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	4.1 Circle Intersect	5 6	#*	
	4.3 Line	6	<pre>#include <bits stdc++.h=""> using namespace std;</bits></pre>	
	4.4 Max_cover_rectangle	6	typedef long long 11;	
	4.5 Point	7	typedef unsigned long long ull;	
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5	Graph	9	#define endl '\n'	
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		10	;	11
	5.5 Euler circuit	10	#define bugp(k) cout << "pair of " << #k << " is " << k.x <<	١.
		10	' << k.y << endl;	
	5.7 Hamilton_cycle	10	<pre>#define bugarr(k) for(auto i : k) cout << i << ' '; cout << endl;</pre>	
	5.9 Minimum Weight Cycle	11	int main()	
	5.10 Prim		{	
	5.11 Union_find	12	<pre>ios::sync_with_stdio(0); cin.tie(0);</pre>	
6	Mathematics	12	return 0;	
		12	}	
	6.2 Combination			
	6.3 CRT		1.4 Python	
	6.5 Fermat		1 + 4 . 3	
	6.6 Hex to Dec		// 輸入 i pau+()	
	6.7 Log		input()	
	6.8 Mod 性質		array = [0] * (N) //N個0	
	6.10 Pow Mod		range(0, N) // 0 ~ N-1	
	6.11 Prime table		line = input().split()	
	6.12 Prime 判斷		D, R, N = map(int, line) // 分三個 int 變數	
	6.13 Round(小數)		│ │// 才是 取除數	
	6.15 公式		/ 是 小數運算	
	6.16 四則運算			
	6.17		pow(a, b, c) // a ^ b % c	
	6.19 數字派法組合		<pre>print(*objects, sep = ' ', end = '\n')</pre>	
	6.20 羅馬數字		// objects 可以一次輸出多個對象	
	6.21 質因數分解		// sep 分開多個objects	
	6.22 質數數量	15	// end 默認值是\n	
7	Other	16	// EOF break	
	v · · · · · · · · · · · · · · · · · · ·	16	try:	
	7.2 Heap sort		while True:	
	7.3 Josephus	16	//input someithing except EOFError:	
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	7.7 Sudoku solution		1.5 Range data	
	7.8 Weighted Job Scheduling	11		
		17	<pre>int (-2147483648 to 2147483647) unsigned int(0 to 4294967295)</pre>	
	8.1 KMP		long(-2147483648 to 2147483647)	
	8.3 Sliding window		unsigned long(0 to 4294967295)	
	8.4 Split		long long(-9223372036854775808 to 9223372036854775807)	
			unsigned long long (0 to 18446744073709551615)	

1.6 Some Function

```
// 四捨五入
 round(double f);
                           // 進入
 ceil(double f);
                           // 捨去
 floor(double f);
  _builtin_popcount(<mark>int</mark> n); // 32bit有多少 1
to_string(int s);
                           // int to string
 cout << setprecision(位數) // cout 小數位設定
printf 型別
"%lf" // long double
"%lld" // long long int
 set_union(all(a), all(b), back_inserter(d)); // 聯集
 set_intersection(all(a), all(b), back_inserter(c)); //交集
 /** 全排列要先 sort !!! **/
 next_permutation(num.begin(), num.end());
 prev_permutation(num.begin(), num.end());
 //用binary search找第一個大於或等於val的位置
 vector<int>::iterator it = lower_bound(v.begin(), v.end(), val)
 //用binary search找第一個大於val的位置
 vector<int>::iterator it = upper_bound(v.begin(), v.end(), val)
 /*找到範圍裏面的最大元素*/
 max_element(n, n + len);
                                // n到n+len範圍內最大值
 max_element(v.begin(), v.end()); // vector 中最大值
 /*找到範圍裏面的最大元素*/
                                // n到n+len範圍內最小值
 min element(n, n + len);
 min_element(v.begin(), v.end()); // vector 中最小值
 /*queue*/
 queue<datatype> q;
front(); /*取出最前面的值(沒有移除掉)*/
back(); /*取出最後面的值(沒有移除掉)*/
pop(); /*移掉最前面的值*/
push(); /*新增值到最後面*/
empty(); /*回傳bool,檢查是不是空的queue*/
 size(); /*queue 的大小*/
 /*stack*/
 stack<datatype> s;
top(); /*取出最上面的值(沒有移除掉)*/
        /*移掉最上面的值*/
 pop();
 push(); /*新增值到最上面*/
empty(); /*bool 檢查是不是空*/
size(); /*stack 的大小*/
 /*unordered_set*/
 unordered_set<datatype> s;
 unordered_set<datatype> s(arr, arr + n);
 /*initial with array*/
 insert(); /*插入值*/
erase(); /*刪除值*/
empty(); /*bool 檢查是不是空*/
 count(); /*判斷元素存在回傳1 無則回傳0*/
 /*tuple*/
tuple<datatype,datatype,datatype> t;
std::get<0>(t) /*Get first element of tuple*/
std::get<1>(t) /*Get second element of tuple*/
 std::get<2>(t) /*Get third element of tuple*/
1.7 Time
cout << 1.0 * clock() / CLOCKS_PER_SEC << endl;</pre>
     DP
```

2.1 3 維 DP 思路

```
解題思路: dp[i][j][k]
i 跟 j 代表 range i ~ j 的 value
k在我的理解裡是視題目的要求而定的
像是 Remove Boxes 當中 k 代表的是在 i 之前還有多少個連續的箱子
所以每次區間消去的值就是(k+1) * (k+1)
換言之‧我認為可以理解成 k 的意義就是題目今天所關注的重點‧就是
老師說的題目所規定的運算
```

2.2 Knapsack Bounded

```
const int N = 100, W = 100000;
int cost[N], weight[N], number[N];
int c[W + 1];
void knapsack(int n, int w)
{
```

```
for (int i = 0; i < n; ++i)
        int num = min(number[i], w / weight[i]);
        for (int k = 1; num > 0; k *= 2)
            if (k > num)
                k = num;
            num -= k;
            }
    cout << "Max Prince" << c[w];</pre>
2.3 Knapsack sample
int Knapsack(vector<int> weight, vector<int> value, int
     bag Weight)
    // vector<int> weight = {1, 3, 4};
// vector<int> value = {15, 20, 30};
    // int bagWeight = 4;
    vector<vector<int>> dp(weight.size(), vector<int>(bagWeight
    + 1, 0));
for (int j = weight[0]; j <= bagWeight; j++)
dp[0][j] = value[0];
    // weight數組的大小就是物品個數
    for (int i = 1; i < weight.size(); i++)</pre>
```

2.4 Knapsack Unbounded

{ // 遍歷背包容量

{ // 遍歷物品

for (int j = 0; j <= bagWeight; j++)</pre>

weight[i]] + value[i]);

cout << dp[weight.size() - 1][bagWeight] << endl;</pre>

if (j < weight[i]) dp[i][j] = dp[i - 1][j];
else dp[i][j] = max(dp[i - 1][j], dp[i - 1][j - 1][j]</pre>

