

Laboratory Observations of the Zeeman Effect

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Abstract

1 Introduction

1.1 Historical Background

1.2 Theoretical Overview

The splitting of the spectra of mercury into hyperfine lines when an external magnetic field is applied is the result of the mercury atom's magnetic-dipole interaction with the external magnetic field.

In its ground state, the mercury atom has 80 electrons in which the $n = 1, 2, 3, 4$, and 5 shells are filled, leaving two 6s valence electrons. The spectral emissions of mercury come from the transitions of the two valence electrons between different quantum states.

When no external magnetic field is present, hyperfine structure in atomic spectra can be observed due to the spin-angular momentum coupling of electrons. See pp. 47 of [1] for a more detailed discussion. In the presence of an external magnetic field, the interaction of the total angular momentum of the electrons with the magnetic field also splits the spectral lines into finer lines of slightly different wavelength. Figure 1 shows how a single transition from the $l = 2$ to $l = 1$ states results in hyperfine structure in the presence of a magnetic field.

The total angular momentum J of mercury is dependent on both the orbital angular momentum of the valence electrons given by the quantum number l , and the spin angular momentum quantum number s . In Russell-Saunders or LS coupling, the total an-

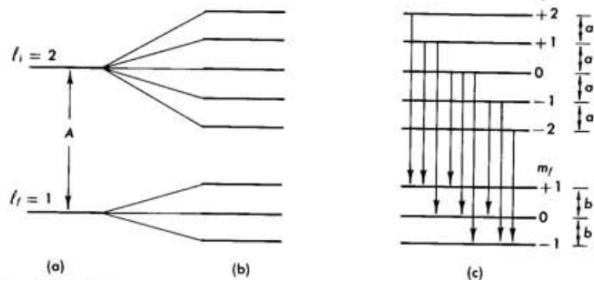


Figure 1: A single spectral line caused by an atomic energy transition will be split into multiple “hyperfine” lines due to the interaction of the total angular momentum of the valence electrons with an external magnetic field. (a) shows the transition in the absence of an external magnetic field. The transition between the $l = 2$ and the $l = 1$ states ($d \rightarrow p$) produces a single spectral line. (b) shows how these formerly single energy-levels are split into multiple states in the presence of an external magnetic field. (c) shows the possible transitions between the new states, each of which produces a different spectral line with slightly different wavelength.

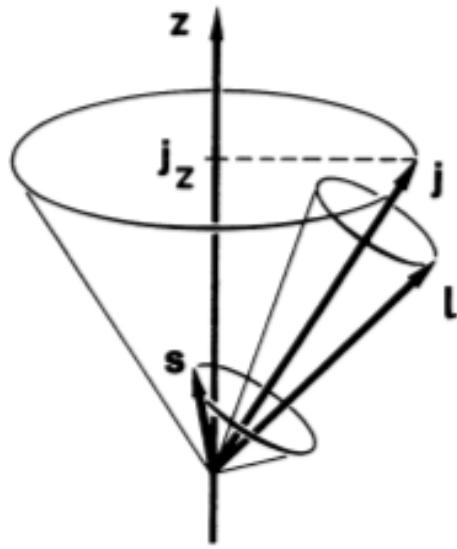


Figure 2: Electron spin angular momentum \mathbf{s} and orbital angular momentum \mathbf{l} sum to create total angular momentum \mathbf{j} .

angular momentum is given by the sum of the orbital angular momentum and the spin angular momentum:

$$j = l + s \quad (1)$$

Figure 2 shows how these two quantities (vectors, actually) combine to form total angular momentum.

