

# Magnetic Hammer Actuation for Tissue Penetration using a Millirobot

Julien Leclerc, Ashwin Ramakrishnan, Nikolaos V. Tsekos, and Aaron T. Becker

**Abstract**—Untethered magnetic navigation of millirobots within a human body using a Magnetic Resonance Imaging (MRI) scanner is a promising technology for minimally invasive surgery or drug delivery. Because MRI scanners have a large static magnetic field, they cannot generate torque on magnetic millirobots and must instead use gradient-based pulling. However, gradient values are too small to produce forces large enough to penetrate tissue. This paper presents a method to produce large pulsed forces on millirobots. A ferromagnetic sphere is placed inside a hollow robot body and can move back and forth. This movement is created by alternating the magnetic gradient direction. On the posterior side, a spring allows the sphere to change direction smoothly. On the anterior side, a hard rod creates a surface for the sphere to impact. This impact results in a large pulsed force. The purpose of this study is to understand the functioning of magnetic hammer actuation and control, as well as demonstration the viability of this mechanism for tissue penetration. This paper begins with modeling and simulating this system. Next, different control strategies are presented and experimentally tested. Finally, preliminary tests inside a clinical MRI scanner demonstrate the potential of this actuation system.

## I. INTRODUCTION

The navigation of millimeter-scale robots through the passageways of bodies is currently being studied as a method to perform highly localized drug delivery or perform minimally invasive surgery [1]–[3]. Untethered navigation can be achieved by placing a ferromagnetic piece inside the robot and producing a controlled magnetic field around a patient. Propulsion and steering of millirobots can be accomplished by either moving a permanent magnet assembly around a patient [4] or by controlling the current inside electromagnets [5]. The latest solution is often realized with an MRI scanner which already includes several electromagnets. In an MRI, the background field magnetizes the ferrous components of the robot, and the gradient coils generate the magnetic gradient necessary to produce forces. The Magnetic Resonance Imaging (MRI) scanner can be used simultaneously to provide real-time imaging of the operating area as well as positioning of the robot.

The force generated on the millirobots is proportional to the field gradient strength. Commercial MRI scanners produce gradients in the range of 20 to 40 mT/m. These gradients are sufficient to maneuver milli-robots inside fluid-filled regions of the body, such as vessels, [6] but insufficient for tissue penetration that requires larger forces [7]; tissue penetration is required for many procedures, including brachytherapy and micro-biopsy. The purpose of this paper

This work was supported by the National Science Foundation, Grant No. 1646566.

Authors are with the Dept. of Electrical and Computer Engineering, University of Houston, Houston, TX 70004, USA [jleclerc@uh.edu](mailto:jleclerc@uh.edu)

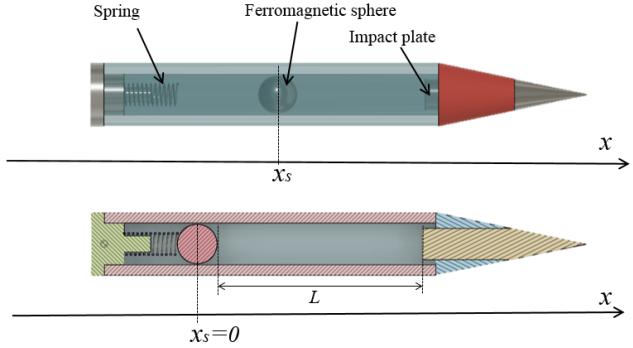


Fig. 1. Schematic representation of a millirobot actuated by a magnetic hammer.

is to present and study a method, denoted *magnetic hammer actuation*, that can generate large pulsed forces for tissue penetration. The paper demonstrates the capability of the device to penetrate tissue and show that an MRI scanner is suitable to produce the external magnetic field and gradient necessary for the actuation. The magnetic hammer is a system embedded into the millirobot. The millirobot has a tubular structure in which a ferromagnetic sphere can move back and forth. This movement is produced by alternately changing the gradient direction. On the posterior side of the millirobot, a spring allows the sphere to change direction smoothly. On the anterior side, a hard rod creates a surface for the sphere to impact, the *impact plate*. This impact results in large pulsed forces that enable penetrating body tissues progressively. A magnetic test bench has been developed to make experimental tests more practical and less expensive. It includes coils, sensors, power electronics, and a real-time controller.

Different control strategies are studied. The open loop control switches the magnetic gradient direction at constant frequency. It is completely independent of the sphere position and uses no feedback. The partially closed loop control detects the impact of the sphere and switch the magnetic gradient direction as soon as the impact is detected. The original gradient direction is reapplied after a constant time  $t_s$ . The perfectly closed loop control assumes a theoretical sensor able to measure the position of the sphere at any time. It is capable to detect the impact of the sphere as well as the change of direction on the posterior side. The controller is therefore able to change the direction of the gradient when the impact is detected and when the change of direction on the posterior side is detected.

The paper is organized as follows: first, the system is mathematically modeled, and its behavior is studied in section II. Secondly, parameters for the model are experi-



Fig. 2. Picture of 3 millirobots prototypes actuated by a magnetic hammer. mentally measured (see section III). Different materials for the impact plate are compared. Thirdly, the magnetic test bench is described and the test of a magnetic hammer is presented (see section IV). Results are compared to the mathematical model. Next, preliminary results from an open-loop test performed in a clinical MRI scanner are presented in section V. The last Section (section VII) is a conclusion of this study.