2.5 LCIS

```
int LCIS_len(vector<int> arr1, vetor<int> arr2)
     int n = arr1.size(), m = arr2.size();
     vector<int> table(m, 0);
     for (int j = 0; j < m; j++)
          table[j] = 0;
     for (int i = 0; i < n; i++)
         int current = 0;
for (int j = 0; j < m; j++)</pre>
              if (arr1[i] == arr2[j])
                   if (current + 1 > table[j])
  table[j] = current + 1;
              if (arr1[i] > arr2[j])
                   if (table[j] > current)
                        current = table[j];
         }
    int result = 0;
for (int i = 0; i < m; i++)</pre>
         if (table[i] > result)
              result = table[i];
     return result:
```

2.6 LCS

```
int LCS(vector<string> Ans, vector<string> num)
{
    int N = Ans.size(), M = num.size();
    vector<vector<int>> LCS(N + 1, vector<int>(M + 1, 0));
    for (int i = 1; i <= N; ++i)
    {
        for (int j = 1; j <= M; ++j)
    }
}</pre>
```

```
if (Ans[i - 1] == num[j - 1])
    LCS[i][j] = LCS[i - 1][j - 1] + 1;
             LCS[i][j] = max(LCS[i - 1][j], LCS[i][j - 1]);
    }
cout << LCS[N][M] << '\n';</pre>
//列印 LCS
int n = N, m = M;
vector<string> k;
while (n && m)
    if (LCS[n][m] != max(LCS[n - 1][m], LCS[n][m - 1]))
         k.push_back(Ans[n - 1]);
         n - - ;
     else if (LCS[n][m] == LCS[n - 1][m])
    n--;
else if (LCS[n][m] == LCS[n][m - 1])
reverse(k.begin(), k.end());
for (auto i : k)
    cout << i << " ";
cout << endl;</pre>
return LCS[N][M];
```

2.7 LIS O(Nlog(N))

2.8 LIS

```
vector<int> ans;
void LIS(vector<int> &arr)
     vector<int> dp(arr.size(), 1);
     vector<int> pos(arr.size(), -1);
     int res = INT_MIN, index = 0;
for (int i = 0; i < arr.size(); ++i)</pre>
          for (int j = i + 1; j < arr.size(); ++j)</pre>
               if (arr[j] > arr[i])
                    if (dp[i] + 1 > dp[j])
                         dp[j] = dp[i] + 1;
                         pos[j] = i;
                   }
               }
          if (dp[i] > res)
               res = dp[i];
               index = i;
     cout << res << endl; // length</pre>
    printLIS(arr, pos, index);
for (int i = 0; i < ans.size(); i++)</pre>
          cout << ans[i];</pre>
          if (i != ans.size() - 1)
    cout << ' ';</pre>
    cout << '\n';
void printLIS(vector<int> &arr, vector<int> &pos, int index)
    if (pos[index] != -1)
```

```
printLIS(arr, pos, pos[index]);
ans.push_back(arr[index]);
2.9 LPS
// manacher
void LPS(string s)
  int maxlen = 0, 1, r;
  int n = n;
  for (int i = 0; i < n; i++)
    while ((s[i - x] == s[i + x]) \&\& (i - x >= 0) \&\& (i + x < n)
        )) //odd length
      x++;
    if (2 * x + 1 > maxlen)
      maxlen = 2 * x + 1;
      l = i - x;
      r = i + x;
    }
    \dot{x} = 0;
    while ((s[i - x] == s[i + 1 + x]) \& (i - x >= 0) \& (i + 1)
         + x < n)) //even length
    if (2^* \times x > maxlen)
      maxlen = 2 * x;
      1 = i - x + 1;
      r = i + x;
   }
 }
                                             // 最後長度
  cout << maxlen << '\n';</pre>
  cout << l + 1 << ' ' << r + 1 << '\n'; //頭到尾
2.10 Max subarray
/*Kadane's algorithm*/
int maxSubArray(vector<int>& nums) {
    int local_max = nums[0], global_max = nums[0];
for(int i = 1; i < nums.size(); i++){</pre>
        local_max = max(nums[i], nums[i]+local_max);
        global_max = max(local_max,global_max);
    return global_max;
```

2.11 Money problem

```
//能否湊得某個價位
void change(vector<int> price, int limit)
     vector<bool> c(limit + 1, 0);
     c[0] = true;
     for (int i = 0; i < price.size(); ++i)</pre>
                                                       // 依序加入各種
          面額
         for (int j = price[i]; j <= limit; ++j) // 由低價位逐步
               到高價位
              c[j] = c[j] | c[j - price[i]];
                                                      // 湊、湊、湊
    if (c[limit]) cout << "YES\n";
else cout << "NO\n";</pre>
// 湊得某個價位的湊法總共幾種
void change(vector<int> price, int limit)
     vector<int> c(limit + 1, 0);
    c[0] = true;
for (int i = 0; i < price.size(); ++i)</pre>
    for (int j = price[i]; j <= limit; ++j)
    c[j] += c[j - price[i]];
cout << c[limit] << '\n';</pre>
}
// 湊得某個價位的最少錢幣用量
void change(vector<int> price, int limit)
     vector<int> c(limit + 1, 0);
    c[0] = true;
for (int i = 0; i < price.size(); ++i)</pre>
         for (int j = price[i]; j <= limit; ++j)
    c[j] = min(c[j], c[j - price[i]] + 1);</pre>
     cout << c[limit] <<</pre>
                            '\n';
//湊得某個價位的錢幣用量‧有哪幾種可能性
void change(vector<int> price, int limit)
     vector<int> c(limit + 1, 0);
     c[0] = true;
for (int i = 0; i < price.size(); ++i)</pre>
         for (int j = price[i]; j <= limit; ++j)</pre>
```

```
c[j] |= c[j-price[i]] << 1; // 錢幣數量加一·每一種
可能性都加一。
for (int i = 1; i <= 63; ++i)
if (c[m] & (1 << i))
cout << "用" << i << "個錢幣可湊得價位" << m;
}
```

