		ntents	8 String 8.1 KM 8.2 Min 8.3 Slid
1	Bas	sic 1 Basic codeblock setting	8.4 Spli
	1.2	Basic vim setting	
	1.3	*	9 data str
		Python	9.1 Bigi
	1.5 1.6	Range data 2 Some Function 2	9.2 Disj
	1.7	Time	9.3 Mat 9.4 分數
	DD		0.1 // 20
2	DP 2.1	2 3 維 DP 思路	
	2.2	Knapsack Bounded	. –
	2.3		1 Ba
	2.4	1	
	2.5	LCIS	1 1 D
		LCS	1.1 B
	2.8		
		LIS	Settings code
		Max_subarray	Settings
		2 Money problem	Delete em
	2.13	B Palindromic Substrings count	Insert sp
3	Flo	w & matching 4	Insert spa
3		Dinic	
	3.2	Edmonds_karp	
	3.3		1.2 B
	$3.4 \\ 3.5$	*	
	3.6	Maximum matching	/*at home
	3.7	Minimum cut	/* vi ~/.
	3.8	Model	syntax en set smart
	3.9	Stable matching 6	set tabst
4	\mathbf{Ge}	ometry 7	set shift
		Circle Intersect	set expan
		Closest Pair	set relat
		Line	
		Point	1.3 C
	4.6		
	4.7	Triangle	#include
5	Gra	aph 10	using nam
	5.1	BCC edge	typedef l
	5.2	BCC vertex	typedef u #define p
	5.3		#define 1
	5.5	BFS-queue	#define a
	5.6	Dijkstra	#define e
	5.7	Euler circuit	#define x #define y
	5.8		#define b
		Hamilton_cycle 12 Kruskal 12	;
		LCA	#define b
		2 Minimum Weight Cycle	' << #define b
		3 Prim	endl
	5.14	4 Union_find	<pre>int main(</pre>
6	Ma	thematics 14	{
	6.1	Catalan	ios:: cin.t
	6.2	Combination	retur
	6.3	CRT 14 Extended Euclidean 14	}
	6.5	Fermat	
	6.6		1 4 D
	6.7	Log	1.4 P
	6.8	Mod 性質	+ 4 1
) Pow Mod	//輸入
		Prime table	input()
		2 Prime 判斷	array = [
		3 Round(小數)	range(0,
		5公式	line = in
	6.16	3 四則運算	D, R, N =
		7 因數表	// 才是 耳
		3 數字乘法組合	/ / / / / / / 走 · ¶ / 是 小數
		7 数于加ぶ組合	/ 足 小数
		. 質因數分解	pow(a, b,
	6.22	2 質數數量	
7	Otl	ner 18	print(*ob
'	7.1	Binary search 三類變化	// object
	7.2	Heap sort	// sep // end
	7.3	Josephus	// end
	7.4	Largest Multi-interval	// EOF br
	$7.5 \\ 7.6$	Merge sort 18 N Queen problem 19	try:
	7.7	Quick sort	while /
	7.8	Sudoku solution	except EO
	7.9	Weighted Job Scheduling	pass

8	String						
	8.1	KMP	20				
	8.2	Min Edit Distance	20				
	8.3	Sliding window	20				
	8.4	Split	20				
		ta structure					
	9.1	Bigint	20				
	9.2	DisjointSet	22				
	9.3	Matirx	22				
	9.4	分數	22				

sic

asic codeblock setting

```
-> Editor -> Keyboard shortcuts -> Plugins -> Source formatter (AStyle)
-> Source Formatter -> Padding pty lines within a function or method ace padding around operators ace padding around parentheses on outside
 ra space padding around parentheses
```

asic vim setting

```
directory*/
/imrc */
able
indent
p=4
.
width=4
ivenumber
```

ode Template

```
bits/stdc++.h>
space std;
ong long 11;
nsigned long long ull;
 push_back
en(k) (int)k.length()
ll(p) p.begin(), p.end()
ndl '\n'
first
second
ug(k) cout << "value of " << #k << " is " << k << endl
ugp(k) cout << "pair of " << #k << " is " << k.x << '
k.y << endl;
ugarr(k) for(auto i : k) cout << i << ' '; cout <<
sync_with_stdio(0);
e(0);
 0;
```

ython

```
0] * (N) //N個0
N) // 0 ~ N-1
out().split()
            map(int, line) // 分三個 int 變數
            運算
            c) // a ^ b % c
            jects, sep = ' ', end = '\n')
s -- 可以一次輸出多個對象
            分開多個objects
            默認值是\n
            eak
            True:
            'input someithing
except EOFError:
```

```
1.5 Range data
int (-2147483648 to 2147483647)
unsigned int(0 to 4294967295)
long(-2147483648 to 2147483647)
unsigned long(0 to 4294967295)
long long(-9223372036854775808 to 9223372036854775807)
unsigned long long (0 to 18446744073709551615)
1.6 Some Function
round(double f);
                             // 四捨五入
ceil(double f);
                             // 進入
                             // 捨去
floor(double f);
 _builtin_popcount(int n); // 32bit有多少 1
to_string(int s);
                             // int to string
cout << setprecision(位數) // cout 小數位設定
```

printf 型別 "%lf" // long double "%lld" // long long int

```
| set_union(all(a), all(b), back_inserter(d)); // 聯集
| set_intersection(all(a), all(b), back_inserter(c)); //交集
| /** 全排列要先 sort !!! **/
| next_permutation(num.begin(), num.end());
| prev_permutation(num.begin(), num.end());
| //用binary search找第一個大於或等於val的位置
| vector<int>::iterator it = lower_bound(v.begin(), v.end(), val)
| ;
| //用binary search找第一個大於val的位置
| vector<int>::iterator it = upper_bound(v.begin(), v.end(), val)
| ;
| /*找到節團車面的最大元素*/
```

```
/*找到範圍裏面的最大元素*/
max_element(n, n + len); // n到n+len範圍內最大值
max_element(v.begin(), v.end()); // vector 中最大值
/*找到範圍裏面的最大元素*/
min_element(n, n + len); // n到n+len範圍內最小值
min_element(v.begin(), v.end()); // vector 中最小值
```

```
queue<datatype> q;
front(); /*取出最前面的值(沒有移除掉)*/
back(); /*取出最後面的值(沒有移除掉)*/
pop(); /*移掉最前面的值*/
push(); /*新增值到最後面*/
empty(); /*回傳bool,檢查是不是空的queue*/
size(); /*queue 的大小*/
/*stack*/
```

/ unordered_set<datatype> s; unordered_set<datatype> s(arr, arr + n); /*initial with array*/ insert(); /*插入值*/

erase(); /*刪除值*/ empty(); /*bool 檢查是不是空*/ count(); /*判斷元素存在回傳1 無則回傳0*/

/*tuple*/ tuple<datatype,datatype,datatype> t;

stack<datatype> s;

std::get<0>(t) /*Get first element of tuple*/
std::get<1>(t) /*Get second element of tuple*/
std::get<2>(t) /*Get third element of tuple*/

1.7 Time

 \mid cout << 1.0 * clock() / CLOCKS_PER_SEC << endl;

2 DP

2.1 3 維 DP 思路

```
|解題思路: dp[i][j][k]
|i 跟 j 代表 range i ~ j 的 value
|k在我的理解裡是視題目的要求而定的
|像是 Remove Boxes 當中 k 代表的是在 i 之前還有多少個連續的箱子
|所以每次區間消去的值就是(k+1) * (k+1)
|換言之·我認為可以理解成 k 的意義就是題目今天所關注的重點·就是
老師說的題目所規定的運算
```

2.2 Knapsack Bounded

2.3 Knapsack sample

2.4 Knapsack Unbounded

```
| const int N = 100, W = 100000;
| int cost[N], weight[N];
| int c[W + 1];
| void knapsack(int n, int w) {
| memset(c, 0, sizeof(c));
| for (int i = 0; i < n; ++i)
| for (int j = weight[i]; j <= w; ++j)
| c[j] = max(c[j], c[j - weight[i]] + cost[i]);
| cout << "最高的價值為" << c[w]; }
```

2.5 LCIS

$2.6 \quad LCS O(Nlog(N))$

```
#define LEN 500004
int a[LEN], b[LEN];
int loc[LEN], n;
int LIS()
     for (int i = 1; i <= n; i++)
   loc[b[i]] = i;
for (int i = 1; i <= n; i++)</pre>
          b[i] = loc[a[i]];
     int k, l, r, mid;
a[1] = b[1], k = 1;
     for (int i = 2; i <= n; i++)
           if (a[k] < b[i])</pre>
                `a[++k] = b[i];
           else
                l = 1;
r = k;
while (1 <= r)</pre>
                      mid = (1 + r) / 2;
                      if (a[mid] < b[i])</pre>
                           l = mid + 1;
                      else
                           r = mid - 1;
                a[1] = b[i];
           }
     return k:
```

2.7 LCS

```
int LCS(vector<string> Ans, vector<string> num)
    int N = Ans.size(), M = num.size();
    vector<vector<int>> LCS(N + 1, vector<int>(M + 1, 0));
    for (int i = 1; i <= N; ++i)
         for (int j = 1; j <= M; ++j)
             if (Ans[i - 1] == num[j - 1])
    LCS[i][j] = LCS[i - 1][j - 1] + 1;
                  LCS[i][j] = max(LCS[i - 1][j], LCS[i][j - 1]);
    cout << LCS[N][M] << '\n';</pre>
    //列印 LCS
    int n = N, m = M;
    vector<string> k;
    while (n && m)
         if (LCS[n][m] != max(LCS[n - 1][m], LCS[n][m - 1]))
             k.push_back(Ans[n - 1]);
             n--;
         else if (LCS[n][m] == LCS[n - 1][m])
         else if (LCS[n][m] == LCS[n][m - 1])
             m - -;
    reverse(k.begin(), k.end());
    for (auto i : k)
    cout << i << " ";</pre>
    cout << endl;
return LCS[N][M];</pre>
```

2.8 LIS O(Nlog(N))

```
3
    return length;
2.9 LIS
vector<int> ans;
void LIS(vector<int> &arr)
    vector<int> dp(arr.size(), 1);
    vector<int> pos(arr.size(), -1);
    int res = INT_MIN, index = 0;
    for (int i = 0; i < arr.size(); ++i)</pre>
         for (int j = i + 1; j < arr.size(); ++j)</pre>
              if (arr[j] > arr[i])
                  if (dp[i] + 1 > dp[j])
                      dp[j] = dp[i] + 1;
                      pos[j] = i;
         if (dp[i] > res)
              res = dp[i];
              index = i;
         }
    cout << res << endl; // length</pre>
    printLIS(arr, pos, index);
for (int i = 0; i < ans.size(); i++)</pre>
         cout << ans[i];
         if (i != ans.size() - 1)
cout << ' ';
    cout << '\n':
void printLIS(vector<int> &arr, vector<int> &pos, int index)
    printLIS(arr, pos, pos[index]);
ans.push_back(arr[index]);
2.10 LPS
// manacher
void LPS(string s)
  int maxlen = 0, 1, r;
  int n = n;
  for (int i = 0; i < n; i++)
  {
    int x = 0;
    while ((s[i - x] == s[i + x]) \&\& (i - x >= 0) \&\& (i + x < n)
         )) //odd length
    if (2 * x + 1 > maxlen)
    {
      maxlen = 2 * x + 1;
      1 = i - x;
      r = i + x;
    }
    while ((s[i - x] == s[i + 1 + x]) \& (i - x >= 0) \& (i + 1)
           + x < n)) //even length
    x++;
if (2 * x > maxlen)
    {
      maxlen = 2 * x;
      1 = i - x + 1;
       r = i + x;
  }
  cout << maxlen << '\n';</pre>
                                              // 最後長度
  cout << l + 1 << ' ' << r + 1 << '\n'; //頭到尾
         Max subarray
/*Kadane's algorithm*/
int maxSubArray(vector<int>& nums) {
    int local_max = nums[0], global_max = nums[0];
for(int i = 1; i < nums.size(); i++){</pre>
```

local_max = max(nums[i],nums[i]+local_max);
global_max = max(local_max,global_max);

return global_max;

