Homogenous Ensemble Learning in Highly Imbalanced Data

Data Science is about understanding the data, 理解数据

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```
In []: # for eda and modeling
   import pandas as pd
   import numpy as np
   pd.options.plotting.backend = 'plotly'
   from utils.dsc80_utils import *
   from itertools import chain
```

Step 1: Introduction

Predictive model (classifier) detecting user preference using **textual features** in combnation with other **numerical features** is the key first step prior to building a recommander system or doing any other further analysis. The challenge that is addressed in this project is related to the high imbalance nature of the recipe data set that we are using.

Random Forest Algorithm

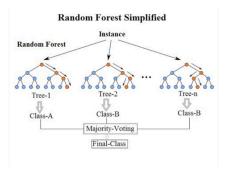
In this project, we will adapt ideas of **homogenous ensemble learning** where we will use multipl **Decision Trees**, and making them into a **Random Forest** for more robust predictions of the data.

A **Decision Tree** essentially learns to come up with questions or decisions at an high dimensional space (depending on the number of features) and then separate the data using "boxes" or "lines" in that way. The core mechanism that allows it to happen is using *entropy minimization* where the model tries to reduce the entropy, or uncertainty of each split, making one catagory fit to one side and the other catagory to the other side.

$$entropy = -\sum_{C} p_C \log_2 p_C \tag{1}$$

A Random Forest essentially is when at the splitting point of data to train/test/val, a random subset of features is taken out instead of choosing from all of them and then spliting the tree base on this subset of the feature, usually speaking m=sqrt(d) seems to work well in practice and it is also the default that sk_e uses. This allows each decision trees to come up with different prediction rules for later on voting an best one

- Notice that we are not doing simple boostrap of the data as each decision tree may not resemble too great of a difference in that way, instead, we are taking different features directly using the same type of model (decision tree), making it a homogenous ensemble learning method.
- We want the individual predictors to have low bias, high variance, and be uncorrelated with each other. In this way, when averaging (taking votes) them together, low bias and low variance would occur.



Step 2: Data Cleaning and Exploratory Data Analysis

```
In [ ]: interactions = pd.read_csv('food_data/RAW_interactions.csv')
    recipes = pd.read_csv('food_data/RAW_recipes.csv')
```

Merging

Initial merging is needed for the two dataset to form 1 big data set

- 1. Left merge the recipes and interactions datasets together.
- 2. In the merged dataset, fill all ratings of 0 with np.nan. (Think about why this is a reasonable step, and include your justification in your website.)
- 3. Find the average rating per recipe, as a Series.
- 4. Add this Series containing the average rating per recipe back to the recipes dataset however you'd like (e.g., by merging). Use the resulting dataset for all of your analysis. (For the purposes of Project 4, the 'review' column in the interactions dataset doesn't have much use.)

Transformation

- 1. Some columns, like nutrition, contain values that look like lists, but are actually strings that look like lists.
 We turned the strings into actual columns for every unique value in those lists
- 2. Convert to list for steps, ingredients, and tags
- 3. Convert date and submitted to Timestamp object and rename as review_date and recipe_date
- 4. Convert Types
- 5. Drop same id (same with recipe_id)

Type Logic

- 1. String: [name, contributor_id, user_id, recipe_id,]
 - quantitative or qualitative, but cannot perform mathamatical operations (quntitative discrete)
 - name is the name of recipe
 - contributor_id is the author id of the recipe (shape=7157)
 - recipe_id is the id of teh recipe (shape=25287)
 - id from the original dataframe also is the id of the recipe, dropped after merging
 - user_id is the id of the reviewer (shape=8402)
- 2. List: [tags, steps, description, ingredients, review]
 - qualitative, no mathamatical operation (qualitative discrete)
- 3. int : [n_steps, minutes, n_ingredients, rating]
 - quantitative mathamatical operations allowed (quantitative continuous)
- 4. float: [avg_rating, calories, total_fat sugar, sodium, protein, sat_fat, carbs]
 - quantitative mathamatical operations allowed (quantitative continuous)
- 5. Timestamp: [recipe_date, review_date]
 - quantitative mathamatical operations allowed (quantitative continuous)

Below are the full implementation of initial, which does the merge conversion, then transform, which carries out the neccessary transformation described above

```
In [ ]: def initial(df):
            '''Initial claeaning and megrging of two df, add average ratings'''
            # fill 0 with np.NaN
            df['rating'] = df['rating'].apply(lambda x: np.NaN if x==0 else x)
            # not unique recipe id
            avg = df.groupby('recipe id')[['rating']].mean().rename(columns={'rating':'avg rating'})
            df = df.merge(avg, how='left', left_on='recipe_id',right_index=True)
            return df
        def transform_df(df):
            '''Transforming nutrition to each of its own catagory,
            tags, steps, ingredients to list,
            submission date to timestamp object,
            convert types,
            and remove 'nan' to np.NaN'''
            # Convert nutrition to its own caatgory
            data = df['nutrition'].str.strip('[]').str.split(',').to_list()
            name = {0:'calories',1:'total_fat',2:'sugar',3:'sodium',4:'protein',5:'sat_fat',6:'carbs'}
            #zipped = data.apply(lambda x: list(zip(name, x)))
            new = pd.DataFrame(data).rename(columns=name)
            df = df.merge(new,how='inner',right_index=True, left_index=True)
            df = df.drop(columns=['nutrition'])
            # Convert to list
            def convert_to_list(text):
                return text.strip('[]').replace("'",'').split(', ')
            df['tags'] = df['tags'].apply(lambda x: convert_to_list(x))
            df['ingredients'] = df['ingredients'].apply(lambda x: convert_to_list(x))
            # it's correct, just some are long sentences, doesn't see "'", notice spelling
            df['steps'] = df['steps'].apply(lambda x: convert_to_list(x)) #some white space need to be hand
            # submission date to time stamp object
            format ='%Y-%m-%d'
            df['submitted'] = pd.to_datetime(df['submitted'], format=format)
            df['date'] = pd.to_datetime(df['date'],format=format)
```

```
# drop not needed & rename
            df = df.drop(columns=['id']).rename(columns={'submitted':'recipe_date','date':'review_date'})
            # Convert data type
            df[['calories','total_fat','sugar',
                'sodium','protein','sat_fat','carbs']] = df[['calories','total_fat','sugar',
                                                              'sodium','protein','sat_fat','carbs']].astype(
            df[['user_id','recipe_id','contributor_id']] = df[['user_id','recipe_id','contributor_id']].ast
            # there are 'nan' values, remove that
            for col in df.select_dtypes(include='object'):
                df[col] = df[col].apply(lambda x: np.NaN if x=='nan' else x)
            return df
In [ ]: merged = recipes.merge(interactions, how='left', left_on='id', right_on='recipe_id')
        cleaned = (merged
                   .pipe(initial)
                   .pipe(transform_df))
```

In []: display_df(cleaned)

	name	minutes	contributor_id	recipe_date	 sodium	protein	sat_fat	carbs
0	1 brownies in the world best ever	40	985201	2008-10-27	 3.0	3.0	19.0	6.0
1	1 in canada chocolate chip cookies	45	1848091	2011-04-11	 22.0	13.0	51.0	26.0
2	412 broccoli casserole	40	50969	2008-05-30	 32.0	22.0	36.0	3.0
					 	•••	•••	
234426	cookies by design sugar shortbread cookies	20	506822	2008-04-15	 4.0	4.0	11.0	6.0
234427	cookies by design sugar shortbread cookies	20	506822	2008-04-15	 4.0	4.0	11.0	6.0
234428	cookies by design sugar shortbread cookies	20	506822	2008-04-15	 4.0	4.0	11.0	6.0

234429 rows × 23 columns

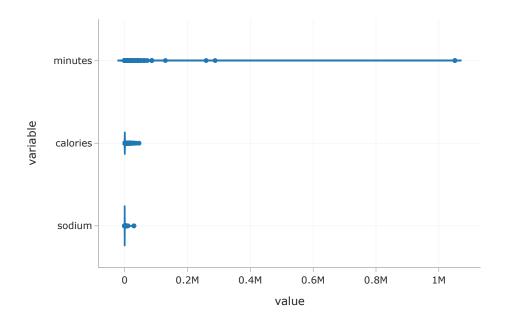
Now this code would be used later on when we need to groupby using the recipe id column or the user id column for different purposes. The handling for different columns are also defined as below, which is different according to waht we need the columns are for later on in the modeling process.