2.12 Palindromic Substrings count

3 Flow & matching

3.1 Dinic

```
const long long INF = 1LL<<60;
struct Dinic { //O(VVE), with minimum cut
     static const int MAXN = 5003;
     struct Edge{
          int u, v;
          long long cap, rest;
    int n, m, s, t, d[MAXN], cur[MAXN];
vector<Edge> edges;
     vector<int> G[MAXNj;
     void init(){
          edges.clear();
for ( int i = 0 ; i < n ; i++ ) G[i].clear();</pre>
     // min cut start
    bool side[MAXN];
     void cut(int u) {
          side[u] = 1;
for ( int i : G[u] ) {
   if ( !side[ edges[i].v ] && edges[i].rest )
               cut(edges[i].v);
          }
    // min cut end
int add_node(){
          return n++:
     void add_edge(int u, int v, long long cap){
  edges.push_back( {u, v, cap, cap} );
  edges.push_back( {v, u, 0, OLL} );
          m = edges.size();
G[u].push_back(m-2);
          G[v].push_back(m-1);
    bool bfs(){
          fill(d,d+n,-1);
          queue<int> que
          que.push(s); d[s]=0;
while (!que.empty()){
               int u = que.front(); que.pop();
               for (int ei : G[u]){
    Edge &e = edges[ei];
                    if (d[e.v] < 0 && e.rest > 0){
    d[e.v] = d[u] + 1;
                          que.push(e.v);
                    }
               }
          return d[t] >= 0;
     long long dfs(int u, long long a){
          if ( u == t || a == 0 ) return a;
          f = dfs(e.v, min(a, e.rest));
if (f > 0) {
               e.rest -= f
                edges[ G[u][i]^1 ].rest += f;
               flow += f;
```

```
a -= f;
    if ( a == 0 ) break;
}

return flow;
}
long long maxflow(int _s, int _t){
    s = _s, t = _t;
    long long flow = 0, mf;
    while ( bfs() ){
        fill(cur,cur+n,0);
        while ( (mf = dfs(s, INF)) ) flow += mf;
}
return flow;
}
dinic;
```

3.2 Edmonds_karp

```
*Flow - Edmonds-karp*/
/*Based on UVa820*/
#define inf 1000000
int getMaxFlow(vector<vector<int>> &capacity, int s, int t, int
       n){
   int ans = 0;
   vector<vector<int>> residual(n+1, vector<int>(n+1, 0)); //
         residual network
   while(true){
      vector<int> bottleneck(n+1, 0);
      bottleneck[s] = inf;
      queue<int> q;
      q.push(s);
      vector<int> pre(n+1, 0);
while(!q.empty() && bottleneck[t] == 0){
        int cur = q.front();
        q.pop();
for(int i = 1; i <= n ; i++){
   if(bottleneck[i] == 0 && capacity[cur][i] > residual[
                 cur][i]){
              q.push(i);
              pre[i] = cur;
              bottleneck[i] = min(bottleneck[cur], capacity[cur][i]
                      residual[cur][i]);
           }
        }
     for(int cur = t; cur != s; cur = pre[cur]){
    residual[pre[cur]][cur] += bottleneck[t];
    residual[cur][pre[cur]] -= bottleneck[t];
      ans += bottleneck[t];
   return ans;
int main(){
   int testcase = 1;
   int n;
   while(cin>>n){
      if(n == 0)
        break:
      vector<vector<int>> capacity(n+1, vector<int>(n+1, 0));
     int s, t, c;
cin >> s >> t >> c;
      int a, b, bandwidth;
     for(int i = 0 ; i < c ; ++i){
  cin >> a >> b >> bandwidth;
  capacity[a][b] += bandwidth;
  capacity[b][a] += bandwidth;
     cout << "Network " << testcase++ << endl;
cout << "The bandwidth is " << getMaxFlow(capacity, s, t, n
    ) << "." << endl;</pre>
      cout << endl;</pre>
   return 0;
```

3.3 hungarian

```
int ans = 0:
    vector<int> pre(m,-1);
for(int i = 0;i < n; i++){</pre>
         vector<bool> pass(m, false);
         if(dfs(mp,pass,pre,i))
             ans += 1:
    return ans;
int main(){
    int m,n,e;
    while(cin>>n){
         if(n == 0) break;
         cin>>m>>e;
         int a,b;
         vector<vector<bool>> mp(n, vector<bool>(m, false));
         for(int i = 0;i < e; i++){</pre>
              cin>>a>>b;
              mp[a][b] = true;
         cout<<hungarian(mp,n,m)<<endl;</pre>
    return 0;
}
```

3.4 Maximum matching

```
/*bipartite - maximum matching*/
bool dfs(vector vector bool>> res,int node,vector int>& x,
    vector int>& y, vector bool> pass){
    for (int i = 0; i < res[0].size(); i++){</pre>
           if(res[node][i] && !pass[i]){
                pass[i] = true;
if(y[i] == -1 || dfs(res,y[i],x,y,pass)){
                     x[node] = i;
                     y[i] = node;
                     return true;
                }
          }
     return false;
int main(){
     int n,m,1;
      while(cin>>n>>m>>l){
           vector<vector<bool>> res(n, vector<bool>(m, false));
           for (int i = 0; i < 1; i++){
               int a, b;
cin >> a >> b;
                res[a][b] = true;
           int ans = 0;
           vector<int> x(n, -1);
           vector<int> y(n, -1);
for (int i = 0; i < n; i++){
    vector<bool> pass(n, false);
                if(dfs(res,i,x,y,pass))
                     ans += 1;
           cout << ans << endl;
     return 0:
}
/*
4 3 5 //n matching m, 1 links
0 2
1 0
3 1
answer is 3
```

3.5 MFlow Model

```
void Add(int from, int to, ll cp, ll flw)
          u[tot] = from;
          v[tot] = to;
          cap[tot] = cp;
flow[tot] = flw;
next[tot] = first[u[tot]];
          first[u[tot]] = tot;
     bool bfs()
          ++tim;
          dis[s] = 0;
          vi[s] = tim;
          int head, tail;
          head = tail = 1;
          que[head] = s;
          while (head <= tail)</pre>
               for (int i = first[que[head]]; i != -1; i = next[i
                   if (vi[v[i]] != tim \&\& cap[i] > flow[i])
                        vi[v[i]] = tim;
dis[v[i]] = dis[que[head]] + 1;
que[++tail] = v[i];
                   }
              ++head:
          return vi[t] == tim;
     11 dfs(int x, 11 a)
          if (x == t || a == 0)
               return a;
          11 flw = 0, f;
          int &i = cur[x];
          for (i = first[x]; i != -1; i = next[i])
              if (dis[x] + 1 == dis[v[i]] && (f = dfs(v[i], min(a
                    , cap[i] - flow[i]))) > 0)
                   flow[i] += f;
flow[i ^ 1] -= f;
                   a -= f;
                   flw += f;
                   if (a == 0)
                        break;
              }
          return flw;
     11 MaxFlow(int s, int t)
          this -> s = s;
          this->t = t;
          11 flw = 0;
          while (bfs())
               for (int i = 1; i <= n; ++i)
cur[i] = 0;
               flw += dfs(s, oo);
          return flw;
     }
 };
// MF Net;
 // Net.n = n;
 // Net.Clear();
 // a 到 b (注意從1開始!!!!)
 // Net.Add(a, b, w, 0);
 // Net.MaxFlow(s, d)
// s 到 d 的 MF
```