}

2.12 Money problem

```
//能否湊得某個價位
void change(vector<int> price, int limit)
    vector<bool> c(limit + 1, 0);
    c[0] = true;
    for (int i = 0; i < price.size(); ++i)</pre>
                                                      // 依序加入各種
         for (int j = price[i]; j <= limit; ++j) // 由低價位逐步
              到高價位
             c[j] = c[j] | c[j - price[i]];
    if (c[limit]) cout << "YES\n";
else cout << "NO\n";</pre>
// 湊得某個價位的湊法總共幾種
void change(vector<int> price, int limit)
    vector<int> c(limit + 1, 0);
    c[0] = true;
    for (int i = 0; i < price.size(); ++i)</pre>
    // 湊得某個價位的最少錢幣用量
void change(vector<int> price, int limit)
    vector<int> c(limit + 1, 0);
    c[0] = true;
    for (int i = 0; i < price.size(); ++i)
    for (int j = price[i]; j <= limit; ++j)
        c[j] = min(c[j], c[j - price[i]] + 1);
cout << c[limit] << '\n';</pre>
    cout << c[limit] <<
·
//湊得某個價位的錢幣用量,有哪幾種可能性
void change(vector<int> price, int limit)
    vector<int> c(limit + 1, 0);
    c[0] = true;
for (int i = 0; i < price.size(); ++i)</pre>
        for (int j = price[i]; j <= limit; ++j)
c[j] |= c[j-price[i]] << 1; // 錢幣數量加一、每一種
                   可能性都加一
    for (int i = 1; i <= 63; ++i)
    if (c[m] & (1 << i))</pre>
             cout << "用" << i << "個錢幣可湊得價位" << m;
}
```

2.13 Palindromic Substrings count

3 Flow & matching

3.1 Dinic

```
const long long INF = 1LL<<60;
struct Dinic { //O(VVE), with minimum cut
    static const int MAXN = 5003;
    struct Edge{
        int u, v;
        long long cap, rest;
    };
    int n, m, s, t, d[MAXN], cur[MAXN];
    vector<Edge> edges;
    vector<int> G[MAXN];
    void init(){
        edges.clear();
        for ( int i = 0 ; i < n ; i++ ) G[i].clear();
        n = 0;
    }
    // min cut start
    bool side[MAXN];
    void cut(int u) {</pre>
```

```
side[u] = 1;
for ( int i : G[u] ) {
    if ( !side[ edges[i].v ] && edges[i].rest )
      // min cut end
      int add_node(){
            return n++;
      void add_edge(int u, int v, long long cap){
  edges.push_back( {u, v, cap, cap} );
  edges.push_back( {v, u, 0, 0LL} );
  m = edges.size();
            G[u].push_back(m-2);
G[v].push_back(m-1);
      bool bfs(){
    fill(d,d+n,-1);
            queue<int> que;
            que.push(s); d[s]=0;
            while (!que.empty()){
                 int u = que.front(); que.pop();
                  for (int ei : G[u]){
    Edge &e = edges[ei];
    if (d[e.v] < 0 && e.rest > 0){
        d[e.v] = d[u] + 1;
                               que.push(e.v);
                  }
            return d[t] >= 0;
      long long dfs(int u, long long a){
            if ( u == t || a == 0 ) return a;
            long long flow = 0, f;
for ( int &i=cur[u]; i < (int)G[u].size() ; i++) {
    Edge &e = edges[ G[u][i] ];
    if ( d[u] + 1 != d[e.v] ) continue;</pre>
                   f = dfs(e.v, min(a, e.rest) );
                   if (f > 0 ) {
                   e.rest -= f
                   edges[ G[u][i]^1 ].rest += f;
                   flow += f;
                   a -= f;
                   if ( a == 0 ) break;
            return flow:
      long long maxflow(int _s, int _t){
            s = _s, t = _t;
long long flow = 0, mf;
while ( bfs() ){
                  fill(cur,cur+n,0);
                  while ( (mf = dfs(s, INF)) ) flow += mf;
            return flow;
} dinic;
```

3.2 Edmonds_karp

```
/*Flow - Edmonds-karp*/
/*Based on UVa820*/
#define inf 1000000
int getMaxFlow(vector<vector<int>> &capacity, int s, int t, int
       n){
   int ans = 0;
   vector<vector<int>> residual(n+1, vector<int>(n+1, 0)); //
        residual network
   while(true){
     vector<int> bottleneck(n+1, 0);
     bottleneck[s] = inf;
     queue<int> q;
     q.push(s);
     vector<int> pre(n+1, 0);
while(!q.empty() && bottleneck[t] == 0){
        int cur = q.front();
        q.pop();
for(int i = 1; i <= n ; i++){
   if(bottleneck[i] == 0 && capacity[cur][i] > residual[
                cur][i]){
             q.push(i);
             pre[i] = cur;
bottleneck[i] = min(bottleneck[cur], capacity[cur][i]
                     - residual[cur][i]);
          }
       }
     if(bottleneck[t] == 0) break;
     for(int cur = t; cur != s; cur = pre[cur]){
    residual[pre[cur]][cur] += bottleneck[t];
    residual[cur][pre[cur]] -= bottleneck[t];
     ans += bottleneck[t];
```

3.3 Hungarian

```
/*bipartite - hungarian*/
/*Based on 2017 ICPC Taiwan regional final Problem I*/
bool dfs(vector<vector<bool>> mp, vector<bool> pass, vector<int</pre>
      >& pre,int cur){
     for(int i = 0;i < mp[cur].size(); i++){
    if(mp[cur][i] && !pass[i]){
        pass[i] = true;
        if(pre[i] == -1 || dfs(mp,pass,pre,pre[i])){</pre>
                    pre[i] = cur;
                     return true;
          }
     return false:
int hungarian(vector<vector<bool>> mp,int n,int m){
     int ans = 0;
     vector<int> pre(m,-1);
for(int i = 0;i < n; i++){
    vector<bool> pass(m,false);
          if(dfs(mp,pass,pre,i))
               ans += 1;
     return ans;
int main(){
     int m,n,e;
     while(cin>>n){
          if(n == 0) break;
          cin>>m>>e;
          int a,b;
          vector<vector<bool>> mp(n,vector<bool>(m,false));
          for(int i = 0;i < e; i++){
               cin>>a>>b;
               mp[a][b] = true;
          cout<<hungarian(mp,n,m)<<endl;</pre>
     return 0;
```

3.4 Independent set

```
int mp[30][30];
int vis[30];
int n, m;
int dfs(int now){
   for(int i = 0;i < now; i++){</pre>
        if(mp[now][i]&&(vis[now] == vis[i]))//與now相鄰的結點與
            now有相同的頻率
            return 0;
    if(now == n - 1){//遍歷結束
        return 1;
   for(int i = 1;i <= 3; i++){//選顏色
vis[now+1] = i;
        if(dfs(now+1))
            return 1;
   return 0:
int main(){
   int t;
    cin >> t:
    while(t--){
```

memset(vis,0,sizeof(vis));

```
memset(mp,0,sizeof(mp));
cin >> n >> m;
while(m--){
    int a, b;
    cin >> a >> b;
    mp[a][b] = 1;
    mp[b][a] = 1;
}
vis[0] = 1;//第一個節點任意選一種顏色
if(dfs(0))
    cout <<"Y"<<endl;
else
    cout <<"N"<<endl;
//print vis = print result of combinaton
}
return 0;
```

3.5 Maximum general weighted matching

```
From NCTU codebook
 // Minimum Weight Perfect Matching (Perfect Match)
 struct Graph {
       static const int MAXN = 105;
      int n, e[MAXN][MAXN];
int match[MAXN], d[MAXN], onstk[MAXN];
       void init(int _n) {
            n = _n;
for( int i = 0 ; i < n ; i ++ )
for( int j = 0 ; j < n ; j ++ )</pre>
                  e[i][j] = 0;
       void add_edge(int u, int v, int w) {
            e[u][v] = e[v][u] = w;
      bool SPFA(int u){
    if (onstk[u]) return true;
            stk.push_back(u);
            for ( int v = 0 ; v < n ; v++ ) {
   if (u != v && match[u] != v && !onstk[v] ){</pre>
                        int m = match[v];
                        if ( d[m] > d[u] - e[v][m] + e[u][v] ){
   d[m] = d[u] - e[v][m] + e[u][v];
   onstk[v] = 1;
                             stk.push_back(v);
                             if (SPFA(m)) return true;
stk.pop_back();
onstk[v] = 0;
                        }
                 }
            onstk[u] = 0;
            stk.pop_back();
return false;
       int solve() {
            for ( int i = 0 ; i < n ; i += 2 ) {
                  match[i] = i+1;
match[i+1] = i;
            while (true){
                 fe (true);
int found = 0;
for ( int i = 0 ; i < n ; i++ )
    onstk[ i ] = d[ i ] = 0;
for ( int i = 0 ; i < n ; i++ ) {</pre>
                        stk.clear();
                        if ( !onstk[i] && SPFA(i) ) {
                             found = 1;
while ( stk.size() >= 2 ) {
                                   int u = stk.back(); stk.
                                   pop_back();
                                   int v = stk.back(); stk.
                                   pop_back();
                                   match[u] = v;
match[v] = u;
                             }
                        }
                  }
if (!found) break;
             int ret = 0;
            for ( int i = 0 ; i < n ; i++ )
                 ret += e[i][match[i]];
            ret /= 2;
            return ret;
} graph;
```

3.6 Maximum matching

```
/*bipartite - maximum matching*/
bool dfs(vector<vector<bool>> res,int node,vector<int>& x,
    vector<int>& y, vector<bool> pass){
    for (int i = 0; i < res[0].size(); i++){</pre>
```

```
if(res[node][i] && !pass[i]){
                pass[i] = true;
if(y[i] == -1 || dfs(res,y[i],x,y,pass)){
                     x[node] = i;
                     y[i] = node;
return true;
                }
          }
     return false;
int main(){
     int n,m,1;
     while(cin>>n>>m>>l){
           vector<vector<bool>> res(n, vector<bool>(m, false));
           for (int i = 0; i < 1; i++){
                int a, b;
cin >> a >> b;
res[a][b] = true;
          int ans = 0;
           vector<int> x(n, -1);
          vector<int> y(n, -1);
for (int i = 0; i < n; i++){
    vector<bool> pass(n, false);
    if(dfs(res,i,x,y,pass))
                     ans += 1;
           cout << ans << endl;
     return 0:
}
/*
input:
4 3 5 //n matching m, 1 links
0 0
0 2
1 0
2 1
answer is 3
```

3.8 Model

- Theorem
 - 最大匹配 + 最小邊覆蓋 = V
 - 最大獨立集 + 最小點覆蓋 = V
 - 最大匹配 = 最小點覆蓋
 - 最小路徑覆蓋數 = V 最大匹配數
 - o maximum flow minimum cut
 - 找到一個最大流 = 至少產生一個最小割
 - 找最大流的bottleneck就可以找到最小割
- Maximum Independent Set
 - o General: [NPC] maximum clique of complement of G
 - o Bipartite Graph: [P] Maximum Cardinality Bipartite Matching
 - o Tree: [P] dp
- Minimum Dominating Set
 - o General: [NPC] backtracking
 - o Bipartite Graph: [NPC] backtracking
 - Tree: [P] DP
- Minimum Vertex Cover
 - o General: [NPC] (?)maximum clique of complement of G
 - o Bipartite Graph: [P] Maximum Cardinality Bipartite Matching
 - o Tree: [P] Greedy, from leaf to root
- Minimum Edge Cover
 - o General: [P] V Maximum Matching
 - o Bipartite Graph: [P] Greedy, strategy: cover small degree node first.
 - o (Min/Max)Weighted: [P]: Minimum/Maximum Weight Matching

3.7 Minimum cut

```
/*from 演算法筆記*/
typedef int Graph[9][9];
                          // adjacency matrix
Graph C, F, R;
                          // 分別是容量上限、流量、剩餘容量
bool visit[9];
void DFS(int i)
   visit[i] = true;
    for (int j=0; j<9; ++j)
    if (!visit[j] && F[i][j] < C[i][j])</pre>
           DFS(j);
}
void minimum_s_t_cut(int s, int t)
    // 求一個最大源匯流,源點為s點,匯點為t點。
   Edmonds_Karp(s, t);
    // 從源點開始遍歷,找出流量瓶頸。
   memset(visit, false, sizeof(visit));
    // 找出其中一個最小源匯割,會是源點側點數最少的最小源匯割。
   for (int i=0; i<9; ++i)
                                 // 窮舉源點側的點
       if (visit[i])
           for (int j=0; j<9; ++j) // 窮舉匯點側的點
if (!visit[j])
                  if (C[i][j] > 0)
                                     // 要確定有邊
                      cout << "割上的邊有"
                          << "曲" << i << "到" << j;
```

