

Predictive modeling for house price prediction

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Abstract—This paper summarizes the background, problem, methodology and results of our analysis on predicting house price in Ames, Iowa. To make full use of statistical models and machine learning techniques we have learned from Stats 159 Reproducible and Collaborative Statistical Data Science, we participate in Kaggle Competition, "House Price: Advanced Regression Techniques". We use the Ames Housing dataset compiled by Dean De Cock for use in data science education. While the competition only emphasizes the accuracy of predicted values, this paper elaborates thorough explanations on exploratory analysis, feature engineering and statistical modeling. Furthermore, we put our effort on reproducibility of this analysis, so that the reader can reproduce the exact same result from our code.

I. INTRODUCTION

The competition sets the background of the project: Ask a home buyer to describe their dream house, and they probably do not begin with the height of the basement ceiling or the proximity to an east-west railroad. But this playground competition's dataset proves that there are a number of influential factors that affect house price aside from the number of bedrooms or a white-picket fence.

With 79 explanatory variables describing almost every aspect of residential homes in Ames, Iowa, this competition requires participants to predict the final price of each home. We therefore use the exploratory analysis and experiment different machine learning techniques to accurately predict the final sale price of each house.

II. DATA DESCRIPTION

The datasets are obtained from the Kaggle Competition website. We have access to four files:

- *data description*, which provides the official definition for fields.
- *train.csv*, which provides 1459 real observations that can be used for model construction.
- *test.csv*, which is used to fit the predictive model and create submission entry for the final sales price of 1460 observations
- *sample submission*, which provides an example of the submission file format.

The train dataset has in total 80 variables, 79 predictors and 1 target variable called *SalePrice*. We observe both categorical predictors, such as *FireplaceQu*, *GarageCond* and *MasVnrType* as well as numerical predictors, such as *PoolArea*, *EnclosedPorch* and *YrSold*. Since we can potentially create a lot of different new variables, our goal is to understand the relationship between *SalePrice* and these

predictors with statistical fitting procedures that minimizes Mean Square Error.

III. EXPLORATORY DATA ANALYSIS

In order to choose the model to accurately predict the housing price, we first need to understand the provided dataset by conducting exploratory data analysis (aka EDA). Separating categorical predictors and numerical predictors, we can explore in two perspectives: 1) the distributions of variables, and 2) the relationships between explanatory variables and response variable.

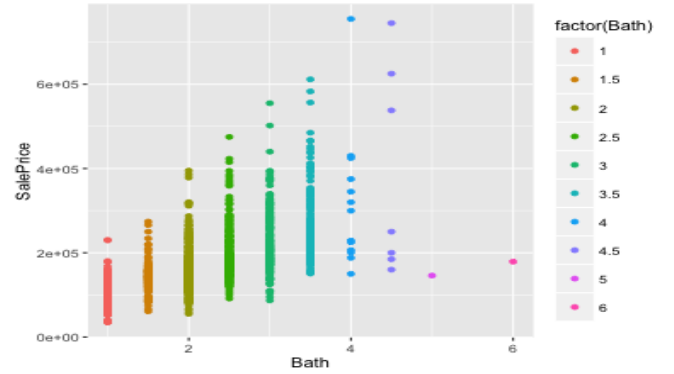


Fig. 1. Exploratory Data Analysis - Relationship Between Bath and SalePrice

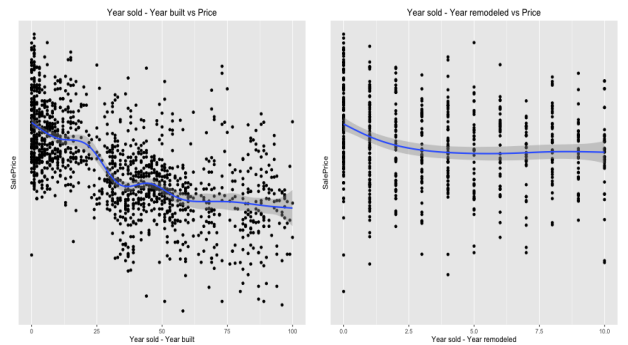


Fig. 2. Exploratory Data Analysis - scatter plot of year sold - year built vs. sale price as well as year sold - year remodeled vs sale price

Figure 1 is an example of explanatory data analysis, which presents the relationship between explanatory variable bath and the response variable SalePrice. Figure 2 is a more complicated yet informative plot, which shows the relationship between sales price and the difference of year sold and year built, namely the age of house after being built,

as well as the difference of year sold and year remodeled, namely the age of house after being remodeled.

