CS 4504 Parallel and Distributed Computation

OpenMP

Kun Suo

Computer Science, Kennesaw State University

https://kevinsuo.github.io/

Scope of Variables



Scope

• *In serial programming*, the scope of a variable consists of those parts of a program in which the variable can be used.

```
#include <stdio.h>
int main()
{
    int i;
    for (i=1; i<=3; i++)
    {
        printf("%d\n", i);
    }
    return 0;
}</pre>
```

Scope

 In OpenMP, the scope of a variable refers to the set of threads that can access the variable in a parallel block.

```
double sum = 0.0;

# pragma omp parallel for num_threads(thread_count) \
    default(none) reduction(+:sum) private(k, factor) \
    shared(n)

for (k = 0; k < n; k++) {
    if (k % 2 == 0)
        factor = 1.0;
    else
        factor = -1.0;
        sum += factor/(2*k+1);
        ...</pre>
```

The default clause

 Let the programmer specify the scope of each variable in a block.

default (none)

 With this clause the compiler will <u>require that</u> <u>we specify the scope</u> of each variable we use in the block and that has been declared outside the block.

The default clause

```
double sum = 0.0;
pragma omp parallel for num_threads(thread_count) \
    default(none) reduction(+:sum) private(k, factor) \
    shared(n)

for (k = 0; k < n; k++) {
    if (k % 2 == 0)
        factor = 1.0;
    else
        factor = -1.0;
    sum += factor/(2*k+1);
}</pre>
```

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Scope in OpenMP

 A variable that can be accessed by all the threads in the team has shared scope.

 A variable that can only be accessed by a single thread has private scope.

 The default scope for variables declared before a parallel block is shared.

The default clause

Vairable k and factor are private;
Variable n is shared.

```
double sum = 0.0;
pragma omp parallel for num_threads(thread_count) \
    default(none) reduction(+:sum) private(k, factor) \
    shared(n)

for (k = 0; k < n; k++) {
    if (k % 2 == 0)
        factor = 1.0;
    else
        factor = -1.0;
    sum += factor/(2*k+1);
}</pre>
```

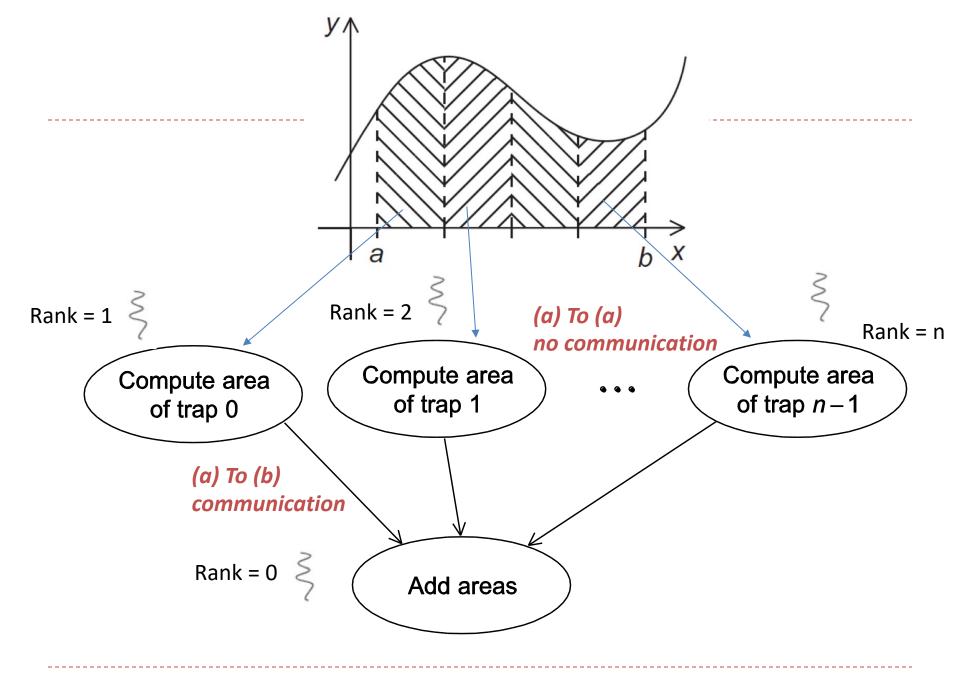


Our example

If we write the code like this...

```
global_result = 0.0;
# pragma omp parallel num_threads(thread_count)
{
# pragma omp critical
global_result += Local_trap(double a, double b, int n);
}
```

... we force the threads to execute sequentially.