3.9 Stable matching

```
/*based on UVa1175*/
/*stable marriage problem*/
void engage(vector<int>& bm, vector<int>& gm, int a, int b,
     queue<int>& q){
    int tmp = gm[b];
if(tmp != -1){
   bm[tmp] = -1;
         q.push(tmp);
    bm[a] = b;
gm[b] = a;
int main(){
     bool blank = false;
     cin>>cases;
     while(cases--){
         if(blank) cout<<endl;</pre>
         int n,a;
         cin>>n:
         queue<int> q; // proposal
vector<vector<int>> boy(n+1,vector<int>(n+1,0)),girl(n
               +1, vector < int > (n+1,0));
         vector<int> p(n+1,1);
for(int i = 1;i <= n; i++){</pre>
              for(int j = 1; j <= n; j++){
                   cin>>a;
                   boy[i][j] = a;
              q.push(i);
          for(int i = 1;i <= n; i++){
              for(int j = 1; j <= n; j++){
                   cin>>a;
                   girl[i][a] = j;
              }
          vector<int> bm(n+1,-1),gm(n+1,-1);
         while(!q.empty()){
              int cur = q.front();
              q.pop();
```

4 Geometry

4.1 Circle Intersect

```
bool same(double a, double b)
                    return abs(a - b) < 0;</pre>
 struct P
                      double x, y;
                   double x, y;
P() : x(0), y(0) {}
P(double x, double y) : x(x), y(y) {}
P operator+(P b) { return P(x + b.x, y + b.y); }
P operator-(P b) { return P(x - b.x, y - b.y); }
P operator*(double b) { return P(x * b, y * b); }
P operator*(double b) { return P(x / b, y / b); }
double operator*(P b) { return x * b.x + y * b.y; }
// double operator*(P b) { return x * h.y - y * h.y. - y * 
                      // double operator^(P b) { return x * b.y - y * b.x; }
                   double abs() { return x *
double abs() { return hypot(x, y); }
P unit() { return *this / abs(); }
P rot(double o)
                                         double c = cos(o), s = sin(o);
return P(c * x - s * y, s * x + c * y);
                    double angle() { return atan2(y, x); }
 struct C
                      double r
                    C(P \ c = P(0, 0), double \ r = 0) : c(c), r(r) \{\}
 vector<P> Intersect(C a, C b)
                    if (a.r > b.r)
                                         swap(a, b);
                   swap(a, b);
double d = (a.c - b.c).abs();
vector<P> p;
if (same(a.r + b.r, d))
    p.pb(a.c + (b.c - a.c).unit() * a.r);
else if (a.r + b.r > d && d + a.r >= b.r)
                                          double o = acos((sqrt(a.r) + sqrt(d) - sqrt(b.r)) / (2
                                       return p;
}
```

4.2 Closest Pair

4.3 Line

return d:

```
template <typename T>
struct line
    line() {}
    point<T> p1, p2;
T a, b, c; //ax+by+c=0
    line(const point<T> &x, const point<T> &y) : p1(x), p2(y)
    void pton()
    { //轉成一般式
        b = p1.y - p2.y;
b = p2.x - p1.x;
c = -a * p1.x - b * p1.y;
    T ori(const point<T> &p) const
    { //點和有向直線的關係·>0左邊、=0在線上<0右邊
         return (p2 - p1).cross(p - p1);
    T btw(const point<T> &p) const
    { //點投影落在線段上<=0
         return (p1 - p).dot(p2 - p);
    bool point_on_segment(const point<T> &p) const
    { //點是否在線段上
        return ori(p) == 0 && btw(p) <= 0;</pre>
    T dis2(const point<T> &p, bool is_segment = 0) const
    { //點跟直線/線段的距離平方 point<T> v = p2 - p1, v1 = p - p1;
         if (is_segment)
             point<T> v2 = p - p2;
             if (v.dot(v1) <= 0)</pre>
                 return v1.abs2();
             if (v.dot(v2) >= 0)
                 return v2.abs2();
         T tmp = v.cross(v1);
        return tmp * tmp / v.abs2();
    T seg_dis2(const line<T> &1) const
    { //兩線段距離平方
        return min({dis2(l.p1, 1), dis2(l.p2, 1), l.dis2(p1, 1)
              , l.dis2(p2, 1)});
    point<T> projection(const point<T> &p) const
    { //點對直線的投影
        point<T> n = (p2 - p1).normal();
return p - n * (p - p1).dot(n) / n.abs2();
    point<T> mirror(const point<T> &p) const
         //點對直線的鏡射·要先呼叫pton轉成一般式
        point<T> R;
T d = a * a + b * b;
        R.x = (b * b * p.x - a * a * p.x - 2 * a * b * p.y - 2
        * a * c) / d;

R.y = (a * a * p.y - b * b * p.y - 2 * a * b * p.x - 2

* b * c) / d;
        return R;
    bool equal(const line &1) const
    { //直線相等
         return ori(1.p1) == 0 && ori(1.p2) == 0;
    bool parallel(const line &1) const
         return (p1 - p2).cross(l.p1 - l.p2) == 0;
    bool cross_seg(const line &1) const
         return (p2 - p1).cross(l.p1 - p1) * (p2 - p1).cross(l.
              p2 - p1) <= 0; //直線是否交線段
    int line_intersect(const line &1) const { //直線相交情況·-1無限多點、1交於一點、0不相交
         return parallel(l) ? (ori(l.p1) == 0 ? -1 : 0) : 1;
    int seg_intersect(const line &1) const
        T c1 = ori(1.p1), c2 = ori(1.p2);
T c3 = 1.ori(p1), c4 = 1.ori(p2);
if (c1 == 0 && c2 == 0)
         { //共線
             bool b1 = btw(1.p1) >= 0, b2 = btw(1.p2) >= 0;
             T a3 = 1.btw(p1), a4 = 1.btw(p2);
if (b1 && b2 && a3 == 0 && a4 >= 0)
                  return 2;
             if (b1 && b2 && a3 >= 0 && a4 == 0)
                  return 3;
```

```
if (b1 && b2 && a3 >= 0 && a4 >= 0)
                return 0;
            return -1; //無限交點
        else if (c1 * c2 <= 0 && c3 * c4 <= 0)
           return 1;
        return 0; //不相交
    point<T> line_intersection(const line &1) const
    { /*直線交點*/
        point<T> a = p2 - p1, b = l.p2 - l.p1, s = l.p1 - p1;
        // if (a.cross(b) == 0)
              return INF;
        return p1 + a * (s.cross(b) / a.cross(b));
    point<T> seg_intersection(const line &1) const
    { //線段交點
        int res = seg_intersect(1);
        if (res <= 0)
            assert(0);
        if (res == 2)
            return p1;
        if (res == 3)
            return p2;
        return line_intersection(1);
};
```

4.4 Max cover rectangle

```
const double PI = atan2(0.0, -1.0);
const double eps = 1e-10;
typedef point<double> p; // data type 依照題目更改int mycmp(double a) { return fabs(a) < eps ? 0 : (a < 0 ? -1 :
double turnAngle(p a, p b) { return mycmp(a.dot(b)) == 1 ?
    angle(a, b) : PI + angle(a, b); }
double> po)
    double h1 = distanceOfpAndLine(po.p[a], po.p[b], po.p[b] +
    double h2 = distanceOfpAndLine(po.p[c], po.p[d], po.p[d] +
         cd);
    return h1 * h2;
double max_cover_rectangle(polygon<double> po)
    po.p.pb(po.p[0]);
    int m = po.p.size();
if (m < 3)</pre>
    return 0; // 沒凸包哪來外包矩形
double Max = -1;
    double Minx = po.p[0].x, Miny = po.p[0].y, Maxx = po.p[0].x
          , Maxy = po.p[0].y;
    int p1 = 0, p2 = 0, p3 = 0, p4 = 0;
    p v1, v2, ori;
    ori = v1 = p(1, 0);
v2 = p(0, 1);
    for (int i = 1; i < m; i++)
         if (mycmp(Minx - po.p[i].x) == 1)
             Minx = po.p[i].x, p3 = i;
         if (mycmp(Maxx - po.p[i].x) == -1)
    Maxx = po.p[i].x, p4 = i;
         if (mycmp(Miny - po.p[i].y) == 1)
         Miny = po.p[i].y, p1 = i;
if (mycmp(Maxy - po.p[i].y) == -1)
             Maxy = po.p[i].y, p2 = i;
    while (mycmp(ori.cross(v1)) >= 0)
         double minRad = 1e20;
         minRad = min(minRad, turnAngle(v1, po.p[p1 + 1] - po.p[
             p1]));
         minRad = min(minRad, turnAngle(v1 * (-1), po.p[p2 + 1]
        - po.p[\dot{p}2]));
minRad = min(minRad, turnAngle(v2 * (-1), po.p[p3 + 1]
         - po.p[p3]));
minRad = min(minRad, turnAngle(v2, po.p[p4 + 1] - po.p[
         p4]));
double 1 = 0, r = minRad;
         while (mycmp(1 - r))
             double len = (r - 1) / 3;
double midl = 1 + len;
             double midr = r - len;
```

```
1 = mid1:
        Max = max(Max, Area(p1, p2, p3, p4, Rotate(v1, 1),
            Rotate(v2, 1), po));
        v1 = Rotate(v1, minRad);
        v2 = Rotate(v2, minRad);
        if (mycmp(angle(v1, po.p[p1 + 1] - po.p[p1])) == 0)
    p1 = (p1 + 1) % m;
        if (mycmp(angle(v1 * (-1), po.p[p2 + 1] - po.p[p2])) ==
             0)
            p2 = (p2 + 1) \% m;
        if (mycmp(angle(v2 * (-1), po.p[p3 + 1] - po.p[p3])) ==
             0)
            p3 = (p3 + 1) \% m:
        if (mycmp(angle(v2, po.p[p4 + 1] - po.p[p4])) == 0)
    p4 = (p4 + 1) % m;
    return Max;
}
```

4.5 Point

```
const double PI = atan2(0.0, -1.0);
template <typename T>
struct point
    point() {}
    point(const T &x, const T &y) : x(x), y(y) {}
    point operator+(const point &b) const
        return point(x + b.x. v + b.v):
    point operator-(const point &b) const
        return point(x - b.x, y - b.y);
    point operator*(const T &b) const
        return point(x * b, y * b);
    point operator/(const T &b) const
        return point(x / b, y / b);
    bool operator==(const point &b) const
        return x == b.x && y == b.y;
    T dot(const point &b) const
        return x * b.x + y * b.y;
      cross(const point &b) const
        return x * b.y - y * b.x;
    point normal() const
    { //求法向量
        return point(-y, x);
    T abs2() const
    { //向量長度的平方
        return dot(*this);
    T rad(const point &b) const
    { //兩向量的弧度
        return fabs(atan2(fabs(cross(b)), dot(b)));
    T getA() const
                           //對x軸的弧度
        T A = atan2(y, x); //超過180度會變負的
if (A <= -PI / 2)
A += PI * 2;
        return A;
```

