# 1 Basic

# 1.1 Basic codeblock setting

# 1.2 Basic vim setting

```
1  /*at home directory*/
2  /* vi ~/.vimrc */
3  syntax enable
4  set smartindent
5  set tabstop=4
6  set shiftwidth=4
7  set expandtab
8  set relativenumber
```

# 1.3 Code Template

```
1 #include <bits/stdc++.h>
using namespace std;
3 typedef long long 11;
4 typedef unsigned long long ull;
5 typedef pair<int, int> pii;
6 #define x first
7 #define y second
8 #define pb push_back
9 #define len length()
#define all(p) p.begin(), p.end()
11 #define endl '\n'
12 #define bug(x) cout << "value of " << #x <<
       " is " << x << endl;
13 #define bugarr(x)
      for (auto i : x)
           cout << i << ' '; \
      cout << endl;</pre>
  int main()
18
       ios::sync_with_stdio(0);
      cin.tie(0);
      return 0;
```

# 1.4 Python

```
1 | // 輸入
 2 import sys
 3 line = sys.stdin.readline() // 會讀到換行
 4 input().strip()
 7 \mid \text{range}(0, N) // 0 \sim N-1
 s \mid D, R, N = map(int, line[:-1].split()) // \mathcal{D}
        三個 int 變數
10 pow(a, b, c) // a ^ b % c
12 print(*objects, sep = ' ', end = '\n')
13 // objects -- 可以一次輸出多個對象
14 // sep -- 分開多個objects
15 // end -- 默認值是\n
   // EOF break
17
18 try:
      while True:
           //input someithing
20
21 except EOFError:
       pass
```

# 1.5 Range data

```
int (-2147483648 to 2147483647)
unsigned int(0 to 4294967295)
long(-2147483648 to 2147483647)
unsigned long(0 to 4294967295)
long long(-9223372036854775808 to 9223372036854775807)
unsigned long long (0 to
18446744073709551615)
```

#### 1.6 Some Function

```
// 四捨五入
1 | round(double f);
                            // 進入
2 | ceil(double f);
3 floor(double f);
                            //捨去
   builtin popcount(int n); // 32bit有多少 1
  to string(int s);
                            // int to string
 7 / /** 全排列要先 sort !!! **/
8 next_permutation(num.begin(), num.end());
9 prev_permutation(num.begin(), num.end());
10 //用binary search找大於或等於val的最小值的位
11 vector<int>::iterator it = lower_bound(v.
       begin(), v.end(), val);
12 //用binary search找大於val的最小值的位置
13 vector<int>::iterator it = upper bound(v.
       begin(), v.end(), val);
14 /*queue*/
```

```
16 queue < datatype > q;
17 front(); /*取出最前面的值(沒有移除掉)*/
18 | back(); /*取出最後面的值(沒有移除掉)*/
19 pop(); /*移掉最前面的值*/
20 push(); /*新增值到最後面*/
21 empty(); /*回傳bool,檢查是不是空的queue*/
22 size(); /*queue 的大小*/
24 /*stack*/
25 stack<datatype> s;
26 | top(); /*取出最上面的值(沒有移除掉)*/
27 pop(); /*移掉最上面的值*/
28 push(); /*新增值到最上面*/
29 empty(); /*bool 檢查是不是空*/
30 | size(); /*stack 的大小*/
32 /*unordered set*/
33 unordered set<datatype> s;
34 unordered set<datatype> s(arr, arr + n);
35 /*initial with array*/
36 insert(); /*插入值*/
37 erase(); /*刪除值*/
38 empty(); /*bool 檢查是不是空*/
39 count(); /*判斷元素存在回傳1 無則回傳0*/
```

# 1.7 Time

```
1 cout << 1.0 * clock() / CLOCKS_PER_SEC << endl;</pre>
```

# 2 DP

# 2.1 3 維 DP 思路

```
1 | 解題思路: dp[i][j][k]
2 | i 跟 j 代表 range i ~ j 的 value
3 | k在我的理解裡是視題目的要求而定的
4 | 像是 Remove Boxes 當中 k 代表的是在 i 之前還有多少個連續的箱子
5 | 所以每次區間消去的值就是(k+1) * (k+1)
6 | 换言之·我認為可以理解成 k 的意義就是題目今天所關注的重點·就是老師說的題目所規定的運算
```

# 2.2 Knapsack Bounded

```
const int N = 100, W = 100000;
int cost[N], weight[N], number[N];
int c[W + 1];
void knapsack(int n, int w)
{
```

```
for (int i = 0; i < n; ++i)
           int num = min(number[i], w / weight[
           for (int k = 1; num > 0; k *= 2)
11
               if (k > num)
                    k = num;
12
13
               num -= k;
               for (int j = w; j >= weight[i] *
14
                      k; --j)
                    c[j] = max(c[j], c[j -
15
                         weight[i] * k] + cost[i]
                          * k);
16
17
       cout << "Max Prince" << c[w];</pre>
18
19
```

# 2.3 Knapsack sample

```
int Knapsack(vector<int> weight, vector<int>
        value, int bag_Weight)
       // vector<int> weight = {1, 3, 4};
      // vector<int> value = {15, 20, 30};
      // int bagWeight = 4;
      vector<vector<int>> dp(weight.size(),
           vector<int>(bagWeight + 1, 0));
       for (int j = weight[0]; j <= bagWeight;</pre>
           dp[0][j] = value[0];
      // weight數組的大小就是物品個數
      for (int i = 1; i < weight.size(); i++)</pre>
      { // 遍歷物品
           for (int j = 0; j <= bagWeight; j++)</pre>
          { // 遍歷背包容量
               if (j < weight[i]) dp[i][j] = dp</pre>
                    [i - 1][j];
               else dp[i][j] = max(dp[i - 1][j]
                   ], dp[i - 1][j - weight[i]]
                   + value[i]);
16
      cout << dp[weight.size() - 1][bagWeight]</pre>
            << endl;
```

# 2.4 Knapsack Unbounded

```
const int N = 100, W = 100000;
int cost[N], weight[N];
int c[W + 1];
void knapsack(int n, int w)
{
    memset(c, 0, sizeof(c));
    for (int i = 0; i < n; ++i)
    for (int j = weight[i]; j <= w; ++j)</pre>
```

```
2.10 Money problem
               c[j] = max(c[j], c[j - weight[i
                                                        vector<string> k:
                                                                                                             if (i != ans.size() - 1)
                                                        while (n && m)
                                                                                                                  cout << ' ';
                    11 + cost[i]);
                                                 19
                                                                                                  39
       cout << "最高的價值為" << c[w];
                                                 20
                                                                                                   40
                                                            if (LCS[n][m] != max(LCS[n - 1][m],
                                                                                                         cout << '\n';
                                                 21
                                                                                                  41
11 }
                                                                 LCS[n][m - 1]))
                                                 22
                                                 23
                                                                k.push back(Ans[n - 1]);
                                                                                                                                                     1 / / 能否湊得某個價位
                                                 24
  2.5 LCIS
                                                                n--;
                                                                                                                                                     void change(vector<int> price, int limit)
                                                 25
                                                                                                     2.8 LPS
                                                 26
                                                                                                                                                           vector<bool> c(limit + 1, 0);
                                                 27
                                                            else if (LCS[n][m] == LCS[n - 1][m])
int LCIS len(vector<int> arr1, vetor<int>
                                                                                                                                                           c[0] = true;
                                                                                                   1 | void LPS(string s)
                                                                                                                                                           for (int i = 0; i < price.size(); ++i)</pre>
                                                            else if (LCS[n][m] == LCS[n][m - 1])
                                                 29
                                                                                                                                                                     // 依序加入各種面額
                                                 30
       int n = arr1.size(), m = arr2.size();
                                                                                                         int maxlen = 0, 1, r;
                                                                                                                                                               for (int j = price[i]; j <= limit;</pre>
                                                 31
       vector<int> table(m, 0);
                                                                                                         int n = n:
                                                 32
                                                        reverse(k.begin(), k.end());
                                                                                                                                                                    ++i) // 由低價位逐步到高價位
      for (int j = 0; j < m; j++)
                                                                                                         for (int i = 0; i < n; i++)
                                                        for (auto i : k)
                                                 33
                                                                                                                                                                   c[j] = c[j] | c[j - price[i]];
          table[j] = 0;
                                                            cout << i << " ":
                                                 34
                                                                                                                                                                            // 湊、湊、湊
       for (int i = 0; i < n; i++)
                                                                                                             int x = 0:
                                                        cout << endl:
                                                 35
                                                                                                                                                           if (c[limit]) cout << "YES\n";</pre>
                                                                                                              while ((s[i - x] == s[i + x]) \&\& (i
                                                        return LCS[N][M];
                                                 36
                                                                                                                                                           else cout << "NO\n";</pre>
           int current = 0;
                                                                                                                  -x >= 0) && (i + x < n)) //odd
           for (int j = 0; j < m; j++)
                                                                                                                  length
                                                                                                                                                    12 // 湊得某個價位的湊法總共幾種
                                                                                                                  x++;
                                                                                                                                                       void change(vector<int> price, int limit)
                                                                                                   10
               if (arr1[i] == arr2[j])
                                                                                                   11
                                                                                                              if (2 * x + 1 > maxlen)
                                                    2.7 LIS
                                                                                                                                                           vector<int> c(limit + 1, 0);
                   if (current + 1 > table[j])
                                                                                                   12
                                                                                                                                                           c[0] = true;
                       table[i] = current + 1:
                                                                                                   13
                                                                                                                  maxlen = 2 * x + 1;
                                                                                                                                                           for (int i = 0; i < price.size(); ++i)</pre>
                                                                                                                 l = i - x;
                                                  1 | vector<int> ans:
                                                                                                                                                               for (int j = price[i]; j <= limit;</pre>
               if (arr1[i] > arr2[j])
                                                                                                                  r = i + x:
                                                  void printLIS(vector<int> &arr, vector<int>
                   if (table[j] > current)
                                                                                                             }
                                                                                                   16
                                                         &pos, int index)
                                                                                                                                                                   c[j] += c[j - price[i]];
19
                       current = table[j];
                                                                                                   17
20
                                                                                                                                                           cout << c[limit] << '\n';</pre>
                                                                                                              while ((s[i - x] == s[i + 1 + x]) \&\&
                                                                                                   18
                                                        if (pos[index] != -1)
21
                                                                                                                   (i - x >= 0) \&\& (i + 1 + x < n)
                                                            printLIS(arr, pos, pos[index]);
                                                                                                                                                    22 // 湊得某個價位的最少錢幣用量
22
       int result = 0;
                                                                                                                  ) //even length
                                                        // printf("%d", arr[index]);
23
       for (int i = 0; i < m; i++)</pre>
                                                                                                                                                       void change(vector<int> price, int limit)
                                                                                                   19
                                                                                                                  x++;
                                                        ans.push_back(arr[index]);
24
          if (table[i] > result)
                                                                                                                                                    24
                                                                                                              if (2 * x > maxlen)
                                                                                                   20
              result = table[i];
25
                                                                                                                                                    25
                                                                                                                                                           vector<int> c(limit + 1, 0);
                                                                                                   21
                                                  9 void LIS(vector<int> &arr)
       return result:
26
                                                                                                                  maxlen = 2 * x;
                                                                                                                                                    26
                                                                                                                                                           c[0] = true;
                                                                                                   22
                                                 10
27 }
                                                                                                                                                    27
                                                                                                                                                           for (int i = 0; i < price.size(); ++i)</pre>
                                                                                                                  l = i - x + 1;
                                                                                                   23
                                                 11
                                                        vector<int> dp(arr.size(), 1);
                                                                                                                                                               for (int j = price[i]; j <= limit;</pre>
                                                                                                                  r = i + x:
                                                                                                  24
                                                        vector<int> pos(arr.size(), -1);
                                                 12
                                                                                                                                                                    ++j)
                                                        int res = INT MIN, index = 0;
                                                                                                   25
                                                 13
                                                                                                                                                                   c[j] = min(c[j], c[j - price[i]]
                                                                                                   26
                                                        for (int i = 0; i < arr.size(); ++i)</pre>
                                                 14
  2.6 LCS
                                                                                                                                                                         + 1);
                                                                                                   27
                                                                                                         cout << maxlen << '\n'; // 最後長度
                                                 15
                                                                                                                                                           cout << c[limit] << '\n';</pre>
                                                                                                         cout << 1 + 1 << ' ' << r + 1 << '\n':
                                                            for (int j = i + 1; j < arr.size();</pre>
                                                                                                   28
                                                 16
                                                                                                                                                    31 }
                                                                                                              //頭到尾
                                                                 ++j)
                                                                                                                                                    32 | // 湊得某個價位的錢幣用量,有哪幾種可能性
1 int LCS(vector<string> Ans, vector<string>
                                                                                                                                                       void change(vector<int> price, int limit)
       num)
                                                                if (arr[j] > arr[i])
                                                 18
                                                                                                                                                    34
2
                                                 19
                                                                                                                                                           vector<int> c(limit + 1, 0);
       int N = Ans.size(), M = num.size();
                                                 20
                                                                    if (dp[i] + 1 > dp[j])
                                                                                                                                                           c[0] = true;
       vector<vector<int>> LCS(N + 1, vector
                                                 21
                                                                                                     2.9 Max subarray
                                                                                                                                                           for (int i = 0; i < price.size(); ++i)</pre>
            int>(M + 1, 0));
                                                                        dp[j] = dp[i] + 1;
                                                 22
                                                                                                                                                               for (int j = price[i]; j <= limit;</pre>
       for (int i = 1; i <= N; ++i)
                                                 23
                                                                        pos[j] = i;
                                                                                                                                                                   c[j] |= c[j-price[i]] << 1; //</pre>
                                                                                                   1 /*Kadane's algorithm*/
           for (int j = 1; j <= M; ++j)
                                                                                                                                                                        錢幣數量加一,每一種可能性都
                                                                                                     int maxSubArray(vector<int>& nums) {
               if (Ans[i - 1] == num[j - 1])
                                                                                                         int local max = nums[0], global max =
                                                            if (dp[i] > res)
                                                                                                                                                                        加一。
                                                 27
                   LCS[i][j] = LCS[i - 1][j -
                                                                                                               nums[0];
                       1] + 1;
                                                                                                         for(int i = 1; i < nums.size(); i++){</pre>
                                                                                                                                                           for (int i = 1; i <= 63; ++i)
                                                                res = dp[i];
                                                                                                                                                    41
                                                                                                              local max = max(nums[i],nums[i]+
               else
                                                                                                                                                               if (c[m] & (1 << i))
                                                                index = i;
                                                                                                                                                    42
                                                                                                                  _
local_max);
12
                   LCS[i][j] = max(LCS[i - 1][j]_{31}
                                                                                                                                                                   cout << "用" << i << "個錢幣可湊
                                                                                                                                                    43
                                                                                                              global max = max(local max,
                       ], LCS[i][j - 1]);
                                                 32
                                                                                                                                                                        得價位" << m;
                                                                                                                  global max);
13
                                                        cout << res << endl; // length
                                                                                                                                                    44 }
14
                                                        printLIS(arr, pos, index);
15
       cout << LCS[N][M] << '\n';</pre>
                                                                                                         return global max;
```

for (int i = 0; i < ans.size(); i++)

cout << ans[i];</pre>

36

//列印 LCS

int n = N, m = M;