4 Geometry

4.1 Circle Intersect

```
bool same(double a, double b)
{
    return abs(a - b) < 0;
}
struct P
{
    double x, y;
    P() : x(0), y(0) {}
    P(double x, double y) : x(x), y(y) {}
    P operator+(P b) { return P(x + b.x, y + b.y); }
    P operator-(P b) { return P(x - b.x, y - b.y); }
    P operator*(double b) { return P(x * b, y * b); }</pre>
```

```
P operator/(double b) { return P(x / b, y / b); }
double operator*(P b) { return x * b.x + y * b.y;
// double operator^(P b) { return x * b.y - y * b
       double abs() { return hypot(x, y); }
      P unit() { return *this / abs(); }
P rot(double o)
             double c = cos(o), s = sin(o);
return P(c * x - s * y, s * x + c * y);
      double angle() { return atan2(y, x); }
struct C
{
      Р с;
       double r;
      C(P c = P(0, 0), double r = 0) : c(c), r(r) {}
vector<P> Intersect(C a, C b)
      if (a.r > b.r)
      swap(a, b);
double d = (a.c - b.c).abs();
      vector<P> p;
if (same(a.r + b.r, d))
    p.pb(a.c + (b.c - a.c).unit() * a.r);
else if (a.r + b.r > d && d + a.r >= b.r)
      {
             double o = acos((sqrt(a.r) + sqrt(d) - sqrt(b.r)) / (2
     * a.r * d));
P i = (b.c - a.c).unit();
             p.pb(a.c + i.rot(o) * a.r);
p.pb(a.c + i.rot(-o) * a.r);
       return p;
```

4.2 Closest Pair

```
//最近點對 (距離) //台大
vector<pair<double, double>> p;
double closest_pair(int 1, int r)
      p 要對 x 軸做 sort
   if (1 == r)
       return 1e9;
    if (r - 1 == 1)
       return dist(p[l], p[r]); // 兩點距離
    int m = (1 + r) >> 1:
   double d = min(closest_pair(l, m), closest_pair(m + 1, r));
   vector<int> vec;
for (int i = m; i >= 1 && fabs(p[m].x - p[i].x) < d; --i)</pre>
       vec.push_back(i);
   for (int i = m + 1; i \leftarrow r && fabs(p[m].x - p[i].x) < d; ++
        i)
       vec.push_back(i);
   }
```

4.3 Line

```
template <typename T>
struct line
    line() {}
   point<T> p1, p2;
T a, b, c; //ax+by+c=0
    line(const point\langle T \rangle &x, const point\langle T \rangle &y) : p1(x), p2(y)
    void pton()
    { //轉成一般式
       a = p1.y - p2.y;
b = p2.x - p1.x;
c = -a * p1.x - b * p1.y;
    T ori(const point<T> &p) const
    { //點和有向直線的關係, >0左邊、=0在線上<0右邊
        return (p2 - p1).cross(p - p1);
    T btw(const point<T> &p) const
    { //點投影落在線段上<=0
        return (p1 - p).dot(p2 - p);
    bool point_on_segment(const point<T> &p) const
    { //點是否在線段上
        return ori(p) == 0 && btw(p) <= 0;</pre>
    T dis2(const point<T> &p, bool is_segment = 0) const
    { //點跟直線/線段的距離平方
```

```
point < T > v = p2 - p1, v1 = p - p1;
         if (is_segment)
              point < T > v2 = p - p2;
              if (v.dot(v1) <= 0)</pre>
                  return v1.abs2():
              if (v.dot(v2) >= 0)
                  return v2.abs2();
         T tmp = v.cross(v1);
         return tmp * tmp / v.abs2();
     T seg_dis2(const line<T> &1) const
     { //兩線段距離平方
         return min({dis2(l.p1, 1), dis2(l.p2, 1), l.dis2(p1, 1)
              , l.dis2(p2, 1)});
     point<T> projection(const point<T> &p) const
     { //點對直線的投影
         point<T> n = (p2 - p1).normal();
return p - n * (p - p1).dot(n) / n.abs2();
     point<T> mirror(const point<T> &p) const
         //點對直線的鏡射,要先呼叫pton轉成一般式
         point<T> R;
T d = a * a + b * b;
         R.x = (b * b * p.x - a * a * p.x - 2 * a * b * p.y - 2
         * a * c) / d;
R.y = (a * a * p.y - b * b * p.y - 2 * a * b * p.x - 2
              * b * c) /
         return R:
     bool equal(const line &1) const
     { //直線相等
         return ori(1.p1) == 0 && ori(1.p2) == 0;
     bool parallel(const line &1) const
         return (p1 - p2).cross(l.p1 - l.p2) == 0;
     bool cross seg(const line &1) const
         return (p2 - p1).cross(l.p1 - p1) * (p2 - p1).cross(l.
              p2 - p1) <= 0; //直線是否交線段
     int line_intersect(const line &l) const
     { //直線相交情況·-1無限多點、1交於一點、0不相交
         return parallel(l) ? (ori(l.p1) == 0 ? -1 : 0) : 1;
     int seg_intersect(const line &1) const
         T c1 = ori(1.p1), c2 = ori(1.p2);
T c3 = 1.ori(p1), c4 = 1.ori(p2);
if (c1 == 0 && c2 == 0)
         { //共線
             bool b1 = btw(1.p1) >= 0, b2 = btw(1.p2) >= 0;
T a3 = l.btw(p1), a4 = l.btw(p2);
              if (b1 && b2 && a3 == 0 && a4 >= 0)
              if (b1 && b2 && a3 >= 0 && a4 == 0)
              return 3;
if (b1 && b2 && a3 >= 0 && a4 >= 0)
                  return 0:
              return -1; //無限交點
         else if (c1 * c2 <= 0 && c3 * c4 <= 0)
             return 1;
         return 0; //不相交
     point<T> line_intersection(const line &1) const
     { /*直線交點*/
         point < T > a = p2 - p1, b = 1.p2 - 1.p1, s = 1.p1 - p1;
         // if (a.cross(b) == 0)
// return TAIT
         // return INF;
return p1 + a * (s.cross(b) / a.cross(b));
     point<T> seg_intersection(const line &1) const
     { //線段交點
         int res = seg_intersect(1);
         if (res <= 0)
             assert(0);
         if (res == 2)
              return p1;
         if (res == 3)
              return p2;
         return line intersection(1);
     }
};
4.4 Max_cover_rectangle
const double PI = atan2(0.0, -1.0);
```

```
const double eps = 1e-10;
| typedef point<double> p; // data type 依照題目更改
```

```
int mycmp(double a) { return fabs(a) < eps ? 0 : (a < 0 ? -1 :</pre>
     1); }
double Length(p a) { return sqrt(a.dot(a)); }
double turnAngle(p a, p b) { return mycmp(a.dot(b)) == 1 ?
    angle(a, b) : PI + angle(a, b); }
double Area(int a, int b, int c, int d, p ab, p cd, polygon<
     double> po)
    double h1 = distanceOfpAndLine(po.p[a], po.p[b], po.p[b] +
         ab);
    double h2 = distanceOfpAndLine(po.p[c], po.p[d], po.p[d] +
         cd);
    return h1 * h2;
double max_cover_rectangle(polygon<double> po)
    po.p.pb(po.p[0]);
    int m = po.p.size();
if (m < 3)</pre>
        return 0; // 沒凸包哪來外包矩形
    double Max = -1;
double Minx = po.p[0].x, Miny = po.p[0].y, Maxx = po.p[0].x
    , Maxy = po.p[0].y;
int p1 = 0, p2 = 0, p3 = 0, p4 = 0;
    p v1, v2, ori;
ori = v1 = p(1, 0);
v2 = p(0, 1);
for (int i = 1; i < m; i++)</pre>
         if (mycmp(Minx -
                           po.p[i].x) == 1)
             Minx = po.p[i].x, p3 = i;
         if (mycmp(Maxx - po.p[i].x) == -1)
             Maxx = po.p[i].x, p4 = i;
         if (mycmp(Miny - po.p[i].y) == 1)
             Miny = po.p[i].y, p1 = i;
         if (mycmp(Maxy - po.p[i].y) == -1)
    Maxy = po.p[i].y, p2 = i;
    while (mycmp(ori.cross(v1)) >= 0)
         double minRad = 1e20;
         minRad = min(minRad, turnAngle(v1, po.p[p1 + 1] - po.p[
             p1]));
         minRad = min(minRad, turnAngle(v1 * (-1), po.p[p2 + 1]
              - po.p[p2]));
         minRad = min(minRad, turnAngle(v2 * (-1), po.p[p3 + 1]
         - po.p[p3]));
minRad = min(minRad, turnAngle(v2, po.p[p4 + 1] - po.p[
              p4]));
         double 1 = 0, r = minRad;
         while (mycmp(1 - r))
             double len = (r - 1) / 3;
double midl = 1 + len;
double midr = r - len;
             Rotate(v1, midr), Rotate(v2, midr), po)) == 1)
                  r = midr;
             else
         Max = max(Max, Area(p1, p2, p3, p4, Rotate(v1, 1),
         Rotate(v2, 1), po));
v1 = Rotate(v1, minRad);
v2 = Rotate(v2, minRad);
         if (mycmp(angle(v1, po.p[p1 + 1] - po.p[p1])) == 0)
p1 = (p1 + 1) % m;
         if (mycmp(angle(v1 * (-1), po.p[p2 + 1] - po.p[p2])) ==
               0)
             p2 = (p2 + 1) \% m;
         if (mycmp(angle(v2 * (-1), po.p[p3 + 1] - po.p[p3])) ==
             p3 = (p3 + 1) \% m;
         if (mycmp(angle(v2, po.p[p4 + 1] - po.p[p4])) == 0)
    p4 = (p4 + 1) % m;
    return Max;
```