Selection rules place restrictions on how the quantum numbers may change when a valence electron undergoes a transitions. These selection rules are:

1. $\Delta s = 0$
2. $\Delta l = 0, \pm 1$
3. $\Delta J = 0, \pm 1$, but not $\Delta J = 0 \rightarrow \Delta J = 0$
4. $\Delta M_j = 0, \pm 1$, but not $M_j = 0 \rightarrow M_j = 0$ if $\Delta J = 0$

Figure 1 shows that spectral splitting is dependent on the quantum number m , which specifies the projection of the orbital angular momentum along the

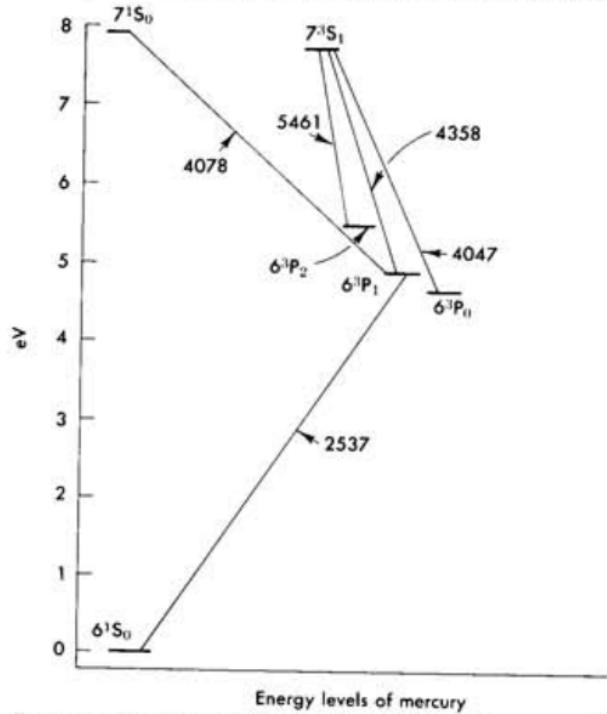


Figure 3: Energy level transitions of mercury between quantum states. For the purposes of our observations, we are interested in the $7^3S_1 \rightarrow 6^3P_2$ transition which produces 546.1 nm light. Figure 7.39 of [1]

z-axis of the atom. m can take on $2l + 1$ the values ranging from l to $-l$.

The resulting polarization of the light emitted in a transition is entirely determined by ΔM_j . For $\Delta M_j = 0$, the emitted photons are polarized linearly and parallel to the field lines of the applied magnetic field \mathbf{B} . For $\Delta M_j = \pm 1$, emitted photons are circularly polarized along the direction of \mathbf{B} and appear linearly polarized perpendicular to \mathbf{B} when viewed side-on to \mathbf{B} .

2 Methods and Procedures

The Pasco Scientific Model SE-9654 Zeeman Effect Experiment was used to make all observations. The

experiment consisted of two large solenoids oriented along the same axis with an air gap between them in which a mercury lamp was placed. An optical rail was used to align a polarizing filter, a collimating lens, an interference filter, a Fabry-Perot interferometer, and a CMOS camera. The basic experimental technique consisted of imaging the interference pattern of the 546.1 nm mercury spectral line through the polarizer and Fabry-Perot interferometer. Figure

To study the Zeeman effect, observations of a mercury lamp were made first with no magnetic field and 90 deg polarization, then with an approximately 1T magnetic field. Observations with a magnetic field included:

- 90 deg (field-perpendicular) polarization
- 0 deg (field-parallel) polarization
- No polarization
- Axial B-field at polarization varying from 90 deg to 0 deg

Figure 6 shows the perpendicular and axial configurations of the magnetic field used for the observations.

The observations and results of each of these field configurations will be presented and discussed in Section 3.

2.1 Method Description

3 Data and Results

With no applied magnetic field, the 546.1nm mercury spectral line as viewed through the Fabry-Perot interferometer produces the interference pattern as shown in Figure 7.