# 3 Flow & matching

## 3.1 Dinic

```
1 const long long INF = 1LL<<60;</pre>
   struct Dinic { //O(VVE), with minimum cut
       static const int MAXN = 5003;
       struct Edge{
           int u, v;
           long long cap, rest;
       int n, m, s, t, d[MAXN], cur[MAXN];
       vector<Edge> edges:
       vector<int> G[MAXN];
10
       void init(){
12
           edges.clear();
13
           for ( int i = 0 ; i < n ; i++ ) G[i]
                ].clear();
           n = 0:
15
       // min cut start
16
       bool side[MAXN];
       void cut(int u) {
           side[u] = 1;
19
           for ( int i : G[u] ) {
20
               if ( !side[ edges[i].v ] &&
                    edges[i].rest )
               cut(edges[i].v);
22
23
24
25
       // min cut end
26
       int add node(){
27
           return n++;
28
29
       void add edge(int u, int v, long long
           edges.push_back( {u, v, cap, cap} );
           edges.push_back( {v, u, 0, 0LL} );
           m = edges.size();
32
33
           G[u].push_back(m-2);
           G[v].push_back(m-1);
34
35
36
       bool bfs(){
           fill(d,d+n,-1);
           queue<int> que;
           que.push(s); d[s]=0;
39
           while (!que.empty()){
               int u = que.front(); que.pop();
               for (int ei : G[u]){
                   Edge &e = edges[ei];
                   if (d[e.v] < 0 && e.rest >
                       d[e.v] = d[u] + 1;
                       que.push(e.v);
           return d[t] >= 0;
       long long dfs(int u, long long a){
           if ( u == t || a == 0 ) return a;
           long long flow = 0, f;
```

```
for ( int \&i=cur[u]; i < (int)G[u].
               size(); i++) {
               Edge &e = edges[ G[u][i] ];
               if ( d[u] + 1 != d[e.v] )
               f = dfs(e.v, min(a, e.rest) );
               if (f > 0) {
               e.rest -= f;
               edges[ G[u][i]^1 ].rest += f;
              flow += f;
              a -= f;
               if ( a == 0 ) break;
           return flow:
       long long maxflow(int s, int t){
          s = _s, t = _t;
           long long flow = 0, mf;
           while ( bfs() ){
               fill(cur,cur+n,0);
               while ( (mf = dfs(s, INF)) )
                   flow += mf:
           return flow:
78 } dinic;
```

# 3.2 Edmonds karp

56

57

59

60

61

62

63

64

65

66

67

68

69

70

71

72

76

77

10

11

14

15

21

22

23

```
1 | /*Flow - Edmonds-karp*/
2 /*Based on UVa820*/
3 #define inf 1000000
4 int getMaxFlow(vector<vector<int>> &capacity
      , int s, int t, int n){
    int ans = 0:
    vector<vector<int>> residual(n+1, vector
         int>(n+1, 0)); //residual network
    while(true){
      vector<int> bottleneck(n+1, 0);
      bottleneck[s] = inf;
      queue<int> q;
      q.push(s);
      vector<int> pre(n+1, 0);
      while(!q.empty() && bottleneck[t] == 0){
       int cur = q.front();
        q.pop();
        for(int i = 1; i <= n; i++){
          if(bottleneck[i] == 0 && capacity[
               cur][i] > residual[cur][i]){
            q.push(i);
            pre[i] = cur;
            bottleneck[i] = min(bottleneck[cur 16
                 ], capacity[cur][i] - residual 17
                 [cur][i]);
      if(bottleneck[t] == 0) break;
      for(int cur = t; cur != s; cur = pre[cur 23
          residual[pre[cur]][cur] +=
               bottleneck[t];
```

```
residual[cur][pre[cur]] -=
                bottleneck[t];
28
                                                    29
       ans += bottleneck[t];
29
                                                    31
30
31
     return ans;
                                                    32
32
                                                    33 } graph;
   int main(){
34
     int testcase = 1;
     int n;
36
     while(cin>>n){
       if(n == 0)
       vector<vector<int>> capacitv(n+1, vector
            <int>(n+1, 0));
       int s, t, c;
                                                     1 /*bipartite - maximum matching*/
       cin >> s >> t >> c:
41
                                                     2 bool dfs(vector<vector<bool>> res,int node,
       int a, b, bandwidth;
       for(int i = 0 ; i < c ; ++i){</pre>
         cin >> a >> b >> bandwidth;
45
         capacity[a][b] += bandwidth;
         capacity[b][a] += bandwidth;
46
47
       cout << "Network " << testcase++ << endl</pre>
       cout << "The bandwidth is " <<
            getMaxFlow(capacity, s, t, n) << "."</pre>
       cout << endl;</pre>
50
                                                    1.1
51
                                                    12
52
     return 0;
                                                    13
                                                    14
```

# 3.3 hungarian

```
1 /*bipartite - hungarian*/
2 struct Graph{
       static const int MAXN = 5003;
       vector<int> G[MAXN];
       int n, match[MAXN], vis[MAXN];
       void init(int n){
           for (int i=0; i<n; i++) G[i].clear()</pre>
       bool dfs(int u){
               for (int v:G[u]){
               if (vis[v]) continue;
               vis[v]=true;
               if (match[v]==-1 || dfs(match[v
                   match[v] = u;
                   match[u] = v;
                   return true;
19
           return false:
20
22
       int solve(){
           int res = 0:
           memset(match,-1,sizeof(match));
           for (int i=0; i<n; i++){</pre>
25
```

if (match[i]==-1){

# 3.4 Maximum matching

vector<int>& x, vector<int>& y, vector<</pre>

return res;

memset(vis,0,sizeof(vis));

if ( dfs(i) ) res++;

```
bool> pass){
       for (int i = 0; i < res[0].size(); i++){</pre>
           if(res[node][i] && !pass[i]){
               pass[i] = true;
               if(y[i] == -1 \mid | dfs(res,y[i],x,
                    v,pass)){
                   x[node] = i;
                   y[i] = node;
                   return true;
           }
       return false:
  int main(){
15
       int n,m,1;
       while(cin>>n>>m>>l){
           vector<vector<bool>> res(n, vector<</pre>
                bool>(m, false));
           for (int i = 0; i < 1; i++){
               int a, b;
               cin >> a >> b;
               res[a][b] = true;
           int ans = 0;
           vector<int> x(n, -1);
           vector<int> y(n, -1);
           for (int i = 0; i < n; i++){
               vector<bool> pass(n, false);
               if(dfs(res,i,x,y,pass))
                   ans += 1;
           cout << ans << endl;</pre>
       return 0;
35
36
37 input:
38 4 3 5 //n matching m, 1 links
39 0 0
40 0 2
41 1 0
42 2 1
43 3 1
44 answer is 3
```

17

20

21

22

23

24

28

29

30

31

32

```
1 typedef long long 11;
2 struct MF
3
       static const int N = 5000 + 5:
       static const int M = 60000 + 5;
       static const 11 oo = 100000000000000L;
       int n, m, s, t, tot, tim;
       int first[N], next[M];
       int u[M], v[M], cur[N], vi[N];
       11 cap[M], flow[M], dis[N];
12
       int que[N + N];
13
       void Clear()
14
15
16
           tot = 0:
           tim = 0:
17
18
           for (int i = 1; i <= n; ++i)
               first[i] = -1:
19
20
21
       void Add(int from, int to, ll cp, ll flw
22
23
           u[tot] = from;
24
           v[tot] = to:
25
           cap[tot] = cp;
26
           flow[tot] = flw;
27
           next[tot] = first[u[tot]];
28
           first[u[tot]] = tot;
29
           ++tot:
30
       bool bfs()
31
32
33
           ++tim;
34
           dis[s] = 0;
35
           vi[s] = tim;
36
           int head, tail:
           head = tail = 1:
           que[head] = s;
           while (head <= tail)
               for (int i = first[que[head]]; i
                     != -1; i = next[i])
                   if (vi[v[i]] != tim && cap[i
                        ] > flow[i])
                        vi[v[i]] = tim;
                        dis[v[i]] = dis[que[head
                            ]] + 1;
                        que[++tail] = v[i];
                   }
               ++head:
           return vi[t] == tim:
       11 dfs(int x, 11 a)
           if (x == t || a == 0)
               return a;
           11 \text{ flw} = 0, f;
```

MFlow Model

61

62

63

64

65

66

67

68

69

70

71

72

73

74

75

76

77

78

82

83

84

85

86

87

```
int &i = cur[x]:
           for (i = first[x]; i != -1; i = next
                                                 16
               if (dis[x] + 1 == dis[v[i]] && (
                   f = dfs(v[i], min(a, cap[i]
                   - flow[i]))) > 0)
                                                 19
                                                 20
                   flow[i] += f;
                   flow[i ^ 1] -= f;
                   a -= f;
                                                 21
                   flw += f:
                   if (a == 0)
                                                 22
                       break:
                                                 23
           return flw:
       11 MaxFlow(int s, int t)
           this->s = s;
           this->t = t:
           11 \text{ flw} = 0:
           while (bfs())
               for (int i = 1; i <= n; ++i)
                   cur[i] = 0;
               flw += dfs(s, oo);
           return flw;
88 };
                                                 11
89 // MF Net:
                                                 12
90 // Net.n = n;
                                                 13
91 // Net.Clear();
92 // a 到 b (注意從1開始!!!!)
                                                 15
93 // Net.Add(a, b, w, 0);
94 // Net.MaxFlow(s, d)
                                                 16
95 // s 到 d 的 MF
                                                 17
                                                 18
                                                 19
                                                 20
  4 Geometry
                                                 21
                                                 22
                                                 23
   4.1 Closest Pair
                                                 ^{24}
                                                 25
                                                 26
 1 | //最近點對 (距離) //台大
 vector<pair<double, double>> p;
                                                 27
3 double closest_pair(int 1, int r)
                                                 28
                                                 29
      // p 要對 x 軸做 sort
                                                 30
       if (1 == r)
                                                 31
           return 1e9;
                                                 32
       if (r - 1 == 1)
                                                 33
                                                34
           return dist(p[1], p[r]); // 兩點距離
                                                 35
       int m = (1 + r) >> 1;
                                                 36
       double d = min(closest pair(1, m),
                                                 37
           closest pair(m + 1, r));
       vector<int> vec:
                                                 38
       for (int i = m; i >= 1 && fabs(p[m].x -
                                                 39
                                                 40
           p[i].x) < d; --i)
```

vec.push back(i);

```
for (int i = m + 1; i <= r && fabs(p[m]. 42|
          x - p[i].x) < d; ++i)
          vec.push back(i);
     sort(vec.begin(), vec.end(), [&](int a,
                                                43
           { return p[a].y < p[b].y; });
     for (int i = 0: i < vec.size(): ++i)</pre>
          for (int j = i + 1; j < vec.size()</pre>
              && fabs(p[vec[j]].y - p[vec[i]]. 47
              v) < d; ++i)
              d = min(d, dist(p[vec[i]], p[vec 48
                   [j]]));
     return d;
                                                50
                                                51
 4.2 Line
1 template <typename T>
2 struct line
                                                57
     line() {}
     point<T> p1, p2;
     T a, b, c; //ax+by+c=0
     line(const point<T> &x, const point<T> &
          y) : p1(x), p2(y) {}
     void pton()
                                                62
     { //轉成一般式
                                                63
         a = p1.y - p2.y;
                                                64
         b = p2.x - p1.x;
         c = -a * p1.x - b * p1.y;
     T ori(const point<T> &p) const
     { //點和有向直線的關係, >0左邊、=0在線上
          return (p2 - p1).cross(p - p1);
                                                69
     T btw(const point<T> &p) const
                                                70
     { //點投影落在線段上<=0
         return (p1 - p).dot(p2 - p);
     bool point on segment(const point<T> &p)
           const
     { //點是否在線段上
                                                74
          return ori(p) == 0 && btw(p) <= 0;</pre>
     T dis2(const point<T> &p, bool
          is_segment = 0) const
     { //點跟直線/線段的距離平方
                                                79
          point < T > v = p2 - p1, v1 = p - p1;
          if (is segment)
                                                81
              point < T > v2 = p - p2:
              if (v.dot(v1) <= 0)</pre>
                                                82
                  return v1.abs2();
              if(v.dot(v2) >= 0)
                                                83
                  return v2.abs2();
                                                84
         T tmp = v.cross(v1):
                                                85
          return tmp * tmp / v.abs2();
                                                86
     T seg_dis2(const line<T> &1) const
```

{ //兩線段距離平方

```
return min({dis2(1.p1, 1), dis2(1.p2
        , 1), l.dis2(p1, 1), l.dis2(p2,
point<T> projection(const point<T> &p)
    const
{ //點對直線的投影
   point < T > n = (p2 - p1).normal();
   return p - n * (p - p1).dot(n) / n.
        abs2();
point<T> mirror(const point<T> &p) const
   //點對直線的鏡射,要先呼叫pton轉成一
        般式
   point<T> R:
   Td = a * a + b * b;
   R.x = (b * b * p.x - a * a * p.x - 2)
         * a * b * p.y - 2 * a * c) / d;
    R.v = (a * a * p.v - b * b * p.v - 2)
          * a * b * p.x - 2 * b * c) / d;
    return R:
bool equal(const line &1) const
{ //直線相等
   return ori(1.p1) == 0 && ori(1.p2)
        == 0:
bool parallel(const line &1) const
   return (p1 - p2).cross(l.p1 - l.p2)
        == 0;
bool cross seg(const line &1) const
    return (p2 - p1).cross(l.p1 - p1) *
        (p2 - p1).cross(1.p2 - p1) <= 0;
         //直線是否交線段
int line_intersect(const line &1) const
{ //直線相交情況·-1無限多點、1交於一
    點、0不相交
    return parallel(1) ? (ori(1.p1) == 0
         ? -1 : 0) : 1;
int seg_intersect(const line &1) const
   T c1 = ori(1.p1), c2 = ori(1.p2);
   T c3 = 1.ori(p1), c4 = 1.ori(p2);
   if (c1 == 0 && c2 == 0)
   { //共線
       bool b1 = btw(l.p1) \Rightarrow 0, b2 =
            btw(1.p2) >= 0;
       T = 3 = 1.btw(p1), a4 = 1.btw(p2)
       if (b1 && b2 && a3 == 0 && a4 >=
             0)
           return 2;
       if (b1 && b2 && a3 >= 0 && a4 ==
             0)
           return 3;
       if (b1 && b2 && a3 >= 0 && a4 >=
             0)
           return 0;
```

28

29

30

31

32

33

34

35

36

37

38

39

40

42

43

44

45

46

47

49

bool c = 0:

for (int i = 0, j = p.size() - 1; i

```
return -1; //無限交點
                                                            return x * b.x + y * b.y;
                                                 30
                                                 31
           else if (c1 * c2 <= 0 && c3 * c4 <=
                                                        T cross(const point &b) const
                                                 32
                                                 33
                                                            return x * b.y - y * b.x;
91
               return 1;
                                                 34
           return 0; //不相交
                                                 35
92
                                                 36
                                                        point normal() const
93
                                                        { //求法向量
       point<T> line intersection(const line &l 37
94
           ) const
                                                            return point(-y, x);
       { /*直線交點*/
95
           point < T > a = p2 - p1, b = 1.p2 - 1.
                                                 40
                                                        T abs2() const
                                                        { //向量長度的平方
                p1, s = 1.p1 - p1;
                                                 41
           //if(a.cross(b)==0)return INF;
                                                            return dot(*this);
                                                 42
           return p1 + a * (s.cross(b) / a.
98
                                                 43
                cross(b));
                                                        T rad(const point &b) const
                                                 44
                                                        { //兩向量的弧度
100
       point<T> seg_intersection(const line &l)
                                                            return fabs(atan2(fabs(cross(b)),
             const
                                                                 dot(b)));
       { //線段交點
101
                                                 47
           int res = seg intersect(1);
                                                        T getA() const
102
                                                 48
           if (res <= 0)
103
                                                  49
                                                                               //對x軸的弧度
104
               assert(0):
                                                            T A = atan2(y, x); //超過180度會變負
                                                 50
105
           if (res == 2)
106
               return p1;
                                                 51
                                                            if (A <= -PI / 2)
           if (res == 3)
107
                                                 52
                                                                A += PI * 2;
108
               return p2;
                                                            return A;
                                                 53
           return line intersection(1):
109
                                                 54
110
                                                 55 };
111 };
```