4.5 Point

```
const double PI = atan2(0.0, -1.0);
template <typename T>
struct point
    point() {}
    point(const T &x, const T &y) : x(x), y(y) {}
```

```
point operator+(const point &b) const
    return point(x + b.x, y + b.y);
point operator-(const point &b) const
    return point(x - b.x, y - b.y);
point operator*(const T &b) const
    return point(x * b, y * b);
point operator/(const T &b) const
    return point(x / b, y / b);
bool operator == (const point &b) const
    return x == b.x && y == b.y;
  dot(const point &b) const
    return x * b.x + y * b.y;
T cross(const point &b) const
    return x * b.y - y * b.x;
point normal() const
{ //求法向量
    return point(-y, x);
T abs2() const
{ //向量長度的平方
    return dot(*this);
T rad(const point &b) const
{ //兩向量的弧度
    return fabs(atan2(fabs(cross(b)), dot(b)));
T getA() const
                       //對x軸的弧度
    T A = atan2(y, x); //超過180度會變負的
if (A <= -PI / 2)
A += PI * 2;
    return A;
```

4.6 Polygon

while (1 <= r)

```
template <typename T>
struct polygon
    polygon() {}
    vector<point<T>> p; //逆時針順序
    T area() const
    { //面積
        T ans = 0;
        for (int i = p.size() - 1, j = 0; j < (int)p.size(); i
            = j++)
           ans += p[i].cross(p[j]);
       return ans / 2;
    point<T> center of mass() const
    { //重心
       T cx = 0, cy = 0, w = 0;
for (int i = p.size() - 1, j = 0; j < (int)p.size(); i
            = j++)
           T a = p[i].cross(p[j]);
           cx += (p[i].x + p[j].x) *
           cy += (p[i].y + p[j].y) * a;
        return point<T>(cx / 3 / w, cy / 3 / w);
    char ahas(const point<T> &t) const
    { //點是否在簡單多邊形內·是的話回傳1、在邊上回傳-1、否則回
        傳0
       bool c = 0;
       for (int i = 0, j = p.size() - 1; i < p.size(); j = i</pre>
            ++)
           if (line<T>(p[i], p[j]).point_on_segment(t))
               return -1
           (p[j].y - p[i].y) + p[i].x)
               c = !c:
       return c;
    char point_in_convex(const point<T> &x) const
       int 1 = 1, r = (int)p.size() - 2;
```

```
{ //點是否在凸多邊形內,是的話回傳1、在邊上回傳-1、否則
         回傳a
        int mid = (1 + r) / 2;
T a1 = (p[mid] - p[0]).cross(x - p[0]);
T a2 = (p[mid + 1] - p[0]).cross(x - p[0]);
if (a1 >= 0 && a2 <= 0)</pre>
             T res = (p[mid + 1] - p[mid]).cross(x - p[mid])
             return res > 0 ? 1 : (res >= 0 ? -1 : 0);
        else if (a1 < 0)
             r = mid - 1;
        else
             1 = mid + 1:
    return 0;
vector<T> getA() const
{//凸包邊對x軸的夾角
    vector<T> res; //一定是遞增的
for (size_t i = 0; i < p.size(); ++i)
    res.push_back((p[(i + 1) % p.size()] - p[i]).getA()
    return res;
bool line_intersect(const vector<T> &A, const line<T> &1)
     const
{ //O(logN)
    int f1 = upper_bound(A.begin(), A.end(), (1.p1 - 1.p2).
    getA()) - A.begin();
int f2 = upper_bound(A.begin(), A.end(), (1.p2 - 1.p1).
         getA()) - A.begin();
    return l.cross_seg(line<T>(p[f1], p[f2]));
polygon cut(const line<T> &1) const
{ //凸包對直線切割,得到直線1左側的凸包
    polygon ans;
    for (int n = p.size(), i = n - 1, j = 0; j < n; i = j
         ++)
        if (1.ori(p[i]) >= 0)
        {
             ans.p.push back(p[i]);
             if (l.ori(p[j]) < 0)
                 ans.p.push_back(1.line_intersection(line<T</pre>
                      >(p[i], p[j])));
        else if (l.ori(p[j]) > 0)
             ans.p.push_back(1.line_intersection(line<T>(p[i
                  ], p[j])));
    return ans;
{ //凸包排序函數 // 起始點不同
    return (a.y < b.y) || (a.y == b.y && a.x < b.x); //Y最
         小開始
void Andrew_Monotone_Chain(vector<point<T>> &s)
{ //凸包 Convexhull 2D
    sort(s.begin(), s.end(), Andrew_Monotone_Chain_angle);
    p.resize(s.size() + 1);
    int m = 0;
    // cross >= 0 順時針。cross <= 0 逆時針旋轉
    for (size_t i = 0; i < s.size(); ++i)
         while (m \ge 2 \&\& (p[m - 1] - p[m - 2]).cross(s[i] -
              p[m - 2]) <= 0)