4.6 Polygon

```
template <typename T>
struct polygon
    polygon() {}
    vector<point<T>> p; //逆時針順序
    T area() const
    { //面積
        for (int i = p.size() - 1, j = 0; j < (int)p.size(); i</pre>
             = j++)
```

```
ans += p[i].cross(p[j]);
return ans / 2;
point<T> center_of_mass() const
{ //重心
    T cx = 0, cy = 0, w = 0;
    for (int i = p.size() - 1, j = 0; j < (int)p.size(); i</pre>
         = j++)
        T a = p[i].cross(p[j]);
cx += (p[i].x + p[j].x) * a;
        cy += (p[i].y + p[j].y) * a;
    return point<T>(cx / 3 / w, cy / 3 / w);
char ahas(const point<T> &t) const
{ //點是否在簡單多邊形內,是的話回傳1、在邊上回傳-1、否則回
     值ρ
    bool c = 0;
    for (int i = 0, j = p.size() - 1; i < p.size(); j = i</pre>
        if (line<T>(p[i], p[j]).point_on_segment(t))
        c = !c;
    return c;
char point_in_convex(const point<T> &x) const
    int 1 = 1, r = (int)p.size() - 2;
    while (1 <= r)
    { //點是否在凸多邊形內,是的話回傳1、在邊上回傳-1、否則
         回傳0
        int mid = (1 + r) / 2;
T a1 = (p[mid] - p[0]).cross(x - p[0]);
        T a2 = (p[mid + 1] - p[0]).cross(x - p[0]);
if (a1 >= 0 && a2 <= 0)
        {
            T res = (p[mid + 1] - p[mid]).cross(x - p[mid])
            return res > 0 ? 1 : (res >= 0 ? -1 : 0);
        else if (a1 < 0)
            r = mid - 1;
        else
            1 = mid + 1:
    return 0;
vector<T> getA() const
{//凸包邊對x軸的夾角
    vector<T> res; //一定是遞增的
for (size_t i = 0; i < p.size(); ++i)
    res.push_back((p[(i + 1) % p.size()] - p[i]).getA()
    return res;
bool line_intersect(const vector<T> &A, const line<T> &1)
     const
{ //O(logN)
    int f1 = upper_bound(A.begin(), A.end(), (1.p1 - 1.p2).
    getA()) - A.begin();
    int f2 = upper_bound(A.begin(), A.end(), (1.p2 - 1.p1).
         getA()) - A.begin();
    return 1.cross_seg(line<T>(p[f1], p[f2]));
polygon cut(const line<T> &1) const
{ //凸包對直線切割·得到直線1左側的凸包
    polygon ans;
    for (int n = p.size(), i = n - 1, j = 0; j < n; i = j
         ++)
    {
        if (l.ori(p[i]) >= 0)
             ans.p.push_back(p[i]);
             if (l.ori(p[j]) < 0)
                 ans.p.push_back(l.line_intersection(line<T
                     >(p[i], p[j])));
        else if (1.ori(p[j]) > 0)
    ans.p.push_back(1.line_intersection(line<T>(p[i
                 ], p[j])));
    return ans:
static bool Andrew_Monotone_Chain_angle(const point<T> &a,
     const point<T> &b)
  //凸包排序函數 // 起始點不同
    return (a.y < b.y) || (a.y == b.y && a.x < b.x); //Y最
         小開始
void Andrew_Monotone_Chain(vector<point<T>> &s)
```

```
{ //凸包 Convexhull 2D
    sort(s.begin(), s.end(), Andrew_Monotone_Chain_angle);
    p.resize(s.size() + 1);
    int m = 0;
    // cross >= 0 順時針。cross <= 0 逆時針旋轉
    for (size_t i = 0; i < s.size(); ++i)</pre>
        while (m >= 2 && (p[m - 1] - p[m - 2]).cross(s[i] - p[m - 2]) <= 0)
            --m;
        p[m++] = s[i];
    for (int i = s.size() - 2, t = m + 1; i >= 0; --i)
        while (m \ge t \&\& (p[m - 1] - p[m - 2]).cross(s[i] - p[m - 2])
             p[m - 2]) <= 0)
              - m;
        p[m++] = s[i];
    if (s.size() > 1) // 重複頭一次需扣掉
    p.resize(m);
    // p.pb(s[0]); // 需要頭在 pb 回去!!
T diam()
{ //直徑
    int n = p.size(), t = 1;
T ans = 0;
    p.push_back(p[0]);
    for (int i = 0; i < n; i++)
        point<T> now = p[i + 1] - p[i];
while (now.cross(p[t + 1] - p[i]) > now.cross(p[t])
             - p[i]))
            t = (t + 1) \% n;
        ans = max(ans, (p[i] - p[t]).abs2());
    return p.pop_back(), ans;
T min_cover_rectangle()
{ // 先做凸包 //最小覆蓋矩形
    int n = p.size(), t = 1, r = 1, l;
    if (n < 3)
        return 0; //也可以做最小周長矩形
    T ans = 1e99;
    p.push_back(p[0]);
    for (int i = 0; i < n; i++)
        point<T> now = p[i + 1] - p[i];
        while (now.cross(p[t + 1] - p[i]) > now.cross(p[t])
             - p[i]))
            t = (t + 1) \% n;
        while (now.dot(p[r + 1] - p[i]) > now.dot(p[r] - p[
            i]))
            r = (r + 1) \% n;
        if (!i)
        while (now.dot(p[1 + 1] - p[i]) \leftarrow now.dot(p[1] - p
             [i]))
            1 = (1 + 1) \% n;
        T d = now.abs2();
        T tmp = now.cross(p[t] - p[i]) * (now.dot(p[r] - p[i])
             i]) - now.dot(p[1] - p[i])) / d;
        ans = min(ans, tmp);
    return p.pop_back(), ans;
T dis2(polygon &pl)
{ //凸包最近距離平方
    vector<point<T>> &P = p, &Q = pl.p;
    int n = P.size(), m = Q.size(), 1 = 0, r = 0;
for (int i = 0; i < n; ++i)</pre>
        if (P[i].y < P[1].y)</pre>
    1 = i;
for (int i = 0; i < m; ++i)
        if (Q[i].y < Q[r].y)</pre>
    P.push_back(P[0]), Q.push_back(Q[0]);
    T ans = 1e99;
    for (int i = 0; i < n; ++i)
        while ((P[1] - P[1 + 1]).cross(Q[r + 1] - Q[r]) <
            0)
r = (r + 1) % m;
        ans = min(ans, line<T>(P[1], P[1 + 1]).seg_dis2(
             line<T>(Q[r], Q[r + 1])));
        1 = (1 + 1) \% n;
    return P.pop back(), O.pop back(), ans;
static char sign(const point<T> &t)
    return (t.y == 0 ? t.x : t.y) < 0;
static bool angle_cmp(const line<T> &A, const line<T> &B)
```

```
int halfplane_intersection(vector<line<T>> &s)
    { //半平面交
        sort(s.begin(), s.end(), angle_cmp); //線段左側為該線段
             半平面
        int L, R, n = s.size();
        vector<point<T>> px(n);
        vector<line<T>> q(n);
        q[L = R = 0] = s[0];
        for (int i = 1; i < n; ++i)
            while (L < R \&\& s[i].ori(px[R - 1]) <= 0)
            while (L < R && s[i].ori(px[L]) <= 0)
            q[++R] = s[i];
            if (q[R].parallel(q[R - 1]))
                if (q[R].ori(s[i].p1) > 0)
                    q[R] = s[i];
            if (L < R)
    px[R - 1] = q[R - 1].line_intersection(q[R]);</pre>
        while (L < R \&\& q[L].ori(px[R - 1]) <= 0)
        p.clear();
        if (R - L <= 1)
            return 0:
        px[R] = q[R].line_intersection(q[L]);
for (int i = L; i <= R; ++i)</pre>
            p.push_back(px[i]);
        return R - L + 1;
};
```

4.7 Triangle

```
template <typename T>
struct triangle
    point<T> a, b, c;
    triangle() {}
    triangle(const point<T> &a, const point<T> &b, const point<</pre>
         T> &c) : a(a), b(b), c(c) {}
    T area() const
    {
        T t = (b - a).cross(c - a) / 2;
return t > 0 ? t : -t;
    point<T> barycenter() const
    { //重心
        return (a + b + c) / 3;
    point<T> circumcenter() const
    { //外心
        static line<T> u, v;
u.p1 = (a + b) / 2;
        u.p2 = point < T > (u.p1.x - a.y + b.y, u.p1.y + a.x - b.x)
        v.p1 = (a + c) / 2;
        v.p2 = point(T)(v.p1.x - a.y + c.y, v.p1.y + a.x - c.x)
        return u.line intersection(v);
    point<T> incenter() const
    { //內心
       point<T> perpencenter() const
    { //垂心
        return barycenter() * 3 - circumcenter() * 2;
    }
};
```

5 Graph

5.1 BCC edge

```
struct BccEdge {
    static const int MXN = 100005;
    struct Edge {
        int v, eid;
    };
    int n, m, step, par[MXN], dfn[MXN], low[MXN];
    vector<Edge> E[MXN];
```

```
DisjointSet djs;
void init(int _n) {
     n = _n;
m = 0;
     for (int i = 0; i < n; i++)
           E[i].clear();
     djs.init(n);
void add_edge(int u, int v) {
      E[u].PB({v, m});
     E[v].PB({u, m});
void DFS(int u, int f, int f eid) {
     par[\dot{u}] = f;
      dfn[u] = low[u] = step++;
     for (auto it : E[u]) {
   if (it.eid == f_eid)
                  continue;
           continue,
int v = it.v;
if (dfn[v] == -1) {
    DFS(v, u, it.eid);
    low[u] = min(low[u], low[v]);
            else {
                  low[u] = min(low[u], dfn[v]);
     }
void solve() {
     step = 0;
     memset(dfn, -1, sizeof(int) * n);
for (int i = 0; i < n; i++) {
    if (dfn[i] == -1)
        DFS(i, i, -1);
    ...</pre>
           djs.init(n);
for (int i = 0; i < n; i++) {
    if (low[i] < dfn[i])</pre>
                        djs.uni(i, par[i]);
     }
graph;
```

5.2 BCC vertex

```
struct BccVertex
     int n, nBcc, step, dfn[MXN], low[MXN], top, stk[MXN];
vector<int> E[MXN], bccv[MXN];
     void init(int _n)
          n = _n;
nBcc = step = 0;
for (int i = 0; i < n; i++)
    E[i].clear();
     void addEdge(int u, int v)
          E[u].push_back(v);
          E[v].push_back(u);
     void DFS(int u, int f)
          dfn[u] = low[u] = step++;
          stk[top++] = u;
for (auto v : E[u])
               if (v == f)
                     continue;
               if (dfn[v] == -1)
                    DFS(v, u);
low[u] = min(low[u], low[v]);
                     if (low[v] >= dfn[u])
                         bccv[nBcc].clear();
                          do
                               z = stk[--top];
                               bccv[nBcc].push_back(z);
                          } while (z != v);
                          bccv[nBcc++].push_back(u);
                    }
               else
                    low[u] = min(low[u], dfn[v]);
     vector<vector<int>> solve()
          vector<vector<int>> res;
          for (int i = 0; i < n; i++)

dfn[i] = low[i] = -1;

for (int i = 0; i < n; i++)
               if (dfn[i] == -1)
```

```
q = p;
                                                                                   queue<int> tmp;
                 top = 0;
                 DFS(i, i);
                                                                                  p = tmp;
                                                                                   count++;
         for (int i = 0; i < nBcc; i++)</pre>
             res.push_back(bccv[i]);
                                                                          }
         return res;
                                                                      int main()
} graph;
                                                                     {
                                                                          cin >> node;
5.3 Bellman-Ford
                                                                          vector<pair<int, int>> edges;
                                                                          int a, b;
while (cin >> a >> b)
  *SPA - Bellman-Ford*/
#define inf 99999 //define by you maximum edges weight
                                                                          {
vector<vector<int> > edges;
                                                                               /*a = b = -1 means input edges ended*/
vector<int> dist;
vector<int> ancestor;
                                                                              if (a == -1 && b == -1)
   break:
void BellmanFord(int start, int node){
                                                                              edges.push_back(pair<int, int>(a, b));
                                                                          vector<int> result(node, -1);
                                                                          BFS(result, edges, node, 0);
                                                                          return 0;
                                                                      5.5 DFS-rec
                 }
             }
                                                                     /*DFS - Recursive version*/
                                                                     map<pair<int,int>,int> edges;
         }
    }
                                                                      vector<int> pass;
                                                                      vector<int> route;
    for(int i = 0; i < node; i++) //negative cycle detection</pre>
                                                                      void DFS(int start){
         for(int j = 0; j < node; j++)</pre>
                                                                          pass[start] = 1;
                                                                          if(dist[i] + edges[i][j] < dist[j])</pre>
                 cout<<"Negative cycle!"<<endl;</pre>
                 return;
                                                                                   route.push_back((*iter).first.second);
                                                                                  DFS((*iter).first.second);
int main(){
                                                                              int node;
    cin>>node:
     edges.resize(node, vector<int>(node, inf));
     dist.resize(node,inf);
    ancestor.resize(node,-1);
                                                                              }
    int a,b,d;
while(cin>>a>>b>>d){
                                                                          }
         /*input: source destination weight*/
if(a == -1 && b == -1 && d == -1)
                                                                      int main(){
                                                                          int node;
                                                                          cin>>node:
         edges[a][b] = d;
                                                                          pass.resize(node,0);
                                                                          int a,b;
    int start;
                                                                          while(cin>>a>>b){
                                                                              if(a == -1 && b == -1)
break;
    cin>>start:
    BellmanFord(start, node);
                                                                              edges.insert(pair<pair<int,int>,int>(pair<int,int>(a,b)
    return 0;
                                                                                   ,0));
                                                                          int start;
5.4 BFS-queue
                                                                          cin>>start;
                                                                          route.push_back(start);
                                                                          DFS(start);
void BFS(vector<int> &result, vector<pair<int, int>> edges, int
      node, int start)
    vector<int> pass(node, 0);
                                                                      5.6 Dijkstra
    queue<int> q;
    queue<int> p;
    q.push(start);
                                                                      /*SPA - Dijkstra*/
    int count = 1;
vector<pair<int, int>> newedges;
                                                                      const int MAXN = 1e5 + 3;
const int inf = INT_MAX;
                                                                     typedef pair<int, int> pii;
vector<vector<pre>vector(pii>> weight(MAXN);
vector<int> isDone(MAXN, false), dist, ancestor;
    while (!q.empty())
         pass[q.front()] = 1;
         for (int i = 0; i < edges.size(); i++)</pre>
                                                                      void dijkstra(int s)
             if (edges[i].first == q.front() && pass[edges[i].
                                                                          priority_queue<pii, vector<pii>, greater<pii>> pq;
                  second] == 0)
                                                                          pq.push(pii(0, s));
ancestor[s] = -1;
                 p.push(edges[i].second);
                                                                          while (!pq.empty())
                 result[edges[i].second] = count;
                                                                              int u = pq.top().second;
             else if (edges[i].second == q.front() && pass[edges
                                                                              pq.pop();
                  [i].first] == 0
                                                                              isDone[u] = true;
                 p.push(edges[i].first);
                 result[edges[i].first] = count;
                                                                              for (auto &pr : weight[u])
                                                                                   int v = pr.first, w = pr.second;
                 newedges.push back(edges[i]);
                                                                                   if (!isDone[v] && dist[u] + w < dist[v])</pre>
         edges = newedges;
                                                                                   {
         newedges.clear();
                                                                                       dist[v] = dist[u] + w;
```

q.pop();

if (q.empty() == true)

pq.push(pii(dist[v], v));

ancestor[v] = u;