Some interesting observations we made include: 1) While some variables are equally distributed in their own segments, some variables are skewed in certain directions (either to the left or to the right), which means some potential data transformation can be made to improve the predictive model; 2) We observe some linear relationship between variables, which can be used in the future model selection; and 3) While some variables have strong linear relationship with the response variable SalePrice, other variables do not display the similar pattern. This might encourage us to remove unnecessary predictors from the dataset in terms of model fitting and selecting.

IV. METHODOLOGY

The goal of this analysis is to accurately predict the final price of each home. Therefore, we frame this problem as a regression problem, and decide to use the L2 loss function [1] which is often used in regression problem. Taking this objective into account, we preprocess original dataset so that regression models can work well. Furthermore, we extract more features by involving feature engineering. Finally, we fit two shrinkage models and two ensemble models. The details are explained in the following subsections.

A. Evaluation and objective loss function

We specifically use root mean squared logarithmic error [2], which makes more sense in our problem setting because errors in predicting expensive houses and cheap houses should affect the result equally. The following is the formula of RMSLE.

$$\epsilon = \sqrt{\frac{1}{n} \sum_{i=1}^n (\log(p_i + 1) - \log(a_i + 1))^2}$$

Since L2 loss function minimizes the squared differences between the estimated and existing target values [1], L2 error will be much larger in the case of outlier compared to L1 and therefore L2 loss function is highly sensitive to outliers in the dataset. So, in the preprocessing step, we eliminate outliers to remedy this issue.

B. Preprocess

According to the exploratory data analysis, we find a lot of NA values in most of predictors. Since regression models cannot handle missing data, we need to either remove or impute data using appropriate methods [3]. The data description provided by the competition host [4] indicates that some of the missing values are actually none value. In that case, we replace NA value with factor variable named None. However, there are some numerical predictors with missing values in an unsystematical manner. In that case, we impute them with mean values of predictors.

As a next step, we apply log transformations to SalePrice and other predictors related to area such as GrLivArea and LotArea. Figure 3 (left) shows an original SalePrice

distribution. It is skewed to the right. The log transformation has an effect to remedy skewness of data [5] by making original distributions of predictors to close to the normal distribution. Consequently, it helps regression model to work better. Figure 3 (right) shows the log transformed SalePrice distribution.

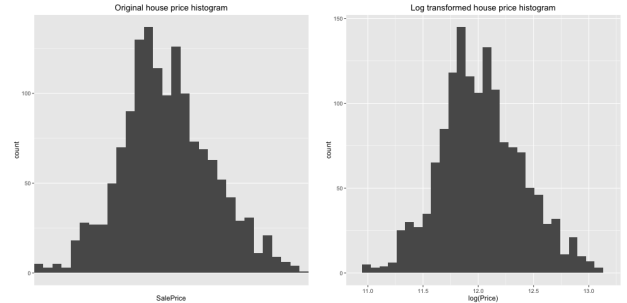


Fig. 3. Effect of Log Transformation - the distribution of original sale price and the distribution of sales price after log transformation

After the log transformation, we still notice few outliers and eliminate lowest and highest 0.1% data points. Furthermore, majority of predictors are categorical under which regression models cannot be used directly. Therefore, we apply one-hot encoding [6] to convert categorical values to numerical ones. It consequently expands features from 79 to approximately 500. The Table 1 below summarizes this procedure.

Factorization	Log Transformation	Removing Outliers
MSSubClass	SalePrice	Remove 17 points that are below 10.91511 and above SalePrice
YearBuilt	LotArea	
YrSold	GrLivArea	
MoSold		
GarageYrBlt		

Table 1: Summary: Data Preprocess and Variable Transformation

C. Data preparation

Before fitting the model, we first split dataset into train and test. We could have a separate validation set. However, R library caret has a built-in cross validation as a generic interface. So it automatically takes care of cross validation. We use train data to train and tune our models using 5-fold cross validation, and later compare RMSLE using hold-out test data [7].

D. Featuring engineering

Considering the complexity of the problem as well as the number of observations and predictors, we assume that the success of this analysis is largely dependent on informative, feature engineered predictors that can reveal the subtle relationship to our target variable. Given the small size of dataset with 1460 observations, we conclude that feature learning, which is a set of techniques that learn a feature: a transformation of raw data input to a representation that can be effectively exploited in machine learning tasks [8], is

not a feasible option because feature learning often involves very complicated models with multiple layers, which tends to cause an overfitting issue when dataset is small [9].