15

18

# 4.3 Point

```
1 const double PI = atan2(0.0, -1.0);
   template <typename T>
3 struct point
4 {
      T x, y;
       point() {}
       point(const T &x, const T &y) : x(x), y(
       point operator+(const point &b) const
           return point(x + b.x, y + b.y);
11
       point operator-(const point &b) const
13
14
           return point(x - b.x, y - b.y);
15
       point operator*(const T &b) const
17
           return point(x * b, y * b);
19
       point operator/(const T &b) const
20
22
           return point(x / b, y / b);
23
24
       bool operator == (const point &b) const
25
                                                  24
26
           return x == b.x && y == b.y;
27
       T dot(const point &b) const
```

# 4.4 Polygon

```
1 | template <typename T>
                                                50
2 struct polygon
                                                51
                                                52
      polygon() {}
                                                53
      vector<point<T>> p; //逆時針順序
                                                54
      T area() const
                                                55
      { //面積
                                                56
          T ans = 0;
           for (int i = p.size() - 1, j = 0; j
               < (int)p.size(); i = j++)
               ans += p[i].cross(p[j]);
11
          return ans / 2;
                                                60
12
      point<T> center of mass() const
                                                61
14
                                                62
          T cx = 0, cy = 0, w = 0;
                                                63
          for (int i = p.size() - 1, j = 0; j
16
               < (int)p.size(); i = j++)
                                                64
17
              T a = p[i].cross(p[j]);
              cx += (p[i].x + p[j].x) * a;
19
                                                66
20
              cy += (p[i].y + p[j].y) * a;
21
              w += a;
22
           return point<T>(cx / 3 / w, cy / 3 / 67
23
      char ahas(const point<T> &t) const
                                                69
25
      { //點是否在簡單多邊形內,是的話回傳1
26
                                                70
           在邊上回傳-1、否則回傳0
```

```
< p.size(); j = i++)</pre>
                                        73
       if (line<T>(p[i], p[j]).
                                        74
            point_on_segment(t))
                                        75
           return -1;
       else if ((p[i].y > t.y) != (p[j
            ].y > t.y) &&
                t.x < (p[j].x - p[i].x)
                      * (t.y - p[i].y) /
                      (p[j].y - p[i].y)
                    + p[i].x)
           c = !c;
                                        80
    return c:
char point in convex(const point<T> &x)
                                        83
    int 1 = 1, r = (int)p.size() - 2;
                                        84
    while (1 <= r)
   { //點是否在凸多邊形內,是的話回傳1
         、在邊上回傳-1、否則回傳0
       int mid = (1 + r) / 2;
       T a1 = (p[mid] - p[0]).cross(x -
             p[0]);
       T = 2 = (p[mid + 1] - p[0]).cross
            (x - p[0]);
       if (a1 >= 0 && a2 <= 0)
                                        90
           T res = (p[mid + 1] - p[mid
               ]).cross(x - p[mid]);
           return res > 0 ? 1 : (res >=
                 0 ? -1 : 0);
       else if (a1 < 0)
           r = mid - 1;
       else
           1 = mid + 1;
                                        97
    return 0:
vector<T> getA() const
                                        99
{//凸包邊對x軸的夾角
                                        100
    vector<T> res; //一定是遞增的
                                        101
    for (size t i = 0; i < p.size(); ++i</pre>
       res.push back((p[(i + 1) \% p.
                                        103
            size()] - p[i]).getA());
                                       104
    return res;
bool line intersect(const vector<T> &A.
    const line<T> &1) const
                                        106
{ //O(logN)
                                        107
    int f1 = upper bound(A.begin(), A.
        end(), (1.p1 - 1.p2).getA()) - A
        .begin();
    int f2 = upper_bound(A.begin(), A.
        end(), (1.p2 - 1.p1).getA()) - A<sup>110</sup>
        .begin():
   113
        f2]));
                                       114
                                       115
polygon cut(const line<T> &1) const
                                       116
{ //凸包對直線切割,得到直線1左側的凸包
    polygon ans;
```

```
for (int n = p.size(), i = n - 1, j
                         = 0; i < n; i = j++)
                       if (1.ori(p[i]) >= 0)
                                  ans.p.push back(p[i]);
                                  if (1.ori(p[i]) < 0)</pre>
                                              ans.p.push_back(1.
                                                           line intersection(
                                                           line<T>(p[i], p[j]))
                       else if (l.ori(p[j]) > 0)
                                  ans.p.push back(1.
                                                 line intersection(line<T
                                                >(p[i], p[j])));
           return ans;
static bool graham cmp(const point<T> &a
              , const point<T> &b)
{ //凸包排序函數 // 起始點不同
           // return (a.x < b.x) || (a.x == b.x) || (a.
                            && a.v < b.v); //最左下角開始
           return (a.y < b.y) || (a.y == b.y &&
                           a.x < b.x); //Y最小開始
void graham(vector<point<T>> &s)
{ //凸包 Convexhull 2D
           sort(s.begin(), s.end(), graham_cmp)
           p.resize(s.size() + 1);
           int m = 0;
           // cross >= 0 順時針。cross <= 0 逆
           for (size_t i = 0; i < s.size(); ++i</pre>
                       while (m >= 2 \&\& (p[m - 1] - p[m
                                        - 2]).cross(s[i] - p[m -
                                    2]) <= 0)
                                  --m;
                       p[m++] = s[i];
           for (int i = s.size() - 2, t = m +
                         1; i >= 0; --i)
                       while (m >= t && (p[m - 1] - p[m
                                        - 2]).cross(s[i] - p[m -
                                    2]) <= 0)
                                  --m:
                       p[m++] = s[i];
           if (s.size() > 1) // 重複頭一次需扣
                       --m;
           p.resize(m);
T diam()
{ // 直徑
           int n = p.size(), t = 1;
           T ans = 0:
           p.push back(p[0]);
            for (int i = 0; i < n; i++)
```

```
triangle(const point<T> &a, const point< 15
118
119
                point \langle T \rangle now = p[i + 1] - p[i]; 171
                                                           static char sign(const point<T> &t)
                                                                                                                    T> &b, const point\langle T \rangle &c): a(a), b( 16
                while (now.cross(p[t + 1] - p[i 172
                                                                                                                    b), c(c) {}
                                                                                                                                                                           }
120
                     ]) > now.cross(p[t] - p[i]))173
                                                                return (t.y == 0 ? t.x : t.y) < 0;
                                                                                                               T area() const
                                                                                                                                                           18
                                                                                                                                                                       }
                    t = (t + 1) \% n;
121
                                                   174
                                                                                                                                                           19
                                                                                                                   T t = (b - a).cross(c - a) / 2;
122
                ans = max(ans, (p[i] - p[t]).
                                                   175
                                                           static bool angle cmp(const line<T> &A,
                                                                                                                                                           20
                     abs2()):
                                                                const line<T> &B)
                                                                                                                   return t > 0 ? t : -t:
                                                                                                                                                           21
                                                                                                                                                                   for(int i = 0: i < node: i++) //</pre>
                                                                                                        10
                                                                                                                                                                        negative cycle detection
123
                                                   176
124
            return p.pop back(), ans;
                                                   177
                                                                point < T > a = A.p2 - A.p1, b = B.p2 -
                                                                                                       12
                                                                                                               point<T> barycenter() const
                                                                                                                                                           22
                                                                                                                                                                       for(int j = 0; j < node; j++)</pre>
                                                                                                                                                                           if(dist[i] + edges[i][j] < dist[</pre>
125
                                                                                                                                                           23
                                                                                                               { //重心
126
       T min cover rectangle()
                                                                return sign(a) < sign(b) || (sign(a)</pre>
                                                   178
                                                                                                                                                                                j])
                                                                                                       14
                                                                                                                   return (a + b + c) / 3;
                                                                     == sign(b) && a.cross(b) > 0); 15
        { //最小覆蓋矩形
127
                                                                                                                                                           24
                                                                                                                                                                               cout<<"Negative cycle!"<<</pre>
            int n = p.size(), t = 1, r = 1, 1;
                                                   179
                                                                                                               point<T> circumcenter() const
                                                                                                                                                           25
128
            if (n < 3)
                                                   180
                                                           int halfplane intersection(vector<line<T</pre>
                                                                                                                                                                                    endl:
129
                                                                                                               { //外心
                                                                >> &s)
                                                                                                                                                           26
                                                                                                                                                                               return:
                return 0; //也可以做最小周長矩形
130
                                                                                                                   static line<T> u, v;
                                                                                                        18
                                                           { //半平面交
                                                                                                                                                           27
                                                   181
            T ans = 1e99:
                                                                                                                   u.p1 = (a + b) / 2;
131
                                                                                                                                                           28
                                                               sort(s.begin(), s.end(), angle\_cmp); 20
                                                   182
132
            p.push_back(p[0]);
                                                                                                                   u.p2 = point < T > (u.p1.x - a.y + b.y,
                                                                                                                                                              int main(){
                                                                                                                                                           29
133
            for (int i = 0; i < n; i++)
                                                                     //線段左側為該線段半平面
                                                                                                                        u.p1.y + a.x - b.x;
                                                                                                                                                                  int node:
                                                                                                                                                           30
                                                                int L, R, n = s.size();
                                                                                                                   v.p1 = (a + c) / 2;
134
                                                   183
                                                                                                        21
                                                                                                                                                                  cin>>node:
                point < T > now = p[i + 1] - p[i];
                                                               vector<point<T>> px(n);
                                                                                                                   v.p2 = point < T > (v.p1.x - a.y + c.y,
135
                                                  184
                                                                                                        22
                                                                                                                                                           32
                                                                                                                                                                   edges.resize(node, vector<int>(node, inf))
                while (now.cross(p[t + 1] - p[i 185])
                                                               vector<line<T>> q(n);
136
                                                                                                                        v.p1.y + a.x - c.x);
                     ]) > now.cross(p[t] - p[i]))186
                                                                q[L = R = 0] = s[0];
                                                                                                                   return u.line_intersection(v);
                                                                                                        23
                                                                                                                                                                  dist.resize(node.inf):
                                                                                                                                                           33
                                                                for (int i = 1; i < n; ++i)
137
                    t = (t + 1) \% n;
                                                                                                        24
                                                                                                                                                                  ancestor.resize(node,-1);
                                                                                                                                                           34
                while (now.dot(p[r + 1] - p[i]) <sub>188</sub>
                                                                                                               point<T> incenter() const
138
                                                                                                        ^{25}
                                                                                                                                                           35
                                                                                                                                                                  int a,b,d;
                     > now.dot(p[r] - p[i]))
                                                   189
                                                                    while (L < R \&\& s[i].ori(px[R -
                                                                                                               { //內心
                                                                                                        26
                                                                                                                                                                  while(cin>>a>>b>>d){
                    r = (r + 1) \% n;
                                                                        1]) <= 0)
139
                                                                                                                   T A = sqrt((b - c).abs2()), B = sqrt
                                                                                                                                                                       /*input: source destination weight*/
                if (!i)
140
                                                   190
                                                                        --R;
                                                                                                                        ((a - c).abs2()), C = sqrt((a -
                                                                                                                                                                       if(a == -1 \&\& b == -1 \&\& d == -1)
                                                                    while (L < R \&\& s[i].ori(px[L])
141
                    1 = r:
                                                   191
                                                                                                                        b).abs2()):
                                                                                                                                                                           break;
                while (now.dot(p[l + 1] - p[i])
142
                                                                         <= 0)
                                                                                                                   return point<T>(A * a.x + B * b.x +
                                                                                                        28
                                                                                                                                                                       edges[a][b] = d;
                     <= now.dot(p[1] - p[i]))
                                                   192
                                                                        ++L;
                                                                                                                        C * c.x, A * a.y + B * b.y + C *
                                                                                                                                                           41
                    1 = (1 + 1) \% n;
                                                                    q[++R] = s[i];
143
                                                   193
                                                                                                                         c.v) / (A + B + C);
                                                                                                                                                                  int start;
                                                                                                                                                           42
144
                T d = now.abs2();
                                                   194
                                                                    if (q[R].parallel(q[R - 1]))
                                                                                                        29
                                                                                                                                                                  cin>>start:
                                                                                                                                                           43
145
                T tmp = now.cross(p[t] - p[i]) * 195
                                                                                                        30
                                                                                                               point<T> perpencenter() const
                                                                                                                                                                  BellmanFord(start, node);
                                                                                                                                                           44
                      (now.dot(p[r] - p[i]) - now_{196}
                                                                                                               { //垂心
                                                                                                                                                                  return 0;
                                                                                                                                                           45
                                                                        if (q[R].ori(s[i].p1) > 0)
                      .dot(p[l] - p[i])) / d;
                                                   197
                                                                                                        32
                                                                                                                   return barycenter() * 3 -
146
                ans = min(ans, tmp);
                                                   198
                                                                            q[R] = s[i];
                                                                                                                        circumcenter() * 2;
147
                                                   199
                                                                                                        33
                                                                    if (L < R)
148
            return p.pop_back(), ans;
                                                   200
                                                                                                        34 };
                                                                        px[R - 1] = q[R - 1].
149
                                                   201
                                                                                                                                                              5.2 BFS-queue
150
       T dis2(polygon &pl)
                                                                             line intersection(q[R]);
        { //凸包最近距離平方
151
                                                                while (L < R \&\& q[L].ori(px[R - 1])
            vector<point<T>> &P = p, &Q = pl.p;
152
                                                                                                                                                            1 /*BFS - queue version*/
                                                                    <= 0)
                                                                                                                Graph
            int n = P.size(), m = Q.size(), l =
153
                                                                                                                                                            void BFS(vector<int> &result, vector<pair</pre>
                                                                    --R;
                                                   204
                0, r = 0;
                                                                                                                                                                   int, int>> edges, int node, int start)
                                                                p.clear();
            for (int i = 0; i < n; ++i)</pre>
                                                   205
154
                                                   206
                                                                if (R - L <= 1)
155
                if (P[i].y < P[1].y)</pre>
                                                                                                           5.1 Bellman-Ford
                                                                                                                                                                  vector<int> pass(node, 0);
                                                                    return 0;
156
                                                   207
                    1 = i:
                                                                                                                                                                  queue<int> q;
            for (int i = 0; i < m; ++i)</pre>
                                                   208
                                                                px[R] = q[R].line intersection(q[L])
157
                                                                                                                                                                  queue<int> p;
                if (Q[i].y < Q[r].y)</pre>
158
                                                                                                        1 /*SPA - Bellman-Ford*/
                                                                                                                                                                  q.push(start);
                                                                for (int i = L; i \leftarrow R; ++i)
159
                    r = i;
                                                                                                        2 #define inf 99999 //define by you maximum
                                                                                                                                                                  int count = 1;
                                                                   p.push back(px[i]);
            P.push_back(P[0]), Q.push_back(Q[0])
                                                  210
160
                                                                                                                edges weight
                                                                                                                                                                  vector<pair<int, int>> newedges;
                                                                return R - L + 1;
                                                   211
                                                                                                                                                                  while (!q.empty())
                                                                                                         3 vector<vector<int> > edges;
                                                                                                                                                           10
                                                   212
161
            T ans = 1e99;
                                                                                                         4 vector<int> dist;
                                                                                                                                                           11
                                                   213 };
162
            for (int i = 0; i < n; ++i)
                                                                                                         5 vector<int> ancestor;
                                                                                                                                                           12
                                                                                                                                                                       pass[q.front()] = 1;
163
                                                                                                                                                                       for (int i = 0; i < edges.size(); i</pre>
                                                                                                        6 | void BellmanFord(int start, int node){
                                                                                                                                                           13
                while ((P[1] - P[1 + 1]).cross(Q
164
                                                                                                               dist[start] = 0;
                                                                                                                                                                            ++)
                     [r + 1] - Q[r] < 0
                                                                                                               for(int it = 0; it < node-1; it++){</pre>
                    r = (r + 1) \% m;
165
                                                       4.5 Triangle
                                                                                                                   for(int i = 0; i < node; i++){</pre>
                                                                                                                                                                           if (edges[i].first == q.front()
                ans = min(ans, line<T>(P[1], P[1
166
                                                                                                                       for(int j = 0; j < node; j++){</pre>
                                                                                                                                                                                && pass[edges[i].second] ==
                      + 1]).seg dis2(line<T>(Q[r
                                                                                                        11
                                                                                                                            if(edges[i][j] != -1){
                     ], Q[r + 1])));
                                                     1 template <typename T>
                                                                                                        12
                                                                                                                                if(dist[i] + edges[i][j] 16
167
                l = (l + 1) \% n;
                                                     2 struct triangle
                                                                                                                                      < dist[j]){
                                                                                                                                                                               p.push(edges[i].second);
168
                                                     3 | {
                                                                                                        13
                                                                                                                                    dist[i] = dist[i] +
                                                                                                                                                                               result[edges[i].second] =
            return P.pop_back(), Q.pop_back(),
                                                           point<T> a, b, c;
                                                                                                                                         edges[i][j];
                                                                                                                                                                                    count;
                ans;
                                                           triangle() {}
                                                                                                                                    ancestor[j] = i;
```