             --m;
        p[m++] = s[i];
    for (int i = s.size() - 2, t = m + 1; i >= 0; --i)
        while (m \ge t \&\& (p[m - 1] - p[m - 2]).cross(s[i] - p[m - 2])
              p[m - 2]) <= 0)
             --m;
        p[m++] = s[i];
    if (s.size() > 1) // 重複頭一次需扣掉
    p.resize(m);
    // p.pb(s[0]); // 需要頭在 pb 回去!!
T diam()
{ //直徑
    int n = p.size(), t = 1;
T ans = 0;
    p.push_back(p[0]);
    for (int i = 0; i < n; i++)
        \begin{array}{lll} point<T> \ now = p[i+1] - p[i]; \\ while \ (now.cross(p[t+1] - p[i]) > now.cross(p[t] \end{array}
              - p[i]))
```

```
t = (t + 1) \% n;
        ans = max(ans, (p[i] - p[t]).abs2());
    return p.pop_back(), ans;
T min_cover_rectangle()
{ // 先做凸包 //最小覆蓋矩形
    int n = p.size(), t = 1, r = 1, l;
    if (n < 3)
        return 0; //也可以做最小周長矩形
    T ans = 1e99;
    p.push_back(p[0]);
    for (int i = 0; i < n; i++)
        - p[i]))
        t = (t + 1) % n;
while (now.dot(p[r + 1] - p[i]) > now.dot(p[r] - p[
            i]))
            r = (r + 1) \% n;
        if (!i)
            1 = r;
        while (now.dot(p[1 + 1] - p[i]) \le now.dot(p[1] - p
             [i]))
            1 = (1 + 1) \% n;
        T d = now.abs2();
        T tmp = now.cross(p[t] - p[i]) * (now.dot(p[r] - p[
    i]) - now.dot(p[l] - p[i])) / d;
        ans = min(ans, tmp);
    return p.pop back(), ans;
T dis2(polygon &pl)
{ //凸包最近距離平方
    vector<point<T>> &P = p, &Q = pl.p;
int n = P.size(), m = Q.size(), l = 0, r = 0;
for (int i = 0; i < n; ++i)</pre>
        if (P[i].y < P[1].y)</pre>
    1 = i; for (int i = 0; i < m; ++i)
        if (Q[i].y < Q[r].y)</pre>
    P.push_back(P[0]), Q.push_back(Q[0]);
    T ans = 1e99;
    for (int i = 0; i < n; ++i)
        while ((P[1] - P[1 + 1]).cross(Q[r + 1] - Q[r]) <
            0)
r = (r + 1) % m;
        ans = min(ans, line<T>(P[1], P[1 + 1]).seg_dis2( line<T>(Q[r], Q[r + 1])));
        1 = (1 + 1) \% n;
    return P.pop_back(), Q.pop_back(), ans;
static char sign(const point<T> &t)
    return (t.y == 0 ? t.x : t.y) < 0;
static bool angle_cmp(const line<T> &A, const line<T> &B)
    point<T> a = A.p2 - A.p1, b = B.p2 - B.p1;
    return sign(a) < sign(b) || (sign(a) == sign(b) && a. cross(b) > 0);
int halfplane_intersection(vector<line<T>> &s)
{ //半平面交
    sort(s.begin(), s.end(), angle_cmp); //線段左側為該線段
         半平面
    int L, R, n = s.size();
    vector<point<T>> px(n);
    vector<line<T>> q(n);
    q[L = R = 0] = s[0];
    for (int i = 1; i < n; ++i)
        while (L < R \&\& s[i].ori(px[R - 1]) <= 0)
        while (\hat{L} < R \&\& s[i].ori(px[L]) <= 0)
        ++L;
q[++R] = s[i];
        if (q[R].parailel(q[R - 1]))
            if (q[R].ori(s[i].p1) > 0)
                a[R] = s[i]:
            px[R - 1] = q[R - 1].line_intersection(q[R]);
    p.clear();
    if (R - L <= 1)
        return 0;
    px[R] = q[R].line_intersection(q[L]);
```

4.7 Triangle

```
template <typename T>
struct triangle
     point<T> a, b, c;
     triangle() {}
     triangle(const point<T> &a, const point<T> &b, const point<</pre>
          T> &c) : a(a), b(b), c(c) {}
     T area() const
    {
         T t = (b - a).cross(c - a) / 2;
return t > 0 ? t : -t;
    point<T> barycenter() const
     { //重心
         return (a + b + c) / 3;
    point<T> circumcenter() const
     { //外心
         static line<T> u, v;
u.p1 = (a + b) / 2;
         u.p2 = point < T > (u.p1.x - a.y + b.y, u.p1.y + a.x - b.x)
         v.p1 = (a + c) / 2;
         v.p2 = point(T)(v.p1.x - a.y + c.y, v.p1.y + a.x - c.x)
         return u.line intersection(v);
    point<T> incenter() const
         T A = sqrt((b - c).abs2()), B = sqrt((a - c).abs2()), C
         = sqrt((a - b).abs2());
return point<T>(A * a.x + B * b.x + C * c.x, A * a.y +
B * b.y + C * c.y) / (A + B + C);
    point<T> perpencenter() const
     { //垂心
         return barycenter() * 3 - circumcenter() * 2;
};
```