With this observation, we therefore focus more on manual feature engineering [10]. This process is a important stepping-stone in that it helps reveal significant predictors that are previously not represented well in original dataset. By explicitly designing what the input x 's should be, our predictive models can solve a problem easily.

E. Model description and hyper-parameter tuning

While training each model, we need to find optimal paramters for each model. In order to effectively select hyper-parameters, we use 5-fold cross-validation. For lasso and ridge, lambda is the tuning parameter. It determines how much we will penalize models for high weights on predictors. If lambda is high, it penalizes models more and ends up generating sparse models. This kind of models is called shrinkage method because they shrinken weights or even remove predictors by penalizing models. These models are especially good options when there are many predictors. By penalizing or removing unnecessary predictors, they provide more interpretable results. Thus, they are often utilized in genomic and pharametical analysis.

F. Modeling

We utilize both shrinkage regression models and ensemble models. Practitioners often favor ensemble models [11] due to their conveniences. Ensemble models such as Random Forest [12], which uses the averaged result from the randomly grown decision trees such as CART [7], often work well with unscaled, missing data and are used for both classification and regression problems. Also, since our dataset contains a hug number of predictors, shrinkage methods such Lasso and Ridge regressions [7], which penalize predictors by shrinking their weights, can be highly effective. Furthermore, we utilize a dimension reduction technique called PCA[7] in order to compress information into lower dimension. The results of modeling will be further explained in the following section in detail.

G. Model comparison

As mentioned on in Evaluation section, we use RMSE to compare models and select the best model. Although RMSE does not provide an absolute means of model accuracy, it provides a relative measure to compare models. Thus, we finalize our model with the lowest RMSE. In summary, the following is the the procedure for each model.

- 1) Split the data into train and test, 80% and 20% repeatedly.
- 2) Train a model using train data with 5-fold cross-validation.
- 3) Pick the optimal hyper-parameters.
- 4) Predict balance using the model with the optimal parameters.
- 5) Calculate Mean Square Error.
- 6) Record both Mean Square Error and coefficients.

V. ANALYSIS

Due to the high dimensionality of dataset, we first experiment to decide whether to either project predictors into lower dimensional bases or select predictors using shrinkage methods. First, we try Principal component analysis which is a statistical procedure that uses an orthogonal transformation to convert a set of observations of possibly correlated variables into a set of values of linearly uncorrelated variables called principal components [13]. Since our one-hot encoded dataset has a lot of predictors that have near zero variances, we first need to remove near zero variances. This is because PCA does not work well if predictors are consist of near zero variances among observations.

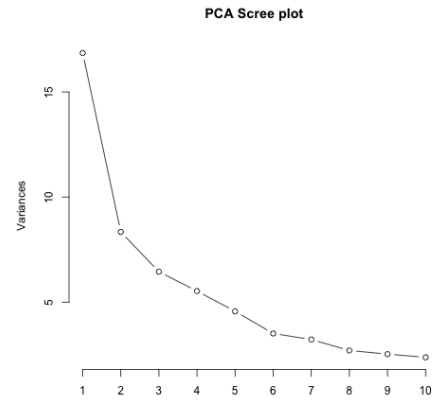


Fig. 4. PCA scree plot for each principal component

After removing near zero variance 519 to 128. This indicates that a great number of predictors have apporoximately identical across observations. Figure 4 shows a PCA scree plot for each principal component. It indicates that first few principal components effectively explain the variances of data, and overall graph exponentially decays. Th cumulative Proportion in indicates that first 10 principal components and 61 principal components can explain approximately 44% and 90% of variances in dataset respectively. It means that if we decide to reduce dimensionality at the expense of a bit little of prediction accuracy, we could use 61 principal components which are approximately 1/8 of total predictors. However, since our goal is to increase prediction accuracy as much as possible, we decide not to use PCA at the end.

Furthermore, we try to fit both lasso and regression and tune lambda values using 5-fold cross validation and then examine coefficients. Figure 5 shows respectively the Mean Square Error for corresponding lambda values for both models. The Figure suggests that MSE decreases as $\log(\lambda)$ increase up to $\log \lambda$ equals -5 and -1.15 respectively. Based on these results, we decide optimal lambda for both model.