Our example

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 We can avoid this problem by declaring a private variable inside the parallel block and moving the critical section after the function call.

```
global_result = 0.0;

# pragma omp parallel num_threads(thread_count {
    double my_result = 0.0; /* private */

    my_result += Local_trap(double a, double b, int n);

# pragma omp critical
    global_result += my_result;
}
Public: Serial
```

computation

ibuted Computation

A common loop is to accumulate variables

```
int sum = 0;
for (int i = 0; i < 100; i++) {
    sum += array[i];
}</pre>
```



```
int sum = 0;

#pragma omp parallel for reduction(+:sum)
for (int i = 0; i < 100; i++) {
        sum += array[i];
}</pre>
```

In the internal implementation, OpenMP provides a *private* sum variable for each thread.

When the thread exits, OpenMP adds the sum of each thread's parts to get the final result.

```
int sum = 0;

#pragma omp parallel for reduction(+:sum)
for (int i = 0; i < 100; i++) {
        sum += array[i];
}</pre>
```

```
global_result = 0.0;

# pragma omp parallel num_threads(thread_count)
{
    double my_result = 0.0; /* private */
    my_result += Local_trap(double a, double b, int n);

# pragma omp critical
    global_result += my_result;
}
```

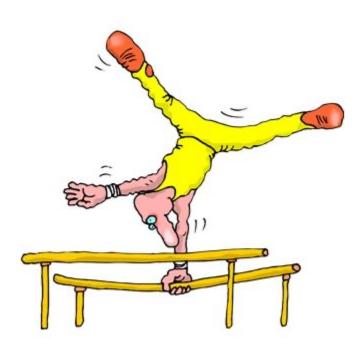
Reduction operators

```
reduction(<operator>: <variable list>)
+, *, -, &, |, ^, &&, ||
```

```
global_result = 0.0;
# pragma omp parallel num_threads(thread_count) \
    reduction(+: global_result)
global_result += Local_trap(double a, double b, int n);
```

The global_result is private for each thread and public for the master thread

The "Parallel For" Directive



Pragmas

```
#include <omp.h> 
#include <stdio.h>
                       omp.h file
#include <stdlib.h>
void Hello(void)
                                                          Return 0,1,2,3
        int my_thread_ID = omp_get_thread_num();
        int thread_count = omp_get_num_threads();
        printf( "Hello from thread %d of %d\n", my_thread_ID , thread_count );
int main (int argc, char *argv[]) {
#pragma omp parallel
        Hello();
        return 0;
                            Thread number is
                        decided by core number
```

Parallel for

 Forks a team of threads to execute the following structured block.

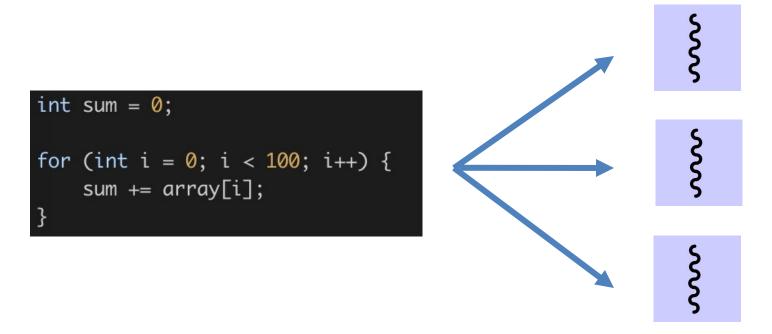
 However, the structured block following the parallel for directive must be a for loop.

```
int sum = 0;

#pragma omp parallel for reduction(+:sum)
for (int i = 0; i < 100; i++) {
        sum += array[i];
}</pre>
```

Parallel for

• Furthermore, with the parallel for directive the system parallelizes the for loop by dividing the iterations of the loop among the threads.



