



• First, update rules for  $\rho$  (UT density)

$$\rho_m(k+1) = \left[ \rho_m(k) - \left( \frac{j_R - j_L}{\Delta r} \right) \Delta t \right] - b \rho_m(k) \Delta t + a \underbrace{(m+1)}_r \Delta r \Delta \theta \Delta t \left( \sum_{j=-j_{\max}}^{+j_{\max}} \phi_{m,n-j}(k) \right)$$

Annotations: "time" points to  $k$ ; "this [stuff] stays the same as before" points to the bracketed term; "advective currents" points to the  $\frac{j_R - j_L}{\Delta r}$  term.

Where  $j_{\max} = \frac{d}{(m+1) \Delta r \Delta \theta} - \frac{1}{2}$   
 $d = (j_{\max} + \frac{1}{2}) r \Delta \theta$

Round this up to the nearest integer

For example, in the above drawing,  $j_{\max} = 2$ , so  $j$  goes from  $-2$  to  $+2$  ( $-2, -1, 0, 1, 2$ )

• Next, update rules for  $\phi$  (DL density)

For those  $n$  that are within the zone of exchange around a given MT (i.e. the yellow zone)

$$\phi_{m,n}(k+1) = \left[ \phi_{m,n}(k) - \frac{\Delta t}{(m+1) \Delta r} \left( (m+2) J_R^r - (m+1) J_L^r \right) - \frac{\Delta t}{(m+1) \Delta r \Delta \theta} \left( J_R^\theta - J_L^\theta \right) \right] - a \underbrace{\phi_{m,n}(k) \Delta t}_{\text{tubules within the range}} + \sum_{\text{tubules}} b \rho_m(k) \Delta t$$

Annotations: "this [stuff]" points to the bracketed term; "this sum is only if the yellow zones overlap" points to the summation term.

For those  $n$  that are outside the zone of exchange around any of the MTs, the last two terms are absent. (I believe you follow this idea in your current code)