## II. THEORETICAL STUDY

### A. Mechanical modelization

The motion of the sphere between two consecutive impacts can be divided into two phases, based on the forces that act on it. The magnetic gradient force  $F_{mag}$  and friction force  $F_{friction}$  act on the sphere during its motion along the free length of the tube,  $L$  (See Fig. 3 (i),(iii)). When the spring is compressed, its reaction force  $F_{spring}$  acts on the ball as well (See Fig. 3 (ii)). The directions of  $F_{mag}$  and  $F_{friction}$  change depending on the direction of motion of the sphere. Inside the homogeneous region of an MRI scanner, the magnitude of  $F_{mag}$  is constant [8]. The same has been assumed for developing analytical and numerical models in this paper. The formula for calculating  $F_{mag}$  is presented in Section II-B. Friction is considered to be negligible, but the assumption will be relaxed in later sections. The spring force is straightforward, and is given by

$$F_{spring} = kx, \quad (1)$$

where  $x$  is the compression length, and  $k$  is the spring constant. In the perfectly closed loop system, the magnetic gradient direction is changed when the sphere hits the impact plate and when the spring reaches full compression. These two moments also corresponds to the two changes in the sphere movement direction. In addition, to maximize the impact velocity, the magnetic force, and therefore, the magnetic gradient, are oriented in the same direction as the sphere velocity vector. In the simulations, the sphere will naturally

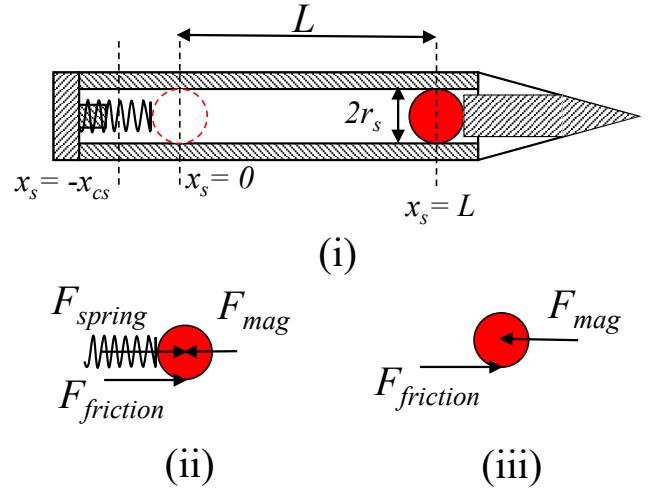


Fig. 3. (i) Free length of sphere travel,  $L$ ; (ii) free body diagram of sphere when spring is compressed, (iii) when spring is not compressed.

change direction after impact and after the full compression of the spring. The perfectly closed loop system can, indeed, be easily modeled by applying a magnetic gradient in the same direction as the sphere velocity.

An analytical model was developed by solving the system of differential equations to predict the impact velocity for each impact, given a set of input parameters. The sphere-impact plate system is assumed to have a coefficient of restitution,  $e$ . This model assumes that the robot capsule does not move. For all values of  $e$ , the impact velocity initially increases and ultimately saturates, reaching a resonant value. This happens when the energy lost by the sphere during impact equals the energy gained by it during the rest of the cycle. A higher  $e$  results in a higher impact velocity. Figure 4 shows a sample closed-loop pulsed magnetic gradient input for 50 impacts. The frequency initially varies until it settles to a constant value at resonance. An analytical formula was derived to predict the resonant impact velocity, for a given set of input parameters. This is given by eq. (2).

$$v_{res} = \frac{2\sqrt{\frac{F_{mag}(e^2+1)F_{mag} + (e^2-1)(-k)L + \sqrt{(2-2e^4)kL F_{mag} + (1+e^2)^2 F_{mag}^2}}{km_s}}}{1-e^2} \quad (2)$$

In the above equation,  $m_s$  is the mass of the sphere in kgs. The radius of the ball  $r_s$  indirectly influences the impact velocity through  $F_{mag}$  and  $m_s$ , both of which depend on the volume of the sphere. The variation of  $v_{res}$  with changes in  $L, e, k, m_s, r_s, F_{mag}$  were plotted and they were all found to be monotonic functions with no critical points. In eq. (2),  $v_{res}$  tends towards infinity as  $e$  tends to 1. In this case there is no loss of energy during collision and hence, the impact velocity indefinitely increases with subsequent impacts. Further, the time between impacts at resonance  $t_{res}$ , is a constant value and is given by ??.

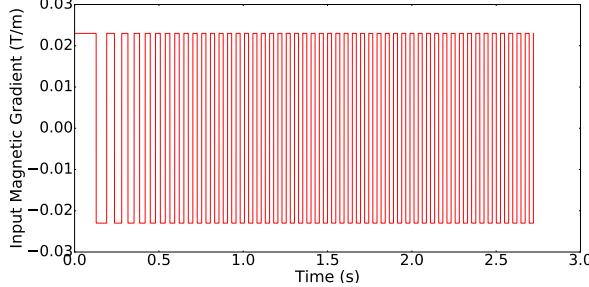


Fig. 4. Closed loop input gradient for 50 impacts;  $k = 50 \text{ N/m}$ ;  $e = 0.9$ ;  $F_{\text{mag}} = 1.5 \text{e-3 N}$ ;  $L = 0.03 \text{ m}$ ;  $m_s = 5.58 \text{e-4 kg}$ ;  $r_s = 0.0025 \text{ m}$ .

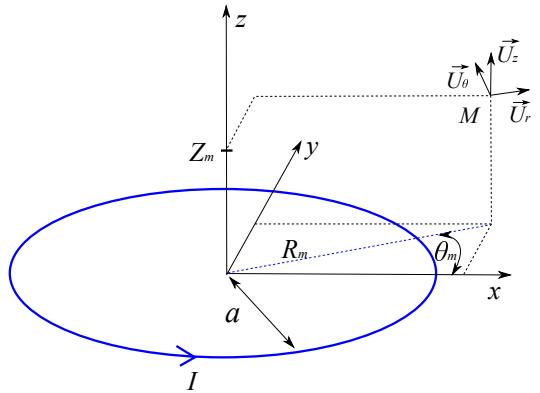


Fig. 5. Geometry and variables used in equation eqs. (9) to (12)

$$t_{\text{res}} = t_{\text{pos},1} + t_{\text{pos},2} + t_{\text{ant},1} + t_{\text{ant},2} t_{\text{pos},1} = \frac{\sqrt{e^2 v_{\text{res}}^2 + \frac{2LF_{\text{mag}}}{m_s}} - ev_{\text{res}}}{\frac{F_{\text{mag}}}{m_s}} \quad (3)$$