32 // weight[a - 1].push back(pii(b - 1, w));

distance[i][j] =

else if((\*iter).first.second ==

else if (edges[i].second == q.

```
start && (*iter).second == 0 && 33 // weight[b - 1].push back(pii(a - 1, w));
                    front() && pass[edges[i].
                                                                                                                                                                                distance[i][k] +
                                                                 pass[(*iter).first.first] == 0){ 34 // dist.resize(n, inf);
                    first] == 0)
                                                                                                                                                                                distance[k][j];
                                                                route.push back((*iter).first.
                                                                                                  35 // ancestor.resize(n, -1);
                                                                                                                                                                            ancestor[i][j] =
                   p.push(edges[i].first);
                                                                                                   36 // dist[0] = 0;
                                                                                                                                                                                ancestor[k][j];
22
                   result[edges[i].first] =
                                                                DFS((*iter).first.first);
                                                                                                   37 // dijkstra(0);
                       count:
                                                 16
                                                                                                                                                    25
                                                 17
               else
                                                 18
                                                                                                                                                    26
                   newedges.push_back(edges[i])
                                                 19 int main(){
                                                                                                                                                    27
                                                                                                           Euler circuit
                                                 20
                                                        int node;
                                                                                                                                                    28
                                                        cin>>node:
                                                                                                                                                       vector<vector<int>> distance(n, vector<int>(
                                                 21
           edges = newedges;
                                                        pass.resize(node,0);
                                                 22
          newedges.clear():
                                                        int a.b:
                                                                                                    1 /*Euler circuit*/
                                                                                                                                                       vector<vector<int>> ancestor(n, vector<int>(
          q.pop();
                                                 24
                                                        while(cin>>a>>b){
                                                                                                    2 /*From NTU kiseki*/
                                                                                                                                                            n, -1));
           if (q.empty() == true)
                                                 25
                                                            if(a == -1 \&\& b == -1)
                                                                                                    3 /*G is graph, vis is visited, la is path*/
                                                                                                                                                       distance[a][b] = w;
32
                                                                                                                                                       ancestor[a][b] = w;
                                                 26
                                                                                                    4 bool vis[N];
33
                                                 27
                                                            edges.insert(pair<pair<int,int>,int
                                                                                                                                                       floyd_warshall(distance, ancestor, n);
                                                                                                    5 size t la[K];
               q = p;
                                                                 >(pair<int,int>(a,b),0));
                                                                                                                                                       /*Negative cycle detection*/
34
               queue<int> tmp;
                                                                                                    6 void dfs(int u, vector<int> &vec)
                                                                                                                                                       for (int i = 0; i < n; i++)
35
               p = tmp;
                                                 28
36
               count++;
                                                 29
                                                        int start;
                                                                                                          while (la[u] < G[u].size())</pre>
                                                                                                                                                    36
                                                        cin>>start:
                                                                                                                                                           if (distance[i][i] < 0)</pre>
37
                                                 30
                                                                                                                                                    37
38
                                                 31
                                                        route.push back(start);
                                                                                                   10
                                                                                                              if (vis[G[u][la[u]].second])
                                                                                                                                                    38
39
                                                 32
                                                        DFS(start);
                                                                                                                                                    39
                                                                                                                                                               cout << "Negative cycle!" << endl;</pre>
                                                                                                   11
   int main()
40
                                                 33
                                                        return 0;
                                                                                                   12
                                                                                                                  ++la[u];
                                                                                                                                                    40
                                                                                                                                                               break;
                                                 34 }
                                                                                                                                                    41
41
                                                                                                   13
                                                                                                                  continue;
42
       int node;
                                                                                                   14
       cin >> node:
                                                                                                   15
                                                                                                              int v = G[u][la[u]].first;
       vector<pair<int, int>> edges;
                                                                                                              vis[G[u][la[u]].second] = true;
44
                                                                                                   16
                                                    5.4 Dijkstra
45
       int a, b;
                                                                                                   17
                                                                                                              ++la[u];
46
      while (cin >> a >> b)
                                                                                                   18
                                                                                                              dfs(v, vec);
                                                                                                                                                       5.7 Hamilton cycle
                                                                                                   19
                                                                                                              vec.push back(v);
          /*a = b = -1 means input edges ended 1 /*SPA - Diikstra*/
                                                                                                   20
                                                  _{2} const int MAXN = 1e5 + 3;
          if (a == -1 && b == -1)
                                                  3 const int inf = INT_MAX;
                                                                                                                                                     1 /*find hamilton cycle*/
                                                                                                                                                     void hamilton(vector<vector<int>> gp, int k,
                                                  4 typedef pair<int, int> pii;
50
               break;
           edges.push_back(pair<int, int>(a, b)
                                                  5 vector<vector<pii>>> weight;
                                                                                                                                                             int cur, vector<int>& solution, vector<</pre>
                                                  6 vector<int> isDone(MAXN, false), dist,
                                                                                                                                                            bool> pass,bool& flag){
                                                                                                     5.6 Floyd-warshall
52
                                                         ancestor:
                                                                                                                                                           if(k == gp.size()-1){
53
       vector<int> result(node, -1);
                                                    void dijkstra(int s)
                                                                                                                                                               if(gp[cur][1] == 1){
      BFS(result, edges, node, 0);
                                                                                                                                                                   cout << 1 << " '
54
55
                                                        priority queue<pii, vector<pii>, greater
                                                                                                                                                                   while(cur != 1){
                                                                                                   1 /*SPA - Floyd-Warshall*/
                                                             <pii>>> pq;
                                                                                                                                                                       cout << cur << " ";
56
       return 0;
                                                                                                    2 // 有向圖,正邊
                                                                                                                         O(V3)
                                                        pq.push(pii(0, s));
                                                                                                                                                                       cur = solution[cur];
                                                 10
                                                                                                    3 // 有向圖,無負環 O(V3)
                                                        ancestor[s] = -1;
                                                 11
                                                                                                    4 // 有向圖,有負環
                                                                                                                         不適用
                                                 12
                                                        while (!pq.empty())
                                                                                                                                                                   cout << cur << endl;</pre>
                                                 13
                                                                                                                                                    11
                                                                                                                                                                   flag = true;
  5.3 DFS-rec
                                                                                                    6 // 無向圖,正邊
                                                                                                                         O(V^3)
                                                 14
                                                            int u = pq.top().second;
                                                                                                                                                    12
                                                                                                                                                                   return;
                                                                                                    7 // 無向圖,無負環 不適用
                                                 15
                                                            pq.pop();
                                                                                                                                                    13
                                                                                                    8 // 無向圖,有負環 不適用
                                                 16
                                                                                                                                                    14
1 /*DFS - Recursive version*/
                                                            isDone[u] = true;
                                                                                                    9 /*Find min weight cycle*/
                                                                                                                                                           for (int i = 0; i < gp[cur].size() && !</pre>
                                                 17
                                                                                                   10 #define inf 99999
2 map<pair<int,int>,int> edges;
                                                                                                                                                                flag; i++){
                                                                                                   void floyd warshall(vector<vector<int>> &
3 vector<int> pass;
                                                            for (auto &pr : weight[u])
                                                                                                                                                               if(gp[cur][i] == 1 && !pass[i]){
                                                 19
4 vector<int> route;
                                                 20
                                                                                                          distance, vector<vector<int>> &ancestor, 17
                                                                                                                                                                   pass[i] = true;
  void DFS(int start){
                                                 21
                                                                int v = pr.first, w = pr.second;
                                                                                                           int n)
                                                                                                                                                                    solution[i] = cur;
                                                                                                                                                                   hamilton(gp, k + 1, i, solution,
      pass[start] = 1;
                                                                                                                                                    19
       map<pair<int,int>,int>::iterator iter;
                                                                if (!isDone[v] && dist[u] + w <</pre>
                                                                                                  13
                                                                                                          for (int k = 0; k < n; k++)
                                                                                                                                                                         pass, flag);
                                                                     dist[v])
       for(iter = edges.begin(); iter != edges.
                                                                                                                                                                    pass[i] = false;
            end(); iter++){
                                                                                                   15
                                                                                                              for (int i = 0; i < n; i++)
                                                                                                                                                    ^{21}
           if((*iter).first.first == start &&
                                                                     dist[v] = dist[u] + w;
                                                                                                   16
                                                                                                                                                    22
                (*iter).second == 0 && pass[(*
                                                                     pq.push(pii(dist[v], v));
                                                                                                                                                    23
                                                                                                   17
                                                                                                                  for (int j = 0; j < n; j++)
               iter).first.second] == 0){
                                                 27
                                                                     ancestor[v] = u;
                                                                                                   18
                                                                                                                                                       int main(){
               route.push back((*iter).first.
                                                                                                                      if (distance[i][k] +
                                                                                                                                                    25
                                                                                                                                                           int n;
                    second);
                                                 29
                                                                                                                           distance[k][i] <
                                                                                                                                                           while(cin>>n){
               DFS((*iter).first.second);
                                                                                                                           distance[i][j])
                                                                                                                                                               int a,b;
                                                 30
                                                                                                                                                               bool end = false;
```

```
vector<vector<int>> gp(n+1,vector
                                                          while(!pq.empty() && edge < n - 1){</pre>
                                                                                                                              if (w[k][i] + d[i][j] +
                                                                                                                                                                int edge = 0;
                                                                                                                                                                int cost = 0; //evaluate cost of mst
                int>(n+1,0));
                                                   28
                                                              edges cur = pq.top();
                                                                                                                                   w[j][k] < weight)
           while(cin>>a>>b){
                                                              int from = find(cur.from, union set)
                                                                                                                                                                priority queue<edges> pq;
30
                                                   29
                                                                                                      27
                                                                                                                                  weight = w[k][i] + d 19
                                                                                                                                                                for (int i = 0; i < n; i++)
31
               if(a == 0 && b == 0)
                                                              int to = find(cur.to, union set);
                                                                                                                                       [i][j] + w[j][k 20
32
                                                   30
                                                                                                                                                                    if (gp[start][i] != inf)
               gp[a][b] = 1;
                                                   31
                                                              if(from != to){
                                                                                                                                       1;
                                                                                                                                                         21
34
               gp[b][a] = 1;
                                                   32
                                                                  merge(from, to, union set);
                                                                                                      29
                                                                                                                                                         22
                                                                  edge += 1;
                                                                                                                                  trace(i, j);
35
                                                   33
                                                                                                      30
                                                                                                                                                         23
                                                                                                                                                                        edges tmp;
                                                                                                                                  cycle[c++] = k;
           vector<int> solution(n + 1, -1);
                                                   34
                                                                  cost += cur.weight;
                                                                                                      31
                                                                                                                                                         24
                                                                                                                                                                         tmp.from = start;
           vector<bool> pass(n + 1, false);
                                                   35
                                                                                                                                                         25
                                                                                                                                                                        tmp.to = i;
                                                                                                      32
                                                                                                                                                                        tmp.weight = gp[start][i];
           solution[1] = 0;
                                                   36
                                                              pq.pop();
                                                                                                      33
                                                                                                                                                         26
           pass[1] = true:
                                                                                                                 for (int i = 0; i < n; ++i)
                                                                                                                                                                        pq.push(tmp);
39
                                                  37
                                                                                                      34
                                                                                                                                                         27
           bool flag = false;
                                                          if(edge < n-1)</pre>
40
                                                   38
                                                                                                      35
                                                                                                                                                         28
                                                              cout << "No mst" << endl:
           hamilton(gp, 1,1 ,solution,pass,flag
                                                                                                      36
                                                                                                                     for (int i = 0: i < n: ++i)
                                                                                                                                                         29
                                                   40
                                                                                                      37
                                                                                                                                                         30
                                                                                                                                                                pass[start] = true;
           if(!flag)
                                                              cout << cost << endl;</pre>
                                                                                                      38
                                                                                                                          if (d[i][k] + d[k][j] < d[i</pre>
                                                                                                                                                         31
                                                                                                                                                                while (!pq.empty() && edge < n - 1)</pre>
42
                                                   41
               cout << "N" << endl:
43
                                                   42 }
                                                                                                                              ][j])
                                                                                                                                                         32
                                                   43 int main(){
                                                                                                                                                                    edges cur = pq.top();
44
                                                                                                      39
                                                                                                                          {
                                                                                                                                                         33
       return 0;
                                                   44
                                                          int n;
                                                                                                      40
                                                                                                                              d[i][j] = d[i][k] + d[k]
                                                                                                                                                         34
45
                                                                                                                                                                    pq.pop();
                                                          cin >> n:
                                                                                                                                                                    if (!pass[cur.to])
46
                                                   45
                                                                                                                                   ][j];
                                                                                                                                                         35
47
                                                   46
                                                          int a, b, d;
                                                                                                                              p[i][j] = p[i][k];
                                                                                                                                                         36
                                                                                                      41
                                                          priority_queue<edges> pq;
                                                                                                                                                                         for (int i = 0; i < n; i++)
48
                                                   47
                                                                                                      42
                                                                                                                                                         37
                                                   48
                                                          while(cin>>a>>b>>d){
                                                                                                      43
                                                                                                                     }
                                                                                                                                                         38
                                                   49
                                                              if(a == -1 \&\& b == -1 \&\& d == -1)
                                                                                                                                                         39
                                                                                                                                                                             if (gp[cur.to][i] != inf)
                                                                                                      44
                                                                                                                 }
                                                   50
                                                                  break:
                                                                                                      45
                                                                                                                                                         40
52 3 4
                                                   51
                                                              edges tmp;
                                                                                                             if (weight == 1e9)
                                                                                                      46
                                                                                                                                                         41
                                                                                                                                                                                 edges tmp;
53 3 1
                                                   52
                                                              tmp.from = a;
                                                                                                      47
                                                                                                                 cout << "No exist";</pre>
                                                                                                                                                                                 tmp.from = cur.to;
                                                                                                                                                         42
54 0 0
                                                   53
                                                              tmp.to = b:
                                                                                                      48
                                                                                                             else
                                                                                                                                                                                 tmp.to = i:
                                                                                                                                                         43
55 output: 1 3 4 2 1
                                                                                                                                                                                 tmp.weight = gp[cur.to][
                                                   54
                                                              tmp.weight = d;
                                                                                                      49
                                                                                                                                                         44
56 */
                                                   55
                                                              pq.push(tmp);
                                                                                                      50
                                                                                                                 bug(weight);
                                                   56
                                                                                                      51
                                                                                                                 bug(c);
                                                                                                                                                                                 pq.push(tmp);
                                                                                                                                                         45
                                                   57
                                                          kruskal(pq, n);
                                                                                                      52
                                                                                                                 bugarr(cycle);
                                                                                                                                                         46
                                                   58
                                                          return 0:
                                                                                                      53
                                                                                                                                                         47
   5.8 Kruskal
                                                                                                                                                                        pass[cur.to] = true;
                                                                                                      54
                                                                                                                                                         48
                                                                                                      55 w.resize(n, vector<int>(n, INF));
                                                                                                                                                         49
                                                                                                                                                                        edge += 1;
                                                                                                      56 d.resize(n, vector<int>(n, INF));
                                                                                                                                                         50
                                                                                                                                                                        cost += cur.weight;
1 /*mst - Kruskal*/
                                                                                                      57 p.resize(n, vector<int>(n));
                                                                                                                                                         51
   struct edges{
                                                                                                      58 cycle.resize(n);
                                                                                                                                                         52
                                                      5.9 Minimum Weight Cycle
       int from:
                                                                                                      59 //Edge input
                                                                                                                                                         53
                                                                                                                                                                if (edge < n - 1)
       int to;
                                                                                                      60 w[a][b] = w;
                                                                                                                                                         54
                                                                                                                                                                    cout << "No mst" << endl;
                                                                                                      61 | d[a][b] = w;
                                                                                                                                                         55
       int weight;
       friend bool operator < (edges a, edges b 1 // 最小環
                                                                                                      62 p[a][b] = b;
                                                                                                                                                         56
                                                                                                                                                                    cout << cost << endl;</pre>
                                                    2 // 圖上無負環!!!!
                                                                                                      63 init(n);
                                                                                                                                                         57
           return a.weight > b.weight;
                                                   3 #define INF 99999
                                                                                                      64 minimum cycle(n);
                                                                                                                                                            int main()
                                                                                                                                                         59
                                                    4 vector<vector<int>> w, d, p;
9
   };
                                                   5 vector<int> cycle;
                                                                                                                                                                int n;
   int find(int x, vector < int > & union set){
                                                    6 | int c = 0;
                                                                                                                                                                cin >> n;
                                                                                                         5.10 Prim
       if(x != union_set[x])
                                                     void trace(int i, int j)
                                                                                                                                                                int a, b, d;
           union_set[x] = find(union_set[x],
                                                                                                                                                                vector<vector<int>> gp(n, vector<int>(n,
                                                          cycle[c++] = i;
                union set);
       return union_set[x];
                                                          if (i != j)
                                                                                                       1 /*mst - Prim*/
                                                                                                                                                                while (cin >> a >> b >> d)
                                                   10
                                                                                                       2 #define inf 99999
14 }
                                                   11
                                                              trace(p[i][j], j);
                                                                                                                                                         65
                                                                                                       3 struct edges
   void merge(int a,int b,vector<int>&
                                                                                                                                                                    if (a == -1 && b == -1 && d == -1)
                                                   12 }
       union_set){
                                                   13 void init(int n)
                                                                                                                                                                        break;
       int pa = find(a, union set);
                                                                                                             int from;
                                                                                                                                                                    if (gp[a][b] > d)
       int pb = find(b, union_set);
                                                          for (int i = 0; i < n; ++i)
                                                                                                                                                                        gp[a][b] = d;
       if(pa != pb)
                                                   16
                                                              d[i][i] = 0;
                                                                                                             int weight;
           union set[pa] = pb;
                                                   17 }
                                                                                                             friend bool operator<(edges a, edges b)</pre>
                                                                                                                                                                Prim(gp, n, 0);
                                                   18 | void minimum_cycle(int n)
                                                                                                                                                         72
                                                                                                                                                                return 0;
   void kruskal(priority queue<edges> pq,int n)
                                                                                                      10
                                                                                                                 return a.weight > b.weight;
                                                          int weight = 1e9;
                                                                                                      11
       vector<int> union set(n, 0);
                                                   21
                                                          for (int k = 0; k < n; ++k)
                                                                                                      12 };
       for (int i = 0; i < n; i++)
                                                   22
                                                                                                      13 void Prim(vector<vector<int>> gp, int n, int
           union set[i] = i;
                                                   23
                                                              for (int i = 0; i < k; ++i)
                                                                                                                                                            5.11 Union find
```