3.1 Spectra Through a Perpendicular Magnetic Field

The first observations were made such that the mercury lamp was viewed through a magnetic field perpendicular to the travel of the mercury spectra, as is shown in 6a. With this magnetic field configuration,

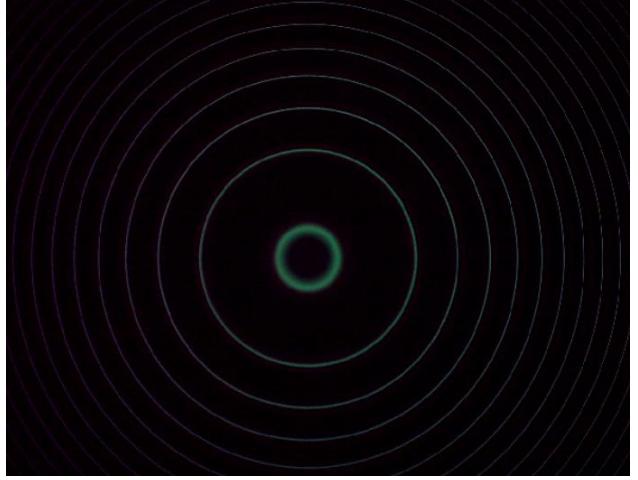


Figure 7: Interference pattern of the 546.1nm mercury line with no applied magnetic field. The interference lines are singular.

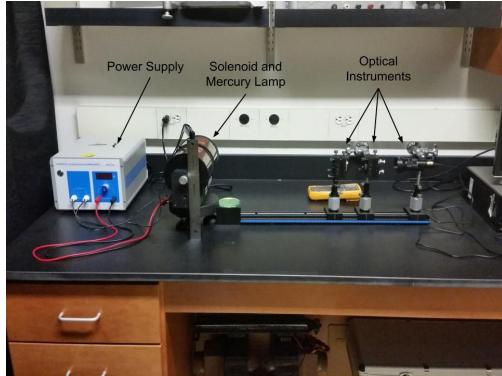
| k | Radius (m) |
|---|---------------------------------|
| 4 | $0.7956 \pm 0.1 \times 10^{-3}$ |
| 3 | $0.6911 \pm 0.2 \times 10^{-3}$ |
| 2 | $0.5678 \pm 0.1 \times 10^{-3}$ |
| 1 | $0.4096 \pm 0.1 \times 10^{-3}$ |

Table 1: Interference ring radii of the mercury 546.1 nm spectra with no magnetic field.

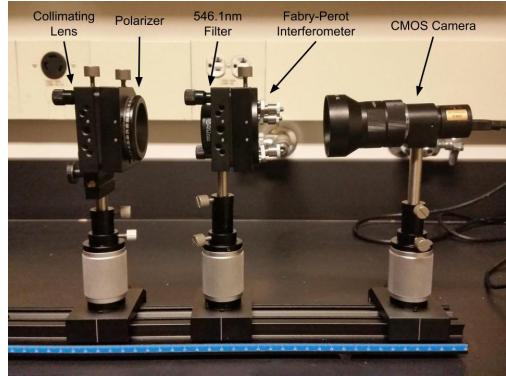
observations were made with the polarizer at 0° (Parallel to the field lines), and 90° (perpendicular to the field lines). This allowed us to observe the hyperfine spectral lines with polarization parallel and perpendicular to the magnetic field lines, which correspond to photons created in $\Delta M_z = 0$ and $\Delta M_Z = \pm 1$ transitions, respectively, of the mercury electrons.

3.1.1 Spectra with Field-Perpendicular Polarization

With the polarizer set to 90°, we observed the mercury spectra with polarization perpendicular to the applied magnetic field. A distinct triple ring structure can be seen Figure 8 in which each interference ring consists of a bright central ring surrounded by two fainter rings.