We also examine coefficients of lasso regression. Figure 6 indicates that most of weights for corresponding predictors become zeros, which effectively eliminates a great portion of predictors. After elimination, only 78 predictors are left. We

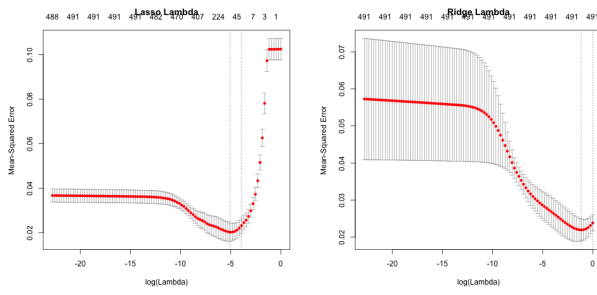


Fig. 5. MSE values for Lambda Values - Lasso Regression (left) and Ridge Regression (right)

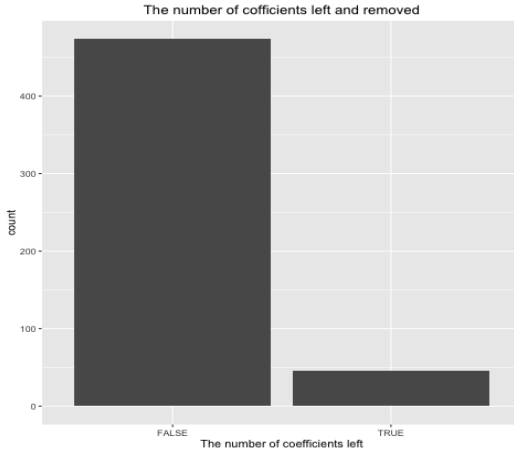


Fig. 6. Number of Coefficients - Lasso Regression

plot top 10 coefficients for both lasso and ridge to investigate how much each coefficient is associated with target variable.

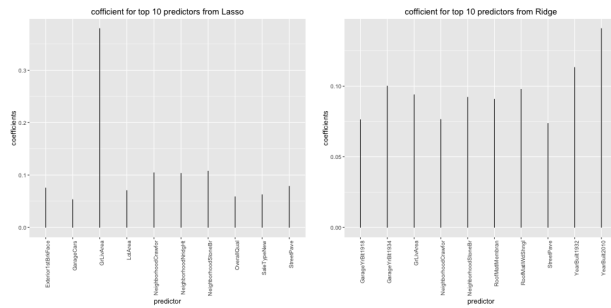


Fig. 7. Top 10 Coefficients - Lasso Regression (left) and Ridge Regression (right)

Figure 7 shows the top 10 coefficients from both models. It is noteworthy that GrivArea has the highest coefficient in Lasso and YearBuilt2010 has the highest coefficient in Ridge. Both make sense because the area and built year are important aspects when it comes to making a decision about purchasing house. Both models indicate that GrLiArea, NeighborhoodCrawfor and NeighborhoodStoneBr belong to top 10 highest coefficients and are highly associated with house price. Furthermore, we try to figure out feature importance using Gradient boosting machine. Feature importance is automatically measured as GBM grows its tree while min-

imizing entropy. Figure 8 below shows that overall quality has the highest feature importance

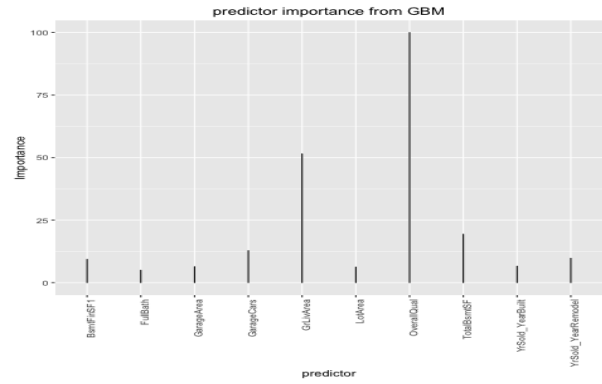


Fig. 8. Model GBM Predictor Importance

VI. RESULTS

As a result, Figure 9 shows model comparison between true price and predicted price.

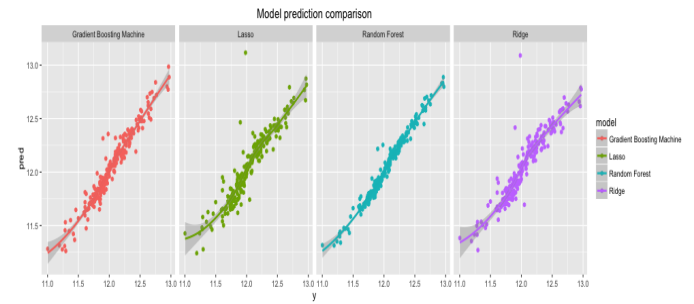


Fig. 9. Model Comparison between True Price and Predicted Price

Four models are fairly accurate and most of data points are located on a diagonal line, which indicates the strong linear relationship between true price and predicted. Especially, Random Forest is especially fitted well among these four.