```
In [ ]: def group_recipe(df):
            func = lambda x: list(x)
           'ingredients':func, 'user_id':func, 'contributor_id':func,
'review_date':func, 'review':func, 'recipe_date':func,
                       'tags':lambda x: list(chain.from_iterable(x))}
           grouped = df.groupby('recipe id').agg(check dict)
           #grouped['rating'] = grouped['rating'].astype(int)
           return grouped
        def group_user(df):
            '''function for grouping by unique user_id and concating all steps/names/tags of recipe and av\epsilon
```

Univariate & Bivariate Analysis

Okay, after data cleaning, let's draw some graph to see what kind of data we are dealing with

```
In []: px.violin(cleaned, x=['sodium', 'calories', 'minutes'])
```



In []: px.violin(cleaned, x='rating', title='rating univariate distribution')

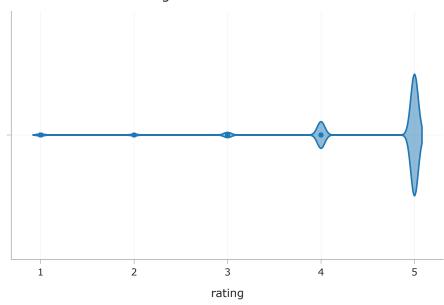
Looks like that our data have a lot of outliers! we might want to write a function to deal with that. Here we are writing the function outlier, which will be used quite often later on.

```
In []:
    def outlier(df):
        '''take care of outliers in the data frame'''
        # Remove outlier in graph dierctly

    check = ['minutes', 'n_steps', 'n_ingredients', 'calories', 'total_fat', 'sugar', 'sodium', 'pr
    for col in check:#df.select_dtypes(include='number'):
        q_low = df[col].quantile(0.01)
        #print(q_low)
        q_hi = df[col].quantile(0.99)
        #print(q_hi)
        df = df[(df[col]<q_hi) & (df[col]>q_low)]

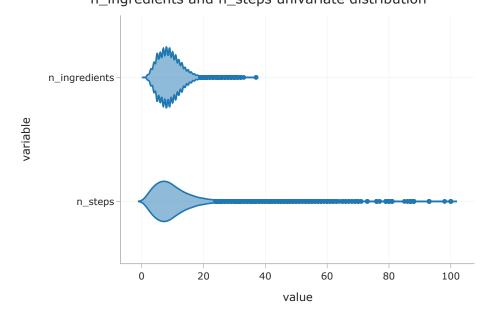
    return df #same name so update df
```

rating univariate distribution



Looks like the data are kind of **imbalanced** in rating (at this point, we thought that this wouldn't effect our modle too much, but it turns out later to be one of the main challenge that we need to deal with during the moeling phase)

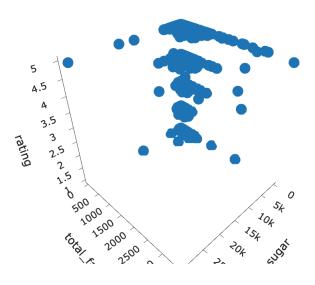
In []: px.violin(cleaned, x=['n_steps', 'n_ingredients'], title='n_ingredients and n_steps univariate dist n_ingredients and n_steps univariate distribution

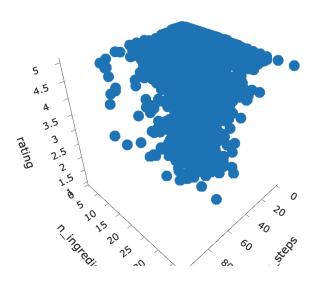


Seems like there is a **threshold point** for $n_ingredients$ and n_steps , this will be utilized later in our **feature engineering** section

In []: px.scatter_3d(cleaned, x='sugar', y='total_fat', z='rating', title='calories, total_fat, and rating

calories, total_fat, and rating correlations





Seems like there is some sort of relationships between <code>n_steps</code> , <code>n_ingredients</code> , and the <code>rating</code> column. However, this relationship doesn't seem to be that exact. In a later section we might use this idea.

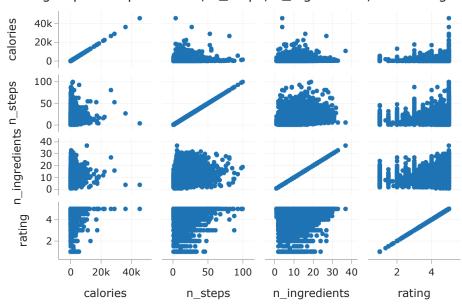
It also seems like more sugar and more total_fat (transformed from nutrition) seems to be related to higher rating! This is quite suprising!

Aggregated Analysis

Now we can first use the groupby function that we have implemented to look at some aggregated data first before using it for the next few sections

```
In [ ]: recipe_group = cleaned.pipe(group_recipe)
In [ ]: px.scatter_matrix(recipe_group, dimensions=['calories','n_steps','n_ingredients','rating'], title='
```

grouped recipe calories, n steps, n ingredients, and rating

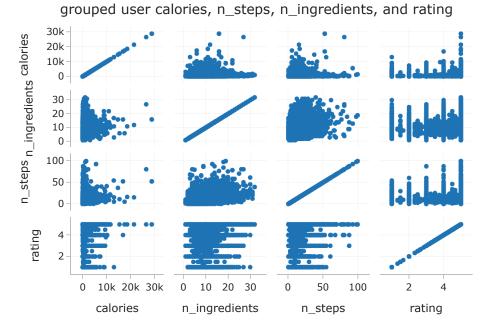


Looking at the right column of graph, it seems like the previous relationships taht we observed in no aggregation data is still preserved in the aggregated version where higher calories seems to be correlated to higher rating and n_ingredients and n_steps seems to have some relationships with rating as well.

In []: user_group = cleaned.pipe(group_user)

/var/folders/yt/5gdjwln55x9_stgx851x0yb80000gn/T/ipykernel_53177/2735721666.py:20: FutureWarning: Indexing with multiple keys (implicitly converted to a tuple of keys) will be deprecated, use a list instead.

In []: px.scatter_matrix(user_group, dimensions=['calories','n_ingredients','n_steps','rating'], title='gr



When aggregating by user, something interesting appears, it seems like that rating column is not so much correlated with teh n_steps and n_ingrredients column though it is still quite correlated with the calories column. Though we will not be working with this version of the aggregated data frame firectly when we are making our predictive model, this ideas may be taken into considerations when choosing features.

Textual Features

We actually made more edas and feature engineering with **textual features**, but we will introduce those later in the section as it is much more relevant to our modeling process. For now, we will show some technique with TF-IDF that we will use later on in this project by checking the top 5 **most important** words in each of the rows (recipe_id) in the **original cleaned** data frame filtered by getting only the **5 rating recipes**(note, recipe_id is not unique here).

• We will probably not directly use this approach here as it runs really slow! But we may use a similar approach that have a better runtime complexity!