$$t_{\text{pos},2} = \frac{\pi - \tan^{-1} \left( \frac{k\sqrt{e^2 v_{\text{res}}^2 + \frac{2LF_{\text{mag}}}{m_s}}}{\omega F_{\text{mag}}} \right)}{\omega}; \omega = \sqrt{\frac{k}{m_s}} \quad (4)$$

$$t_{\text{ant},1} = \frac{\cos^{-1} \left( \frac{F_{\text{mag}}}{F_{\text{mag}} + kx_{cs}} \right)}{\omega} \quad (5)$$

$$t_{\text{ant},2} = \frac{v_{\text{res}} - \sqrt{v_{\text{res}}^2 - \frac{2LF_{\text{mag}}}{m_s}}}{\frac{F_{\text{mag}}}{m_s}} \quad (6)$$

$$x_{cs} = \frac{\sqrt{e^2 km_s v_{\text{res}}^2 + 2kLF_{\text{mag}} + F_{\text{mag}}^2} + F_{\text{mag}}}{k} \quad (7)$$

In the above equations,  $x_{cs}$  is the maximum compression distance of the spring (See Fig. 3 (i)), and  $\omega$  represents the natural frequency of the spring-mass system. The value of  $x_{cs}$  can be used to select an appropriate free length for the spring, to ensure that it does not bottom out during compression. The values  $t_{\text{pos},1}$ ,  $t_{\text{pos},2}$ ,  $t_{\text{ant},1}$  and  $t_{\text{ant},2}$  represent the time for the ball to move from  $x_S =$  (i)  $L$  to 0, (ii) 0 to  $-x_{cs}$ , (iii)  $-x_{cs}$  to 0, and (iv) 0 to  $L$  respectively, in a perfectly closed-loop system with optimal gradient switching.

### B. Magnetic field calculation

The magnetic field generated by an MRI scanner can be separated into two components. The first is a constant and strong magnetic field  $B_0$  along the z-axis. This field is used to align the magnetic moments of the protons. Commercial MRI scanners have  $B_0$  typically ranging from 1.5 to 3 T. The second component of the field is the magnetic gradient. It is used to encode the MRI signal spatially. The flux density  $\mathbf{G}$  produced by the gradient coils is added to  $\mathbf{B}_0$  and linearly varies with position. A computer controls this value.

The modelization of the field inside the uniformity sphere of an MRI scanner is straightforward.  $\mathbf{G}$  is directly proportional to the current inside the gradient coils.

$$\mathbf{B} = \mathbf{B}_0 + \mathbf{G}, \quad \mathbf{B}_0 = \begin{bmatrix} 0 \\ 0 \\ B_0 \end{bmatrix}, \quad \mathbf{G} = \begin{bmatrix} k_x I_x \\ k_y I_y \\ k_z I_z \end{bmatrix} \quad (8)$$

where  $k_x$ ,  $k_y$  and  $k_z$  are the coil constants (T/A) and  $I_x$ ,  $I_y$  and  $I_z$  are the electrical current values.

The flux density is more complicated to calculate outside of the uniformity sphere. The same problem is present in our magnetic test bench because the flux density and gradient are not constant. To calculate forces accurately, it is necessary to compute the magnetic field precisely. A semi analytical method was used to calculate the field produced in all space by a solenoid assembly. It was tested on our magnetic test bench.

According to [9], the magnetic flux density produced by a current loop in all space can be calculated using equations eqs. (9) to (12) and fig. 5.  $E(k)$  and  $K(k)$  are the complete elliptical integrals of first and second kind respectively.

$$B_z = \frac{\mu_0 I}{2\pi\delta^2\beta} [(a^2 - \rho^2 - z^2)(E(k^2) + \delta^2 K(k^2))] \quad (9)$$

$$B_\theta = \frac{\mu_0 I \cdot z}{2\pi\delta^2\beta\rho} [(a^2 - \rho^2 - z^2)(E(k^2) - \delta^2 K(k^2))] \quad (10)$$

$$\delta = \sqrt{a^2 + R_m^2 + Z_m^2 - 2aR_m} \quad (11)$$

$$\beta = \sqrt{a^2 + R_m^2 + Z_m^2 + 2aR_m} \quad (12)$$

The cross-section  $S$  of any solenoid can be divided into infinitesimal sections  $dS$ . Each  $dS$  is subjected to a current  $dI = JdS$ . This current  $dI$  forms an infinitesimal loop, and the field it produces can be calculated using eqs. (9) to (12). By integrating this equation over the solenoid cross-section, one can obtain the value of the flux density generated by the solenoid.

The flux density must be calculated for each solenoid. The total flux density is the vectorial sum of the flux density produced by each solenoid. The results obtained via this semi analytical method is compared to the solution obtained via finite element calculations with the software FEMM (Finite Elements Method Magnetics) [10] (see fig. 6). The results are identical. The semi-analytical method is faster to compute

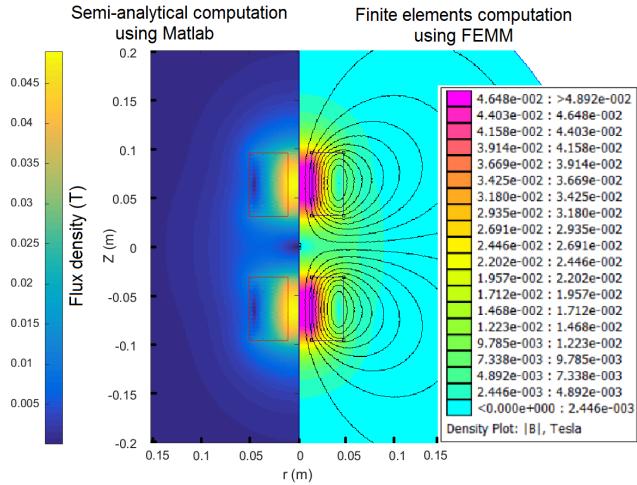


Fig. 6. Comparison between the flux density computed with the semi-analytical method with MATLAB and the flux density computed via a finite element method with FEMM. The maximum difference is 0.8 %.