14 {

vector<bool> pass(n, false);

for (int j = 0; j < k; ++j)

if (i != j)

24

int edge = 0;

int cost = 0; //evaluate cost of mst

```
1 // union find from 台大
2 vector<int> father;
  vector<int> people;
   void init(int n)
       for (int i = 0; i < n; i++)
           father[i] = i;
           people[i] = 1;
   int Find(int x)
13
      if (x != father[x])
           father[x] = Find(father[x]);
      return father[x];
17
   void Union(int x, int y)
20
       int m = Find(x);
21
      int n = Find(y);
      if (m != n)
           father[n] = m;
25
           people[m] += people[n];
```

# Mathematics

#### 6.1 Catalan

```
Catalan number
```

```
• 0~19項的catalan number
    0 1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 16796, 58786,
      208012, 742900, 2674440, 9694845, 35357670, 129644790,
      477638700, 1767263190
 \circ 公式: C_n = \frac{1}{n+1} {2n \choose n} = \frac{(2n)!}{(n+1)!n!}
```

# 6.2 Combination

```
1 /*input type string or vector*/
  for (int i = 0; i < (1 << input.size()); ++i <sup>43</sup>
      string testCase = "";
      for (int j = 0; j < input.size(); ++j)</pre>
           if (i & (1 << j))</pre>
               testCase += input[j];
```

### 6.3 Extended Euclidean

pair<long long, long long> extgcd(long long

 $1 \mid // ax + by = gcd(a,b)$ 

if (b == 0)

a, long long b)

return {1, 0};

long long k = a / b;

```
pair<long long, long long> p = extgcd(b,
             a - k * b);
       //cout << p.first << " " << p.second <<
       //cout << "商數(k)= " << k << endl <<
       return {p.second, p.first - k * p.second
11 }
12
13 int main()
14 {
       int a, b;
       cin >> a >> b;
       pair<long long, long long> xy = extgcd(a
            , b); //(x0,y0)
       cout << xy.first << " " << xy.second <<</pre>
       cout << xy.first << " * " << a << " + "
            << xy.second << " * " << b << endl;
20
       return 0;
21 }
|22| // ax + by = gcd(a,b) * r
23 /*find |x|+|y| -> min*/
24 int main()
25
       long long r, p, q; /*px+qy = r*/
       int cases;
       cin >> cases;
       while (cases--)
           cin >> r >> p >> q;
           pair<long long, long long> xy =
                extgcd(q, p); //(x0,y0)
           long long ans = 0, tmp = 0;
           double k, k1;
           long long s, s1;
           k = 1 - (double)(r * xv.first) / p:
           s = round(k);
           ans = llabs(r * xy.first + s * p) +
                llabs(r * xy.second - s * q);
                                                  14
           k1 = -(double)(r * xy.first) / p;
39
                                                  15
40
           s1 = round(k1):
           /*cout << k << endl << k1 << endl;
               cout << s << endl << s1 << endl;</pre>
           tmp = llabs(r * xy.first + s1 * p) +
                 llabs(r * xy.second - s1 * q);
                                                  21
           ans = min(ans, tmp);
44
45
46
           cout << ans << endl;</pre>
                                                  24
47
                                                  ^{25}
       return 0;
```

#### 6.4 Fermat

# 6.6 Log

```
• a^{(p-1)} \equiv 1 \pmod{p} \iff a * a^{(p-2)} \equiv 1
     \circ a^{(p-2)} \equiv 1/a
• 同餘因數定理
```

- $\circ \ a \equiv b \pmod{p} \iff k|a-b|$
- 同餘加法性質  $\circ \ a \equiv b \pmod{p}$  and  $c \equiv d \pmod{p}$

 $\langle = \rangle a + c \equiv b + d \pmod{p}$ 

- 同餘相乘件質
  - $\circ \ a \equiv b \pmod{p}$  and  $c \equiv d \pmod{p}$  $\langle = \rangle \ ac \equiv bd \ (mod \ p)$
- 同餘次方件質
  - $\circ \ a \equiv b \pmod{p} \iff a^n \equiv b^n \pmod{p}$
- 同餘倍方件質
  - $\circ \ a \equiv b \pmod{p} \iff am \equiv bm \pmod{p}$

#### 6.5 Hex to Dec

1 int HextoDec(string num) //16 to 10

#### 6.7 Mod

1 double mylog(double a, double base)

return log(a) / log(base);