```
In []: from sklearn.feature_extraction.text import TfidfVectorizer

In []: # df = cleaned[cleaned['rating']==5]
    # lst = df['description'].explode().astype(str)
    # count = TfidfVectorizer()
    # count.fit(lst.values)

# tfidf = pd.DataFrame(count.transform(lst.values).toarray(),
    # columns=count.get_feature_names_out())

In []: # def top_tfidf(row):
    # return ', '.join(row.index[row.argsort()][-5:])

# keywords = tfidf.apply(top_tfidf, axis=1)
# keywords = pd.concat([df.reset_index()['recipe_id'], keywords], axis=1)
# key = keywords.set_index('recipe_id')
# key
```

For runtime complexity, we use a picture here for the outout of the code above:



Step 3: Assessment of Missingness

There are data missing! Why is that happening?

We are specifically working with the version of the data set that have been grouped by with <code>recipe_id</code> to check the missingness, each <code>recipe_id</code> in this case would be unique. We can start with checking which column is missing. For the easiness of graphing, we will first slice out the outliers in each of the numerical columns using <code>outlier</code> function, which slices out ouliers that's out of the 99th percentile of the dataset

```
In []: missed = pd.DataFrame(df.isna().sum())
    missed[missed[0]!=0]
```

```
0ut[]: 0

avg_rating 1679

rating 1679

description 48
```

NMAR Analysis

However, on the other hand, the rating column seems to be **Not Missing At Random (NMAR)** because from what the website is showing, some people just didn't give rating, so the rating itself doesn't exist during the data collection process, so it makes sense for it to be null. We manually added <code>np.NaN</code> into the data set where previously it was filled a zero in the data set. Since <code>avg_rating</code> is calculated from using the <code>rating</code> column, <code>avg_rating</code> would then be **Missing At Random (MAR)** dependent on <code>rating</code>.

One interesting one to analyze is description, because it is hard to say directly how it may be correlated to any other columns in this data set, we suspect it to be MAR, but we will prove it to be MAR in the next section.

MAR Analysis

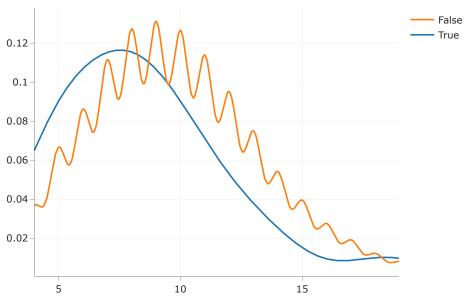
Decision Rule for description

Let's assume that the missingess of description column is related to the col column for continuous columns, wouldn't depend on discrete columns.

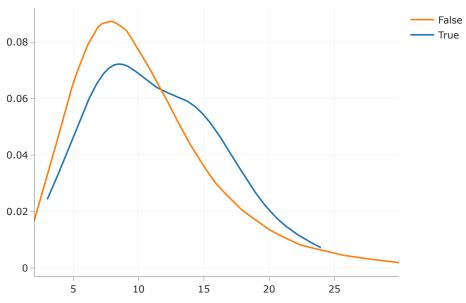
The below functions are used for conducting graphing for checking potential MAR columns and also for conducting permutation testing

```
In [ ]: def create_kde_plotly(df, group_col, group1, group2, vals_col, title=''):
            '''Create the kde plot for checking column potential dependencies'''
            fig = ff.create distplot(
                hist_data=[df.loc[df[group_col] == group1, vals_col], df.loc[df[group_col] == group2, vals_
                group_labels=[group1, group2],
                show_rug=False, show_hist=False
            return fig.update_layout(title=title)
        def mar_check_continuous(df,miss_col, dep_col):
            '''Full checking mar by simulating mar data then graphing it,
            miss_col must be catagorical and dep_col must be continuous'''
            missing = df[miss_col].isna()
            df missing = df.assign(mar missing = missing)[['mar missing', dep col]]
            fig = create_kde_plotly(df_missing, 'mar_missing', True, False, dep_col, title=f'MAR Graph of {
            return fig.show()
In [ ]: def permutation_ks(df, miss_col, dep_col, rep):
            '''conduct permutation testing for testing mar in data frame '''
            def permutation_test(df, rep, dep_col):
                '''test_statistics is the KS statistics'''
                # line of missing of description that may base on dep_col?
                observe = ks_2samp(df_missing.query('mar_missing')[dep_col],
                                   df_missing.query('not mar_missing')[dep_col]).statistic
                # making a distrbution where missing of description does not depend on dep_col
                n_repetitions = rep
                null = []
```

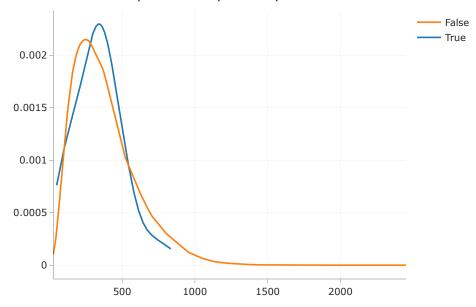
MAR Graph of description Dependent on n_ingredients







MAR Graph of description Dependent on calories



description seems to also depend on n_ingredients. This is a very interesting graph because looks like the graph **shape** is quite different with the **mean** the same, instead of using permutation test statistics that involves **mean** we use **K-S statistics** insteadd (we have also down a test using differences in mean as well, which fail to identify any results).

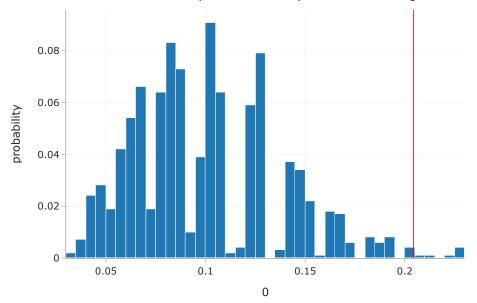
Permutation Testing Using K-S Statistics

Now we want to perform permutation testing with each of the continuous variable within the data set (assuming that the missingness of description depends on them) and plot the distribution

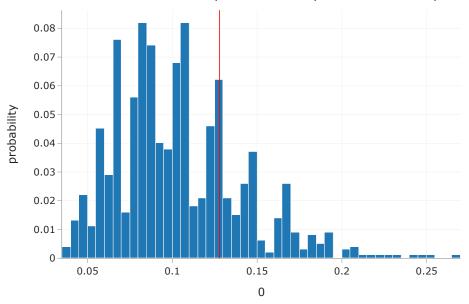
We decide to use a testing threshold of $p=0.05\,$