12

```
NCNU - No idea codebook
    }
                                                                              }
// weight[a - 1].push_back(pii(b - 1, w));
// weight[b - 1].push_back(pii(a - 1, w));
// dist.resize(n, inf);
// ancestor.resize(n, -1);
// dist[0] = 0;
// dijkstra(0);
5.7 Euler circuit
                                                                          }
/*Euler circuit*/
/*From NTU kiseki*/
/*G is graph, vis is visited, la is path*/
bool vis[N];
size_t la[K];
void dfs(int u, vector<int> &vec)
    while (la[u] < G[u].size())</pre>
        if (vis[G[u][la[u]].second])
             ++la[u];
            continue;
        int v = G[u][la[u]].first;
        vis[G[u][la[u]].second] = true;
        ++la[u];
        dfs(v, vec);
        vec.push_back(v);
}
5.8 Floyd-warshall
/*SPA - Floyd-Warshall*/
                                                                      4
// 有向圖,正邊
                                                                      1 2
                    O(V^3)
// 有向圖,無負環
                    O(V^3)
                                                                      2 4
// 有向圖·有負環
                    不適用
                                                                      3 4
                                                                      3 1
// 無向圖·正邊
                    O(V^3)
                                                                      0 0
// 無向圖,無負環
                    不適用
// 無向圖,有負環 不適用
/*Find min weight cycle*/
#define inf 99999
void floyd_warshall(vector<vector<int>> &distance, vector<</pre>
     vector<int>> &ancestor, int n)
    for (int k = 0; k < n; k++)
        for (int i = 0; i < n; i++)
             for (int j = 0; j < n; j++)
                 if (distance[i][k] + distance[k][j] < distance[</pre>
                 {
                     distance[i][j] = distance[i][k] + distance[
                          k][j];
                     ancestor[i][j] = ancestor[k][j];
                 }
            }
        }
    }
}
vector<vector<int>> distance(n, vector<int>(n, inf));
vector<vector<int>> ancestor(n, vector<int>(n, -1));
distance[a][b] = w;
ancestor[a][b] = w;
floyd_warshall(distance, ancestor, n);
/*Negative cycle detection*,
for (int i = 0; i < n; i++)
    if (distance[i][i] < 0)</pre>
        cout << "Negative cycle!" << endl;</pre>
}
5.9 Hamilton_cycle
/*find hamilton cycle*/
void hamilton(vector<vector<int>> gp, int k, int cur, vector<</pre>
     int>& solution, vector < bool > pass, bool & flag){
    if(k == gp.size()-1){
        if(gp[cur][1] == 1){
    cout << 1 << " ";
                                                                          int n;
```

```
while(cur != 1){
    cout << cur << " "
     cur = solution[cur];
cout << cur << endl;</pre>
```

```
flag = true:
              return:
     for (int i = 0; i < gp[cur].size() && !flag; i++){
   if(gp[cur][i] == 1 && !pass[i]){
      pass[i] = true;</pre>
              solution[i] = cur;
              hamilton(gp, k + 1, i, solution, pass,flag);
              pass[i] = false;
int main(){
     while(cin>>n){
         int a,b;
         bool end = false;
vector<vector<int>> gp(n+1,vector<int>(n+1,0));
         while(cin>>a>>b){
              if(a == 0 && b == 0)
                   break;
              gp[a][b] = 1;
              gp[b][a] = 1;
         vector<int> solution(n + 1, -1);
         vector<bool> pass(n + 1, false);
          solution[1] = 0;
         pass[1] = true;
         bool flag = false;
hamilton(gp, 1,1 ,solution,pass,flag);
         if(!flag)
              cout << "N" << endl;
     return 0;
output: 1 3 4 2 1
5.10 Kruskal
 *mst - Kruskal*/
```

```
struct edges{
     int from;
     int to;
     int weight;
     friend bool operator < (edges a, edges b){</pre>
          return a.weight > b.weight;
int find(int x,vector<int>& union_set){
     if(x != union_set[x])
    union_set[x] = find(union_set[x], union_set);
return union_set[x];
void merge(int a,int b,vector<int>& union_set){
     int pa = find(a, union_set);
int pb = find(b, union_set);
     if(pa != pb)
          union_set[pa] = pb;
void kruskal(priority_queue<edges> pq,int n){
     vector<int> union_set(n, 0);
for (int i = 0; i < n; i++)</pre>
          union_set[i] = i;
     int edge = 0;
int cost = 0; //evaluate cost of mst
     while(!pq.empty() && edge < n - 1){</pre>
          int from = find(cur.from, union_set);
int to = find(cur.to, union_set);
if(from != to){
               merge(from, to, union_set);
               edge += 1;
               cost += cur.weight;
          pq.pop();
     if(edge < n-1)
          cout << "No mst" << endl;</pre>
          cout << cost << endl;</pre>
int main(){
     cin >> n;
     int a, b, d;
     priority_queue<edges> pq;
     while(cin>>a>>b>>d){
```

```
if(a == -1 && b == -1 && d == -1)
                                                                                              p[i][j] = p[i][k];
             break;
        edges tmp;
         tmp.from = a;
                                                                                 }
        tmp.to = b;
        tmp.weight = d;
                                                                             if (weight == 1e9)
                                                                                 cout << "No exist";
        pq.push(tmp);
                                                                             else
    kruskal(pq, n);
                                                                                 bug(weight);
    return 0;
                                                                                 bug(c);
                                                                                 bugarr(cycle);
5.11 LCA
                                                                             }
                                                                        void simple_minimum_cycle(int n) // No use vector p
bool adj[9][9]; // adjacency matrix
bool visit[9]; // DFS當下已經拜訪過的點
                                                                             int weight = INF;
int lca[9][9]; // 所有兩點之間的LCA
                                                                             for (int k = 0; k < n; ++k)
                 // Disjoint-sets Forest
// 最多兩步
                                                                                 for (int i = 0; i < k; ++i)
                                                                                      for (int j = 0; j < k; ++j)
if (i != j)
int find(int x)
    return x == p[x] ? x : (p[x] = find(p[x]));
                                                                                              weight = min(mp[k][i] + d[i][j] + mp[j][k],
                                                                                                    weight);
int DFS(int x)
                                                                                 for (int i = 0; i < n; ++i)
    for (int j = 0; j < n; ++j)
        d[i][j] = min(d[i][k] + d[k][j], d[i][j]);</pre>
    if (visit[x])
         return;
    visit[x] = true;
    // 計算LCA
                                                                             if (weight == INF)
    cout << "Back to jail\n";</pre>
    for (int y = 0; y < 9; ++y)
         if (visit[y])
                                                                             else
                                                                                 cout << weight << endl;</pre>
             lca[x][y] = lca[y][x] = find(y);
    // DFS
                                                                        w.resize(n, vector<int>(n, INF));
d.resize(n, vector<int>(n, INF));
    for (int y = 0; y < 9; ++y)
    if (adj[x][y])</pre>
                                                                        p.resize(n, vector<int>(n));
             DFS(y);
                                                                        cycle.resize(n);
                                                                        //Edge input
             p[y] = x; // merge(y, x)·並讓x是樹根。
                                                                        w[a][b] = w;
                                                                        d[a][b] = w;
}
                                                                        p[a][b] = b;
                                                                        init(n);
void demo()
                                                                        minimum_cycle(n);
    for (int i = 0; i < 9; ++i)
                                                                        5.13 Prim
        p[i] = i;
    for (int i = 0; i < 9; ++i)
        visit[i] = false;
                                                                        /*mst - Prim*/
                                                                        #define inf 99999
    DFS(0); // 假設樹根為0
                                                                        struct edges
    int x, y;
    while (cin >> x >> y)
                                                                             int from;
        cout << "x點與y點的LCA是" << lca[x][y];
                                                                             int to;
}
                                                                             int weight;
                                                                             friend bool operator<(edges a, edges b)</pre>
5.12
       Minimum Weight Cycle
                                                                                 return a.weight > b.weight;
// 最小環
// 圖上無負環 !!!!
                                                                        void Prim(vector<vector<int>> gp, int n, int start)
#define INF 99999
vector<vector<int>> w, d, p;
                                                                             vector<bool> pass(n, false);
vector<int> cycle;
int c = 0;
                                                                             int edge = 0;
void trace(int i, int j)
                                                                             int cost = 0; //evaluate cost of mst
                                                                             priority_queue<edges> pq;
    cycle[c++] = i;
                                                                             for (int i = 0; i < n; i++)
    if (i != j)
                                                                                 if (gp[start][i] != inf)
        trace(p[i][j], j);
void init(int n)
                                                                                      edges tmp;
                                                                                      tmp.from = start;
    for (int i = 0; i < n; ++i)</pre>
                                                                                     tmp.to = i;
        d[i][i] = 0;
                                                                                     tmp.weight = gp[start][i];
                                                                                     pq.push(tmp);
void minimum_cycle(int n)
    int weight = 1e9;
                                                                             pass[start] = true;
    for (int k = 0; k < n; ++k)
                                                                             while (!pq.empty() && edge < n - 1)</pre>
        for (int i = 0; i < k; ++i)
  for (int j = 0; j < k; ++j)
    if (i != j)</pre>
                                                                                 edges cur = pq.top();
                                                                                 pq.pop();
                                                                                 if (!pass[cur.to])
                      if (w[k][i] + d[i][j] + w[j][k] < weight)
                                                                                      for (int i = 0; i < n; i++)
                          weight = w[k][i] + d[i][j] + w[j][k];
                                                                                          if (gp[cur.to][i] != inf)
                          c = 0:
                          trace(i, j);
                          cvcle[c++] = k;
                                                                                              edges tmp;
                                                                                              tmp.from = cur.to;
         for (int i = 0; i < n; ++i)
                                                                                              tmp.weight = gp[cur.to][i];
                                                                                              pq.push(tmp);
             for (int j = 0; j < n; ++j)</pre>
                                                                                          }
```

pass[cur.to] = true;

cost += cur.weight;

edge += 1;

if (d[i][k] + d[k][j] < d[i][j])</pre>

d[i][j] = d[i][k] + d[k][j];

5.14 Union_find

```
// union_find from 台大
vector<int> father;
vector<int> people;
void init(int n)
    father.clear();
    people.clear();
    father.resize(n);
    people.resize(n);
    for (int i = 0; i < n; i++)
        father[i] = i;
        people[i] = 1;
int Find(int x)
   if (x != father[x])
   father[x] = Find(father[x]);
    return father[x];
void Union(int x, int y)
    int m = Find(x);
    int n = Find(y);
    if (m != n)
        father[n] = m;
        people[m] += people[n];
```

6 Mathematics

6.1 Catalan

```
Catalan number
```

```
• 0~19項的catalan number \circ 1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 16796, 58786, \\ 208012, 742900, 2674440, 9694845, 35357670, 129644790, \\ 477638700, 1767263190 \\ \circ 公式: <math>C_n = \frac{1}{n+1} \binom{2n}{n} = \frac{(2n)!}{(n+1)!n!}
```