Parallel for Example

```
int sum = 0;
for (int i = 0; i < 100; i++) {
    sum += array[i];
}</pre>
```



```
int sum = 0;

#pragma omp parallel for reduction(+:sum)
for (int i = 0; i < 100; i++) {
        sum += array[i];
}</pre>
```

Data dependencies: fibonacci series

$$F_n = F_{n-1} + F_{n-2}$$

Data dependencies

Fibonacci in serial

```
#include <stdio.h>
int main()
        int fibo[10];
        fibo[0] = fibo[1] = 1;
        int i;
        printf("%d\n", fibo[0]);
        printf("%d\n", fibo[1]);
        for (i = 2; i < 10; i++)
                fibo[i] = fibo[i-1] + fibo[i-2];
                printf("%d\n", fibo[i]);
        return 0;
```

```
ksuo@ksuo-VirtualBox ~/cs7172> ./fibonacci.o

1
1
2
3
5
8
13
21
34
55
```

Data dependencies

$$fibo[\ 0\] = fibo[\ 1\] = 1;$$

$$for\ (i = 2;\ i < n;\ i++)$$

$$fibo[\ i\] = fibo[\ i-1\] + fibo[\ i-2\];$$

$$fibo[\ 0\] = fibo[\ 1\] = 1;$$

$$\# \ pragma\ omp\ parallel\ for\ num_threads(2)$$

$$for\ (i = 2;\ i < n;\ i++)$$

$$fibo[\ i\] = fibo[\ i-1\] + fibo[\ i-2\];$$

$$F_n = F_{n-1} + F_{n-2}$$

Data dependencies

Fibonacci in openmp

\$ gcc -fopenmp xxx.c -o xxx.o

```
#include <stdio.h>
#include <omp.h>
int main()
        int fibo[10];
        fibo[0] = fibo[1] = 1;
        int i:
        printf("%d\n", fibo[0]);
        printf("%d\n", fibo[1]);
#pragma omp parallel for num_threads(2)
        for (i = 2; i < 10; i++)
                fibo[i] = fibo[i-1] + fibo[i-2];
                printf("%d\n", fibo[i]);
        return 0;
```

```
ksuo@ksuo-VirtualBox ~/cs7172> ./fibonacci-omp.o

1

2

3

5

8

303804267

303804275

607608542

911412817
```



What happened?



 OpenMP compilers don't check for dependences among iterations in a loop that's being parallelized with a parallel for directive.

 A loop in which the results of one or more iterations depend on other iterations cannot be correctly parallelized by OpenMP.

What happened?

```
#pragma omp parallel for num_threads(2)
                     for (i = 2; i < 10; i++)
                             fibo[i] = fibo[i-1] + fibo[i-2];
                             printf("%d\n", fibo[i]);
                                                              Thread 2
     Thread 1
                                           fibo[6], fibo[7], fibo[8], fibo[9]
fibo[2], fibo[3], fibo[4], fibo[5]
                             data dependency
                                                   What will happen if thread
                                                   2 runs ahead of thread 1?
```

Example: Estimating π

$$\pi = 4\left[1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \cdots\right] = 4\sum_{k=0}^{\infty} \frac{(-1)^k}{2k+1}$$

```
double factor = 1.0;
double sum = 0.0;
for (k = 0; k < n; k++) {
    sum += factor/(2*k+1);
    factor = -factor;
}
pi_approx = 4.0*sum;</pre>
```

loop dependency: the factor in kth iteration has dependency of the k-1th iteration

```
double factor = 1.0;
double sum = 0.0;

pragma omp parallel for num_threads(thread_count) \
    reduction(+: sum)

for (k = 0; k < n; k++) {
    sum += factor/(2*k+1);
    factor = -factor;
}

pi_approx = 4.0*sum;</pre>
```

```
#include <stdio.h>
#include <stdlib.h>
#include <omp.h>
#define n 100000
int main(int argc, char *argv[]) {
        double factor = 1.0;
        double sum, pi_approx = 0.0;
        int k = 0;
        pragma omp parallel for reduction(+:sum)
        for (k=0; k< n; k++) {
                sum += factor/(2*k+1);
                factor = -factor;
        pi_approx = 4.0 * sum;
        printf("pi is %f\n", pi_approx);
        return 0;
```

gcc pi-cal.c -o pi-cal.o -fopenmp

```
ksuo@ksuo-VirtualBox ~/openmp> ./pi-cal.o
pi is 3.141753
ksuo@ksuo-VirtualBox ~/openmp> ./pi-cal.o
pi is -3.141179
ksuo@ksuo-VirtualBox ~/openmp> ./pi-cal.o
pi is -3.141540
ksuo@ksuo-VirtualBox ~/openmp> ./pi-cal.o
pi is 3.141406
ksuo@ksuo-VirtualBox ~/openmp> ./pi-cal.o
pi is 3.141462
ksuo@ksuo-VirtualBox ~/openmp> ./pi-cal.o
pi is -4.857996
ksuo@ksuo-VirtualBox ~/openmp> ./pi-cal.o
pi is -4.842982
ksuo@ksuo-VirtualBox ~/openmp> ./pi-cal.o
pi is 3.141690
ksuo@ksuo-VirtualBox ~/openmp> ./pi-cal.o
pi is 3.141630
ksuo@ksuo-VirtualBox ~/openmp> ./pi-cal.o
pi is -3.142635
```