```
In []: for col in ['n_ingredients','n_steps','calories']: #df.drop(columns=['avg_rating','rating']).select
    permutation_ks(df, 'description', col, 1000)
```

5 Distribution for Null description_col is dependent on n_ingredients_c

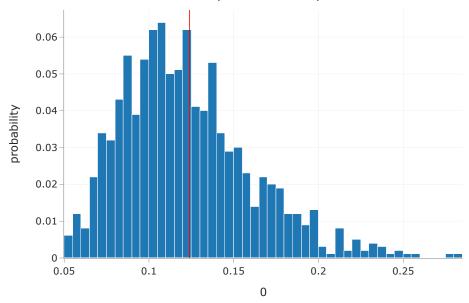


p_value is 0.234 KS Distribution for Null description_col is dependent on n_steps_col



p_value is 0.422

KS Distribution for Null description_col is dependent on calories_col



From what the plot have suggest, it seems like missingess for description is related to n_ingredients and it seems like missingness in description is not related to calories or n steps

Step 4: Hypothesis Testing

For this section, we will be working with the same data frame that was used in the missingness mechanism section, so a data frame that is grouped by recipe_id.

Since we want to do certain textual feature analysis for our predictive model, we were wondering whether TF-IDF of the description columns would actually play a role in determining the rating of an recipe. This can be deemed as a mini-warmup for our modeling procedure later on.

Term Frequency Inverse Document Frequency

TF-IDF is a very naive but common and well performing technique that people use to understand textual features. It essentially measures the **how important** an word t is for an sentence in comparison with all sentences in the document. The TF-IDF Formula is a as follows:

$$\begin{split} \text{tfidf}(t,d) &= \text{tf}(t,d) \cdot \text{idf}(t) \\ &= \frac{\text{$/\#$ of occurrences of t in d}}{\text{total $/\#$ of words in d}} \cdot \log \bigg(\frac{\text{total $/\#$ of documents}}{\text{$/\#$ of documents in which t appears}} \bigg) \end{split}$$

We will be using TfidfVectorizer to help our calculation

```
In [ ]: # import here first as it is usef for computing TF-IDF
from sklearn.feature_extraction.text import TfidfVectorizer
```

In here we are just splitting the data frame into high_score and low_score

```
In []: df = df[['name', 'description', 'tags', 'steps', 'ingredients', 'contributor_id', 'rating']] # avg_rating
    df_high = df[df['rating']>=4]
    df_low = df[df['rating']<4]

lst_high = df_high['description'].explode().astype(str)
lst_low = df_low['description'].explode().astype(str)</pre>
```

In this step we are first using the TfidfVectorizer from sk learn to compute the TF-IDF table

Differences in Max for TF-IDF

We want to see whether the distibution of high_rated recipes and the distribution of low_rated recipes actually come from the same distribution. Thus, we will be performing a **permutation test** here with the following hypothesis:

- **Null hypothesis**: There **are no** differences in the distribution for the **high_rated** recipes and low_rated` recipes.
- Alternative hypothesis: There are differences in the distribution for the high_rated recipes and low_rated` recipes.

We decide to use a testing threshold of p=0.05

As for the test statistics, we actually have many options, but they all circles around the differences of something:

- Using sum -> longer sentences have greater sum
- Using mean -> very easy to be influenced by outlier
- Using partial-mean -> get the most essence part of the sentence, however, complexity too high because of the sorting
- Using max -> most important one word's TF-IDF

With all these considerations, we pick our test statistics to be differences in max of TF-IDF for each sentence

This section provide a solid prove of why we are using TF-IDF as a feature for our predictive model!

```
In []: tfidf_max_high = high_tfidf.max(axis=1)
    tfidf_max_low = low_tfidf.max(axis=1)

max_high = df_high.reset_index().assign(tfidf = tfidf_max_high, good=True)
    max_low = df_low.reset_index().assign(tfidf = tfidf_max_low, good=False)

big_df = pd.concat([max_high, max_low], axis=0)
big_df
```

Out[]:	recipe_id		name	description	tags		contributor_id	rating	tfidf	good
	0	275030.0	paula deen s caramel apple cheesecake	thank you paula deen! hubby just happened to	[60-minutes- or-less, time- to-make, course, pre		[666723, 666723, 666723, 666723, 666723, 66672	5.0	0.28	True
	1	275033.0	penne with bacon spinach mushrooms	from woman's day magazine.	[bacon, 30- minutes-or- less, time-to- make, cour		[166642]	5.0	0.72	True
	2	275036.0	easy weeknight corn	i threw some things together in a dutch oven a	[15-minutes- or-less, time- to-make, course, mai		[590640, 590640]	5.0	0.33	True
	•••				•••					
	3642	535783.0	cheesesteak stuffed onion rings	surprise your family and friends with an onion	[60-minutes- or-less, time- to-make, main-ingred		[33186, 33186]	3.0	0.36	False
	3643	536688.0	coco oatmeal honey cookies	the fiber-rich cookies are good for snacking.h	[30-minutes- or-less, time- to-make, course, pre	•••	[2002170767, 2002170767]	3.0	0.37	False
	3644	536843.0	sheet pan turkey caprese meatballs with rosema	description: try these turkey caprese meatball	[60-minutes- or-less, time- to-make, course, mai	•••	[2001112113, 2001112113]	3.0	0.36	False

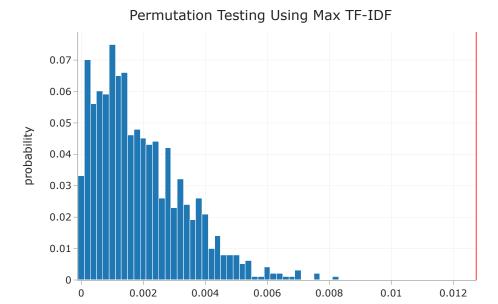
54873 rows × 10 columns

Permutation Testing

```
In []: observe = big_df.groupby('good')['tfidf'].mean().diff().abs().iloc[-1]

# making a distrbution where missing of description does not depend on dep_col
n_repetitions = 1000
null = []
for _ in range(n_repetitions):
    with_shuffled = big_df.assign(shuffle = np.random.permutation(big_df['good']))
    difference = with_shuffled.groupby('shuffle')['tfidf'].mean().diff().abs().iloc[-1]
    null.append(difference)

fig = px.histogram(pd.DataFrame(null), x=0, histnorm='probability', title=f'Permutation Testing Usi
fig.add_vline(x=observe, line_color='red', line_width=1, opacity=1)
```



0

The result is significant! We reject the null hypothesis! There is a difference in the distribution for high_rated recipes and low rated recipes.

Step 5: Framing a Prediction Problem

From the previous section we have learned that Recipe's Max TF-IDF distribution is different for high_rated recipe than low_rated recipe, so now we want to go a step further: we want to predict rating as a classfication problem to demonstrate user preference and as a potential prior to recommander system

Specifically, we want to predict rating (5 catagories) in the original data frame to demonstarte understanding of user preference. In this section we will be using the original big DataFrame for predicting rating.

Step 6: Baseline Model

Just to keep everything clear, we recalled all the cleaning function here and some neccessary extraction performed