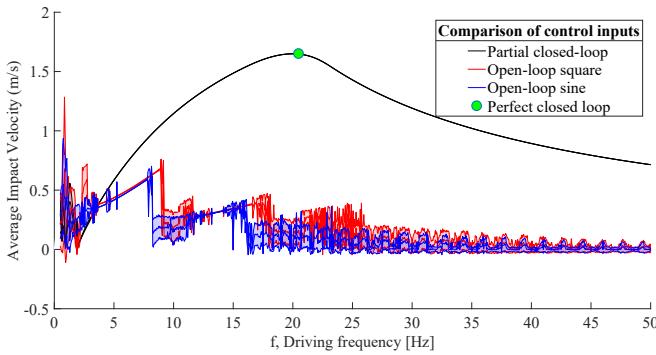


Fig. 7. Comparison of average impact velocities between impacts 100 and 1100 for three different control inputs: Open-loop vs. Partially closed-loop vs. Ideally closed-loop

for this model. Indeed, the magnetic field only needs to be calculated at the sphere position. The semi-analytical method can calculate the magnetic field at one point only whereas, finite elements methods must compute the magnetic field in the full domain.

### C. Magnetic force calculation

This section calculates the force applied by the magnetic field to the sphere.

The ferromagnetic sphere is small compared to the coil system and can be considered as a infinitely small magnetic moment  $\mathbf{m}$ . Assuming a constant material magnetization  $\mathbf{M}$ , one can calculate  $\mathbf{m}$  from eq. (13).

$V$  is the volume of the sphere. The ferromagnetic sphere is magnetized by the externally applied field  $\mathbf{H}_{app} = \mathbf{B}_{app}/\mu_0$ . Ferromagnetic materials create a demagnetizing field  $\mathbf{H}_d$  when subjected to an external field. The actual field  $\mathbf{H}$  seen by the sphere is the sum of  $\mathbf{H}_{app}$  and  $\mathbf{H}_d$ . This effect must be taken into account to calculate the magnetization accurately.  $\mathbf{H}_d$  is related to  $\mathbf{H}_{app}$  by eq. (14). The demagnetization factor  $N$  for a sphere is  $-1/3$ . Its magnetization can be calculated using eq. (15). Once the magnetic moment  $\mathbf{m}$  is

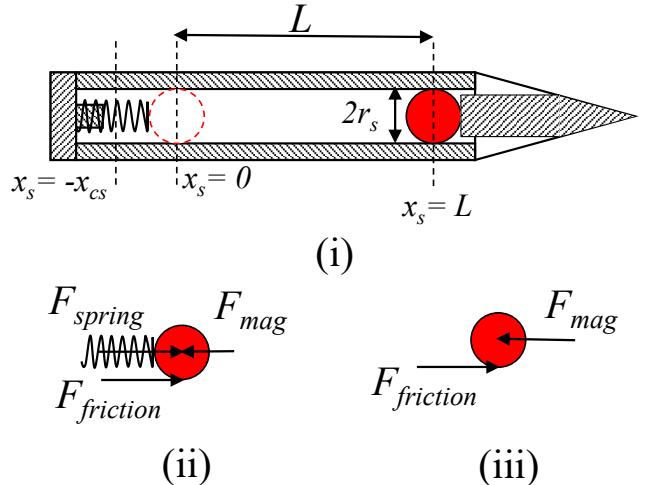


Fig. 8. Six domains for spring-end switching time; green and red represent  $F_{mag}$  towards anterior and posterior respectively. Direction of colored arrow represents direction of ball motion.

obtained, the force on the sphere can be calculated using eq. (16).

$$\mathbf{m} = \mathbf{M} \cdot V \quad (13)$$

$$\mathbf{H}_d = N \cdot \mathbf{H}_{app} \quad (14)$$

$$\mathbf{M} = \frac{\mathbf{H}_{app} (\mu_r - 1)}{2 \cdot N \cdot \mu_r - 1} \quad (15)$$

$$\mathbf{F} = \nabla(\mathbf{m} \cdot \mathbf{B}) \quad (16)$$

### D. Simulation results

1) *Perfectly closed loop vs. open loop system:* A numerical model was used to simulate the system dynamics for different input gradients. Average impact velocities over impacts 100 to 200 were compared for a perfectly closed loop pulsed input, and open loop inputs with sinusoidal and square profiles. As seen in figure 7, closed loop control produces approximately three times greater average impact velocity as compared to open loop sinusoidal and square waves, over all frequencies. As with the analytical model in Section II-A, the simulation assumes that the robot capsule does not translate along its axis. While the absolute values of impact velocity and force will be different when the capsule is free to move, the closed-loop input can still be expected to produce higher forces than open-loop inputs. Further, for a given open-loop frequency, the variation of impact velocity over multiple contacts was found to be random for both square and sinusoidal inputs. It is not possible to reach the resonant state using a constant frequency input of any form. For a given set of input parameters, there exists only one path, or control input, that enables the system to reach a resonant state.

2) *Partially closed loop system:* To implement a perfectly closed loop system, sensing is required at both the spring and impact ends. While sensing at the impact end can be done using a microphone sensor (see Section III-B), it is harder to

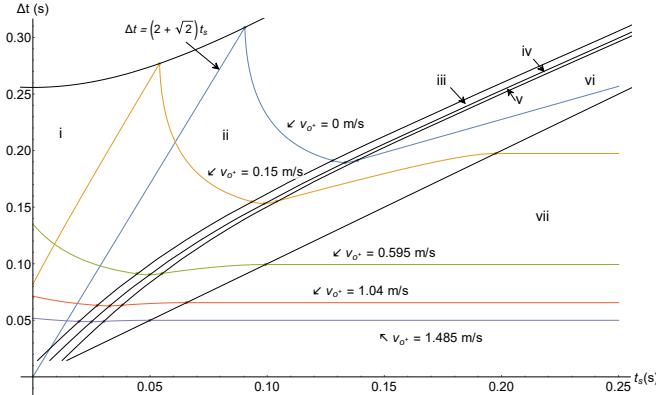


Fig. 9. Plot of  $\Delta t$  vs.  $t_s$  for different values of  $v_{o+}$ .