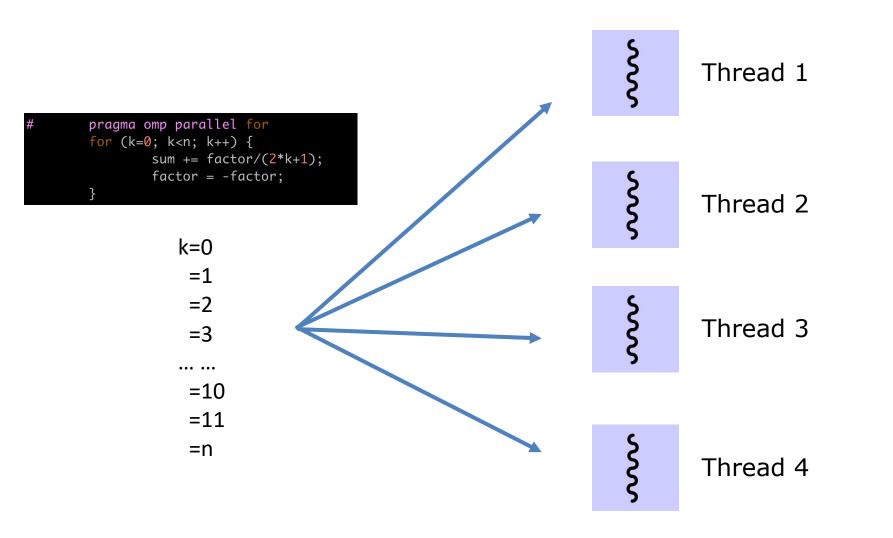
```
double sum = 0.0;
pragma omp parallel for num_threads(thread_count) \
    reduction(+:sum) private(factor)

for (k = 0; k < n; k++) {
    if (k % 2 == 0)
        factor = 1.0;
    else
        factor = -1.0;
    sum += factor/(2*k+1);
}</pre>
Insures factor has
```

```
#include <stdio.h>
#include <stdlib.h>
#include <omp.h>
#define n 100000
int main(int argc, char *argv[]) {
        double factor = 1.0;
        double sum, pi_approx = 0.0;
        int k = 0;
        pragma omp parallel for reduction(+:sum) private(factor)
        for (k=0; k<n; k++) {
                if (k \% 2 == 0)
                        factor = 1.0;
                else
                        factor = -1.0;
                sum += factor/(2*k+1);
        pi_approx = 4.0 * sum;
        printf("pi is %f\n", pi_approx);
        return 0;
```

```
ksuo@ksuo-VirtualBox ~/openmp> ./pi-cal.o
pi is 3.141583
```

Which thread executes which round of loop?



schedule (type, chunksize)

Type can be:

- static: the iterations can be assigned to the threads before the loop is executed.
- dynamic or guided: the iterations are assigned to the threads while the loop is executing.
- auto: the compiler and/or the run-time system determine the schedule.
- runtime: the schedule is determined at run-time.

The chunksize is a positive integer.

The Schedule Clause

Default schedule:

```
# pragma omp parallel for num_threads(thread_count) \
    reduction(+:sum)
for (i = 0; i <= n; i++)
    sum += f(i);</pre>
```

Cyclic schedule:

```
# pragma omp parallel for num_threads(thread_count) \
    reduction(+:sum) schedule(static,1)

for (i = 0; i <= n; i++)
    sum += f(i);</pre>
```

The Static Schedule Type

• twelve iterations, 0, 1, . . . , 11, and three threads

```
schedule(static, 1)
```

Thread 0: 0, 3, 6, 9

Thread 1: 1,4,7,10

Thread 2: 2,5,8,11

The Static Schedule Type

• twelve iterations, 0, 1, . . . , 11, and three threads

schedule(static, 2)

Thread 0: 0, 1, 6, 7

Thread 1: 2,3,8,9

Thread 2: 4,5,10,11

The Static Schedule Type

• twelve iterations, 0, 1, . . . , 11, and three threads

schedule(static, 4)

Thread 0: 0, 1, 2, 3

Thread 1: 4,5,6,7

Thread 2: 8,9,10,11

The Dynamic Schedule Type

 The iterations are also broken up into chunks of chunksize consecutive iterations.