```
In [ ]: # for modeling transformation
        from sklearn.preprocessing import FunctionTransformer, OneHotEncoder, Binarizer, RobustScaler
        from sklearn.base import BaseEstimator, TransformerMixin
        from sklearn.pipeline import Pipeline
        from sklearn.compose import ColumnTransformer
        from sklearn.feature_extraction.text import CountVectorizer
        from sklearn.feature_extraction.text import TfidfVectorizer
        from sklearn.decomposition import PCA
        # for modeling hyperparameter tuning
        from sklearn.model_selection import train_test_split
        from sklearn.model_selection import GridSearchCV, RandomizedSearchCV
        from sklearn.ensemble import RandomForestClassifier
        from sklearn.dummy import DummyClassifier
        # for modeling evaluation
        from sklearn.metrics import ConfusionMatrixDisplay, precision_recall_fscore_support
        from sklearn import metrics
        from sklearn.metrics import classification_report
        from sklearn.metrics import roc_auc_score
```

Out[]:		n_ingredients	minutes	n_steps	description	•••	recipe_date	review	is_good	is_low
	0	9	40	10	these are the most; chocolatey, moist, rich, d	•••	2008-10-27	These were pretty good, but took forever to ba	False	False
	1	11	45	12	this is the recipe that we use at my school ca		2011-04-11	Originally I was gonna cut the recipe in half	True	False
	2	9	40	6	since there are already 411 recipes for brocco		2008-05-30	This was one of the best broccoli casseroles t	True	False
	•••	•••	•••	•••				•••	•••	
	234426	7	20	5	i've heard of the 'cookies by design' company,		2008-04-15	This recipe tastes nothing like the Cookies by	False	True
	234427	7	20	5	i've heard of the 'cookies by design' company,		2008-04-15	yummy cookies, i love this recipe me and my sm	True	False
	234428	7	20	5	i've heard of the 'cookies by design' company,		2008-04-15	I work at a Cookies By Design and can say this	False	False

154763 rows × 15 columns

Notice that in here we did create a extra feature of <code>is_low</code> and <code>is_good</code>, which will be use for later. We have conider the problem of ptential **data leakage**. However, this is prior to train/val/test split and the test data (not being used for fit) would not have such problem.

Handling Missing Data

- 1. It have been shwon earlier that the missingness of the rating columns seems to be **NMAR**, so it is not dependent on the column but rather depending on itself. Thus, the naive approach taht we will be imputing the ratings through **random imputation**. However, because of the high imbalance nature of the data set, this may cause more rating of 5 to come up.
 - Regarding this issue, we ran the model on both imupting randomly and also on dropping the missing data
 directly for the rating column (second choise make sure that the target column is not randomly imputed,
 this may cause error)
 - After experimentation, drpping the missing rating directly results in both a training/validation and testing accuracy
- 2. For the missingness in description , we make sure that the distribution of the data is the same by not dropping it but rather imputing it with simple white space. It is true that the description column missgness

is MAR, but it would be quite difficult to try to impute it, so we pick an naive solution in this project

3. For missingness in name, because it is MCAR, we drop it directly.

```
In []:
    def prob_impute(s):
        s = s.copy()
        num_null = s.isna().sum()
        fill_values = np.random.choice(s.dropna(), num_null)
        s[s.isna()] = fill_values
        return s

def impute_des(s):
        s = s.copy()
        s[s.isna()] = ' '
        return s

# base_df['rating'] = prob_impute(base_df['rating'])
base_df['description'] = impute_des(base_df['description'])
base_df = base_df.dropna()
```

Train/Validate/Test Split

We are splitting the main data set into 3 components of train, validate, and test. The main data set is plit to big_train and test first with big_train being 75% of the data. Then, the big_train data set is split again into the validate and the actual train data set with 75% in the train data set again. Each set is taking the percentatge as calculated below:

```
Test: 25%Train_big: 75%Validate: 18.75%Train: 56.25%
```

```
In []: X = base_df.drop('rating', axis=1)
    y = base_df['rating']
    X_big_train, X_test, y_big_train, y_test = train_test_split(X, y, test_size=0.25, random_state=1, s
    X_train, X_val, y_train, y_val = train_test_split(X_big_train, y_big_train, test_size=0.25, random_
```

Feature Engineering & Transformations

```
In [ ]: class StdScalerByGroup(BaseEstimator, TransformerMixin):
            '''takes in two separate, fitting data may not be transforming data (training)'''
            def __init__(self):
                pass
            def fit(self, X, y=None):
                '''fit using one type of data'''
                # X might not be a pandas DataFrame (e.g. a np.array)
                df = pd.DataFrame(X)
                # Compute and store the means/standard-deviations for each column (e.g. 'c1' and 'c2'), for
                mean_group = df.groupby(df.columns[0]).mean()
                std_group = df.groupby(df.columns[0]).std()
                for col in mean_group:
                    mean_group = mean_group.rename(columns={col:f'{col}_mean'})
                    std_group = std_group.rename(columns={col:f'{col}_std'})
                self.grps_ = pd.concat([mean_group,std_group],axis=1)
                return self
            def transform(self, X, y=None):
                '''may be different data'''
```

```
getattr(self, "grps_")
                except AttributeError:
                    raise RuntimeError("You must fit the transformer before tranforming the data!")
                def standardize(x, col):
                    group = x.name
                    mean = self.grps_.loc[group, f'{col}_mean']
                    std = self.grps_.loc[group, f'{col}_std']
                    norm = (x - mean) / std
                    return norm
                df = pd.DataFrame(X)
                new=pd.DataFrame()
                for col in df.columns[1:]:
                    out = df.groupby(df.columns[0])[col].transform(lambda x: standardize(x, col)) # think i
                    new = pd.concat([new, out], axis=1)
                return new.assign(group=df[df.columns[0]]).set_index('group')
In [ ]: def tag_counts(df):
            '''number of tags counted'''
            return pd.DataFrame(df['tags'].apply(lambda x: len(x)).rename('counts'))
```

Baseline Model's Pipeline

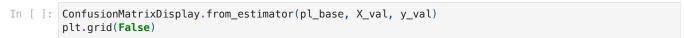
In the basic model pipeline we are working with not a great number of features:

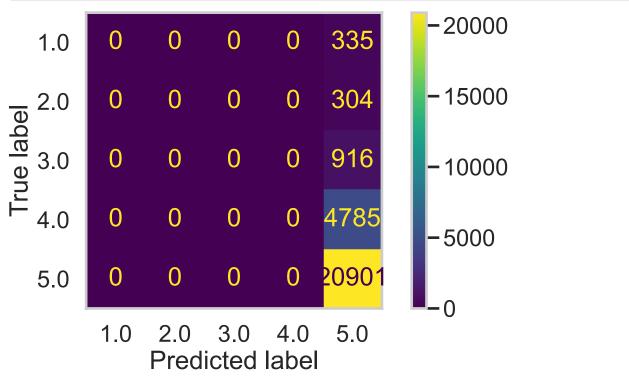
- 1. binarized n_step with threshold 25
- 2. binarized n_ingredients with threshold 20
- 3. normalized minutes with respects to binarized n_steps using the customized class StdScalerByGroup
- 4. normalized minutes with respects to binarized n_ingredients using the customized class as above
- 5. simple counts of tags column

The pipeline for the model is constituted with a simple **Random Forest** multi-class classfier with hyperparameter tuned

```
In [ ]: norm_relative = Pipeline([
            ('bi_nsteps',Binarizer(threshold=25)),
            ('norm_minutes_binary_nsteps', FunctionTransformer(lambda x: StdScalerByGroup().fit(x).transfor
        1)
        preproc_rf = ColumnTransformer(
            transformers=[
                ('bi_nsteps', Binarizer(threshold=25),['n_steps']),
                ('bi_ningredients', Binarizer(threshold=20),['n_ingredients']),
                ('norm_minutes_binary_nsteps',norm_relative,['n_steps','minutes']),
                ('norm_minutes_binary_ningredients',norm_relative,['n_ingredients','minutes']),
                ('tag_counts', FunctionTransformer(tag_counts), ['tags']),
            ],
            remainder='drop'
        pl_base = Pipeline([
            ('preprocessor', preproc_rf),
            ('rfc', RandomForestClassifier(max_depth=2,
                                           n_estimators=140,
                                            criterion='entropy'
                                            min_samples_split=2))
        ])
```

