Solutions to STAT 300 Midterm Exam (Version II)

Problem 1.

- 1. F 2. T 3.
 - 3. F 4. T
- 5. T

- 6. T
- 7. F
- 8. F
- 9. F.
- 10. T

Problem 2.

- 1. A. 2. D.
- 3. C.
- 4. B
- 5. C

- 6. B. 7. D.
- 8. D.
- 9. A.
- 10. A.

Problem 3.

- (1) (2 pts each) (i) A
- (ii) C
- (2) (2 pts each) (i) 6.55
- (ii) 0.46
- (iii) 14.24
- (iv) F(2, 63) or $F_{2,63}$
- (v)

0.46

- (3) (2 pts each) 0.0167, because we are doing three tests simultaneously.
- (4) (2 pts each) Method I: paired t-test, Method II: sign test. The reason is that data for each subject in this design are paired (or correlated).
- (5) (1 pt, 2 pts) Interaction. When there is an interaction, we should analyze data for male and female separately.
- (6) $H_0: \frac{\mu_1 + \mu_2}{2} = \mu_3.$

Problem 4.

The data in this study can be summarized by the following 2 by 2 table

	Lab I	Lab II		Total
Pass	18	16		34
Fail	2	4		6
	20	20	1	40

(1) (2 pts each) (i) Fisher's exact test, χ^2 test. (ii) The Fisher's exact test may be more reliable here since the cell count 2 (and 4) are small (or the sample size is small).

(2) (2 pts each)
$$e_{11} = 40 * (34/40) * (20/40) = 17$$
 and $o_{11} - e_{11} = 18 - 17 = 1$.

- (3) No (since there is no randomization).
- (4) Let p be the proportion of students who like activity-based labs. The hypotheses to be tested are

$$H_0: p < 0.05$$
 vs $H_1: p > 0.5.$

Let X be the number of students in Lab I who like activity-based labs. Then, under H_0 , we have

$$X \sim Binomial(20, 0.5).$$

(1) (4 pts) The significance level is

$$\alpha = P(reject \ H_0|H_0 \ holds) = P(X \ge 14|H_0 \ holds) = \sum_{k=14}^{20} C_{20}^k 0.5^k \times 0.5^{20-k}.$$

(2) (4 pts) The power is

power =
$$P(reject\ H_0|H_1\ holds) = P(X \ge 14|p = 0.6) = \sum_{k=14}^{20} C_{20}^k 0.6^k \times 0.4^{20-k}$$
.

(3) (2 pts) Note that, under H_0 , $E(X) = np = 20 \times 0.5 = 10$ and Var(X) = np(1-p) = 5. Thus, the normal approximation for the null distribution of X is N(10, 5) (or N(0.5, 0.25) if one use $\hat{p} = X/n$ as a test statistic). (Note that here we use $N(\mu, \sigma^2)$ to denote a normal distribution. Some may also use notation $N(\mu, \sigma)$.)