 Each thread executes a chunk, and when a thread finishes a chunk, it requests another one from the run-time system.

This continues until all the iterations are completed.

The allocation results are unpredictable.

The Dynamic Schedule Type

• twelve iterations, 0, 1, . . . , 11, and three threads

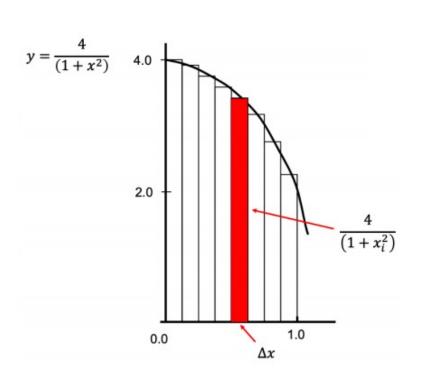
Thread 0: 0, 1, 2, 3, 6, 7

Thread 1: 4,5

Thread 2: 8,9,10,11

Approximate the value of π

$$\int_0^1 \frac{4}{(1+x^2)} dx = \pi$$



$$\begin{split} \int_a^b f(x)dx &= y_0 \Delta x + y_1 \Delta x + \dots + y_{n-1} \Delta x \in D \\ \Delta x &= (b-a)/n \in D \\ y &= f(x) \in D \\ y_i &= f(a+i*(b-a)/n) \quad i = 0,1,2,\dots,n \in D \end{split}$$

Approximate the value of π

```
ksuo@ksuo-VirtualBox ~/Desktop> ./pi.o
#include <stdio.h>
                                                           elapsed time = 15139145 nanoseconds
#include <omp.h>
                                                           3.141593
                                                           ksuo@ksuo-VirtualBox ~/Desktop> ./pi.o
#include <time.h>
                                                           elapsed time = 14786384 nanoseconds
                                                           3.141593
static long num_steps = 1000000;
                                                           ksuo@ksuo-VirtualBox ~/Desktop> ./pi.o
double step;
                                                           elapsed time = 14896299 nanoseconds
void main(){
                                                           3.141593
        struct timespec start, end;
        clock_gettime(CLOCK_MONOTONIC, &start);
        int i;
        double x, pi, sum = 0.0;
                                                      https://github.com/kevinsuo/CS7172
        step = 1.0/(double)num_steps;
                                                      /blob/master/pi-non-openmp.c
        for(i=1;i<= num_steps;i++){</pre>
                x = (i-0.5)*step;
                sum = sum + 4.0/(1.0 + x*x);
        pi=step*sum;
        clock_gettime(CLOCK_MONOTONIC, &end);
        double diff = 1000000000L * (end.tv_sec - start.tv_sec) + end.tv_nsec - start.tv_nsec;
        printf("elapsed time = %llu nanoseconds\n", (long long unsigned int) diff);
        printf("%lf\n",pi);
```