//a 的對數底數 b = 自然對數 (a) / 自然對

```
int base = 1;
       int temp = 0;
       for (int i = num.length() - 1; i >= 0; i
                                                   1 int pow mod(int a, int n, int m) // a ^ n
                                                          mod m;
           if (num[i] >= '0' && num[i] <= '9')</pre>
                                                                                      // a, n, m
                                                          < 10 ^ 9
               temp += (num[i] - 48) * base;
                                                         if (n == 0)
               base = base * 16;
                                                             return 1;
                                                         int x = pow mid(a, n / 2, m);
           else if (num[i] >= 'A' && num[i] <=</pre>
                                                         long long ans = (long long)x * x % m;
                                                         if (n % 2 == 1)
                                                             ans = ans * a % m;
               temp += (num[i] - 55) * base;
                                                         return (int)ans;
               base = base * 16;
                                                    int inv(int a, int n, int p) // n = p-2
       return temp;
                                                         long long res = 1;
                                                         for (; n; n >>= 1, (a *= a) %= p)
20 void DecToHex(int p) //10 to 16
                                                             if (n & 1)
                                                                 (res *= a) %= p;
       char *1 = new (char);
                                                         return res;
       sprintf(1, "%X", p);
       //int l intResult = stoi(l);
       cout << 1 << "\n";
       //return l_intResult;
```

```
Mod 性質
                                                           3 bitset<maxn> is notp:
                                                           4 void PrimeTable()
                                                                                                                      40 }
                                                                                                                                                                                          double L = 0, R = /*區間*/, M;
                                                                                                                      41 bool Miller Rabin(ll n)
                                                                                                                                                                                          while (R - L >= eps)
   加法: (a+b) \mod p = (a \mod p + b \mod p) \mod p
                                                                   is notp.reset();
                                                                                                                      42
   減法: (a-b) \mod p = (a \mod p - b \mod p + p) \mod p
                                                                   is notp[0] = is notp[1] = 1;
                                                                                                                      43
                                                                                                                               11 x, pre, u = n - 1;
                                                                                                                                                                                               M = (R + L) / 2;
                                                                   for (int i = 2; i \leftarrow \max_{i \in A} (i + i)
                                                                                                                               int i, j, k = 0;
                                                                                                                                                                                               if (/*函數*/ > /*方程式目標*/)
   乘法: (a * b) \mod p = (a \mod p \cdot b \mod p) \mod p
                                                                                                                               if (n == 2 || n == 3 || n == 5 || n == 7
                                                                        if (!is notp[i])
                                                                                                                                      || n == 11)
   次方: (a^b) \mod p = ((a \mod p)^b) \mod p
                                                                                                                                                                                               else
                                                                             p.push back(i);
                                                                                                                                                                                                    R = M:
   加法結合律: ((a+b) \mod p + c) \mod p = (a+(b+c)) \mod p
                                                                        for (int j = 0; j < (int)p.size();</pre>
                                                                                                                               if (n == 1 || !(n % 2) || !(n % 3) || !(
                                                                              ++i)
                                                                                                                                    n % 5) || !(n % 7) || !(n % 11))
   乘法結合律: ((a \cdot b) \mod p \cdot c) \mod p = (a \cdot (b \cdot c)) \mod p
                                                                                                                                                                                  13
                                                                                                                                                                                          printf("%.31f\n", R);
                                                                                                                                    return 0:
                                                           13
   加法交換律: (a+b) \mod p = (b+a) \mod p
                                                                             if (i * p[j] > maxn)
                                                          14
                                                                                                                      49
                                                                                                                               while (!(u & 1))
                                                                                 break;
                                                           15
                                                                                                                      50
   乘法交換律: (a \cdot b) \mod p = (b \cdot a) \mod p
                                                                             is notp[i * p[j]] = 1;
                                                           16
                                                                                                                      51
                                                                                                                                   k++;
   結合律: ((a+b) \bmod p \cdot c) = ((a \cdot c) \bmod p + (b \cdot c) \bmod p) \bmod p
                                                                             if (i % p[j] == 0)
                                                                                                                      52
                                                                                                                                   u >>= 1;
                                                                                                                                                                                     6.14 公式
                                                                                  break:
                                                                                                                      53
   如果 a \equiv b \pmod{m} · 我們會說 a, b 在模 m 下同餘
                                                                                                                               srand((long long)12234336);
                                                          19
                                                                                                                      54
                                                                                                                                                                                     S_n = \frac{a(1-r^n)}{1-r} a_n = \frac{a_1 + a_n}{2} \sum_{k=1}^n k = \frac{n(n+1)}{2}
                                                                                                                      55
                                                                                                                               for (i = 1; i <= 50; i++)
                                                          20
   以下為性質
                                                          21 }
                                                                                                                      56
    • 整除性: a \equiv b \pmod{m} \Rightarrow c \cdot m = a - b, c \in \mathbb{Z}
                                                                                                                      57
                                                                                                                                   x = rand() % (n - 2) + 2;
                                                                                                                                                                                     \sum_{k=1}^{n} k^{2} = \frac{n(n+1)(2n+1)}{6} \sum_{k=1}^{n} k^{3} = \left[\frac{n(n+1)}{2}\right]^{2}
            \Rightarrow a \equiv b \pmod{m} \Rightarrow m \mid a - b
                                                                                                                      58
                                                                                                                                    if (!(n % x))
                                                                                                                      50
                                                                                                                                        return 0:
    6.11 Prime 判斷
                                                                                                                                   x = qpow(x, u, n);
                                                                                                                      60
             則 a \equiv d \pmod{c}
                                                                                                                                   pre = x;
                                                                                                                      61

    保持基本運算:

                                                                                                                                   for (j = 1; j <= k; j++)
                                                                                                                      62
                                                                                                                                                                                                四則運算
                                                                                                                                                                                     6.15
         \left\{ \begin{aligned} a &\equiv b (\operatorname{mod} m) \\ c &\equiv d (\operatorname{mod} m) \end{aligned} \right. \Rightarrow \left\{ \begin{aligned} a &\pm c \equiv b \pm d (\operatorname{mod} m) \\ a \cdot c &\equiv b \cdot d (\operatorname{mod} m) \end{aligned} \right.
                                                           1 typedef long long 11;
                                                                                                                      63
                                                           2 11 modmul(11 a, 11 b, 11 mod)
                                                                                                                      64
                                                                                                                                        x = modmul(x, x, n);
                                                                                                                                        if (x == 1 && pre != 1 && pre !=
                                                                                                                      65
                                                                                                                                                                                   1 | string s = ""; //開頭是負號要補0

    放大縮小模數

                                                                   11 \text{ ret} = 0:
                                                                                                                                               n - 1)
                                                                                                                                                                                   2 long long int DFS(int le, int ri) // (0,
      k \in \mathbb{Z}^+, a \equiv b \pmod{m} \Leftrightarrow k \cdot a \equiv k \cdot b \pmod{k \cdot m}
                                                                   for (; b; b >>= 1, a = (a + a) % mod)
                                                                                                                                             return 0;
                                                                                                                      66
                                                                                                                                                                                           string final index)
    模逆元是取模下的反元素 · 即為找到 a^{-1} 使得 aa^{-1} \equiv 1 \mod c 。
                                                                        if (b & 1)
                                                                                                                      67
                                                                                                                                        pre = x;
                                                                            ret = (ret + a) % mod:
                                                                                                                      68
   整數 a \in \text{mod } c 下要有模反元素的充分必要條件為 a, c 互質
                                                                                                                                                                                          int c = 0;
                                                                                                                                   if (x != 1)
                                                                   return ret;
                                                                                                                      69
                                                                                                                                                                                          for (int i = ri; i >= le; i--)
                                                                                                                                        return 0;
                                                                                                                      70
    模逆元如果存在會有無限個,任意兩相鄰模逆元相差 c
                                                           10 11 qpow(11 x, 11 u, 11 mod)
                                                                                                                      71
                                                                                                                                                                                               if (s[i] == ')')
   費馬小定理
                                                          11
                                                                                                                      72
                                                                                                                               return 1;
                                                                                                                                                                                                    C++;
                                                                   ll ret = 111;
   給定一個質數 p 及一個整數 a · 那麼 : a^p \equiv a \pmod{p} 如果 \gcd(a,p) = 1
                                                                                                                                                                                               if (s[i] == '(')
                                                                   for (; u; u >>= 1, x = modmul(x, x, mod) 74 / /  if (Miller Rabin(n)) puts("Prime");
   a^{p-1} \equiv 1 \pmod{p}
                                                                                                                                                                                                    c - - :
                                                                                                                                                                                               if (s[i] == '+' && c == 0)
                                                                        if (u & 1)
                                                                                                                                                                                                    return DFS(le, i - 1) + DFS(i +
   歐拉定理
                                                                            ret = modmul(ret, x, mod);
                                                           15
                                                                                                                         6.12 Round(小數)
                                                                   return ret;
   歐拉定理是比較 general 版本的費馬小定理。給定兩個整數 n 和 a ,如果 gcd(a,n)
                                                                                                                                                                                               if (s[i] == '-' && c == 0)
   a^{\Phi(n)} \equiv 1 \pmod{n} 如果 n 是質數 \Phi(n) = n-1 也就是費馬小定理。
                                                                                                                                                                                                    return DFS(le, i - 1) - DFS(i +
                                                                                                                                                                                  14
                                                          18 11
                                                                 gcd(ll a, ll b)
                                                                                                                                                                                                         1. ri):
                                                           19
                                                                                                                       1 double myround(double number, unsigned int
   Wilson's theorem
                                                                                                                                                                                  15
                                                                   return b ? gcd(b, a % b) : a;
                                                                                                                               bits)
                                                                                                                                                                                          for (int i = ri; i >= le; i--)
                                                                                                                                                                                  16
                                                          21 | }
   給定一個質數 p \cdot \mathbb{H} : (p-1)! \equiv -1 \pmod{p}
                                                                                                                                                                                  17
                                                                                                                               LL integerPart = number;
                                                          22 | 11 Pollard_Rho(11 n, 11 c)
                                                                                                                                                                                               if (s[i] == ')')
                                                                                                                                                                                  18
                                                                                                                               number -= integerPart;
                                                          23
                                                                                                                                                                                                    c++;
                                                                   11 i = 1, j = 2, x = rand() % (n - 1) +
                                                                                                                               for (unsigned int i = 0; i < bits; ++i)</pre>
                                                                                                                                                                                               if (s[i] == '(')
                                                                        1, y = x;
                                                                                                                                   number *= 10;
                                                                   while (1)
                                                                                                                               number = (LL)(number + 0.5);
                                                          25
         _{\rm PI}
  6.9
                                                                                                                                                                                               if (s[i] == '*' && c == 0)
                                                           26
                                                                                                                               for (unsigned int i = 0; i < bits; ++i)</pre>
                                                                                                                                                                                                    return DFS(le, i - 1) * DFS(i +
                                                          27
                                                                                                                                   number /= 10;
                                                                                                                                                                                                         1, ri);
                                                                        x = (modmul(x, x, n) + c) % n;
                                                                                                                               return integerPart + number;
                                                           28
1 #define PI acos(-1)
                                                                                                                                                                                               if (s[i] == '/' \&\& c == 0)
                                                                                                                                                                                  24
                                                                        11 p = gcd((y - x + n) \% n, n);
                                                                                                                      11 }
                                                           29
2 #define PI M PI
                                                                                                                                                                                                    return DFS(le, i - 1) / DFS(i +
                                                                                                                                                                                  25
                                                                                                                      12 //printf("%.1f\n", round(3.4515239, 1));
                                                           30
                                                                        if (p != 1 && p != n)
                                                                                                                                                                                                          1, ri);
                                                          31
                                                                            return p;
                                                                                                                                                                                               if (s[i] == '%' && c == 0)
                                                                                                                                                                                  26
                                                           32
                                                                        if (y == x)
                                                                                                                                                                                                    return DFS(le, i - 1) % DFS(i +
                                                                                                                                                                                  27
                                                           33
                                                                            return n;
  6.10 Prime table
                                                                                                                         6.13 一分逼折法
                                                                                                                                                                                                         1, ri);
                                                          34
                                                                        if (i == j)
                                                                                                                                                                                  28
                                                           35
                                                                                                                                                                                          if ((s[le] == '(') && (s[ri] == ')'))
                                                                                                                                                                                  29
                                                           36
                                                                            y = x;
                                                                                                                                                                                               return DFS(le + 1, ri - 1); //去除刮
1 const int maxn = sqrt(INT MAX);
                                                                                                                       1 #define eps 1e-14
                                                          37
                                                                            j <<= 1;
```

void half interval()

vector<int>p;

```
if (s[le] == ' ' && s[ri] == ' ')
          return DFS(le + 1, ri - 1); //去除左
32
      if (s[le] == ' ')
33
          return DFS(le + 1, ri); //去除左邊空
34
      if (s[ri] == ' ')
35
          return DFS(le, ri - 1); //去除右邊空
36
      long long int num = 0;
      for (int i = le; i <= ri; i++)
          num = num * 10 + s[i] - '0';
39
40
       return num;
```

# 6.16 因數表

```
1 vector<vector<int>> arr(10000000);
2 const int limit = 10e7;
3 for (int i = 1; i <= limit; i++)</pre>
5
      for (int j = i; j <= limit; j += i)</pre>
6
          arr[i].pb(i): // i 為因數
```

# 數字乘法組合

```
1 void dfs(int j, int old, int num, vector<int</pre>
        > com, vector<vector<int>> &ans)
       for (int i = j; i <= sqrt(num); i++)</pre>
           if (old == num)
                com.clear();
           if (num % i == 0)
                vector<int> a;
                a = com;
                a.push back(i);
                finds(i, old, num / i, a, ans);
                a.push back(num / i);
                ans.push_back(a);
17
   vector<vector<int>> ans:
   vector<int> zero;
  dfs(2, num, num, zero, ans);
   /*/num 為 input 數字*/
   for (int i = 0; i < ans.size(); i++)</pre>
23
       for (int j = 0; j < ans[i].size() - 1; j</pre>
24
           cout << ans[i][j] << " ";</pre>
25
       cout << ans[i][ans[i].size() - 1] <<</pre>
26
```

# 6.18 數字加法組合

```
1 | void recur(int i, int n, int m, vector<int>
        &out, vector<vector<int>> &ans)
       if (n == 0)
           for (int i : out)
               if (i > m)
                    return;
           ans.push back(out);
10
       for (int j = i; j <= n; j++)
11
12
           out.push back(j);
13
           recur(j, n - j, m, out, ans);
14
           out.pop back();
15
16
   vector<vector<int>> ans;
   vector<int> zero;
19 recur(1, num, num, zero, ans);
20 // num 為 input 數字
21 for (int i = 0; i < ans.size(); i++)
22 {
       for (int j = 0; j < ans[i].size() - 1; j</pre>
24
           cout << ans[i][j] << " ";
25
       cout << ans[i][ans[i].size() - 1] <<</pre>
            endl:
26 }
```

#### 羅馬數字 6.19

11

12

14

15

16

17

18

19

```
1 int romanToInt(string s)
      unordered map<char, int> T;
      T['I'] = 1;
      T['V'] = 5:
      T['X'] = 10;
      T['L'] = 50;
      T['C'] = 100;
      T['D'] = 500;
      T['M'] = 1000;
      int sum = T[s.back()];
      for (int i = s.length() - 2; i >= 0; --i
          if (T[s[i]] < T[s[i + 1]])</pre>
              sum -= T[s[i]];
              sum += T[s[i]];
      return sum:
```

#### 質因數分解 6.20

```
1 LL ans:
2 void find(LL n, LL c) // 配合質數判斷
      if (n == 1)
          return;
      if (Miller Rabin(n))
          ans = min(ans, n);
          // bug(ans); //質因數
10
          return:
11
12
      LL x = n, k = c;
      while (x == n)
13
          x = Pollard_Rho(x, c--);
14
      find(n / x, k);
15
      find(x, k);
16
```

# 6.21 質數數量

```
1 // 10 ^ 11 左右
2 #define LL long long
                                                    64
3 const int N = 5e6 + 2;
                                                    65
 4 bool np[N];
5 int prime[N], pi[N];
6 int getprime()
                                                    67
                                                    68
       int cnt = 0;
       np[0] = np[1] = true;
       pi[0] = pi[1] = 0;
10
11
       for (int i = 2; i < N; ++i)
12
           if (!np[i])
13
14
               prime[++cnt] = i;
15
           pi[i] = cnt;
           for (int j = 1; j <= cnt && i *
16
                prime[j] < N; ++j)</pre>
17
18
               np[i * prime[j]] = true;
               if (i % prime[j] == 0)
19
20
                    break;
21
22
23
       return cnt;
24
25 const int M = 7;
26 const int PM = 2 * 3 * 5 * 7 * 11 * 13 * 17;
27 int phi[PM + 1][M + 1], sz[M + 1];
28 void init()
29
30
       getprime();
       sz[0] = 1;
31
32
       for (int i = 0; i \leftarrow PM; ++i)
33
           phi[i][0] = i;
34
       for (int i = 1; i <= M; ++i)
35
36
           sz[i] = prime[i] * sz[i - 1];
37
           for (int j = 1; j <= PM; ++j)</pre>
               phi[j][i] = phi[j][i - 1] - phi[ 96
38
                    i / prime[i]][i - 1];
39
40 }
```

```
42
43
       LL r = (LL) sqrt(x - 0.1);
44
       while (r * r <= x)
45
       return int(r - 1);
47
  int sqrt3(LL x)
48
49
       LL r = (LL)cbrt(x - 0.1);
51
       while (r * r * r <= x)
52
           ++r;
       return int(r - 1);
53
54
55
  LL getphi(LL x, int s)
56
       if (s == 0)
57
58
           return x;
59
       if (s <= M)
           return phi[x % sz[s]][s] + (x / sz[s
                ]) * phi[sz[s]][s];
       if (x <= prime[s] * prime[s])</pre>
61
62
           return pi[x] - s + 1;
63
       if (x <= prime[s] * prime[s] * prime[s]</pre>
            && x < N
           int s2x = pi[sqrt2(x)];
66
           LL ans = pi[x] - (s2x + s - 2) * (
                s2x - s + 1) / 2;
           for (int i = s + 1; i <= s2x; ++i)
               ans += pi[x / prime[i]];
69
           return ans;
70
       return getphi(x, s - 1) - getphi(x /
71
            prime[s], s - 1);
72
73
  LL getpi(LL x)
74
75
       if(x < N)
           return pi[x];
76
       LL ans = getphi(x, pi[sqrt3(x)]) + pi[
77
            sqrt3(x)] - 1;
       for (int i = pi[sqrt3(x)] + 1, ed = pi[
            sqrt2(x)]; i <= ed; ++i)
           ans -= getpi(x / prime[i]) - i + 1;
       return ans;
81
  LL lehmer pi(LL x)
       if(x < N)
           return pi[x];
       int a = (int)lehmer pi(sqrt2(sqrt2(x)));
       int b = (int)lehmer pi(sqrt2(x));
       int c = (int)lehmer_pi(sqrt3(x));
       LL sum = getphi(x, \overline{a}) + (LL)(\overline{b} + \overline{a} - 2)
            * (b - a + 1) / 2;
       for (int i = a + 1; i <= b; i++)
           LL w = x / prime[i];
           sum -= lehmer pi(w);
           if (i > c)
               continue;
           LL lim = lehmer pi(sqrt2(w));
           for (int j = i; j <= lim; j++)
               sum -= lehmer_pi(w / prime[j]) -
                      (j - 1);
```

41 int sqrt2(LL x)

21

```
return sum;
102 // lehmer pi(n)
```

# Other

# 7.1 binary search 三類變化

```
1 / / 查找和目標值完全相等的數
  int find(vector<int> &nums, int target)
      int left = 0, right = nums.size();
      while (left < right)
          int mid = left + (right - left) / 2;
          if (nums[mid] == target)
              return mid;
          else if (nums[mid] < target)</pre>
              left = mid + 1;
          else
              right = mid;
13
14
15
      return -1;
16
   // 找第一個不小於目標值的數 == 找最後一個小
       於目標值的數
   /*(lower bound)*/
   int find(vector<int> &nums, int target)
      int left = 0, right = nums.size();
22
      while (left < right)</pre>
          int mid = left + (right - left) / 2;
          if (nums[mid] < target)</pre>
              left = mid + 1;
              right = mid;
30
      return right;
     找第一個大於目標值的數 == 找最後一個不大
       於目標值的數
   /*(upper bound)*/
   int find(vector<int> &nums, int target)
35
      int left = 0, right = nums.size();
37
      while (left < right)</pre>
38
          int mid = left + (right - left) / 2;
39
          if (nums[mid] <= target)</pre>
              left = mid + 1;
              right = mid;
      return right;
```