detect sphere reversal at the spring end. For experiments of the magnetic hammer on our test bench, a partially closed-loop system was implemented with only impact end sensing using a microphone. The sensor detected each impact and triggered a reversal in the direction of the gradient force. The switching time  $t_s$  at the spring end was manually set at different values. There are six regimes for  $t_s$ , for a given set of geometric and material properties as shown in fig. 8. In fig. 8(i), the initial velocity  $v_{o+}$  and  $t_s$  are low enough that the sphere reverses direction before reaching the spring. In this case,  $v_{o+} < 2aL$ , where  $a = F_{mag}/m_s$ . Fig. 8(ii) represents the case when  $v_{o+}$  is high enough that spring compression is unavoidable even for  $t_s = 0$ . In fig. 8(iii), the signal switch happens after spring compression starts but before it bottoms out. Fig. 8(iv) represents perfect closed loop switching. In fig. 8(v), the signal is switched after maximum compression, but before the sphere reaches  $x_s = 0$ . Fig. 8(vi) represents switching after spring rebound and before the next impact. There is also a possible seventh case where the switching happens after one entire impact cycle. This case is not relevant and serves more as an upper limit of practical  $t_s$  values.

Simulations were done for the partially closed loop system to identify effects of different  $t_s$  values. The variation of time between impacts  $\Delta t_{imp}$ , with changes in  $t_s$  and initial velocity  $v_{o+}$  have been plotted. Fig. 9 shows  $\Delta t_{imp}$  as a function of  $t_s$ . For  $v_{o+} = 0.15$  m/s, there is a linear increase in  $\Delta t_{imp}$  till  $t_s$  reaches a critical point. This linear region represents the case shown in fig. 8(i). Beyond this,  $\Delta t_{imp}$  decreases with increasing  $t_s$  (fig. 8(ii),(iii)), until the latter reaches its perfectly closed-loop value. At this point  $\Delta t_{imp}$  reaches a minimum value (fig. 8(iv)). As  $t_s$  increases beyond this, the  $\Delta t_{imp}$  keeps increasing (fig. 8(v),(vi)), until it saturates because the signal is switched after the duration of the entire impact cycle. The linear range does not exist for higher values of  $v_{o+}$ . Using these models, we intend to design a control law that will help push  $t_s$  values closer to perfectly closed-loop values for subsequent impacts.

3) *Effect of Coulomb friction:* In all the above models, the friction force was assumed to be zero. Average impact velocities over 100 impacts are plotted for varying values of

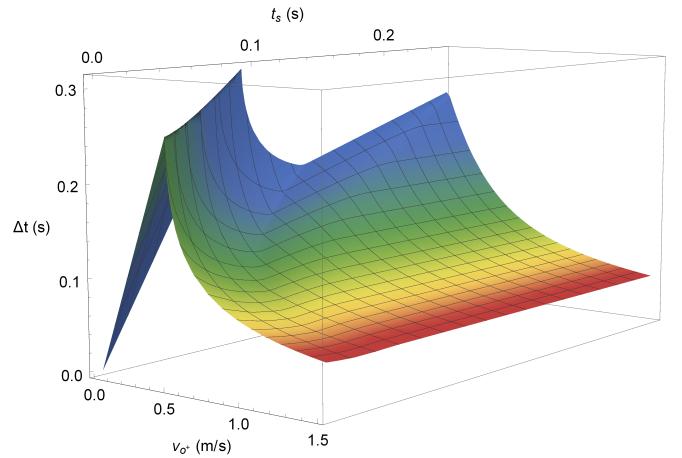


Fig. 10. 3D contour plot of  $\Delta t$  vs.  $t_s$  plotted for different values of  $v_{o+}$ .  $t_s$  is a control parameter and  $\Delta t$  can be obtained by sensing. Together,  $\Delta t$  and  $t_s$  can be used to estimate  $v_{o+}$  with our estimator.

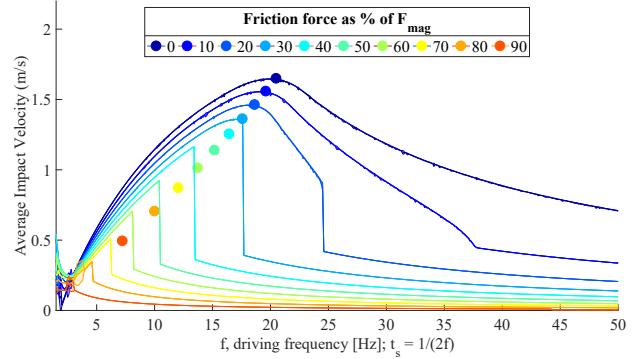


Fig. 11. Comparison of simulated impact velocities. The velocities for impacts 100 to 200 are averaged and plotted for different values of Coulomb friction force. Colored circles represent the ideal closed-loop values. Lines represent the partially closed-loop values.

the friction force in Fig. 11. The circles represent the ideally-closed loop values, while the curves represent the partially closed-loop values using impact times. Much like the step-out frequency of a stepper motor, average impact velocities drop suddenly for the partially closed-loop system beyond a cut-off driving frequency. This is due to the sphere reversing direction before spring contact, leading to a drop in its net kinetic energy. As friction force increases as a percentage of  $F_{mag}$ , the partially closed loop system reaches its cutoff frequency, before resonance. This drop in impact velocity is not seen in the fully closed-loop system, for any values of friction. Hence, partially closed-loop control will not produce the maximum possible impact velocity for high values of Coulomb friction force.

