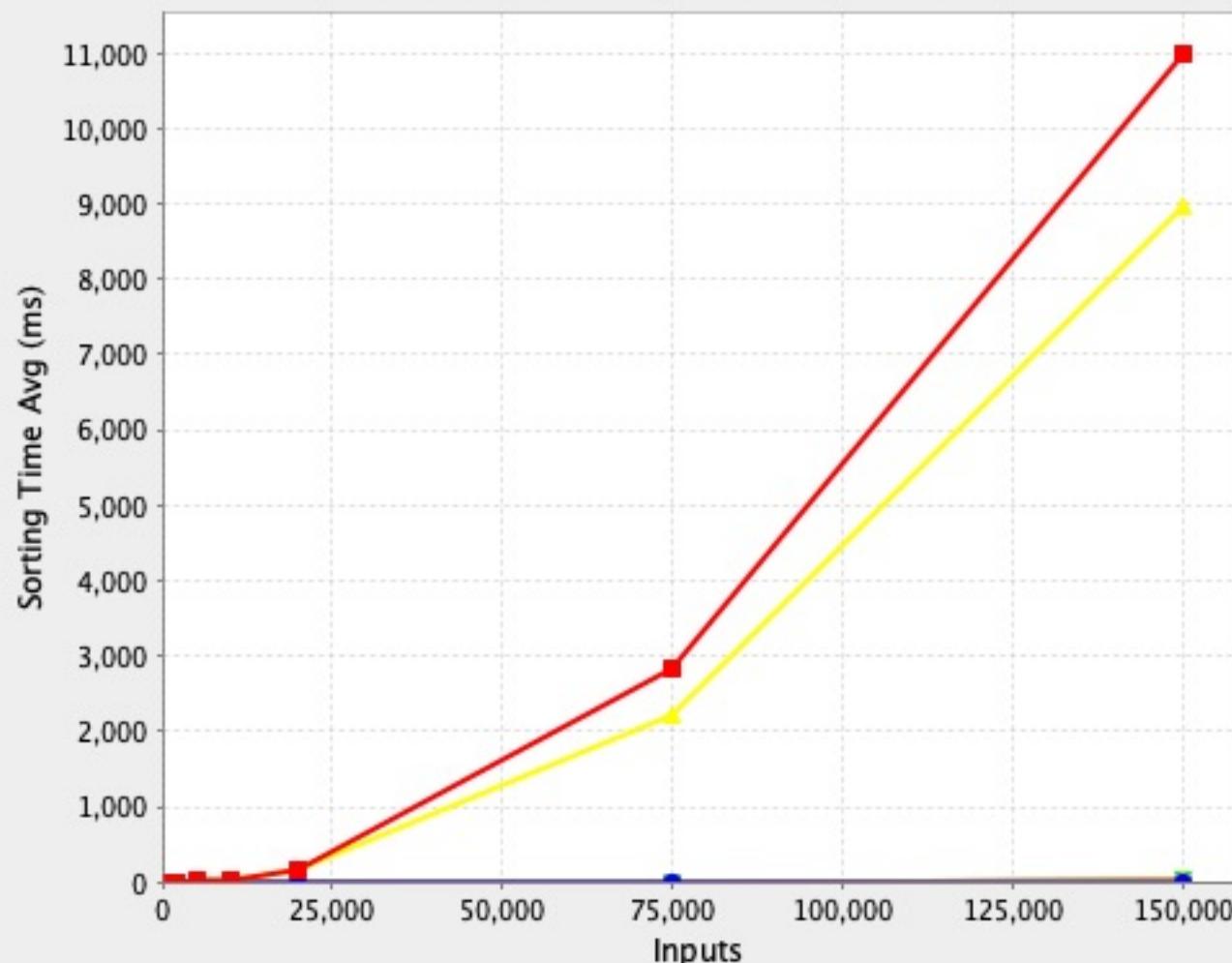
Quicksort at tie with shell sort because they share the same $O(n^2)$ complexity, but technically has a better best case than shellsort.

As for the last 3, its a tie because they would more often be slow unless you always have small lists.

10. Yes, as expected, the algorithms that ranked high managed to run in similar speed and matched my prediction. Additionally, I predicted that bubblesort and selection sort took insanely long when it came to giant lists. This would be because of their worst case iterate through the whole list one by one.

12. The algorithms for k sort was pretty much the same but faster with every algorithm. Something that caught me off-guard was how the performance gap between ~~bubblesort~~ bubble sort and selection sort became significantly smaller. My guess would be because k-sort begins already sorted by a bit.

Sorting Runtimes (K-Sorted)



Legend:
BubbleSort (Red Line)
InsertionSort (Blue Line)
SelectionSort (Yellow Line)
ShellSort (Orange Line)
QuickSort (Purple Line)
MergeSort (Green Line)

Sorting Runtimes (Normal)