# 7.2 heap sort

, int length)

int left = 2 \* root,

```
right = 2 * root + 1,
                                                   23
           largest;
       if (left <= length && array[left] >
            array[root])
                                                   25
           largest = left;
                                                   26
       else
                                                   27
           largest = root;
                                                   28
       if (right <= length && array[right] >
                                                   29
            array[largest])
                                                   30
           largest = right;
                                                   31
       if (largest != root)
^{12}
                                                   32
13
                                                   33
           swap(array[largest], array[root]);
14
           MaxHeapify(array, largest, length);
15
   void HeapSort(vector<int> &array)
       array.insert(array.begin(), 0);
       for (int i = (int)array.size() / 2; i >=
             1: i--)
           MaxHeapify(array, i, (int)array.size 2 {
22
                () - 1);
       int size = (int)array.size() - 1;
23
24
       for (int i = (int)array.size() - 1; i >=
             2; i--)
25
26
           swap(array[1], array[i]);
27
           MaxHeapify(array, 1, size);
28
29
       array.erase(array.begin());
30
```

1 | void MaxHeapify(vector<int> &array, int root

# 7.3 Merge sort

```
1 | void Merge(vector<int> &arr, int front, int
       mid, int end)
       vector<int> LeftSub(arr.begin() + front, 22
             arr.begin() + mid + 1);
       vector<int> RightSub(arr.begin() + mid + 23
             1, arr.begin() + end + 1);
       LeftSub.insert(LeftSub.end(), INT_MAX); 25
       RightSub.insert(RightSub.end(), INT MAX) 26 }
       int idxLeft = 0, idxRight = 0;
       for (int i = front; i <= end; i++)</pre>
11
12
           if (LeftSub[idxLeft] <= RightSub[</pre>
                idxRight])
               arr[i] = LeftSub[idxLeft];
14
               idxLeft++;
```

#### else arr[i] = RightSub[idxRight]; idxRight++; 20 22

```
void MergeSort(vector<int> &arr, int front,
    // front = 0 , end = arr.size() - 1
    if (front < end)</pre>
        int mid = (front + end) / 2:
        MergeSort(arr, front, mid);
```

MergeSort(arr, mid + 1, end);

Merge(arr, front, mid, end);

int Partition(vector<int> &arr, int front,

# 7.4 Quick

```
int end)
       int pivot = arr[end];
       int i = front - 1;
       for (int j = front; j < end; j++)</pre>
           if (arr[j] < pivot)</pre>
                i++;
                swap(arr[i], arr[j]);
12
13
       i++;
       swap(arr[i], arr[end]);
14
       return i:
16 }
  void QuickSort(vector<int> &arr, int front,
        int end)
       // front = 0 , end = arr.size() - 1
       if (front < end)</pre>
20
```

# 7.5 Weighted Job Scheduling

int pivot = Partition(arr, front,

QuickSort(arr, front, pivot - 1);

QuickSort(arr, pivot + 1, end);

```
int start, finish, profit;
5 bool jobComparataor(Job s1, Job s2)
```

```
return (s1.finish < s2.finish);</pre>
  int latestNonConflict(Job arr[], int i)
       for (int j = i - 1; j >= 0; j--)
11
12
           if (arr[j].finish <= arr[i].start)</pre>
15
16
       return -1;
17
  int findMaxProfit(Job arr[], int n)
18
19
20
       sort(arr, arr + n, jobComparataor);
21
       int *table = new int[n];
       table[0] = arr[0].profit;
22
23
       for (int i = 1; i < n; i++)
24
           int inclProf = arr[i].profit;
25
26
           int 1 = latestNonConflict(arr, i);
           if (1 != -1)
27
28
               inclProf += table[1]:
29
           table[i] = max(inclProf, table[i -
                1]);
30
       int result = table[n - 1];
31
32
       delete[] table;
33
34
       return result;
```

#### 7.6 數獨解法

```
int getSquareIndex(int row, int column, int
     return row / n * n + column / n;
 bool backtracking(vector<vector<int>> &board
      , vector<vector<bool>> &rows, vector<</pre>
      vector<bool>> &cols,
                    vector<vector<bool>> &boxs
                         , int index, int n)
     int n2 = n * n;
     int rowNum = index / n2, colNum = index
          % n2:
     if (index >= n2 * n2)
         return true;
     if (board[rowNum][colNum] != 0)
         return backtracking(board, rows,
               cols, boxs, index + 1, n);
     for (int i = 1; i <= n2; i++)
         if (!rows[rowNum][i] && !cols[colNum
              ][i] && !boxs[getSquareIndex(
               rowNum, colNum, n)][i])
              rows[rowNum][i] = true;
```

```
8.3 Sliding window
               cols[colNum][i] = true;
                                                            while (k > 0 \&\& s[k] != s[q])
23
               boxs[getSquareIndex(rowNum,
                                                 10
                                                                k = next[k];
                    colNum, n)][i] = true;
                                                            if(s[k] == s[q])
                                                 11
               board[rowNum][colNum] = i;
                                                 12
                                                                k++;
               if (backtracking(board, rows,
                                                 13
                                                            next[q] = k;
                   cols, boxs, index + 1, n)
                                                 14
                   return true:
                                                 15 }
               board[rowNum][colNum] = 0;
                                                 16 void KMPMatcher(string text, string pattern)
                                                                                                             letterCnt[t[i]]++;
27
               rows[rowNum][i] = false;
                                                 17
               cols[colNum][i] = false;
                                                        int n = text.length();
                                                                                                         int left = 0, matchCnt = 0;
                                                 18
               boxs[getSquareIndex(rowNum,
                                                 19
                                                        int m = pattern.length();
                    colNum, n) | [i] = false:
                                                        int next[pattern.length()];
                                                 20
                                                        ComputePrefix(pattern, next);
31
                                                 21
                                                                                                  10
32
                                                 22
                                                                                                  11
                                                                                                                 matchCnt++:
33
      return false:
                                                 23
                                                        for (int i = 0, q = 0; i < n; i++)
                                                                                                  12
34
                                                 24
                                                            while (q > 0 && pattern[q] != text[i
35 | /*用法 main*/
                                                                ])
                                                                                                  15
36 int n = sqrt(數獨邊長大小) /*e.g. 9*9 n=3*/
                                                                q = next[q];
                                                                                                  16
  vector<vector<int>> board(n * n + 1, vector
                                                            if (pattern[q] == text[i])
                                                                                                                     minStart = left:
                                                                                                  17
       int>(n * n + 1, 0));
                                                                                                  18
                                                                q++;
  vector<vector<bool>> isRow(n * n + 1, vector
                                                            if (q == m)
                                                                                                  19
       <bool>(n * n + 1, false));
                                                 30
                                                                                                  20
                                                                                                                     matchCnt--:
39 vector<vector<bool>> isColumn(n * n + 1,
                                                                cout << "Pattern occurs with
                                                                                                  21
                                                                                                                 left++;
                                                 31
       vector<bool>(n * n + 1, false));
                                                                     shift " << i - m + 1 << endl 22
  vector<vector<bool>> isSquare(n * n + 1,
                                                                                                  23
       vector<bool>(n * n + 1, false));
                                                                q = 0;
                                                                                                  24
                                                 32
                                                 33
   for (int i = 0; i < n * n; ++i)
42
                                                 34
43
                                                 35 }
44
       for (int j = 0; j < n * n; ++j)
                                                 36 // string s = "abcdabcdebcd":
45
                                                 37 // string p = "bcd";
46
           int number;
                                                 38 // KMPMatcher(s, p);
                                                                                                     8.4 Split
          cin >> number;
                                                 39 // cout << endl;
          board[i][j] = number;
          if (number == 0)
               continue:
          isRow[i][number] = true;
          isColumn[j][number] = true;
                                                    8.2 Min Edit Distance
          isSquare[getSquareIndex(i, j, n)][
                                                                                                         string token;
               number1 = true:
                                                                                                         vector<string> res;
54
55
                                                 int EditDistance(string a, string b)
   if (backtracking(board, isRow, isColumn,
                                                 2 {
       isSquare, 0, n))
                                                        vector<vector<int>> dp(a.size() + 1,
       /*有解答*/
                                                                                                             ps = pe + dl;
                                                             vector<int>(b.size() + 1, 0));
58 else
                                                                                                  10
                                                                                                             res.push back(token);
                                                        int m = a.length(), n = b.length();
       /*解答*/
                                                        for (int i = 0; i < m + 1; i++)
                                                                                                  11
                                                                                                  12
                                                                                                         res.push back(s.substr(ps));
                                                                                                  13
                                                                                                         return res;
                                                            for (int j = 0; j < n + 1; j++)
                                                                if (i == 0)
       String
                                                                    dp[i][j] = j;
                                                                else if (j == 0)
                                                                    dp[i][j] = i;
                                                 12
                                                                else if (a[i - 1] == b[j - 1])
                                                 13
```

else

return dp[m][n];

14

15

16

17

18

19

```
static const int BIGMOD = 10000; //10為
     正常位數
int s;
int v1, v[LEN];
// vector<int> v;
Bigint() : s(1) { vl = 0; }
Bigint(long long a)
   s = 1;
   v1 = 0;
   if (a < 0)
   {
        s = -1:
        a = -a:
    while (a)
        push back(a % BIGMOD);
        a /= BIGMOD:
Bigint(string str)
   s = 1:
   v1 = 0;
    int stPos = 0, num = 0;
    if (!str.empty() && str[0] == '-')
        stPos = 1:
        s = -1;
    for (int i = str.length() - 1, q =
         1: i >= stPos: i--)
        num += (str[i] - '0') * a:
        if ((q *= 10) >= BIGMOD)
            push back(num);
            num = 0;
            a = 1:
    if (num)
        push_back(num);
   n();
int len() const
   return vl; //return SZ(v);
bool empty() const { return len() == 0;
void push_back(int x)
   v[v]++] = x; //v.PB(x);
void pop back()
   vl--; //v.pop_back();
int back() const
    return v[vl - 1]; //return v.back();
void n()
```

## 8.1 KMP

```
1 // 用在在一個 S 內查找一個詞 W 的出現位置
void ComputePrefix(string s, int next[])
3 {
     int n = s.length();
     int q, k;
     next[0] = 0;
     for (k = 0, q = 1; q < n; q++)
```

```
1 string minWindow(string s, string t)
      unordered map<char, int> letterCnt;
      for (int i = 0: i < t.length(): i++)</pre>
      int minLength = INT MAX, minStart = -1;
      for (int i = 0; i < s.length(); i++)
          if (--letterCnt[s[i]] >= 0)
          while (matchCnt == t.length())
              if (i - left + 1 < minLength)</pre>
                  minLength = i - left + 1;
              if (++letterCnt[s[left]] > 0)
      return minLength == INT MAX ? "" : s.
           substr(minStart, minLength):
```

11

14

15

16

17

20

21

22

23

24

26

27

28

31

32

33

36 37

40

41

45

46

47

48

49

50

51

52

57

59

61

62

63

64

```
1 vector<string> mysplit(string s, string d)
      int ps = 0, pe, dl = d.length();
      while ((pe = s.find(d, ps)) != string::
          token = s.substr(ps, pe - ps);
```

# data structure

# 9.1 Bigint

dp[i][j] = dp[i - 1][j - 1];

dp[i][j] = 1 + min(min(dp[i

dp[i - 1][j - 1]);

- 1][j], dp[i][j - 1]),

```
1 / / 台大 / / 非必要請用python
2 struct Bigint
     static const int LEN = 60;
                                      11
```

```
129
68
            while (!empty() && !back())
                                                     130
69
                 pop_back();
                                                     131
70
                                                     132
        void resize(int nl)
71
                                                     133
72
                                                     134
73
            vl = nl:
                                  //v.resize(nl):
                                                     135
            fill(v, v + vl, 0); //fill(ALL(v),
74
                                                     136
                                                     137
75
                                                     138
76
        void print() const
                                                     139
77
                                                     140
78
            if (empty())
                                                     141
79
                                                     142
                 putchar('0');
                                                     143
                 return;
                                                     144
                                                     145
            if (s == -1)
                                                     146
                 putchar('-');
                                                     147
            printf("%d", back());
                                                     148
            for (int i = len() - 2; i >= 0; i--)
                                                     149
                 printf("%.4d", v[i]);
87
                                                     150
88
                                                     151
        friend std::ostream &operator<<(std::</pre>
89
                                                     152
             ostream &out, const Bigint &a)
                                                     153
                                                     154
90
91
            if (a.empty())
                                                     155
92
                                                     156
                 out << "0";
93
                                                     157
                 return out;
                                                     158
94
                                                     159
95
            if (a.s == -1)
                                                     160
                 out << "-"
                                                     161
            out << a.back();
                                                     162
            for (int i = a.len() - 2; i >= 0; i
99
                                                     163
                 --)
                                                     164
100
                                                     165
101
                 char str[10];
                                                     166
                 snprintf(str, 5, "%.4d", a.v[i]) 167
102
                 out << str;
103
                                                     168
104
                                                     169
105
            return out;
                                                     170
106
                                                     171
107
        int cp3(const Bigint &b) const
                                                     172
108
                                                     173
            if (s != b.s)
109
                                                     174
110
                 return s - b.s;
                                                     175
111
            if (s == -1)
                                                     176
                 return -(-*this).cp3(-b);
                                                     177
            if (len() != b.len())
                                                     178
                 return len() - b.len(); //int
                                                     179
             for (int i = len() - 1; i >= 0; i--)
116
                 if (v[i] != b.v[i])
                     return v[i] - b.v[i];
                                                     182
            return 0;
118
                                                     183
119
                                                     184
        bool operator < (const Bigint &b) const
120
121
                                                     186
            return cp3(b) < 0;
                                                     187
122
123
                                                     188
124
        bool operator <= (const Bigint &b) const
                                                     189
125
                                                     190
126
            return cp3(b) <= 0;
                                                     191
127
                                                     192
128
        bool operator==(const Bigint &b) const
```

```
194
    return cp3(b) == 0;
                                             195
                                             196
bool operator!=(const Bigint &b) const
                                             197
                                             198
    return cp3(b) != 0;
                                             199
                                             200
bool operator>(const Bigint &b) const
                                             201
                                             202
    return cp3(b) > 0;
                                             203
                                             204
bool operator>=(const Bigint &b) const
    return cp3(b) >= 0;
                                             206
                                             207
Bigint operator-() const
                                             208
                                             209
    Bigint r = (*this);
                                             210
    r.s = -r.s;
    return r;
                                             211
                                             212
Bigint operator+(const Bigint &b) const
                                             214
    if (s == -1)
                                             215
         return -(-(*this) + (-b));
                                             216
    if (b.s == -1)
                                             217
         return (*this) - (-b);
                                             218
    Bigint r;
                                             219
    int nl = max(len(), b.len());
                                             220
    r.resize(nl + 1);
                                             221
    for (int i = 0; i < nl; i++)
                                             222
        if (i < len())</pre>
                                             223
             r.v[i] += v[i];
                                             224
         if (i < b.len())
                                             225
             r.v[i] += b.v[i];
         if (r.v[i] >= BIGMOD)
                                             226
                                             227
             r.v[i + 1] += r.v[i] /
                                             228
                  BIGMOD;
                                             229
             r.v[i] %= BIGMOD;
                                             230
                                             231
                                             232
    r.n();
                                             233
    return r;
                                             234
Bigint operator-(const Bigint &b) const
    if (s == -1)
                                             238
         return -(-(*this) - (-b));
                                             239
    if (b.s == -1)
                                             240
         return (*this) + (-b);
                                             241
    if ((*this) < b)</pre>
                                             242
        return -(b - (*this));
                                             243
    Bigint r;
                                             244
    r.resize(len());
                                             245
    for (int i = 0; i < len(); i++)
                                             246
                                             247
        r.v[i] += v[i];
         if (i < b.len())</pre>
             r.v[i] -= b.v[i];
         if (r.v[i] < 0)</pre>
             r.v[i] += BIGMOD;
             r.v[i + 1]--;
```

```
r.n();
            return r;
       Bigint operator*(const Bigint &b)
            Bigint r:
            r.resize(len() + b.len() + 1);
            r.s = s * b.s;
            for (int i = 0; i < len(); i++)
                for (int j = 0; j < b.len(); j</pre>
                     ++)
                    r.v[i + j] += v[i] * b.v[j];
                                                  15
                    if (r.v[i + j] >= BIGMOD)
                        r.v[i + j + 1] += r.v[i
                             + j] / BIGMOD;
                        r.v[i + j] \% = BIGMOD;
           r.n();
            return r;
       Bigint operator/(const Bigint &b)
            Bigint r;
            r.resize(max(1, len() - b.len() + 1)
                );
            int oriS = s;
            Bigint b2 = b; // b2 = abs(b)
            s = b2.s = r.s = 1;
            for (int i = r.len() - 1; i >= 0; i
                --)
                int d = 0, u = BIGMOD - 1;
                while (d < u)
                    int m = (d + u + 1) >> 1;
                    r.v[i] = m;
                    if ((r * b2) > (*this))
                        u = m - 1;
                    else
                r.v[i] = d;
            s = oriS;
            r.s = s * b.s;
            r.n();
            return r;
       Bigint operator%(const Bigint &b)
            return (*this) - (*this) / b * b;
248 };
          DisjointSet
```