```
In [ ]: pl_base.fit(X_train, y_train)
   pl_base.score(X_val, y_val)
```





```
base_df['rating'].value_counts() / base_df.shape[0]
```

Out[]: 5.0 0.77 4.0 0.18 3.0 0.03 1.0 0.01 2.0 0.01

Name: rating, dtype: float64

Turns out the original dataset is highly imbalanced, making the model always predicting a rating of 5 not missing many of the other details. This also means that as long as the model is always predicting the rating of 5, it will get an accuracy of 77% because 77% of the rating is 5 -> accuracy doesn't entell everything!. Thus, we need a better model than this that can capture some what more feature information, more engineering is needed!

Step 7: Final Model

"A good model is the combination of model section" + feature engineering + hyperparameter tuning"*

Now with the previous baseline model's problem in mind, let's make some actual useful feature engineering, mainly we will be utilizing these features:

The previous features are carried over to this model, which includes:

- 1. binarized n_step with threshold 25, this is a result from eda
- 2. binarized n_ingredients with threshold 20, this is a result from eda
- 3. normalized minutes with respects to binarized n_steps
- 4. normalized minutes with respects to binarized n_ingredients
- 5. simple counts of tags column, showing how many tags are in each tag column

In addition, awe also added afew more features to capture the relationship we saw from EDA, which includes:

- Some numerical columns of sugar, sodium, calories, total_fat that have being standerlized using RobustScaler
- 2. Two TF-IDF that have been one hot encoded:
 - In particular, the naive approach is to use the highest TF-IDF for each of the words are extracted for each of the sentence using argmax, representing the most important words in a sentence (we are using argmax here is for considering the complexity of this model, later implementations can utilzie more words that have high TF-IDF)
 - We then construct a pool of highest TF-IDF words in the **low** rating dataset, which was originally defined as rating lower than or equal to 3 and it is stored as a boolean indicator in the is low column.
 - Finally, we want to see whether or not the current sentence's highest TF-IDF word is in such pool of words
 - We perform such operations with both the name column and also the description column
 - Remark: this feature improved the final model by roughly 10% accuracy, this is the detect_key_low(df) function
 - We ahve also tried to trade off some complexity with better accuracy by using the count of the 5 top
 TF-IDF words in each row (just this function runs for about 3m)
 - However, the performance didn't perform as well as argmax, whihch may be due to extra noise added
 (48% accuracy with 5 words and 50% accuracy with one word)
- 3. The recipe_dtae column have also being taken out with only the year of the recipe and then one hot encoded as well.
- 4. At last, we also used the tag column of each of the sentence to perform one hot encoding
 - We first performed one hot encoding to transform each tag to a numerical boolean representation.

 However, this makes the feature space to reahc to about 500 features, which adds too much **sparsity** to the feature space and may introduces **noises**
 - Thus we filtered out all the **irrelevant** or **low counted** tags (<1000 counts) and reduces teh feature spac to only adding 80 more features
 - At last, we conducted pca to reduce the adding feature space to just abou 10 features and this value seems to work well with the data set experimentally.
 - The tag_ohe_pca(df) function takes care of this step
- 5. Analyzing whether the review columns contain certain sentiment words in it, evaluated by the is sentiment(df) function
- 6. We have taken out irrelevant features such as the naive_bayes encoder taht we have implemented

```
In [ ]: def tag_counts(df):
            '''number of tags counted'''
            return pd.DataFrame(df['tags'].apply(lambda x: len(x)).rename('counts'))
        def detect_key_low(df):
            '''transforming description's tfidf to actual most important word in a description then compare
            def key_largest(row):
                return row.index[row.argmax()] #[row.argsort()][-5:]
            def make tfidf(series):
                lst = series.explode().astype(str).values # this may be slow
                count = TfidfVectorizer()
                return pd.DataFrame(count.transform(lst).toarray(), columns=count.get_feature_names_out())
            tfidf_low = make_tfidf(df[df['is_low']==True][df.columns[1]])
            tfidf_base = make_tfidf(df[df.columns[1]])
            keyword_all = tfidf_base.apply(key_largest, axis=1) #argmax a bit faster
            keyword_low = tfidf_low.apply(key_largest, axis=1)
            pool_low = keyword_low.unique() #.explode().unique()
            in_low = keyword_all.apply(lambda x: x in pool_low) #.apply(lambda x: sum([word in pool_low for
            return pd.DataFrame(in_low)
        def tag ohe pca(df):
```

```
'''OHE all the tag result after it have being pca dimension reduced to 50'''
    # getting all the unique one quick
    set = [j for i in df['tags'].tolist() for j in i] # explode in a time complexity efficient way
    count = CountVectorizer()
    count.fit(set).transform(set)
    my_dict = np.array(list(count.vocabulary_.keys()))
    def helper_function(list,dict):
        return np.array([i in list for i in dict])
    a = df["tags"].apply(lambda x:helper_function(x, my_dict))
    # change array of array into 2D array
    df_pca = pd.DataFrame(data = np.stack(a.to_numpy()),columns=my_dict)
    flipped = df pca.T
    filter_df = flipped[flipped.sum(axis=1)>1000].T # keep only useful tags
    # conduct PCA to reduce to just 50 dimensions
    pca = PCA(n_components=10)
    reduced = pca.fit_transform(filter_df)
    return reduced
def is_sentiment(df):
    '''For detecting sentiment words in the review column'''
    word_list = ['awful', 'fav', 'well',
             'yet', 'fantastic',
             'pretty good','dislike','hate', 'bad',
'delicious', 'wonderful',
             'great', 'but', 'good', 'next',
             'excellent', 'nice', 'bland', 'maybe',
             'loved', 'sorry', 'think', 'however', 'would',
             'perfect', 'very', 'keeper', 'liked', 'made']
    out = df['review'].apply(lambda x: word in x for word in word_list)#.sum(axis=1)
    return pd.DataFrame(out.astype(int))
```

Final Model's Pipeline

Since this is a **multi-class classifictaion** problem and the data is also highly **imbalanced**, we are also adding a **dummy** classifier that classifies uniformally at random to bench mark our modle's performances. Of course, we will also use different evaluation metrics later to demonstarte the model's performances as well, the dummy classfier is just an "easy to view" example.

```
In []: # dummy classfier with uniformally selections
dummy_clf = DummyClassifier(strategy="uniform")
dummy = dummy_clf.fit(X_train, y_train)
```

For the pipeline, we are still doing an **Homogenous Ensemble Learning** with decision tree as it have being shown to perform the best experimentally (we have tried hetergenous ensemble learning using voting/stacking with models such as SVM and logistic regression, but none of the perform as well as the simple random forest).

We balanced the dataset by using automatic balaning argumnet "balanced", we have also tried to use self customized dictionaries for assigning weights, However, this wouldn't be generalizable to unseen data as the distribution of data changes. The sk learn packages does automatic weight assigning by the following formula:

```
n_samples/(n_classes*np.bincount(y))
```

This model pipeline takes about 50 seconds to fit

```
In [ ]: norm_relative = Pipeline([
            ('bi_nsteps',Binarizer(threshold=25)),
            ('norm_minutes_binary_nsteps', FunctionTransformer(lambda x: StdScalerByGroup().fit(x).transfor
        1)
        key_ohe = Pipeline([
            ('tfidf',FunctionTransformer(detect_key_low)),
            ('key_ohe', OneHotEncoder(drop='first'))
        1)
        date_ohe = Pipeline([
            ('date_get', FunctionTransformer(lambda x: pd.DataFrame(x['recipe_date'].dt.year))),
            ('date_ohe', OneHotEncoder())
        1)
        preproc_rf = ColumnTransformer(
            transformers=[
                ('tfidf_key_ohe_description', key_ohe, ['is_low', 'description']),
                ('tfidf_key_ohe_name', key_ohe, ['is_low', 'name']),
                ('bi_nsteps', Binarizer(threshold=25),['n_steps']),
                ('bi_ningredients', Binarizer(threshold=20),['n_ingredients']),
                ('norm_minutes_binary_nsteps',norm_relative,['n_steps','minutes']),
                ('norm_minutes_binary_ningredients',norm_relative,['n_ingredients','minutes']),
                ('tag counts', FunctionTransformer(tag counts), ['tags']), # good for predict 5
                ('robust_nutrition',RobustScaler(),['sugar','sodium','calories','total_fat']),
                ('date_ohe', date_ohe,['recipe_date']), # can't be too sparse, 10 max
                ('tag_pca',FunctionTransformer(tag_ohe_pca),['tags']),
                ('is_sentiment',FunctionTransformer(is_sentiment),['review'])
            ],
            remainder='drop'
        class_weight= 'balanced' # balanced weighting automatically calculates th best weighting!
        pl_rf = Pipeline([
            ('preprocessor', preproc_rf),
            ('rfc', RandomForestClassifier(max_depth=18,
                                           n_estimators=130,
                                           criterion='entropy',
                                           min_samples_split=2,
                                           class_weight=class_weight
                                           ))
        ])
        pl_rf.fit(X_train, y_train)
```