(a)

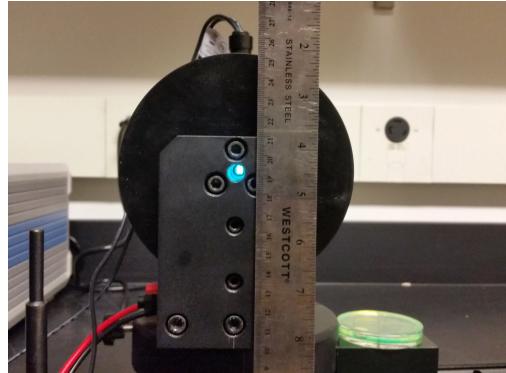


(b)

Figure 4: Overview of the Experiment configuration. Figure 4a shows the entire apparatus with the variable power supply for the solenoid and mercury lamp, the solenoid, the mercury lamp (hidden by the solenoid), the optical track, and the optical instruments. Figure 4b shows the optical instruments in detail.

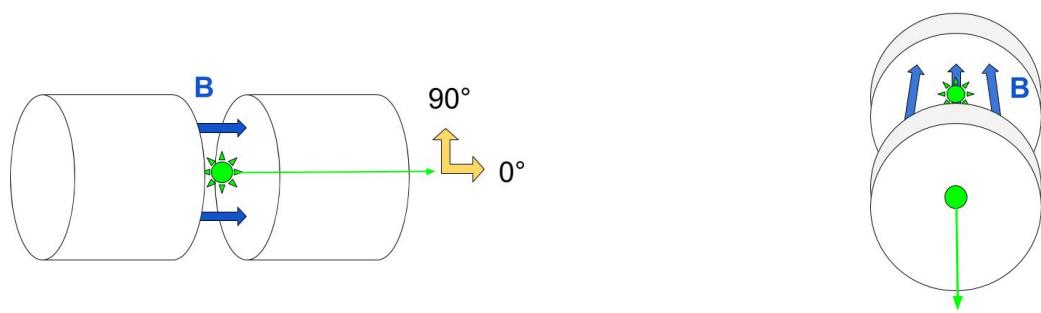


(a)



(b)

Figure 5: Detail view of the solenoid with the mercury lamp source. Figure 5a shows the configuration with the magnetic field lines perpendicular to the light source. Figure 5b shows the axial field configuration looking down the sight-hole of the solenoid to the mercury lamp.



(a) Perpendicular field configuration.

(b) Axial field configuration.

Figure 6: The two magnetic field configurations observed. In (6a), the magnetic field is oriented perpendicularly to the path of the observed light from the mercury lamp. 90° polarization is defined to be perpendicular to the field lines, while 0° polarization is parallel to the field lines. In configuration (6b), light from the lamp travels along the magnetic field lines down the center of one of the solenoids through a sight hole.

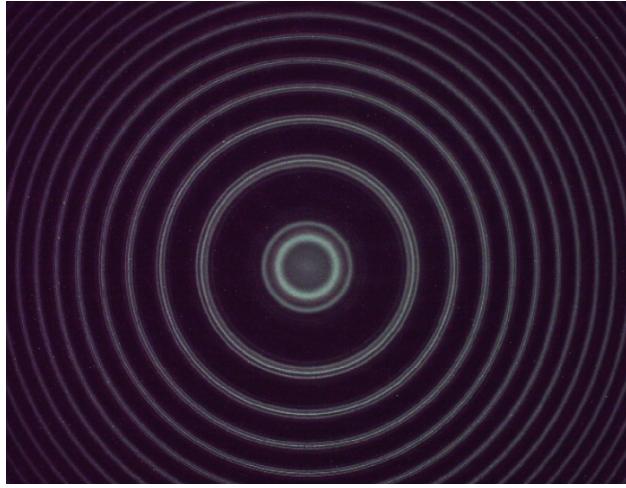


Figure 8: Interference pattern of the mercury spectrum with a 1T applied magnetic through a polarizer oriented perpendicular to the magnetic field lines. The interference rings correspond to light produced by $\Delta M_z = 0$ transitions polarized perpendicularly to the magnetic field.