5 Graph

5.1 Bellman-Ford

```
*SPA - Bellman-Ford*/
#define inf 99999 //define by you maximum edges weight
vector<vector<int> > edges;
vector<int> dist;
vector<int> ancestor;
void BellmanFord(int start,int node){
     dist[start] = 0;
     for(int it = 0; it < node-1; it++){</pre>
          for(int i = 0; i < node; i++){
   for(int j = 0; j < node; j++){
      if(edges[i][j] != -1){</pre>
                         if(dist[i] + edges[i][j] < dist[j]){
                              dist[j] = dist[i] + edges[i][j];
                               ancestor[j] = i;
                    }
               }
          }
     }
     for(int i = 0; i < node; i++) //negative cycle detection
    for(int j = 0; j < node; j++)</pre>
               if(dist[i] + edges[i][j] < dist[j])</pre>
               {
                    cout<<"Negative cycle!"<<endl;</pre>
                    return;
int main(){
     int node:
     cin>>node;
     edges.resize(node, vector<int>(node, inf));
     dist.resize(node,inf);
     ancestor.resize(node,-1);
     int a,b,d;
     while(cin>>a>>b>>d){
          /*input: source destination weight*/
if(a == -1 && b == -1 && d == -1)
               break;
          edges[a][b] = d;
```

```
int start;
cin>>start;
BellmanFord(start,node);
return 0;
}
```

5.2 BFS-queue

```
/*BFS - queue version*/
void BFS(vector<int> &result, vector<pair<int, int>> edges, int
     node, int start)
    vector<int> pass(node, 0);
    queue<int> q;
    queue<int> p;
    q.push(start);
    int count = 1;
    vector<pair<int, int>> newedges;
    while (!q.empty())
        pass[q.front()] = 1;
for (int i = 0; i < edges.size(); i++)</pre>
             if (edges[i].first == q.front() && pass[edges[i].
                 second] == 0)
             {
                 p.push(edges[i].second);
                 result[edges[i].second] = count;
             else if (edges[i].second == q.front() && pass[edges
                 [i].first] == 0)
             {
                 p.push(edges[i].first);
                 result[edges[i].first] = count;
             else
                 newedges.push back(edges[i]);
        edges = newedges;
        newedges.clear();
        q.pop();
        if (q.empty() == true)
             q = p;
             queue<int> tmp;
             p = tmp;
             count++;
    }
int main()
    int node;
    cin >> node;
    vector<pair<int, int>> edges;
    int a, b:
    while (cin >> a >> b)
    {
        /*a = b = -1 means input edges ended*/
        if (a == -1 && b == -1)
            break:
        edges.push_back(pair<int, int>(a, b));
    vector<int> result(node, -1);
    BFS(result, edges, node, 0);
    return 0:
```

5.3 DFS-rec

```
/*DFS - Recursive version*/
map<pair<int,int>,int> edges;
vector<int> pass;
vector<int> route;
void DFS(int start){
   pass[start] = 1;
   route.push_back((*iter).first.second);
          DFS((*iter).first.second);
       else if((*iter).first.second == start && (*iter).second
            == 0 && pass[(*iter).first.first] == 0){
          route.push_back((*iter).first.first);
          DFS((*iter).first.first);
       }
   }
int main(){
   int node;
   cin>>node:
   pass.resize(node,0);
   int a,b;
```

```
while(cin>>a>>b){
        if(a == -1 && b == -1)
            break;
        edges.insert(pair<pair<int,int>,int>(pair<int,int>(a,b)
             ,0));
    int start;
    cin>>start;
    route.push_back(start);
    DFS(start);
    return 0;
}
5.4 Dijkstra
```

```
*SPA - Dijkstra*/
const int MAXN = 1e5 + 3;
const int inf = INT_MAX;
typedef pair<int, int> pii;
vector<vector<pii>>> weight(MAXN);
vector<int> isDone(MAXN, false), dist, ancestor;
void dijkstra(int s)
     priority_queue<pii, vector<pii>, greater<pii>> pq;
    pq.push(pii(0, s));
ancestor[s] = -1;
     while (!pq.empty())
          int u = pq.top().second;
         pq.pop();
         isDone[u] = true;
          for (auto &pr : weight[u])
              int v = pr.first, w = pr.second;
              if (!isDone[v] \&\& dist[u] + w < dist[v])
                   dist[v] = dist[u] + w:
                   pq.push(pii(dist[v], v));
                   ancestor[v] = u;
         }
    }
// weight[a - 1].push_back(pii(b - 1, w));
// weight[b - 1].push_back(pii(a - 1, w));
// dist.resize(n, inf);
// ancestor.resize(n, -1);
// dist[0] = 0;
// dijkstra(0);
```

5.5 Euler circuit

```
/*Euler circuit*/
/*From NTU kiseki*/
/*G is graph, vis is visited, la is path*/
bool vis[N];
size_t la[K];
void dfs(int u, vector<int> &vec)
    while (la[u] < G[u].size())</pre>
         if (vis[G[u][la[u]].second])
             ++la[u]:
             continue;
         int v = G[u][la[u]].first;
         vis[G[u][la[u]].second] = true;
         ++la[u];
         dfs(v, vec);
         vec.push_back(v);
}
```

5.6 Floyd-warshall

```
/*SPA - Floyd-Warshall*/
// 有向圖·正邊
                  O(V^3)
// 有向圖,無負環
                  O(V<sup>3</sup>)
// 有向圖,有負環
                  不適用
// 無向圖,正邊
                  0(V3)
// 無向圖,無負環
                  不適用
                 不適用
// 無向圖,有負環
/*Find min weight cycle*/
#define inf 99999
void floyd_warshall(vector<vector<int>> &distance, vector<</pre>
    vector<int>> &ancestor, int n)
    for (int k = 0; k < n; k++)
        for (int i = 0; i < n; i++)
```

```
for (int j = 0; j < n; j++)
                        \label{eq:if_distance} \textbf{if} \ (\texttt{distance}[\texttt{i}][\texttt{k}] \ + \ \texttt{distance}[\texttt{k}][\texttt{j}] \ < \ \texttt{distance}[
                              distance[i][j] = distance[i][k] + distance[
                                     k][j]
                               ancestor[i][j] = ancestor[k][j];
                  }
           }
      }
}
vector<vector<int>> distance(n, vector<int>(n, inf));
vector<vector<int>> ancestor(n, vector<int>(n, -1));
distance[a][b] = w;
ancestor[a][b] = w;
floyd_warshall(distance, ancestor, n);
/*Negative cycle detection*/
for (int i = 0; i < n; i++)</pre>
      if (distance[i][i] < 0)</pre>
            cout << "Negative cycle!" << endl;</pre>
            break;
}
```