ksuo@ksuo-VirtualBox ~/Desktop> ./pi.o

ksuo@ksuo-VirtualBox ~/Desktop> ./pi.o

elapsed time = 14423708 nanoseconds

elapsed time = 14872618 nanoseconds

3.141593

3.141593

Approximate the value of π

#include <stdio.h>

```
#include <omp.h>
#include <time.h>
static long num_steps = 10000000;
double step;
                                                                                               /pi-openmp.c
#define NUM_THREADS 4
void main ()
       struct timespec start, end;
                                                                                 ksuo@ksuo-VirtualBox ~/Desktop> ./pi-openmp.o
       clock_gettime(CLOCK_MONOTONIC, &start);
                                                                                 elapsed time = 10076458 nanoseconds
                                                                                  3.141593
       int i;
       double x, pi, sum[NUM_THREADS];
                                                                                 ksuo@ksuo-VirtualBox ~/Desktop> ./pi-openmp.o
       step = 1.0/(double) num_steps;
                                                                                 elapsed time = 6482826 nanoseconds
       omp_set_num_threads(NUM_THREADS);
                                                                                 3.141593
#pragma omp parallel private(i)
                                                                                 elapsed time = 16829159 nanoseconds
               double x;
                                                                                 3.141593
               int id;
               id = omp_get_thread_num();
               for (i=id, sum[id]=0.0;i< num_steps; i=i+NUM_THREADS){</pre>
                                                                                 elapsed time = 10507221 nanoseconds
                       x = (i+0.5)*step;
                                                                                  3.141593
                       sum[id] += 4.0/(1.0+x*x);
                                                                                 elapsed time = 8458411 nanoseconds
       for(i=0, pi=0.0;i<NUM_THREADS;i++)</pre>
                                                                                 3.141593
               pi += sum[i] * step;
       clock_gettime(CLOCK_MONOTONIC, &end);
       double diff = 1000000000L * (end.tv_sec - start.tv_sec) + end.tv_nsec - start.tv_nsec;
       printf("elapsed time = %llu nanoseconds\n", (long long unsigned int) diff);
                                                                                           el and Distributed Computation
       printf("%lf\n",pi);
```

https://github.com/kevin suo/CS7172/blob/master

ksuo@ksuo-VirtualBox ~/Desktop> ./pi-openmp.o ksuo@ksuo-VirtualBox ~/Desktop> ./pi-openmp.o ksuo@ksuo-VirtualBox ~/Desktop> ./pi-openmp.o

An example of parallel and distributed computation: Matrix multiplication

Matrix multiply

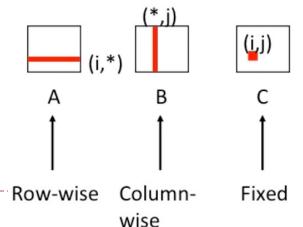
```
int main()
        initMatrix();
        double time_spent = 0.0;
        clock_t begin = clock();
        matrixMultiply();
        clock_t end = clock();
        time_spent += (double)(end - begin) / CLOCKS_PER_SEC;
        printf("Time elpased is %f seconds", time_spent);
        return 0;
```

https://github.com/kevinsuo/CS7172/blob/master/matrix.c

```
#include <stdio.h>
#include <time.h>
#include <stdlib.h>
#define N 1000
double A[N][N], B[N][N], C[N][N];
void initMatrix()
       for (i = 0; i < N; i++) {
               for (j = 0; j < N; j++) {
                        A[i][j] = rand() \% 100 + 1; //generate a number between [1, 100]
                        B[i][j] = rand() \% 100 + 1; //generate a number between [1, 100]
```

https://github.com/kevinsuo/CS7172/blob/master/matrix.c

Inner loop:



Matrix multiply

https://github.com/kevinsuo/CS7172/blob/master/matrix.c



How to run it faster?

Tansmitter (TX)

(LSB)

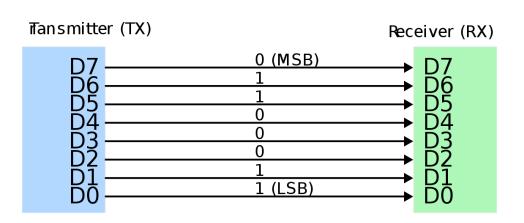
(MSB)

DO D1 D2 D3 D4 D5 D6 D7

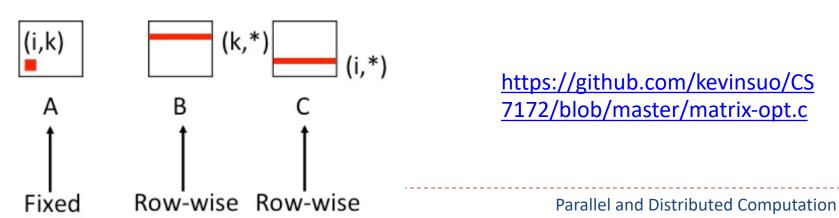
1 1 0 0 0 1 1 0

DI

- 1. Accelerate serial execution Reduce unnecessary steps
- 2. Accelerate in parallel



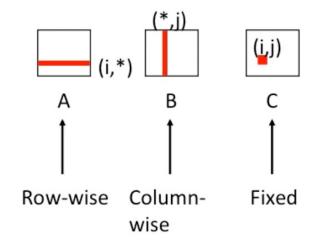
Inner loop:



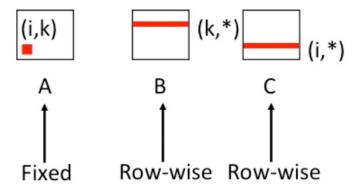
ksuo@ksuo-VirtualBox ~/cs7172> ./a.o
Time elpased is 67.452589 secondsday
ksuo@ksuo-VirtualBox ~/cs7172>
Time elpased is 18.149353 secondsday

N=2000 3.7x

Inner loop:

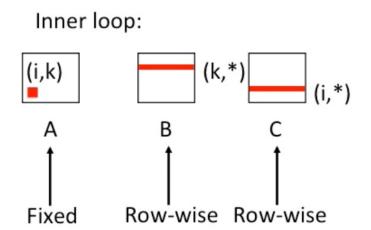


Inner loop:



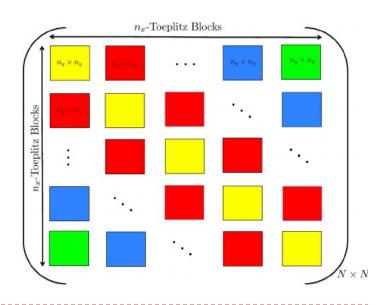
Temporal locality

Every inner loop reuse the value of A[i, k]



Spatial locality

 Divide the large matrix into smaller ones and put it inside the cache during calculation



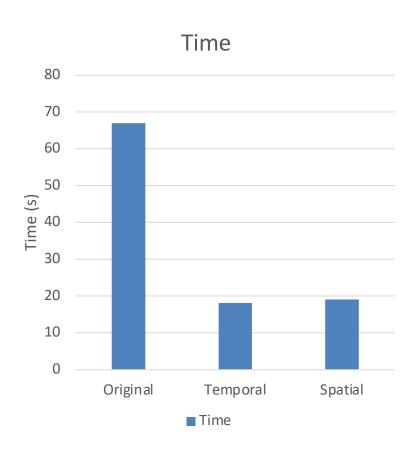
```
void matrixMultiply() {
        int i, j, k = 0;
                                                         https://github.com/kevinsuo/CS7
        int i2, j2, k2 = 0;
                                                         172/blob/master/matrix-opt2.c
        for (k2 = 0; k2 < N; k2+=BLOCK_SIZE) {
                for (i2 = 0; i2 < N; i2+=BLOCK_SIZE) {
                         for (j2 = 0; j2 < N; j2+=BLOCK_SIZE) {
                                 //inside each block
                                 for (k = k2; k < k2+BLOCK_SIZE; k++) {
                                         for (i = i2; i < i2+BLOCK_SIZE; i++) {</pre>
                                                  for (j = j2; j < j2+BLOCK\_SIZE; j++) {
                                                          C[i][j] = A[i][k] * B[k][j];
                                                               0
            CS 4504
```

$$A = \begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{1n} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ \hline a_{31} & a_{32} & a_{33} & a_{34} \\ a_{41} & a_{42} & a_{43} & a_{44} \end{pmatrix} \implies \begin{pmatrix} A_{11} & A_{12} \\ A_{21} & A_{22} \end{pmatrix}$$

$$A_{11} = \begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix}, A_{12} = \begin{pmatrix} a_{13} & a_{14} \\ a_{23} & a_{24} \end{pmatrix}$$

$$A_{21} = \begin{pmatrix} a_{31} & a_{32} \\ a_{41} & a_{42} \end{pmatrix}, A_{22} = \begin{pmatrix} a_{33} & a_{34} \\ a_{43} & a_{44} \end{pmatrix}$$





```
ksuo@ksuo-VirtualBox ~/cs7172> ./a.o
Time elpased is 67.845517 seconds=
ksuo@ksuo-VirtualBox ~/cs7172>
ksuo@ksuo-VirtualBox ~/cs7172>
ksuo@ksuo-VirtualBox ~/cs7172>
ksuo@ksuo-VirtualBox ~/cs7172>
ksuo@ksuo-VirtualBox ~/cs7172>
Time elpased is 19.115410 seconds=
```

