Response Optimization

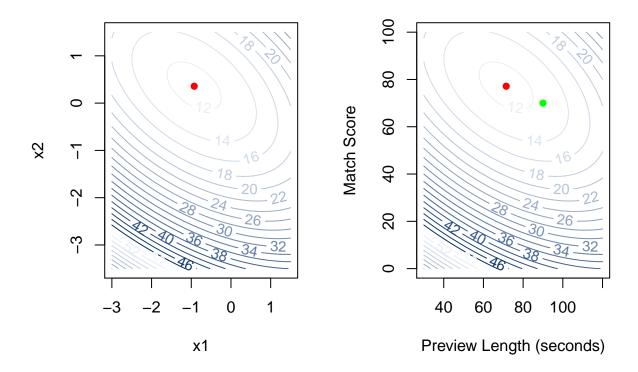
I decided to follow up my results with a response surface experiment so that a full second order model could be fit and the optimum identified. I have already identified the significant factors though factor screening, and found a rough idea of where the optimum lies through the method of steepest descent.

The response surface experiment that I decided to use was the central composite design. A central composite design facilitates estimation of the full second order response surface model, and hence identification of the optimum.

I chose the high and low levels of the factors based on the center point being my estimate of the optimum from steepest descent in phase 2. I also chose the high and low levels based on my selection of a spherical design in order to ensure the estimate of the response surface at each condition is equally precise.

| Condition.Num | Prev.Length | Match.Score | Browse.Time |
|---------------|-------------|-------------|-------------|
| 1 | 70 | 50 | 15.72111 |
| 2 | 70 | 90 | 15.82121 |
| 3 | 110 | 50 | 15.90275 |
| 4 | 110 | 90 | 15.93098 |
| 5 | 90 | 70 | 15.91739 |
| 6 | 120 | 70 | 15.73697 |
| 7 | 60 | 70 | 15.95454 |
| 8 | 90 | 100 | 15.91128 |
| 9 | 90 | 40 | 15.84565 |

I intended to perform axial conditions with $a=\sqrt{2}$, but the corresponding preview times and match scores were messy. Thus, in the interest of defining experimental conditions with more convenient levels, I let a=1.5, yielding the preview lengths and match scores in the table above. I then generated data simulating 100 users randomized into each of these 9 conditions, and recorded their browsing time.



I then fit the full second order response surface by fitting the second order regression model.

From the coefficients in the output, I plotted the contour plot in coded units and found that the stationary point was located at $x_1 = -0.9266421$ and $x_2 = 0.3571865$.

I then converted the contour plot to natural units. The corresponding stationary point is when preview length is 71.47 (70) seconds and match score is 77.14% (77%), represented by the red point. The green point is my rough estimate of the optimal conditions from using the method of steepest descent in phase 2. It suggested a preview length of 90 seconds and a match score of 70%. As can be seen, it is somewhat close to the true optimum.

The estimated browsing time at the optimum is 11.53 seconds and a 95% confidence interval is given by (11.3855,11.675).

Thus, Netflix should utilize preview lengths of 70 seconds and match scores of 77% in order to minimize the browsing time by users.