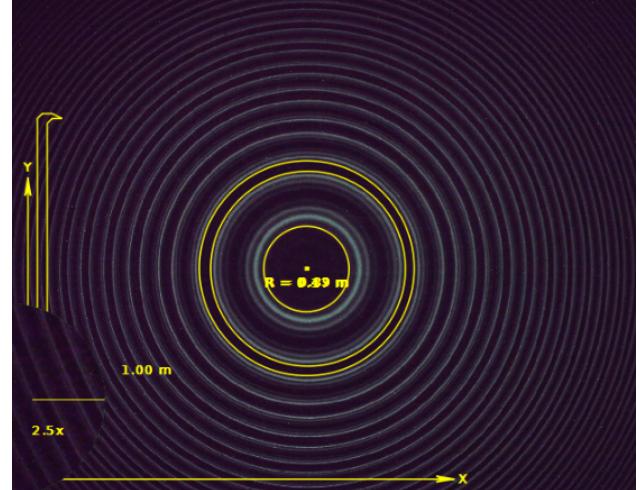


Figure 9

Using PASCO Software, The radii of the inner and outer rings of the $k = 1$ through $k = 4$ interference rings were measured. These radii are given in Table 2.

3.1.2 Spectra with Field-Parallel Polarization

3.2 Spectra Along an Axial Magnetic Field

3.3 Measurement of the Bohr Magneton

With the precise measurement of spectral line splitting in the presence of the perpendicular magnetic field, it was possible to measure the value of the Bohr magneton.

| k | μ_B (J/T) |
|------|--|
| 1 | 9.16×10^{-24} |
| 2 | 9.24×10^{-24} |
| 3 | 9.36×10^{-24} |
| 4 | 9.10×10^{-24} |
| Mean | $9.22 \times 10^{-24} \pm 0.6 \times 10^{-24}$ |

Table 3: Calculated values of the Bohr magneton μ_B for each interference ring, and the mean calculated value for all interference rings.

| $k = 1$ Measurements | R_+ (m) | R_- (m) | ΔR (m) |
|-------------------------|---------------------------------|---------------------------------|---------------------------------|
| 1 | 0.4282 | 0.3893 | 0.0389 |
| 2 | 0.4278 | 0.3896 | 0.0382 |
| 3 | 0.4275 | 0.3887 | 0.0388 |
| Mean | $0.4278 \pm 0.4 \times 10^{-3}$ | $0.3892 \pm 0.5 \times 10^{-3}$ | $0.039 \pm 0.4 \times 10^{-3}$ |
| $k = 2$ Measurements | R_+ (m) | R_- (m) | ΔR (m) |
| 1 | 0.5819 | 0.5539 | 0.0280 |
| 2 | 0.5815 | 0.5536 | 0.0279 |
| 3 | 0.5818 | 0.5536 | 0.0282 |
| Mean | $0.5817 \pm 0.2 \times 10^{-3}$ | $0.5537 \pm 0.2 \times 10^{-3}$ | $0.0280 \pm 0.2 \times 10^{-3}$ |
| $k = 3$ Measurements | R_+ (m) | R_- (m) | ΔR (m) |
| 1 | 0.7035 | 0.679 | 0.0245 |
| 2 | 0.7033 | 0.6798 | 0.0235 |
| 3 | 0.7025 | 0.6805 | 0.0220 |
| Mean | $0.7031 \pm 0.5 \times 10^{-3}$ | $0.6798 \pm 0.8 \times 10^{-3}$ | 0.0233 ± 0.001 |
| $k = 4$ Measurements | R_+ (m) | R_- (m) | ΔR (m) |
| 1 | 0.8058 | 0.7861 | 0.02 |
| 2 | 0.8057 | 0.7865 | 0.02 |
| 3 | 0.8059 | 0.7857 | 0.02 |
| Mean | $0.8058 \pm 0.1 \times 10^{-3}$ | $0.7861 \pm 0.4 \times 10^{-3}$ | 0.020 ± 0.001 |

Table 2: Radius measurements of the hyperfine structure of the $k=1$ through $k=4$ interference rings with a 1T magnetic field and 90° polarization.

4 Conclusion

References

- [1] A. Melissinos, *Experiments in Modern Physics*. Academic Press, 1966.