Optimal 2: Optimization using parallel

$$\begin{pmatrix} A_{1,1} & A_{1,2} \\ A_{2,1} & A_{2,2} \end{pmatrix} \cdot \begin{pmatrix} B_{1,1} & B_{1,2} \\ B_{2,1} & B_{2,2} \end{pmatrix} \rightarrow \begin{pmatrix} C_{1,1} & C_{1,2} \\ C_{2,1} & C_{2,2} \end{pmatrix}$$

$$(a)$$

$$\text{Task 1: } C_{1,1} = A_{1,1}B_{1,1} + A_{1,2}B_{2,1}$$

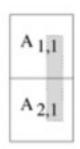
$$\text{Task 2: } C_{1,2} = A_{1,1}B_{1,2} + A_{1,2}B_{2,2}$$

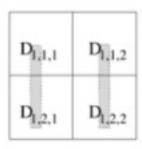
$$\text{Task 3: } C_{2,1} = A_{2,1}B_{1,1} + A_{2,2}B_{2,1}$$

$$\text{Task 4: } C_{2,2} = A_{2,1}B_{1,2} + A_{2,2}B_{2,2}$$

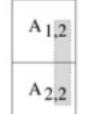
Optimal 2: Optimization using parallel

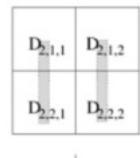


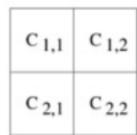




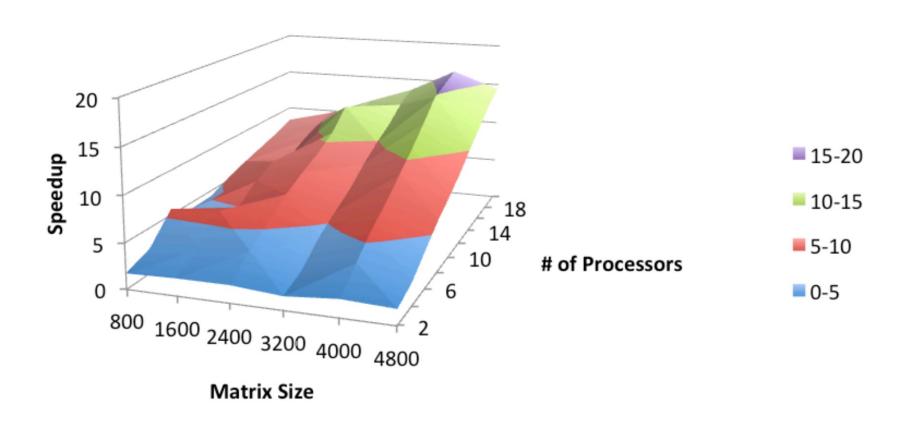
Thread 2:







Optimal 2: Optimization using parallel

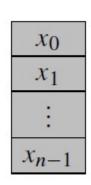


https://www.cse.unr.edu/~fredh/class/415/Nolan/matrix_multiplication/writeup.pdf

Matrix-vector multiplication

$$y_i = a_{i0}x_0 + a_{i1}x_1 + \dots + a_{i,n-1}x_{n-1}$$

a_{00}	<i>a</i> ₀₁		$a_{0,n-1}$
<i>a</i> ₁₀	a ₁₁		$a_{1,n-1}$
:	:		:
a_{i0}	a_{i1}		$a_{i,n-1}$
:	:		
		101	



Уо				
<i>y</i> ₁				
:				
$y_i = a_{i0}x_0 + a_{i1}x_1 + \cdots + a_{i,n-1}x_{n-1}$				
:				
y_{m-1}				

```
for (i = 0; i < m; i++) {
   y[i] = 0.0;
   for (j = 0; j < n; j++)
      y[i] += A[i][j]*x[j];
}</pre>
```

Matrix-vector multiplication

```
# pragma omp parallel for num_threads(thread_count)

    default(none) private(i, j) shared(A, x, y, m, n)

for (i = 0; i < m; i++) {
    y[i] = 0.0;
    for (j = 0; j < n; j++)
        y[i] += A[i][j]*x[j]; Run-times and efficiencies
        of matrix-vector multiplication
        (times are in seconds)</pre>
```

	Matrix Dimension							
	$8,000,000 \times 8$		8000×8000		$8 \times 8,000,000$			
Threads	Time	Eff.	Time	Eff.	Time	Eff.		
1	0.322	1.000	0.264	1.000	0.333	1.000		
2	0.219	0.735	0.189	0.698	0.300	0.555		
4	0.141	0.571	0.119	0.555	0.303	0.275		

Conclusion

Scope of variable

Reduce

Data and loop dependency

Schedule

Examples of OpenMP