6.2 Combination

6.3 CRT

```
// 中國剩餘定理
template <typename T>
tuple<T, T, T> extgcd(T a, T b)
{
    if (!b)
```

6.4 Extended Euclidean

```
// ax + by = gcd(a,b)
pair<long long, long long> extgcd(long long a, long long b)
     if (b == 0)
     return {1, 0};
long long k = a / b;
pair<long long, long long> p = extgcd(b, a - k * b);
//cout << p.first << " " << p.second << endl;
//cout << "商數(k)= " << k << endl << endl;
     return {p.second, p.first - k * p.second};
}
int main()
     int a, b;
cin >> a >> b;
     return 0:
// ax + by = gcd(a,b) * r
/*find |x|+|y| -> min*/
 int main()
     long long r, p, q; /*px+qy = r*/
     int cases:
     cin >> cases:
     while (cases--)
          cin >> r >> p >> q;
         pair<long long, long long> xy = extgcd(q, p); //(x0,y0)
long long ans = 0, tmp = 0;
double k, k1;
long long s, s1;
k = 1 - (double)(r * xy.first) / p;
         s1 = round(k1);
          /*cout << k << endl << k1 << endl;
         cout << ans << endl;</pre>
     return 0;
}
```

6.5 Fermat

- $a^{(p-1)} \equiv 1 \pmod{p} \iff a * a^{(p-2)} \equiv 1$ • $a^{(p-2)} \equiv 1/a$
- 同餘因數定理

$$\circ \ a \equiv b \pmod{p} \iff k|a-b|$$

• 同餘加法性質

o
$$a \equiv b \pmod{p}$$
 and $c \equiv d \pmod{p}$
<=> $a + c \equiv b + d \pmod{p}$

• 同餘相乘性質

$$\circ \ a \equiv b \pmod{p}$$
 and $c \equiv d \pmod{p}$
 $<=> ac \equiv bd \pmod{p}$

• 同餘次方件質

$$\circ \ \ a \equiv b \ (mod \ p) \iff a^n \equiv b^n \ (mod \ p)$$

• 同餘倍方性質

```
\circ \ a \equiv b \pmod{p} \iff am \equiv bm \pmod{p}
```

6.6 Hex to Dec

```
int HextoDec(string num) //16 to 10
{
    int base = 1;
    int temp = 0;
    for (int i = num.length() - 1; i >= 0; i--)
    {
        if (num[i] >= '0' && num[i] <= '9')
        {
            temp += (num[i] - 48) * base;
            base = base * 16;
        }
        else if (num[i] >= 'A' && num[i] <= 'F')
        {
            temp += (num[i] - 55) * base;
            base = base * 16;
        }
    }
    return temp;
}
void DecToHex(int p) //10 to 16
{
    char *l = new (char);
    sprintf(l, "%X", p);
    //int l_intResult = stoi(l);
    cout << l << "\n";
    //return l_intResult;
}</pre>
```

$6.7 \quad \text{Log}$

```
| double mylog(double a, double base)
|{
| //a 的對數底數 b = 自然對數 (a) / 自然對數 (b)。
| return log(a) / log(base);
|}
```

6.8 Mod 性質

```
加法: (a+b) \mod p = (a \mod p + b \mod p) \mod p
減法: (a-b) \operatorname{mod} p = (a \operatorname{mod} p - b \operatorname{mod} p + p) \operatorname{mod} p
乘法: (a*b) \mod p = (a \mod p \cdot b \mod p) \mod p
次方: (a^b) \operatorname{mod} p = ((a \operatorname{mod} p)^b) \operatorname{mod} p
加法結合律: ((a+b) \operatorname{mod} p + c) \operatorname{mod} p = (a+(b+c)) \operatorname{mod} p
乘法結合律: ((a \cdot b) \mod p \cdot c) \mod p = (a \cdot (b \cdot c)) \mod p
加法交換律: (a+b) \mod p = (b+a) \mod p
乘法交換律: (a \cdot b) \mod p = (b \cdot a) \mod p
結合律: ((a+b) \operatorname{mod} p \cdot c) = ((a \cdot c) \operatorname{mod} p + (b \cdot c) \operatorname{mod} p) \operatorname{mod} p
如果 a \equiv b \pmod{m} ・我們會說 a, b 在模 m 下同餘。
以下為性質:
 ・ 整除性: a \equiv b \pmod{m} \Rightarrow c \cdot m = a - b, c \in \mathbb{Z}
              \Rightarrow a \equiv b \pmod{m} \Rightarrow m \mid a - b
  • 遞移性: 若a \equiv b \pmod{c}, b \equiv d \pmod{c}
               則 a \equiv d \pmod{c}

    保持基本運算:

         \left\{ \begin{aligned} a &\equiv b (\operatorname{mod} m) \\ c &\equiv d (\operatorname{mod} m) \end{aligned} \right. \Rightarrow \left\{ \begin{aligned} a &\pm c \equiv b \pm d (\operatorname{mod} m) \\ a \cdot c \equiv b \cdot d (\operatorname{mod} m) \end{aligned} \right.
      k \in \mathbb{Z}^+, a \equiv b \pmod{m} \Leftrightarrow k \cdot a \equiv k \cdot b \pmod{k \cdot m}
 模逆元是取模下的反元素,即為找到 a^{-1} 使得 aa^{-1}\equiv 1 \, \mathrm{mod} \, c 。
 整數 a \in \text{mod } c 下要有模反元素的充分必要條件為 a, c 互質。
 模逆元如果存在會有無限個,任意兩相鄰模逆元相差c。
 給定一個質數 p 及一個整數 a · 那麼: a^p \equiv a \pmod{p} 如果 \gcd(a,p) = 1 · 則:
 a^{p-1} \equiv 1 (\mod \, p)
 歐拉定理是比較 general 版本的費馬小定理。給定兩個整數 n 和 a · 如果 \gcd(a,n)=1 · 貝
 a^{\Phi(n)} \equiv 1 (\mod n) 如果 n 是質數 \cdot \Phi(n) = n-1 \cdot 也就是費馬小定理
 Wilson's theorem
 給定一個質數 p · 則 : (p-1)! \equiv -1 \pmod{p}
6.9 PI
#define PI acos(-1)
#define PI M PI
6.10 Pow Mod
int pow_mod(int a, int n, int m) // a ^ n mod m;
                                                             // a, n, m < 10 ^ 9
       if (n == 0)
              return 1;
       int x = pow_mid(a, n / 2, m);
long long ans = (long long)x * x % m;
if (n % 2 == 1)
    ans = ans * a % m;
return (int)ans;
int inv(int a, int n, int p) // n = p-2
       long long res = 1;
              (; n; n >>= 1, (a *= a) %= p)
if (n & 1)
                      (res *= a) %= p;
       return rès;
6.11 Prime table
const int maxn = 10e9:
vector<int> p;
bitset<maxn> is_notp;
void PrimeTable()
       is_notp.reset();
       is_notp[0] = is_notp[1] = 1;
for (int i = 2; i <= maxn; ++i)</pre>
```

if (!is_notp[i])

p.push_back(i);
for (int j = 0; j < (int)p.size(); ++j)</pre>

if (i * p[j] > maxn)
 break;
is_notp[i * p[j]] = 1;
if (i % p[j] == 0)

break;

```
}
```

6.12 Prime 判斷

```
typedef long long ll;
ll modmul(ll a, ll b, ll mod)
     11 ret = 0;
for (; b; b >>= 1, a = (a + a) % mod)
    if (b & 1)
               ret = (ret + a) % mod;
     return ret;
}
11 qpow(11 x, 11 u, 11 mod)
     ll ret = 111;
     for (; u; u >>= 1, x = modmul(x, x, mod))
    if (u & 1)
               ret = modmul(ret, x, mod);
     return ret;
ll gcd(ll a, ll b)
     return b ? gcd(b, a % b) : a;
11 Pollard_Rho(ll n, ll c)
     ll i = 1, j = 2, x = rand() % (n - 1) + 1, y = x;
     while (1)
          x = (modmul(x, x, n) + c) % n;
ll p = gcd((y - x + n) % n, n);
if (p != 1 && p != n)
               return p;
          if(y == x)
                return n;
          if (i == j)
               y = x;
j <<= 1;
          }
    }
bool Miller_Rabin(ll n)
     ll x, pre, u = n - 1;
int i, j, k = 0;
if (n == 2 || n == 3 || n == 5 || n == 7 || n == 11)
     return 1;

if (n == 1 || !(n % 2) || !(n % 3) || !(n % 5) || !(n % 7)

|| !(n % 11))
     while (!(u & 1))
          k++;
          u >>= 1;
     srand((long long)12234336);
for (i = 1; i <= 50; i++)</pre>
          x = rand() % (n - 2) + 2;
          if (!(n % x))
               return 0;
          x = qpow(x, u, n);
          pre = x;
for (j = 1; j <= k; j++)
               x = modmul(x, x, n);
if (x == 1 && pre != 1 && pre != n - 1)
                    return 0:
               pre = x;
          if (x != 1)
               return 0;
     return 1:
// if (Miller_Rabin(n)) puts("Prime");
```

6.13 Round(小數)

```
double myround(double number, unsigned int bits)
{
    LL integerPart = number;
    number -= integerPart;
    for (unsigned int i = 0; i < bits; ++i)
        number *= 10;
    number = (LL)(number + 0.5);
    for (unsigned int i = 0; i < bits; ++i)
        number /= 10;
    return integerPart + number;
}
//printf("%.1f\n", round(3.4515239, 1));</pre>
```

6.14 二分逼近法

```
#define eps 1e-14
void half_interval()
{

    double L = 0, R = /*區間*/, M;
    while (R - L >= eps)
    {

        M = (R + L) / 2;
        if (/*函數*/ > /*方程式目標*/)
            L = M;
        else
            R = M;
    }
    printf("%.31f\n", R);
}
```

6.15 公式

```
S_n = \frac{a(1-r^n)}{1-r} \ a_n = \frac{a_1+a_n}{2} \sum_{k=1}^n k = \frac{n(n+1)}{2} \sum_{k=1}^n k^2 = \frac{n(n+1)(2n+1)}{6}\sum_{k=1}^n k^3 = \left[\frac{n(n+1)}{2}\right]^2
```

6.16 四則運算

```
string s = ""; //開頭是負號要補0
long long int DFS(int le, int ri) // (0, string final index)
     for (int i = ri; i >= le; i--)
           if (s[i] == ')')
           if (s[i] == '(')
           if (s[i] == '+' && c == 0)
           return DFS(le, i - 1) + DFS(i + 1, ri);
if (s[i] == '-' && c == 0)
                return DFS(le, i - 1) - DFS(i + 1, ri);
     for (int i = ri; i >= le; i--)
           if (s[i] == ')')
           if (s[i] == '(')
           if (s[i] == '*' && c == 0)
    return DFS(le, i - 1) * DFS(i + 1, ri);
if (s[i] == '/' && c == 0)
           return DFS(le, i - 1) / DFS(i + 1, ri);
if (s[i] == '%' && c == 0)
return DFS(le, i - 1) % DFS(i + 1, ri);
     if ((s[le] == '(') && (s[ri] == ')'))
     return DFS(le + 1, ri - 1); //去除刮號
if (s[le] == ' ' && s[ri] == ' ')
     return DFS(le + 1, ri - 1); //去除左右兩邊空格
if (s[le] == ' ')
     return DFS(le + 1, ri); //去除左邊空格
if (s[ri] == ' ')
           return DFS(le, ri - 1); //去除右邊空格
     long long int num = 0;
     for (int i = le; i <= ri; i++)

num = num * 10 + s[i] - '0';
     return num;
```

6.17 因數表

```
| const int limit = 10000000;
| vector<vector<int>> arr(limit);
| for (int i = 1; i <= limit; i++)
| for (int j = i; j <= limit; j += i)
| arr[j].pb(i); // i 為因數
```