### III. EXPERIMENTAL DETERMINATION OF IMPACT COEFFICIENT OF RESTITUTION

The coefficient of restitution  $e$  was determined using the time interval between two consecutive bounces of the sphere when dropped from a given height onto the impact rod. The

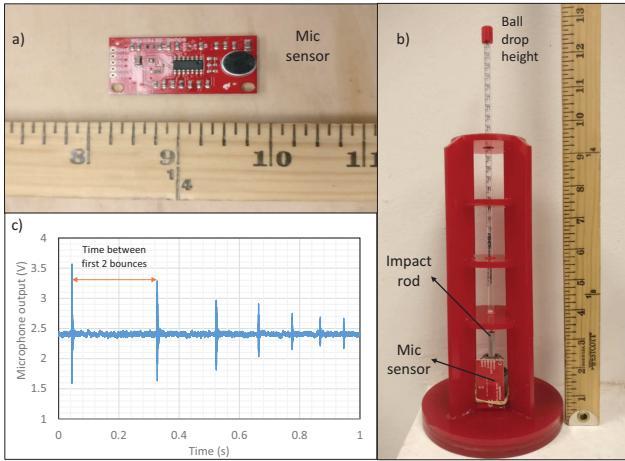


Fig. 12. Experimental setup for measuring the coefficient of restitution  $e$

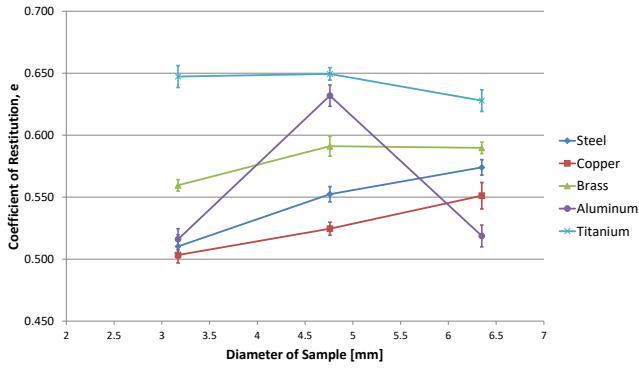


Fig. 13. Measured coefficient of restitution  $e$  as a function of rod diameter for different materials

measurements were made using 38.1 mm long impact rods for five different materials. Impact rods were held by a drill chuck. A length of 10.0 mm of the impact rods was sticking out of the chuck. The experimental setup is shown in fig. 12.

The results, shown in fig. 13, show that aluminum offers the largest coefficient of restitution, followed by titanium and brass. The densities of aluminum, titanium, stainless steel, brass, and copper are 2720, 4500, 7600, 8500, and 8940 kg/m<sup>3</sup> respectively. This data, coupled with a desire for a lightweight millirobot suggests that titanium is the best material for an impact plate. Bio-compatibility of the material used is another constraint.

#### IV. EXPERIMENTAL MAGNETIC HAMMER TESTS

##### A. Magnetic test bench description

A desktop-size, single-axis magnetic setup was built to reduce the cost related to clinical MRI experiments. It is composed of two solenoid coils oriented along the same axis and separated by a distance  $d$ . The coils are used to produce both the magnetizing field and the gradient. The properties of the coils are shown in Table I.

The system is shown in fig. 14. The two coils are held by an acrylic tube. They can slide along this tube and be

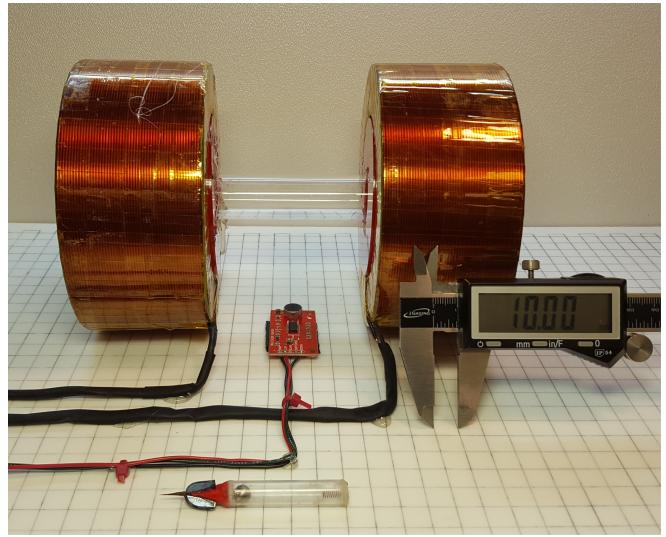


Fig. 14. Picture of the magnetic test bench.

TABLE I  
PROPERTIES OF THE COILS USED IN THE MAGNETIC TEST BENCH

Internal Radius	12.7 mm	Electrical resistance	0.16 $\Omega$
External Radius	45.8 mm	Inductance	1.59 mH
Length	65 mm	Max current change rate Voltage = 25 V	15.7 kA/s
Wire	10 AWG	Max continuous current	15 A
Wire cross-section	5.26 mm <sup>2</sup>	Flux density on system center $I = 15$ A, $d = 50$ mm	11 mT
Number of turns	265	Gradient on system center $I = 15$ A, $d = 50$ mm	0.45 T/m

locked in place to adjust the distance between the two coils and therefore change the maximum field and gradient values. The acrylic tube is transparent, allowing for visual access to the robot. Each coil is powered by a Syren 25 regenerative switching power supply. The Syren 25 are manufactured by Dimension Engineering. They can provide continuously a current of 25 A with a maximum voltage of 24 V. A Hall-effect-based current sensor is used to perform a PID regulation of the current. It is necessary to control the current inside the coils and not only the voltage. Indeed, the produced magnetic field is directly proportional to the current whereas the voltage is related to the magnetic flux variation and the voltage drop produced by Joule effect losses.

Robots are inserted inside the acrylic tube holding the coils. They are held by a second, smaller tube that guides them along the system axis. Robots can be free to move along the coil axis or held in place. A picture of the system is provided in fig. 14.

##### B. Partially closed loop experiment

The coils are driven by square shaped current waveform. The current in the coils can either be  $I_{max}$  or 0 A. The coil will be said to be “on” when  $I = I_{max}$  and “off” when  $I = 0$  A.

As explained in section II-D.1, the magnetic hammer cannot work properly if the magnetic field is not synchronized with the position of the sphere. An open-loop control is inefficient, as shown in Fig. 7. The force applied on the sphere (and therefore the magnetic gradient) must change direction when the sphere hits the impact plate and when the sphere changes direction on the spring side to provide maximum impulse.