```
Out[]: Pipeline(steps=[('preprocessor',
                          ColumnTransformer(transformers=[('tfidf_key_ohe_description',
                                                             Pipeline(steps=[('tfidf',
                                                                               FunctionTransformer(func=<funct</pre>
         ion detect_key_low at 0x1601f7280>)),
                                                                              ('key_ohe',
                                                                               OneHotEncoder(drop='first'))]),
                                                             ['is_low', 'description']),
                                                            ('tfidf_key_ohe_name',
                                                             Pipeline(steps=[('tfidf'
                                                                               FunctionTransformer(func=<funct
         ion detect_key_low at 0x...
                                                                               FunctionTransformer(func=<funct</pre>
         ion <lambda> at 0x160538dc0>)),
                                                                              ('date_ohe',
                                                                               OneHotEncoder())]),
                                                             ['recipe_date']),
                                                            ('tag_pca',
                                                             FunctionTransformer(func=<function tag ohe pca a
         t 0x1601f75e0>),
                                                             ['tags']),
                                                            ('is_sentiment',
                                                             FunctionTransformer(func=<function is_sentiment</pre>
         at 0x1601f7e50>),
                                                             ['review'])])),
                          ('rfc',
                          RandomForestClassifier(class_weight='balanced',
                                                   criterion='entropy', max_depth=18,
                                                   n_estimators=130))])
```

Hyperparameter Tunning

We have performed Grid Search and Random Search for the best parameters for teh Random Forest Classifier. However, for the complexity of running this notebook, we only tuned the model once and then turned this cell off.

```
In []: # %time
        # hyperparameters = {
        # 'rfc__max_depth': np.arange(2, 20, 2),
        # 'rfc__n_estimators': np.arange(100, 150, 10),
        # }
        # grids = GridSearchCV(pl rf,
                               n_{jobs=-1},
        #
                               param_grid=hyperparameters,
        #
                                return_train_score=False,
        #
                                cv=5
        #
        # grids = RandomizedSearchCV(pl rf,
                                      param distributions=hyperparameters,
                                     n_{jobs=-1}
        #
        #
                                      return train score=False,
        #
                                      cv=5
        # grids.fit(X_train, y_train)
        # grids.fit(X train, y train)
        # grids.best_params_
```

Model Evaluation

We will be conducting some simple evaluation with the model in this section with confusion matrix just to see the basic performance of the model. A more detaile performance evaluation would be conducted in the **Test Data Evaluation** section.

To really understand what we are evaluating, we need to first understand what metrics matters to us:

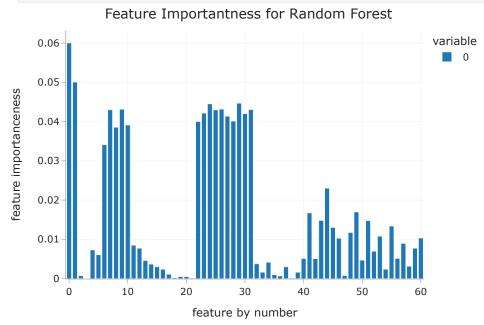
Example:

- Precision for 5: Out of all 5 we predicted, how many are actually 5
- Recall for 5: Out of all actual 5, how many did we get right

We care about getting a correct rating for recommandation, we care about finding **Recall** but still considering precision, accuracy, F1 scores

Feature Importantness Analysis

```
In []: feature = pd.DataFrame(pl_rf.named_steps['rfc'].feature_importances_)
    fig = px.bar(feature, title='Feature Importantness for Random Forest', labels={'value':'feature importantness for Random Forest', l
```

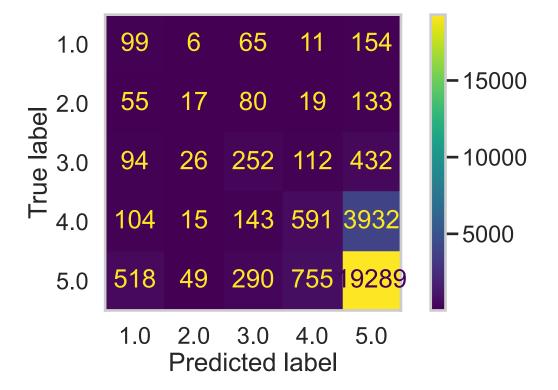


We have 60 features in our model with feature 0 and feature 1 having the most effect! these are the 2 argmax TF-IDF encoder that we have implemented, this is consistent with ou previous **permutation testing** that shows the TF-IDF distribution for high_rated and low_rated recipes are different distributions.

Other than that, the second highest feature importantness is teh forth feature to the 11th feature and 22th feature to 31th feature. These correspond to the tag_pca column!

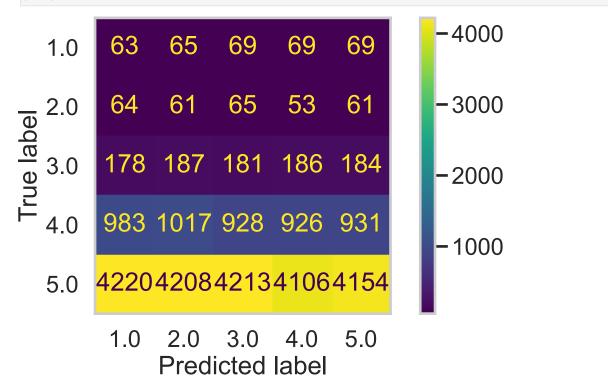
Confusion matrix for random forest classifier