6.18 數字乘法組合

```
// ex tn = 2 * 2 * 3 => {2, 1}
              a.push back(num / i);
                                                                               {
                                                                                     // "2" 個 2, "1" 個 3
vector<int> fac;
              ans.push_back(a);
    }
                                                                                     for (auto pr : p)
vector<vector<int>> ans;
                                                                                          if (pr * pr > tn)
                                                                                               break;
vector<int> zero;
dfs(2, num, num, zero, ans);
/*/num 為 input 數字*/
                                                                                          if (tn % pr == 0)
for (int i = 0; i < ans.size(); i++)</pre>
                                                                                               int cc = 0;
                                                                                               while (tn \% pr == 0)
     for (int j = 0; j < ans[i].size() - 1; j++)
    cout << ans[i][j] << " ";</pre>
     cout << ans[i][ans[i].size() - 1] << endl;
                                                                                                   tn /= pr;
                                                                                               fac.push back(cc);
6.19 數字加法組合
                                                                                     if (tn > 1)
void recur(int i, int n, int m, vector<int> &out, vector<vector</pre>
                                                                                          fac.push_back(1);
     <int>> &ans)
                                                                                     return fac:
                                                                               }
     if (n == 0)
          for (int i : out)
                                                                                6.22 質數數量
              if (i > m)
                   return:
                                                                                // 10 ^ 11 左右
          ans.push_back(out);
                                                                                #define LL long long
                                                                                const int N = 5e6 + 2:
     for (int j = i; j <= n; j++)</pre>
                                                                                bool np[N];
          out.push_back(j);
                                                                                int prime[N], pi[N];
                                                                                int getprime()
          recur(j, n - j, m, out, ans);
out.pop_back();
                                                                                     int cnt = 0;
                                                                                     np[0] = np[1] = true;
pi[0] = pi[1] = 0;
for (int i = 2; i < N; ++i)</pre>
vector<vector<int>> ans:
vector<int> zero:
recur(1, num, num, zero, ans);
                                                                                          if (!np[i])
// num 為 input 數字
                                                                                              prime[++cnt] = i;
for (int i = 0; i < ans.size(); i++)</pre>
                                                                                          pi[i] = cnt;
                                                                                          for (int j = 1; j <= cnt && i * prime[j] < N; ++j)
     for (int j = 0; j < ans[i].size() - 1; j++)
    cout << ans[i][j] << " ";</pre>
     cout << ans[i][]] << " ";
cout << ans[i][ans[i].size() - 1] << endl;</pre>
                                                                                               np[i * prime[j]] = true;
                                                                                               if (i % prime[j] == 0)
}
                                                                                         }
6.20 羅馬數字
                                                                                     }
                                                                                     return cnt;
int romanToInt(string s)
                                                                                const int M = 7;
const int PM = 2 * 3 * 5 * 7 * 11 * 13 * 17;
     unordered_map<char, int> T;
     T['I'] = 1;
T['V'] = 5;
                                                                                int phi[PM + 1][M + 1], sz[M + 1];
                                                                                void init()
    T['V'] = 5;
T['X'] = 10;
T['L'] = 50;
T['C'] = 100;
T['D'] = 500;
                                                                                     getprime();
                                                                                     sz[0] = 1;
for (int i = 0; i <= PM; ++i)</pre>
     T['M'] = 1000;
                                                                                        phi[i][0] = i;
                                                                                     for (int i = 1; i <= M; ++i)
     int sum = T[s.back()];
                                                                                          sz[i] = prime[i] * sz[i - 1];
for (int j = 1; j <= PM; ++j)
    phi[j][i] = phi[j][i - 1] - phi[j / prime[i]][i -</pre>
     for (int i = s.length() - 2; i >= 0; --i)
          if (T[s[i]] < T[s[i + 1]])
              sum -= T[s[i]];
          else
                                                                                     }
              sum += T[s[i]];
                                                                                int sqrt2(LL x)
     return sum;
}
                                                                                     LL r = (LL) sqrt(x - 0.1);
                                                                                     while (r * r <= x)
          質因數分解
                                                                                         ++r;
6.21
                                                                                     return int(r - 1);
vector<int> primeFactorization(int tn) // 配合質數表
                                                                                int sqrt3(LL x)
                                               //重複 or 不重複擇一
{
     vector<int> f:
                                                                                     LL r = (LL)cbrt(x - 0.1);
while (r * r * r <= x)
     f.clear();
     int n = tn:
                                                                                         ++r;
     for (int i = 0; i < (int)p.size(); ++i)</pre>
                                                                                     return int(r - 1);
          if (p[i] * p[i] > n)
                                                                                LL getphi(LL x, int s)
          if (n % p[i])
                                                                                     if (s == 0)
              continue;
                                                                                          return x;
          // f.pb(p[i]); //不重複
                                                                                     if (s <= M)
          while (n \% p[i] == 0)
                                                                                     return phi[x % sz[s]][s] + (x / sz[s]) * phi[sz[s]][s];
if (x <= prime[s] * prime[s])
    return pi[x] - s + 1;</pre>
              n /= p[i];
              // f.pb(p[i]); //重複
                                                                                     if (x <= prime[s] * prime[s] * prime[s] && x < N)</pre>
                                                                                          int s2x = pi[sqrt2(x)];
                                                                                          LL ans = pi[x] - (s2x + s - 2) * (s2x - s + 1) / 2;
for (int i = s + 1; i <= s2x; ++i)
     if (n != 1)
          f.pb(n);
     return f;
                                                                                              ans += pi[x / prime[i]];
```

return ans;

| vector<int> factorcount(int tn) // 質因數個數

```
return getphi(x, s - 1) - getphi(x / prime[s], s - 1);
LL getpi(LL x)
     if(x < N)
          return pi[x];
     LL ans = getphi(x, pi[sqrt3(x)]) + pi[sqrt3(x)] - 1;
for (int i = pi[sqrt3(x)] + 1, ed = pi[sqrt2(x)]; i <= ed;
           ans -= getpi(x / prime[i]) - i + 1;
     return ans;
LL lehmer_pi(LL x)
     if(x < N)
          return pi[x];
     int a = (int)lehmer_pi(sqrt2(sqrt2(x)));
     int b = (int)lehmer_pi(sqrt2(x));
     int c = (int)lehmer_pi(sqrt3(x));
LL sum = getphi(x, a) + (LL)(b + a - 2) * (b - a + 1) / 2;
for (int i = a + 1; i <= b; i++)</pre>
          LL w = x / prime[i];
           sum -= lehmer_pi(w);
          if (i > c)
                continue:
          LL lim = lehmer_pi(sqrt2(w));
for (int j = i; j <= lim; j++)
                sum -= lehmer_pi(w / prime[j]) - (j - 1);
     return sum;
}
// lehmer_pi(n)
```

7 Other

7.1 Binary search 三類變化

```
// 查找和目標值完全相等的數
int find(vector<int> &nums, int target)
    int left = 0, right = nums.size() - 1;
   while (left < right)</pre>
        int mid = left + (right - left) / 2;
        if (nums[mid] == target)
            return mid;
        else if (nums[mid] < target)</pre>
           left = mid + 1;
        else
            right = mid;
   return -1;
// 找第一個不小於目標值的數 == 找最後一個小於目標值的數
/*(lower_bound)*/
int find(vector<int> &nums, int target)
   int left = 0, right = nums.size() - 1;
while (left < right)</pre>
        int mid = left + (right - left) / 2;
        if (nums[mid] < target)</pre>
            left = mid + 1;
        else
            right = mid;
   return right;
·
// 找第一個大於目標值的數 == 找最後一個不大於目標值的數
/*(upper_bound)*/
int find(vector<int> &nums, int target)
   int left = 0, right = nums.size() - 1;
   while (left < right)
    {
        int mid = left + (right - left) / 2;
        if (nums[mid] <= target)</pre>
           left = mid + 1;
        else
           right = mid;
   return right;
```

7.2 Heap sort

```
void MaxHeapify(vector<int> &array, int root, int length)
{
   int left = 2 * root, right = 2 * root + 1, largest;
   if (left <= length && array[left] > array[root])
        largest = left;
   else
        largest = root;
```

7.3 Josephus

```
/*n people kill k for each turn*/
int josephus(int n, int k)
{
    int s = 0;
    for (int i = 2; i <= n; i++)
    {
        s = (s + k) % i;
    }
    /*index start from 1 -> s+1*/
    return s + 1;
}

/*died at kth*/
int kth(int n, int m, int k)
{
    if (m == 1)
        return n - 1;
    for (k = k * m + m - 1; k >= n; k = k - n + (k - n) / (m - 1))
        ;
    return k;
}
```

7.4 Largest Multi-interval

7.5 Merge sort

```
long long merge(vector<int> &arr, int left, int mid, int right)
{
    int *tmp = new int[right - left + 1];
    long long sum = 0;
    int l = left, r = mid + 1, m = 0;
    while (l <= mid && r <= right)
    {
        if (arr[1] <= arr[r])
            tmp[m++] = arr[l++];
        else
        {
            tmp[m++] = arr[r++];
            sum += mid - l + 1;
        }
    }
    while (l <= mid)
        tmp[m++] = arr[l++];
    while (r <= right)
        tmp[m++] = arr[r++];
    for (int i = left; i <= right; ++i)
        arr[i] = tmp[i - left];</pre>
```

```
delete[] tmp;
  return sum;
}
long long mergesort(vector<int> &arr, int left, int right)
{
  long long sum = 0;
  // left = 0, right = P.size() - 1
  if (left < right)
  {
    int mid = (left + right) / 2;
    sum = mergesort(arr, left, mid);
    sum += mergesort(arr, mid + 1, right);
    sum += merge(arr, left, mid, right);
}
return sum; // 回傳為 swap 次數
}</pre>
```

7.6 N Queen problem

```
#define N 18
void printSolution(vector<vector<int>> &board)
     for (int i = 0; i < N; i++)
          for (int j = 0; j < N; j++)
    printf(" %d ", board[i][j]);</pre>
          printf("\n");
bool isSafe(vector<vector<int>> &board, int row, int col)
    int i, j;
/* Check this row on left side */
     for (i = 0; i < col; i++)
          if (board[row][i])
               return false;
     /* Check upper diagonal on left side */ for (i = row, j = col; i >= 0 && j >= 0; i--, j--)
          if (board[i][j])
              return false;
    /* Check lower diagonal on left side */
for (i = row, j = col; j >= 0 && i < N; i++, j--)
    if (board[i][j])
              return false:
    return true:
bool solveNQUtil(vector<vector<int>> &board, int col)
    if (col >= N)
          return true;
     for (int i = 0; i < N; i++)
          if (isSafe(board, i, col))
              /* recur to place rest of the queens */
if (solveNQUtil(board, col + 1))
                    return true;
              board[i][col] = 0; // BACKTRACK
     return false;
bool solveNQ()
    vector<vector<int>> board(N, vector<int>(N, 0));
    if (solveNQUtil(board, 0) == false)
          printf("Solution does not exist");
          return false;
    printSolution(board);
    return true;
```

7.7 Quick sort

```
int Partition(vector<int> &arr, int front, int end)
{
    int pivot = arr[end];
    int i = front - 1;
    for (int j = front; j < end; j++)
    {
        if (arr[j] < pivot)
        {
            i++;
            swap(arr[i], arr[j]);
        }
     }
    i++;
    swap(arr[i], arr[end]);
    return i;
}
void QuickSort(vector<int> &arr, int front, int end)
{
    // front = 0 , end = arr.size() - 1
```

```
if (front < end)
{
    int pivot = Partition(arr, front, end);
    QuickSort(arr, front, pivot - 1);
    QuickSort(arr, pivot + 1, end);
}</pre>
```

7.8 Sudoku solution

```
/*數獨解法*/
int getSquareIndex(int row, int column, int n)
    return row / n * n + column / n;
}
bool backtracking(vector<vector<int>> &board, vector<vector<</pre>
     bool>> &rows, vector<vector<bool>> &cols,
                   vector<vector<bool>> &boxs, int index, int n)
    int n2 = n * n;
    int rowNum = index / n2, colNum = index % n2;
    if (index >= n2 * n2)
        return true;
    if (board[rowNum][colNum] != 0)
         return backtracking(board, rows, cols, boxs, index + 1,
              n);
    for (int i = 1; i <= n2; i++)
        if (!rows[rowNum][i] && !cols[colNum][i] && !boxs[
             getSquareIndex(rowNum, colNum, n)][i])
             rows[rowNum][i] = true;
             cols[colNum][i] = true;
             boxs[getSquareIndex(rowNum, colNum, n)][i] = true;
             board[rowNum][colNum] = i;
             if (backtracking(board, rows, cols, boxs, index +
                 1, n))
                 return true:
             board[rowNum][colNum] = 0;
             rows[rowNum][i] = false;
             cols[colNum][i] = false;
             boxs[getSquareIndex(rowNum, colNum, n)][i] = false;
        }
    return false;
/*用法 main*/
int n = sqrt(數獨邊長大小) /*e.g. 9*9 n=3*/
vector<vector<int>> board(n * n + 1, vector<int>(n * n + 1, 0))
vector<vector<bool>> isRow(n * n + 1, vector<bool>(n * n + 1,
vector<vector<bool>> isColumn(n * n + 1, vector<bool>(n * n +
     1, false));
vector<vector<bool>> isSquare(n * n + 1, vector<bool>(n * n +
     1, false));
for (int i = 0; i < n * n; ++i)
    for (int j = 0; j < n * n; ++j)
        int number;
        cin >> number;
        board[i][j] = number;
        if (number
                   == 0)
             continue;
        isRow[i][number] = true;
        isColumn[j][number] = true;
isSquare[getSquareIndex(i, j, n)][number] = true;
if (backtracking(board, isRow, isColumn, isSquare, 0, n))
else
    /*無解答*/
```