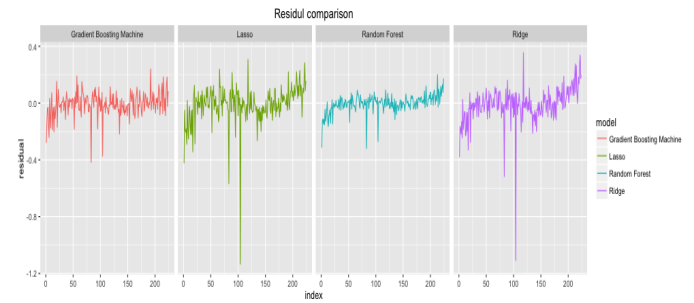


Fig. 10. Model Comparison - Residual Plots of Four Models

Figure 10 shows the residual plots for four models. The residual is the difference between real house price and predicted price from models. We can see from Figure 10 that all models overestimate the price for cheaper house and underestimate the price for expensive house. This phenomenon is not surprising because we have few data points

in cheapest and most expensive houses. Thus, the models incur a high bias in these end zones. This can be alleviated if we gather more data if possible. Compared to Lasso and Ridge, Gradient boosting machine and Random Forest are more stable. Both Lasso and Ridge have huge errors in the middle of graphs.

Lastly, Table 2 as below shows RMSLE for each model, which is measured from hold-out dataset. It indicates that Random Forest predicts target variable the best.

	RMSLE	model
1	0.06	RandomForest
2	0.08	GBM
3	0.13	Ridge
4	0.13	Lasso

TABLE 1

TABLE 2: RMSEL COMPARISON FROM FOUR MODELS

VII. CONCLUSIONS

In conclusions, while participating in the Kaggle competition - "House Price: Advanced Regression Techniques", we get a chance to dig down into real-life dataset that have complicated variables, missing values and large number of data entries. Based our analysis on the train dataset, we try to find the regression model and advanced techniques that most accurately predict the housing price, and use the exact model to predict new entries from test file. Exploring and creating visualization of data, we compare the usage of different regression models to understand the relationship between dependent variable SalePrice and 79 potential predictors. Fortunately, we ranked No.10 among all 2000 participating teams with our prediction, which not only shows the precision of our own predictive model, but also suggests room of improvement and growth.

This course gives us great opportunity to practice project reproducibility, advanced statistical model learning and team-work delegation. By delegating work to each team mate and implementing the model to generate results, we aim to maintain project reproducibility and publicity so that more people can learn from our model and benefit for future researches. If you have any questions or concerns regarding any part of our analysis, please feel free to contact the authors for further clarification.

ACKNOWLEDGMENT

The Ames Housing dataset was compiled by Dean De Cock for use in data science education. It's an incredible alternative for data scientists looking for a modernized and expanded version of the often cited Boston Housing dataset.

REFERENCES

- [1] L1 vs. L2 Loss Function from Rishy Github: <http://rishy.github.io/ml/2015/04/28/l1-vs-l2-loss/>
- [2] Root Mean Squared Logarithmic Error, <https://www.kaggle.com/wiki/RootMeanSquaredLogarithmicError>
- [3] Handbook: General principles for dealing with missing data: <https://goo.gl/G54nBx>
- [4] data-description.txt from Kaggle Competition: <https://goo.gl/XGyi7m>
- [5] Log Transformation Standard: <http://onlinestatbook.com/2/transformations/log.html>
- [6] One-hot, Wikipedia: <https://en.wikipedia.org/wiki/One-hot>
- [7] The Elements of Statistical Learning, Shrinkage methods p.61 p. 305
- [8] Y. Bengio; A. Courville; P. Vincent (2013). "Representation Learning: A Review and New Perspectives". IEEE Trans. PAMI, special issue Learning Deep Architectures. 35: 17981828. doi:10.1109/tpami.2013.50.
- [9] An Open Letter to Yann LeCun - Small Data requires Specialized Deep Learning: <https://medium.com/@ShaliniAnanda1/an-open-letter-to-yann-lecun-22b244fc0a5a#.92x0bez05>
- [10] "What is the intuitive explanation of feature engineering in machine learning? - Quora". www.quora.com. Retrieved 2015-11-11.
- [11] Ensemble learning, http://www.scholarpedia.org/article/Ensemble_learning
- [12] Random forest, <https://www.stat.berkeley.edu/~breiman/randomforest2001.pdf>
- [13] Principal component analysis: https://en.wikipedia.org/wiki/Principal_component_analysis