1 | struct DisjointSet {

```
int p[maxn], sz[maxn], n, cc;
      vector<pair<int*, int>> his;
      vector<int> sh;
      void init(int n) {
          n = n; cc = n;
          for (int i = 0; i < n; ++i) sz[i] =
               1, p[i] = i;
          sh.clear(); his.clear();
      void assign(int *k, int v) {
          his.emplace back(k, *k);
          *k = v:
      void save() {
          sh.push back((int)his.size());
      void undo() {
          int last = sh.back(); sh.pop_back();
          while (his.size() != last) {
              int *k, v;
              tie(k, v) = his.back(); his.
                   pop_back();
               *k = v;
      int find(int x) {
          if (x == p[x]) return x;
          return find(p[x]);
      void merge(int x, int y) {
          x = find(x); y = find(y);
          if (x == y) return;
          if (sz[x] > sz[y]) swap(x, y);
          assign(&sz[y], sz[x] + sz[y]);
          assign(&p[x], y);
          assign(&cc, cc - 1);
37 } ;
  9.3 Matirx
```

11

12

13

14

16

17

18

19

20

21

22

23

24

25

26

27

28

31

32

33

34

35

36

```
1 template <typename T>
  struct Matrix
       using rt = std::vector<T>;
       using mt = std::vector<rt>;
       using matrix = Matrix<T>;
       int r, c; // [r][c]
       Matrix(int r, int c) : r(r), c(c), m(r, r)
            rt(c)) {}
       Matrix(mt a) \{ m = a, r = a.size(), c = a.size() \}
            a[0].size(); }
       rt &operator[](int i) { return m[i]; }
11
       matrix operator+(const matrix &a)
13
14
           matrix rev(r, c);
15
           for (int i = 0; i < r; ++i)
16
                for (int j = 0; j < c; ++j)
                    rev[i][j] = m[i][j] + a.m[i]
17
                         ][j];
18
           return rev;
```

```
matrix operator-(const matrix &a)
                                                                                                      42 };
                                                                                                                                                                                 val[sz] = v:
                                                                                                                                                         99
                                                                                                                                                                                 c[u][index] = sz++;
21
                                                   82
                                                                                                      43
                                                                                                                                                        100
22
           matrix rev(r, c);
                                                              T det = sign ? -1 : 1;
                                                                                                         ostream& operator << (ostream &out, const
                                                   83
                                                                                                                                                        101
           for (int i = 0; i < r; ++i)
                                                                                                                                                                             u = c[u][index];
23
                                                   84
                                                              for (int i = 0; i < r; ++i)
                                                                                                              BigInteger& x){
                                                                                                                                                        102
               for (int j = 0; j < c; ++j)
                                                                                                             out << x.s.back();</pre>
                                                                                                                                                                             max len count++;
24
                                                   85
                                                                                                                                                        103
                   rev[i][j] = m[i][j] - a.m[i
                                                                  det = det * m[i][i];
                                                                                                             for(int i = x.s.size()-2; i >= 0;i--){
25
                                                                                                      46
                                                                                                                                                        1.04
                        1[j];
                                                   87
                                                                  det = det / lazv[i]:
                                                                                                      47
                                                                                                                 char buf[20]:
                                                                                                                                                        105
                                                                                                                                                                         if(max len count >= 50){
                                                                  for (auto &j : m[i])
                                                                                                                 sprintf(buf, "%08d", x.s[i]);
                                                                                                                                                                             break:
26
           return rev;
                                                   88
                                                                                                      48
                                                                                                                                                        106
                                                                                                                 for(int j = 0; j< strlen(buf);j++){</pre>
27
                                                   89
                                                                      j /= lazy[i];
                                                                                                      49
                                                                                                                                                        107
       matrix operator*(const matrix &a)
                                                                                                      50
                                                                                                                     out << buf[i];</pre>
28
                                                   90
                                                                                                                                                        108
29
                                                   91
                                                              return det;
                                                                                                      51
                                                                                                                                                        109
           matrix rev(r, a.c);
                                                                                                                                                                int find(const char* s){
30
                                                   92
                                                                                                      52
                                                                                                                                                        110
           matrix tmp(a.c, a.r);
                                                   93 };
                                                                                                      53
                                                                                                                                                                    int u = 0;
31
                                                                                                             return out;
                                                                                                                                                        111
32
           for (int i = 0; i < a.r; ++i)
                                                                                                      54
                                                                                                                                                        112
                                                                                                                                                                    int n = strlen(s):
33
               for (int j = 0; j < a.c; ++j)
                                                                                                      55
                                                                                                                                                        113
                                                                                                                                                                    for(int i = 0; i < n; ++i)
34
                    tmp[j][i] = a.m[i][j];
                                                                                                         istream& operator >> (istream &in,
                                                                                                                                                        114
                                                      9.4 Trie
           for (int i = 0; i < r; ++i)
                                                                                                              BigInteger& x){
                                                                                                                                                                         int index = getIndex(s[i]);
                                                                                                                                                        115
                                                                                                             string s;
               for (int j = 0; j < a.c; ++j)
                                                                                                                                                                        if(!c[u][index]){
                                                                                                      57
                                                                                                                                                        116
                    for (int k = 0; k < c; ++k)
                                                                                                      58
                                                                                                             if(!(in >> s))
                                                                                                                                                        117
                                                                                                                                                                            return -1;
                        rev.m[i][j] += m[i][k] *
                                                   1 // biginter字典數
                                                                                                      59
                                                                                                                 return in:
                                                                                                                                                        118
                              tmp[j][k];
                                                    2 struct BigInteger{
                                                                                                      60
                                                                                                                                                        119
                                                                                                                                                                        u = c[u][index];
                                                                                                             x = s;
                                                          static const int BASE = 100000000:
39
           return rev:
                                                                                                      61
                                                                                                             return in:
                                                                                                                                                        120
40
                                                          static const int WIDTH = 8:
                                                                                                      62
                                                                                                                                                        121
                                                                                                                                                                    return val[u]:
       bool inverse() //逆矩陣判斷
                                                          vector<int> s;
                                                                                                      63
                                                                                                                                                        122
                                                          BigInteger(long long num = 0){
                                                                                                      64
                                                                                                         struct Trie{
                                                                                                                                                        123 }
42
                                                                                                             int c[5000005][10];
                                                              *this = num:
                                                                                                      65
           Matrix t(r, r + c);
43
                                                                                                             int val[5000005];
                                                                                                      66
44
           for (int y = 0; y < r; y++)
                                                          BigInteger operator = (long long num){
                                                                                                      67
                                                                                                             int sz:
                                                                                                                                                            9.5 分數
                                                                                                             int getIndex(char c){
                                                              s.clear();
                                                                                                      68
                                                   10
               t.m[y][c + y] = 1;
                                                   11
                                                              do{
                                                                                                      69
                                                                                                                 return c - '0';
               for (int x = 0; x < c; ++x)
                                                                  s.push back(num % BASE);
                                                                                                      70
                   t.m[y][x] = m[y][x];
                                                   12
                                                   13
                                                                   num /= BASE;
                                                                                                      71
                                                                                                             void init(){
                                                                                                                                                          1 typedef long long 11;
                                                              }while(num > 0):
                                                                                                      72
                                                                                                                 memset(c[0], 0, sizeof(c[0]));
                                                                                                                                                          2 struct fraction
           if (!t.gas())
                                                   14
                                                              return *this;
                                                                                                      73
                                                                                                                 memset(val, -1, sizeof(val));
                                                   15
               return false:
                                                                                                                 sz = 1:
                                                   16
                                                                                                      74
           for (int y = 0; y < r; y++)
                                                          BigInteger operator = (const string& str
                                                                                                                                                              fraction(const 11 & n = 0, const 11 & d =
                                                   17
                                                                                                     75
               for (int x = 0; x < c; ++x)
                                                              ){
                                                                                                             void insert(BigInteger x, int v){
                                                                                                                                                                   1) : n(_n), d(_d)
                   m[y][x] = t.m[y][c + x] / t.
                                                                                                      76
                                                                                                                 int u = 0;
                        m[y][y];
                                                              s.clear();
                                                                                                      77
                                                                                                                                                                11 t = \_gcd(n, d);
                                                   19
                                                              int x, len = (str.length() - 1) /
                                                                                                      78
                                                                                                                 int max len count = 0;
           return true;
55
                                                                   WIDTH + 1;
                                                                                                                 int firstNum = x.s.back();
                                                                                                                                                                n /= t, d /= t;
                                                                                                      79
56
                                                              for(int i = 0; i < len;i++){</pre>
                                                                                                                 char firstBuf[20];
                                                                                                                                                                if (d < 0)
                                                   20
                                                                                                      80
57
         gas() //行列式
                                                   21
                                                                   int end = str.length() - i*WIDTH 81
                                                                                                                 sprintf(firstBuf, "%d", firstNum);
                                                                                                                                                                  n = -n, d = -d;
                                                                                                                 for(int j = 0; j < strlen(firstBuf); 11</pre>
           vector<T> lazy(r, 1);
                                                                  int start = max(0, end-WIDTH);
                                                                                                                      j++){
                                                                                                                                                              fraction operator-() const
                                                   22
                                                                                                                                                         12
           bool sign = false;
                                                                   sscanf(str.substr(start, end-
                                                                                                                      int index = getIndex(firstBuf[j
                                                                                                                                                         13
                                                   23
           for (int i = 0; i < r; ++i)
                                                                       start).c_str(), "%d", &x);
                                                                                                                                                         14
                                                                                                                                                                return fraction(-n, d);
                                                                  s.push back(x);
                                                                                                                      if(!c[u][index]){
                                                                                                                                                         15
                                                   24
               if (m[i][i] == 0)
                                                                                                                          memset(c[sz], 0 , sizeof(c[
                                                                                                                                                              fraction operator+(const fraction &b)
                                                   25
                                                                                                      85
                                                              return *this;
                                                   26
                                                                                                                               sz]));
                    int j = i + 1;
                                                   27
                                                                                                                          val[sz] = v;
                                                                                                                                                         17
                   while (j < r && !m[j][i])
                                                                                                                          c[u][index] = sz++;
                                                                                                                                                                return fraction(n * b.d + b.n * d, d * b
                                                   28
                                                                                                                                                         18
                       j++;
                                                          BigInteger operator + (const BigInteger&
                                                   29
                    if (j == r)
                                                                b) const{
                                                                                                                      u = c[u][index];
                                                                                                      89
                                                                                                                                                         19
                        continue;
                                                                                                                      max len_count++;
                                                   30
                                                              BigInteger c;
                                                                                                      90
                                                                                                                                                              fraction operator-(const fraction &b)
                   m[i].swap(m[i]);
                                                   31
                                                              c.s.clear();
                                                                                                      91
                   sign = !sign;
                                                              for(int i = 0, g = 0;; i++){}
                                                                                                                 for(int i = x.s.size()-2; i >= 0;i
                                                   32
                                                                                                      92
                                                                                                                                                         21
                                                                   if(g == 0 \&\& i >= s.size() \&\& i
                                                                                                                      --){
                                                                                                                                                                return fraction(n * b.d - b.n * d, d * b
                                                   33
73
               for (int j = 0; j < r; ++j)
                                                                       >= b.s.size()) break;
                                                                                                                      char buf[20];
                                                                                                      93
                                                                                                                      sprintf(buf, "%08d", x.s[i]);
                                                                   int x = g;
                                                                                                      94
                    if (i == i)
                                                                                                                                                              fraction operator*(const fraction &b)
                                                                  if(i < s.size()) x+=s[i];</pre>
                                                                                                      95
                                                                                                                      for(int j = 0; j < strlen(buf)</pre>
                                                   35
76
                       continue;
                                                                  if(i < b.s.size()) x+=b.s[i];</pre>
                                                                                                                           && max len count < 50; j++){
                   lazy[j] = lazy[j] * m[i][i];
                                                                  c.s.push back(x % BASE);
                                                                                                      96
                                                                                                                          int index = getIndex(buf[i])
                                                                                                                                                         25
                   T mx = m[j][i];
                                                                  g = x / BASE;
                                                                                                                                                         26
                                                                                                                                                                return fraction(n * b.n, d * b.d);
                   for (int k = 0; k < c; ++k)
                                                                                                                          if(!c[u][index]){
                        m[j][k] = m[j][k] * m[i]
                                                                                                                              memset(c[sz], 0 , sizeof 28
                                                                                                                                                              fraction operator/(const fraction &b)
                             ][i] - m[i][k] * mx; 40
                                                              return c;
                                                                                                                                   (c[sz]));
```

```
29 {
    return fraction(n * b.d, d * b.n);
    }
    void print()
    {
        cout << n;
        if (d != 1)
        cout << "/" << d;
    }
    }
};
```

To do writing		r K	2.7 2.8	LIS			5.6 Floyd-warshall 5.7 Hamilton_cycle	7 7		6.18 數字加法組合	
N	OT THINKING		2.9 2.10	Max_subarray	2		5.8 Kruskal	8 8		6.20 質因數分解	11
Contents			3.1 3.2 3.3	w & matching  Dinic	<b>3</b> 3 3	6	5.11 Union_find	8 8 <b>9</b> 9	7	Other 7.1 binary search 三類變化 7.2 heap sort 7.3 Merge sort	12
1 Ba	Basic codeblock setting 2 Basic vim setting	1	3.4 3.5 4 <b>Geo</b>	Maximum_matching  MFlow Model			6.2 Combination	9 9 9		7.4 Quick	12 12
$egin{array}{c} 1.5 \ 1.5 \ 1.5 \ 1.5 \ \end{array}$	4 Python	1 1 1	4.1 4.2 4.3 4.4	Closest Pair	4 5 5		6.6 Log	9 9 10 10		String         8.1 KMP          8.2 Min Edit Distance          8.3 Sliding window          8.4 Split	13 13
2 Di 2.1 2.2 2.3 2.4 2.5	1 3維 DP 思路		5 Gra 5.1 5.2 5.3 5.4	aph Bellman-Ford	<b>6</b>		6.11 Prime 判斷	10 10 10 10 11		data structure         9.1 Bigint	13 13 14 14 15
2.6	6 LCS	2	5.5	Euler circuit	7		6.17 數字乘法組合	11		9.5 分數	15