7.9 Weighted Job Scheduling

```
struct Job
{
    int start, finish, profit;
};
bool jobComparataor(Job s1, Job s2)
{
    return (s1.finish < s2.finish);
}
int latestNonConflict(Job arr[], int i)
{
    for (int j = i - 1; j >= 0; j--)
    {
        if (arr[j].finish <= arr[i].start)
            return j;</pre>
```

```
}
return -1;
}
int findMaxProfit(Job arr[], int n)
{
    sort(arr, arr + n, jobComparataor);
    int *table = new int[n];
    table[0] = arr[0].profit;
    for (int i = 1; i < n; i++)
{
        int inclProf = arr[i].profit;
        int 1 = latestNonConflict(arr, i);
        if (l != -1)
            inclProf += table[1];
        table[i] = max(inclProf, table[i - 1]);
    }
    int result = table[n - 1];
    delete[] table;
    return result;
}</pre>
```

8 String

8.1 KMP

```
// 用在在一個 S 內查找一個詞 W 的出現位置
void ComputePrefix(string s, int next[])
    int n = s.length();
    int q, k;
next[0] = 0;
    for (k = 0, q = 1; q < n; q++)
        while (k > 0 \&\& s[k] != s[q])
             k = next[k]:
        if (s[k] == \overline{s[q]})
         next[q] = k;
void KMPMatcher(string text, string pattern)
    int n = text.length();
    int m = pattern.length()
    int next[pattern.length()];
    ComputePrefix(pattern, next);
    for (int i = 0, q = 0; i < n; i++)
         while (q > 0 && pattern[q] != text[i])
            q = next[q];
         if (pattern[q] == text[i])
        q++;
if (q == m)
        {
             cout << "Pattern occurs with shift " << i - m + 1</pre>
                  << endl;
             q = 0;
        }
    }
// string s = "abcdabcdebcd";
// string p = "bcd";
// KMPMatcher(s, p);
// cout << endl:
```

8.2 Min Edit Distance

8.3 Sliding window

```
string minWindow(string s, string t)
     unordered_map<char, int> letterCnt;
    for (int i = 0; i < t.length(); i++)
    letterCnt[t[i]]++;
int minLength = INT_MAX, minStart = -1;</pre>
     int left = 0, matchCnt = 0;
     for (int i = 0; i < s.length(); i++)</pre>
         if (--letterCnt[s[i]] >= 0)
               matchCnt++
          while (matchCnt == t.length())
               if (i - left + 1 < minLength)</pre>
               {
                   minLength = i - left + 1;
minStart = left;
               if (++letterCnt[s[left]] > 0)
                    matchCnt--;
               left++;
     return minLength == INT_MAX ? "" : s.substr(minStart,
          minLength);
```

8.4 Split

```
vector<string> mysplit(const string& str, const string& delim)
{
   vector<string> res;
   if ("" == str)
        return res;

   char *strs = new char[str.length() + 1];
   strcpy(strs, str.c_str());

   char *d = new char[delim.length() + 1];
   strcpy(d, delim.c_str());

   char *p = strtok(strs, d);
   while (p)
   {
      string s = p;
      res.push_back(s);
      p = strtok(NULL, d);
   }
   return res;
```

9 data structure

9.1 Bigint

```
//台大 //非必要請用python
struct Bigint
    static const int LEN = 60;
                                      // maxLEN
    static const int BIGMOD = 10000; //10為正常位數
    int s;
    int v1, v[LEN];
// vector<int> v;
    Bigint() : s(1) { vl = 0; }
    Bigint(long long a)
        s = 1:
        v1 = 0;
        if (a < 0)
            s = -1;
        while (a)
        {
            push back(a % BIGMOD);
            a /= BIGMOD;
    Bigint(string str)
        s = 1;
        v1 = 0;
        int stPos = 0, num = 0;
        if (!str.empty() && str[0] == '-')
            stPos = 1
            s = -1;
        for (int i = str.length() - 1, q = 1; i >= stPos; i--)
            num += (str[i] - '0') * q;
```

```
if ((q *= 10) >= BIGMOD)
              push_back(num);
              q = 1;
         }
    if (num)
         push_back(num);
    n();
int len() const
    return vl; //return SZ(v);
bool empty() const { return len() == 0; }
void push_back(int x)
    v[vl++] = x; //v.PB(x);
void pop_back()
    vl--; //v.pop_back();
int back() const
    return v[vl - 1]; //return v.back();
void n()
     while (!empty() && !back())
         pop_back();
void resize(int nl)
     v1 = n1;
                            //v.resize(nl);
    fill(v, v + vl, 0); //fill(ALL(v), 0);
void print() const
    if (empty())
         putchar('0');
         return;
     if (s == -1)
         putchar('-');
    printf("%d", back());
for (int i = len() - 2; i >= 0; i--)
    printf("%.4d", v[i]);
}
friend std::ostream &operator<<(std::ostream &out, const</pre>
     Bigint &a)
     if (a.empty())
         out << "0";
         return out:
    if (a.s == -1)
out << "-"
     out << a.back();
     for (int i = a.len() - 2; i >= 0; i--)
         char str[10];
         sprintf(str, 5, "%.4d", a.v[i]);
         out << str;
     return out;
int cp3(const Bigint &b) const
    if (s != b.s)
         return s - b.s;
    if (s == -1)
    return -(-*this).cp3(-b);
if (len() != b.len())
     return len() - b.len(); //int
for (int i = len() - 1; i >= 0; i--)
    if (v[i] != b.v[i])
              return v[i] - b.v[i];
     return 0;
bool operator<(const Bigint &b) const
{
     return cp3(b) < 0;</pre>
bool operator<=(const Bigint &b) const
{
     return cp3(b) <= 0;</pre>
bool operator==(const Bigint &b) const
{
     return cp3(b) == 0;
bool operator!=(const Bigint &b) const
```

```
return cp3(b) != 0;
bool operator>(const Bigint &b) const
    return cp3(b) > 0;
bool operator>=(const Bigint &b) const
    return cp3(b) >= 0;
Bigint operator-() const
    Bigint r = (*this);
    r.s = -r.s;
    return r;
Bigint operator+(const Bigint &b) const
    if (s == -1)
    return -(-(*this) + (-b));
if (b.s == -1)
         return (*this) - (-b);
    Bigint r;
    int nl = max(len(), b.len());
    r.resize(nl + 1);
for (int i = 0; i < nl; i++)
         if (i < len())</pre>
              r.v[i] +=
         if (i < b.len())</pre>
         r.v[i] += b.v[i];
if (r.v[i] >= BIGMOD)
             r.v[i + 1] += r.v[i] / BIGMOD;
             r.v[i] %= BIGMOD;
    r.n();
    return r:
Bigint operator-(const Bigint &b) const
    if (s == -1)
    return -(-(*this) - (-b));
if (b.s == -1)
         return (*this) + (-b);
    if ((*this) < b)</pre>
         return -(b - (*this));
    Bigint r;
r.resize(len());
for (int i = 0; i < len(); i++)</pre>
         r.v[i] += v[i];
         if (i < b.len())</pre>
             r.v[i] -= b.v[i];
         if (r.v[i] < 0)</pre>
             r.v[i] += BIGMOD;
             r.v[i + 1]--;
    r.n();
    return r;
Bigint operator*(const Bigint &b)
    Bigint r;
    r.resize(len() + b.len() + 1);
r.s = s * b.s;
    for (int i = 0; i < len(); i++)</pre>
         for (int j = 0; j < b.len(); j++)</pre>
             r.v[i + j] += v[i] * b.v[j];
              if (r.v[i + j] >= BIGMOD)
                  r.v[i + j + 1] += r.v[i + j] / BIGMOD;
                  r.v[i + j] %= BIGMOD;
         }
    r.n();
    return r;
Bigint operator/(const Bigint &b)
    Bigint r:
    r.resize(max(1, len() - b.len() + 1));
    int oriS = s;
    Bigint b2 = b; // b2 = abs(b)
s = b2.s = r.s = 1;
    for (int i = r.len() - 1; i >= 0; i--)
         int d = 0, u = BIGMOD - 1;
while (d < u)</pre>
             int m = (d + u + 1) >> 1;
```

```
r.v[i] = m;
    if ((r * b2) > (*this))
        u = m - 1;
    else
        d = m;
    }
    r.v[i] = d;
}
s = oris;
r.s = s * b.s;
r.n();
return r;
}
Bigint operator%(const Bigint &b)
{
    return (*this) - (*this) / b * b;
}
};
```

9.2 DisjointSet

```
struct DisjointSet {
    int p[maxn], sz[maxn], n, cc;
vector<pair<int*, int>> his;
    vector<int> sh;
     void init(int _n) {
         n = _n; cc = n;
for (int i = 0; i < n; ++i) sz[i] = 1, p[i] = i;
          sh.clear(); his.clear();
    void assign(int *k, int v) {
    his.emplace_back(k, *k);
         *k = v;
    void save() {
         sh.push_back((int)his.size());
    void undo() {
   int last = sh.back(); sh.pop_back();
          while (his.size() != last) {
              int *k, v;
              tie(k, v) = his.back(); his.pop_back();
               *k = v;
         }
    int find(int x) {
         if (x == p[x]) return x;
return find(p[x]);
    assign(&sz[y], sz[x] + sz[y]);
assign(&p[x], y);
assign(&cc, cc - 1);
```

9.3 Matirx

```
template <typename T>
struct Matrix
       using rt = std::vector<T>;
using mt = std::vector<rt>;
using matrix = Matrix<T>;
       int r, c; // [r][c]
       Matrix(int r, int c) : r(r), c(c), m(r, rt(c)) {}
Matrix(mt a) { m = a, r = a.size(), c = a[0].size(); }
rt & operator[](int i) { return m[i]; }
matrix operator+(const matrix &a)
              matrix rev(r, c);
for (int i = 0; i < r; ++i)
    for (int j = 0; j < c; ++j)</pre>
                            rev[i][j] = m[i][j] + a.m[i][j];
              return rev:
       matrix operator-(const matrix &a)
              matrix rev(r, c);
for (int i = 0; i < r; ++i)
    for (int j = 0; j < c; ++j)
        rev[i][j] = m[i][j] - a.m[i][j];</pre>
              return rev;
       matrix operator*(const matrix &a)
              matrix rev(r, a.c);
              matrix tmp(a.c, a.r);
for (int i = 0; i < a.r; ++i)
                     for (int j = 0; j < a.c; ++j)
    tmp[j][i] = a.m[i][j];</pre>
               for (int i = 0; i < r; ++i)
```

```
for (int j = 0; j < a.c; ++j)
    for (int k = 0; k < c; ++k)</pre>
                           rev.m[i][j] += m[i][k] * tmp[j][k];
      bool inverse() //逆矩陣判斷
           Matrix t(r, r + c);
for (int y = 0; y < r; y++)</pre>
                 t.m[y][c + y] = 1;
for (int x = 0; x < c; ++x)
                     t.m[y][x] = m[y][x];
           if (!t.gas())
           return false;

for (int y = 0; y < r; y++)

    for (int x = 0; x < c; ++x)

        m[y][x] = t.m[y][c + x] / t.m[y][y];
      T gas() //行列式
            vector<T> lazy(r, 1);
           bool sign = false:
            for (int i = 0; i < r; ++i)
                 if (m[i][i] == 0)
                      int j = i + 1;
while (j < r && !m[j][i])</pre>
                            j++;
                      if (j = r)
                           continue
                      m[i].swap(m[j]);
                      sign = !sign;
                 for (int j = 0; j < r; ++j)
                      if (i == j)
                            continue;
                      lazy[j] = lazy[j] * m[i][i];
                      T mx = m[j][i];
for (int k = 0; k < c; ++k)
    m[j][k] = m[j][k] * m[i][i] - m[i][k] * mx;</pre>
            T det = sign ? -1 : 1;
            for (int i = 0; i < r; ++i)
                 det = det * m[i][i];
                 det = det / lazy[i];
                 for (auto &j : m[i])
                      j /= lazy[i];
            return det;
      }
};
```

9.4 分數

```
typedef long long 11;
struct fraction
{
  11 n, d;
  fraction(const 11 \& n = 0, const 11 \& d = 1): n(n), d(d)
    11 t = __gcd(n,
n /= t, d /= t;
if (d < 0)</pre>
             gcd(n, d);
      n = -n, d = -d;
  fraction operator-() const
    return fraction(-n, d);
  fraction operator+(const fraction &b) const
    return fraction(n * b.d + b.n * d, d * b.d);
  fraction operator-(const fraction &b) const
    return fraction(n * b.d - b.n * d, d * b.d);
  fraction operator*(const fraction &b) const
    return fraction(n * b.n, d * b.d);
  fraction operator/(const fraction &b) const
    return fraction(n * b.d, d * b.n);
  void print()
  {
    cout << n;
    if (d != 1)
```

```
cout << "/" << d; };
```