Our eventual goal is to use these robots in an MRI scanner, where MRI gradients must be shared for propulsion and position feedback [11]. The nature of our system enables simpler sensing requirements that can be accomplished with a simple microphone. The microphone is used to monitor the noise produced by the system. The impact noise creates a larger pulsed signal on the microphone output and can, therefore, be easily detected. When the impact is detected, the anterior coil is turned off while the posterior coil is turned on. The force applied on the sphere now pushes it backward, toward the spring side.

The current stays constant during a time  $T_s$  after the impact is detected. The anterior coil is subsequently turned on, and the posterior coil is turned off. The force then pushes the sphere forward. The current in the coils is changed again when another impact is detected. This process is repeated indefinitely.

$T_s$  is manually tuned while the system is working. It is set to the value that gives the maximum oscillating frequency. This value corresponds to a gradient that changes direction when the sphere velocity is zero on the spring side. It should give the same results as the perfectly closed-loop simulations.

The partially closed-loop experiment was performed and compared to the model. Section IV shows a comparison of the optimum oscillating frequency as a function of  $I_{max}$ . The simulations are performed for a perfectly-closed loop system. When  $I_{max}$  increases, the oscillating frequency increases. The force on the sphere increases with  $I_{max}$  and consequently increases the moving speed of the sphere. This figure also shows that the model without friction has the same slope as the experimental data. However, the simulation signals are approximately 1 Hz faster than the experiment.

## V. PRELIMINARY TESTS IN CLINICAL MRI

Preliminary tests of magnetic hammers were performed in a clinical 3T Siemens MRI scanner to demonstrate the ability of MRI scanners to produce a force able to drive the device. No closed-loop control was implemented. The magnetic gradient oscillated at a constant frequency. As seen before, the system does not work optimally in these conditions. At low frequencies, the ferromagnetic sphere completely stops on both sides of the millirobot. All the kinetic energy is lost at these times, and the magnetic hammer, therefore, performs poorly. The aim of this test is to prove that MRI scanners are suitable to produce the desired force on the magnetic sphere inside the millirobot and provide a pulsed force.

A 50 mm long, 7 mm diameter robot was built for this test. A 2Hz square gradient with an amplitude of 23 mT/m was applied to it. This frequency is slow enough to allow

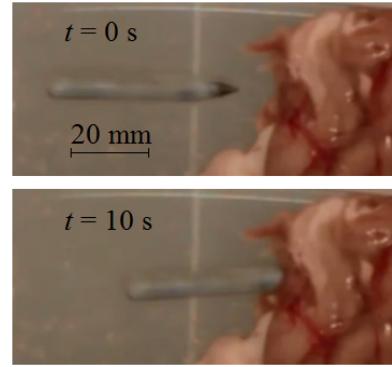


Fig. 15. Picture of the magnetic hammer driven by an MRI scanner. The penetration test is realized on a sheep brain sample.

the sphere to stop on both sides completely. A sheep brain hemisphere was used as tissue sample to penetrate.

Once the gradient wave was started, the sphere began to move back and forth while the robot was moving toward the sample at each impact, at an average speed of 1.9 mm/s. Friction with the plastic container prevent the capsule from moving if a constant gradient is applied. The robot then began to penetrate the sample. It went 9 mm deep inside it and stopped progressing (see fig. 15). This experiment demonstrate the suitability of MRI scanner to drive magnetic hammers. No further measurements were made as this demonstration was the sole purpose of the experiment and the magnetic test bench allows us to perform extensive testing at reduced cost.

Future work will implement closed loop control on the clinical MRI scanner to transfer energy efficiently. The MRI signal could be used to compute the position of the magnetic sphere at a frequency greater than 20 Hz, as we did in [11].

## VI. TISSUE PENETRATION EXPERIMENT

An iterative design process was used to achieve tissue penetration using the magnetic test bench. Seven millirobots were built and tested, varying the tip shape and composition, the tube length, the spring, and the sphere material.

Our observations of the penetration experiments concluded that sharp blades placed on the tip of the millirobot allow for an easier tissue penetration. The blades are placed much like on a hunting arrow tip, and create a fissure in the tissue which allow the movement of the capsule inside the sample. The blades used in our experiments were made of Titanium which a bio-compatible and non-magnetic metal.

Our observations also showed that, when the sphere compresses the spring, the capsule tends to move backward. This effect release the pressure exerted by the millirobot tip on the tissue and therefore make the impact less efficient at penetrating the sample. This issue was solved by using a porcupine needle placed in front of millirobot, at the center of the blades. Porcupine needles are covered with microscopic backward facing barbs. These prevents the needle from being pulled off a tissue once penetrated. Natural porcupine needles cannot be sanitized and so cannot be used in an in-vivo

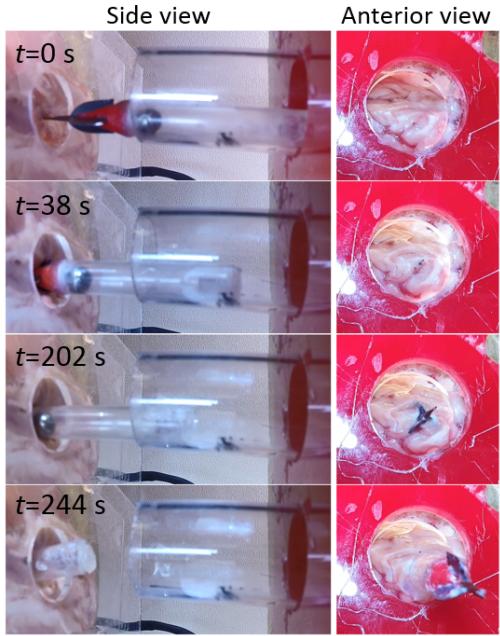


Fig. 16. Picture presenting the penetration of a millirobot prototype inside a lamb brain sample.