```
In [ ]: ConfusionMatrixDisplay.from_estimator(pl_rf, X_val, y_val)
plt.grid(False)
```



Confusion matrix for dummy classifier

In []: ConfusionMatrixDisplay.from_estimator(dummy, X_val, y_val)
 plt.grid(False)



Accuracy for random forest classifier

In []: pl_rf.score(X_val, y_val)

Out[]: 0.7428508498219596

Accuracy for dummy classifier

In []: dummy.score(X_val, y_val)

Out[]: 0.19621159281964687

Full metrics for random forest classfier

In []: metrics_all(pl_rf, X_val, y_val)

Out[]: precision recall f1_score count 1 0.30 0.11 0.16 881.0 2 0.05 80.0 113.0 0.14 3 0.26 0.29 0.28 828.0 4 0.12 0.40 0.19 1494.0 5 0.92 0.81 0.86 23925.0

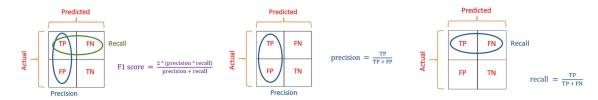
Full metrics for dummy classifier

In []: metrics_all(dummy, X_val, y_val)

Out[]: precision recall f1_score count 1 0.21 1.27e-02 0.02 5419.0 2 0.15 8.46e-03 0.02 5436.0 3 0.22 3.71e-02 0.06 5497.0 4 0.21 1.81e-01 0.19 5427.0 5 0.20 7.72e-01 0.32 5462.0

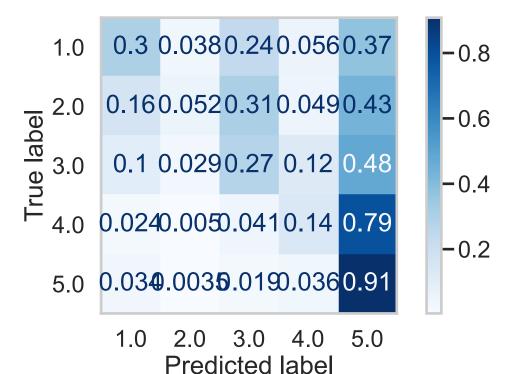
Testing for Evaluation

Recall that when we evaluate a model, we need to look at multiple metrics to really understand how our model is performing. From the baseline model, we know that **accuracy can really lie!** We can borrow a image from here to demonstrate what we are evaluating really quickly



Let's look at the confusion matrix again first, but this time in a percentage form.

In []: ConfusionMatrixDisplay.from_estimator(pl_rf, X_test, y_test, cmap=plt.cm.Blues, normalize='true')
plt.grid(False)



In []: pl_rf.score(X_test, y_test) Out[]: 0.7345888053743014 In []: metrics_all(pl_rf, X_test, y_test) Out[]: precision recall f1_score count 1 0.30 0.09 1412.0 0.14 2 0.05 200.0 0.10 0.07 3 0.28 0.25 0.26 1330.0 4 0.14 0.43 0.21 2064.0 5 0.91 0.81 0.86 31315.0

Let's formalize the test result by using the classification_report function from sk_learn

- The bottom of the table shows 2 different aspects of the prediction evaluation,
 - 1. one is macro avg or the simple average for each of teh column of evaluation metrics
 - one is weighted_avg, which re-evaluate the accuracy of our modle based on the data distribution of the data set, which provide a better representation of the model's performance given imbalanced data like this one.

In []: print(classification_report(y_test, pl_rf.predict(X_test))) precision recall f1-score support 1.0 0.10 0.30 0.15 447 2.0 0.11 0.06 0.08 405 3.0 0.25 0.27 0.26 1222 4.0 0.42 0.14 0.21 6380 27867 0.81 0.91 0.86 5.0 0.73 36321 accuracy 0.34 0.34 0.31 36321 macro avg weighted avg 0.70 0.73 0.70 36321

After the weighted_avg evaluation, it looks like our model achieves a pretty good performance, 3 of them (precision, recall, and f1 score) all being 70%! This is quite good considering we are doing a multi class classification, for comparison, we can intoduce the uniformaly dummy clasfier to make a baseline comparison.

```
In [ ]: print(classification_report(y_test, dummy.predict(X_test)))
                     precision
                                   recall f1-score
                                                      support
                1.0
                          0.01
                                     0.19
                                               0.02
                                                          447
                2.0
                          0.01
                                     0.19
                                               0.02
                                                          405
                3.0
                          0.03
                                     0.21
                                               0.06
                                                         1222
                4.0
                          0.18
                                     0.20
                                               0.19
                                                         6380
                5.0
                          0.77
                                     0.20
                                               0.32
                                                        27867
                                               0.20
                                                        36321
           accuracy
          macro avg
                          0.20
                                     0.20
                                               0.12
                                                        36321
       weighted avg
                          0.62
                                     0.20
                                               0.28
                                                        36321
```

Clearly, there is a difference in the recall and f1 score. There isn't that big of a differences in precision for the weighted avg because the number of 5 rating are plenty in the data set (77%), causing the precision for 5 to reach 77% directly.

Next, we want to also look at the ROC_AUC score or area under the receiver operating characteristic curve.

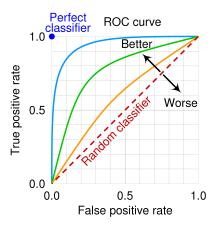
Again, like many metrics, they are originally designed for binary classfications, but we can also apply to multi-class classfications by doing ovr strategy (estimating by making grouped for comparison).

```
In [ ]: y_pred_probs = pl_rf.predict_proba(X_test)

roc_auc_score(
    y_test, y_pred_probs, multi_class="ovr", average="weighted"
)
```

Out[]: 0.7026593973261905

This is pretty good! from here we can show the curve of ROC for different performance of an classfier. Our model's performance shows that about about 70% of teh area are covered, signifying that our model performs quite well!



Step 8: Fairness Analysis

We want to evaluate whether the model is fair for treating all populations. In particular, we want to check in the scope of looking at the predictions for the vegan group and the vegetarian group. Let's first check how many of them are in the data set.

```
In [ ]: X_test['tags'].apply(lambda x: 'vegetarian' in x).sum()
```

```
Out[]: 5387
In [ ]: X_test['tags'].apply(lambda x: 'vegan' in x).sum()
Out[]: 1356
In [ ]: out = X_test.assign(prediction = pl_rf.predict(X_test))
In [ ]: is_in_tag = out['tags'].apply(lambda x: ('vegetarian' in x)|('vegan' in x))
        out = out.assign(is_in = is_in_tag)
        Let's check the grouped by mean first
In [ ]: out.groupby('is_in')['prediction'].mean()
Out[]: is_in
         False
                  4.69
         True
                  4.75
         Name: prediction, dtype: float64
        Difference Significant?
        We run a permutation test to see if the difference in accuracy is significant.
          • Null Hypothesis: The classifier's accuracy is the same for both vegan + vegetarian tags and non vegan
            + vegetarian tags, and any differences are due to chance.
          • Alternative Hypothesis: The classifier's accuracy is higher for non vegan + vegetarian tags.
          • Test statistic: Difference in accuracy (is_in minus not_in).
          • Significance level: 0.05
In [ ]: compute_accuracy = lambda x: metrics.accuracy_score(x['is_in'], x['prediction'])
        obs = out.groupby('is_in').apply(compute_accuracy).diff().iloc[-1]
        diff_in_acc = []
        for _ in range(1000):
             s = (
                 out[['is_in', 'prediction']]
                 .assign(shuffle=np.random.permutation(out['is_in']))
                 .groupby('shuffle')
                 .apply(compute_accuracy)
                 .diff()
                 .iloc[-1]
```

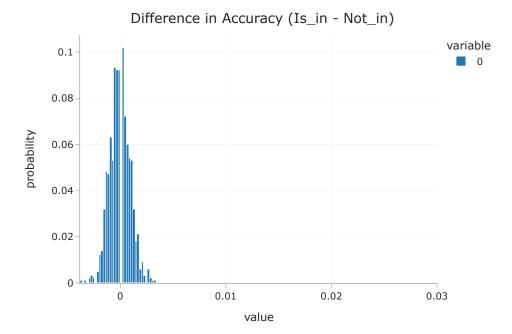
title='Difference in Accuracy (Is_in - Not_in)')

diff_in_acc.append(s)

fig.show()

fig.add_vline(x=obs, line_color='red')

In []: fig = pd.Series(diff_in_acc).plot(kind='hist', histnorm='probability',



```
In [ ]: (obs <= diff_in_acc).mean()</pre>
```

Out[]: 0.0

The result is **significant**, we reject the null hypothesis!