TABLE II  
MILLIROBOT PARAMETERS FOR TISSUE PENETRATION EXPERIMENT

Millirobot diameter	7.5 mm
Sphere diameter	6.35 mm
Free length of sphere travel	15 mm
Spring free length	10 mm
Spring constant	35 N/m

medical intervention. However, synthetic porcupine needles can be built [12].

Fig. 16 show frames of a video from a representative penetration test. We performed five successful penetration tests and no failures with our final millirobot design. The tissue sample used in these experiments were 10 mm thick lamb brain slice. They were placed in a sample holder made with two acrylic sheets, one on each side. Two holes in the sample holder allowed the millirobot to access and cross the tissue. The millirobot used in this experiment had a diameter of 6 mm. It was using three titanium blades, a porcupine needle, and a titanium impact rod. The mechanical parameters of this millirobot is presented in table ???. The flux density applied by the coils had a maximum value of 40 mT and a maximum gradient of 545 mT/m. The control was performed with the partially closed loop method presented in Section II-D.2.

This prototype successfully penetrated the tissue sample in 225 s. This test proves the capability of the magnetic hammer system to penetrate biological tissue.

## VII. CONCLUSIONS

A magnetic hammer system for a millirobot driven by the gradient fields of an MRI scanner was studied. The system enables producing the forces large enough to penetrate body tissue.

The hammer is composed of a ferromagnetic sphere moving inside a tube. On the posterior side of the robot, there is a spring that allows changing the direction of the sphere smoothly. On the anterior side, a hard metal rod act as an impact plate to transfer the momentum of the ferromagnetic sphere to the body of the robot.

The system is driven by an external magnetic field, such as that produced by an MRI scanner. The main field magnetizes the sphere and the gradient produces the forces necessary to move the sphere.

A complex modelization allows the computation of the position of the sphere as a function of time. The magnetic flux density and the gradient are computed using a semi-analytical method and allow an accurate calculation of the force applied to the sphere. The speed of the sphere after impact is computed from the coefficient of restitution. The rotation of the sphere is also calculated, allowing an accurate calculation of the drag produced by the sliding of the sphere inside the tube.

The coefficients of restitution ( $e$ ) depends on the materials of the colliding objects but also on their shape and sizes. Values of  $e$  were experimentally measured. These measurements showed that aluminum impact plates exhibit large values of  $e$ . This material also has the advantage of being lightweight, a useful property to achieve neutral buoyancy of millirobots. Titanium also performs well, is lightweight and is a biocompatible material.

A magnetic test bench was built to reduce experimental cost related to the use of a clinical MRI scanner. A magnetic hammer was tested with a partially closed loop control. The impact of the sphere is detected via a microphone. The posterior coil is turn on during a predetermined time to pull the sphere backward. After this time, the posterior coil is turned off and the anterior coil is turned on until the next impact is detected. Experimental results were compared to the model. The experimental oscillating frequency is in good agreement with the model predictions. This validates our modelization.

In future work, the control of the magnetic hammer will be implemented and tested in a clinical MRI scanner. The impact will be detected with the MRI signal instead of a microphone. The tradeoffs involved in miniaturization of the robot will also be studied.

## REFERENCES

- [1] M. Sitti, H. Ceylan, W. Hu, J. Giltinan, M. Turan, S. Yim, and E. Diller. Biomedical applications of untethered mobile milli/microrobots. *Proceedings of the IEEE*, 103(2):205–224, Feb 2015.
- [2] Ajay Vikram Singh and Metin Sitti. Targeted drug delivery and imaging using mobile milli - microrobots: A promising future towards theranostic pharmaceutical design. *Current pharmaceutical design*, 22(11):1418–1428, 2016.
- [3] Samara Firebaugh, Jenelle Piepmeyer, Elizabeth Leckie, and John Burkhardt. Jitterbot: A mobile millirobot using vibration actuation. *Micromachines*, 2(2):295–305, 2011.
- [4] Russell H Taylor. *Computer-integrated surgery: technology and clinical applications*. Mit Press, 1996.
- [5] Arnaud Chanu, Ouajdi Felfoul, Gilles Beaudoin, and Sylvain Martel. Adapting the clinical mri software environment for real-time navigation of an endovascular untethered ferromagnetic bead for

- future endovascular interventions. *Magnetic Resonance in Medicine*, 59(6):1287–1297, 2008.
- [6] Sylvain Martel, Jean-Baptiste Mathieu, Ouajdi Felfoul, Arnaud Chanu, Eric Aboussouan, Samer Tamaz, Pierre Pouponneau, LHocine Yahia, Gilles Beaudoin, Gilles Soulez, et al. Automatic navigation of an untethered device in the artery of a living animal using a conventional clinical magnetic resonance imaging system. *Applied physics letters*, 90(11):114105, 2007.
  - [7] A. T. Becker, O. Felfoul, and P. E. Dupont. Toward tissue penetration by mri-powered millirobots using a self-assembled gauss gun. In *2015 IEEE International Conference on Robotics and Automation (ICRA)*, pages 1184–1189, May 2015.
  - [8] S.S. Hidalgo-Tobon. Theory of gradient coil design methods for magnetic resonance imaging. *Concepts in Magnetic Resonance Part A*, 36A(4):223–242, 2010.
  - [9] James C Simpson, John E Lane, Christopher D Immer, and Robert C Youngquist. Simple analytic expressions for the magnetic field of a circular current loop. *NASA Technical report*, 2001.
  - [10] Finite Element Method Magnetics. <http://www.femm.info>.
  - [11] Ouajdi Felfoul, Aaron T Becker, Georgios Fagogenis, and Pierre E Dupont. Simultaneous steering and imaging of magnetic particles using mri toward delivery of therapeutics. *Scientific Reports*, 6, 2016.
  - [12] Woo Kyung Cho, James A Ankrum, Dagang Guo, Shawn A Chester, Seung Yun Yang, Anurag Kashyap, Georgina A Campbell, Robert J Wood, Ram K Rijal, Rohit Karnik, et al. Microstructured barbs on the north american porcupine quill enable easy tissue penetration and difficult removal. *Proceedings of the National Academy of Sciences*, 109(52):21289–21294, 2012.