5.7 Hamilton_cycle

```
/*find hamilton cycle*/
void hamilton(vector<vector<int>> gp, int k, int cur, vector<</pre>
     int>& solution,vector<bool> pass,bool& flag){
     if(k == gp.size()-1){
   if(gp[cur][1] == 1){
      cout << 1 << " ";</pre>
              while(cur != 1){
                   cout << cur << " "
                   cur = solution[cur];
              cout << cur << endl;
              flag = true;
              return;
     for (int i = 0; i < gp[cur].size() && !flag; i++){</pre>
         if(gp[cur][i] == 1 && !pass[i]){
    pass[i] = true;
              solution[i] = cur;
hamilton(gp, k + 1, i, solution, pass,flag);
              pass[i] = false;
    }
int main(){
     while(cin>>n){
         int a,b;
         bool end = false;
vector<vector<int>> gp(n+1,vector<int>(n+1,0));
         while(cin>>a>>b){
              if(a == 0 \&\& b == 0)
                  break;
              gp[a][b] = 1;
              gp[b][a] = 1;
         vector<int> solution(n + 1, -1);
         vector<bool> pass(n + 1, false);
          solution[1] = 0;
         pass[1] = true;
         bool flag = false;
hamilton(gp, 1,1 ,solution,pass,flag);
         if(!flag)
              cout << "N" << endl;
     return 0;
4
1 2
2 3
2 4
3 4
3 1
0 0
output: 1 3 4 2 1
```

5.8Kruskal

```
struct edges{
    int from;
    int to;
```

```
int weight;
     friend bool operator < (edges a, edges b){</pre>
          return a.weight > b.weight;
int find(int x,vector<int>& union_set){
     if(x != union_set[x])
  union_set[x] = find(union_set[x], union_set);
     return union_set[x];
void merge(int a,int b,vector<int>& union_set){
     int pa = find(a, union_set);
int pb = find(b, union_set);
     if(pa != pb)
          union_set[pa] = pb;
void kruskal(priority_queue<edges> pq,int n){
     vector<int> union_set(n, 0);
for (int i = 0; i < n; i++)</pre>
     union_set[i] = i;
int edge = 0;
int cost = 0; //evaluate cost of mst
     while(!pq.empty() && edge < n - 1){</pre>
          edges cur = pq.top();
int from = find(cur.from, union_set);
int to = find(cur.to, union_set);
          if(from != to){
               merge(from, to, union_set);
               edge += 1;
               cost += cur.weight;
          pq.pop();
     if(edge < n-1)</pre>
          cout << "No mst" << endl;</pre>
          cout << cost << endl;</pre>
int main(){
     int n;
     cin >> n;
     int a, b, d;
     priority_queue<edges> pq;
     while(cin>>a>>b>>d){
          if(a == -1 && b == -1 && d == -1)
               break;
          edges tmp;
          tmp.from
          tmp.to = b;
tmp.weight = d;
          pq.push(tmp);
     kruskal(pq, n);
     return 0;
```

5.9 Minimum Weight Cycle

```
// 最小環
// 圖上無負環!!!!
#define INF 99999
vector<vector<int>> w, d, p;
vector<int> cycle;
int c = 0;
void trace(int i, int j)
    cycle[c++] = i;
    if (i != j)
    trace(p[i][j], j);
void init(int n)
    for (int i = 0; i < n; ++i)
    d[i][i] = 0;</pre>
void minimum_cycle(int n)
    int weight = 1e9;
    for (int k = 0; k < n; ++k)
         for (int i = 0; i < k; ++i)</pre>
             for (int j = 0; j < k; ++j)
                  if (i != j)
                      if (w[k][i] + d[i][j] + w[j][k] < weight)
                           weight = w[k][i] + d[i][j] + w[j][k];
                           c = 0:
                           trace(i, j);
                          cycle[c++] = k;
                      }
         for (int i = 0; i < n; ++i)</pre>
             for (int j = 0; j < n; ++j)
                  if (d[i][k] + d[k][j] < d[i][j])</pre>
```

```
{
                        d[i][j] = d[i][k] + d[k][j];
                        p[i][j] = p[i][k];
         }
     if (weight == 1e9)
         cout << "No exist";
         bug(weight);
         bug(c);
         bugarr(cycle);
void simple_minimum_cycle(int n) // No use vector p
     int weight = INF;
     for (int k = 0; k < n; ++k)
          for (int i = 0; i < k; ++i)
              for (int j = 0; j < k; ++j)
if (i != j)
                        weight = min(mp[k][i] + d[i][j] + mp[j][k],
                              weight);
          for (int i = 0; i < n; ++i)
    for (int j = 0; j < n; ++j)
        d[i][j] = min(d[i][k] + d[k][j], d[i][j]);</pre>
     if (weight == INF)
    cout << "Back to jail\n";</pre>
     else
          cout << weight << endl;</pre>
v.resize(n, vector<int>(n, INF));
d.resize(n, vector<int>(n, INF));
p.resize(n, vector<int>(n));
cycle.resize(n);
//Edge input
w[a][b] = w;
d[a][b] = w;
p[a][b] = b;
init(n);
minimum_cycle(n);
5.10 Prim
  *mst - Prim*.
#define inf 99999
struct edges
     int from:
     int to;
     int weight;
     friend bool operator<(edges a, edges b)</pre>
         return a.weight > b.weight;
    }
};
void Prim(vector<vector<int>> gp, int n, int start)
{
     vector<bool> pass(n, false);
     int edge = 0;
int cost = 0; //evaluate cost of mst
     priority_queue<edges> pq;
     for (int i = 0; i < n; i++)
         if (gp[start][i] != inf)
               edges tmp;
               tmp.from = start;
              tmp.to = i;
              tmp.weight = gp[start][i];
              pq.push(tmp);
     pass[start] = true;
     while (!pq.empty() && edge < n - 1)
          edges cur = pq.top();
         pq.pop();
          if (!pass[cur.to])
               for (int i = 0; i < n; i++)
                   if (gp[cur.to][i] != inf)
                        edges tmp;
                        tmp.from = cur.to;
                        tmp.r.c...
                        tmp.weight = gp[cur.to][i];
                        pq.push(tmp);
```

pass[cur.to] = true;

5.11 Union_find

```
// union_find from 台大
vector<int> father;
vector<int> people;
void init(int n)
    for (int i = 0; i < n; i++)
         father[i] = i;
         people[i] = 1;
    }
int Find(int x)
    if (x != father[x])
    father[x] = Find(father[x]);
return father[x];
void Union(int x, int y)
    int m = Find(x);
    int n = Find(y);
    if (m != n)
         father[n] = m;
         people[m] += people[n];
}
```

6 Mathematics

6.1 Catalan

Catalan number

```
• 0~19項的catalan number \circ 1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 16796, 58786, \\ 208012, 742900, 2674440, 9694845, 35357670, 129644790, \\ 477638700, 1767263190 \\ \circ 公式: <math>C_n = \frac{1}{n+1} \binom{2n}{n} = \frac{(2n)!}{(n+1)!n!}
```

6.2 Combination

6.3 CRT

```
// 中國剩餘定理
template <typename T>
tuple<T, T, T> extgcd(T a, T b)
{
    if (!b)
        return make_tuple(a, 1, 0);
    T d, x, y;
```

6.4 Extended Euclidean

```
// ax + by = gcd(a,b)
pair<long long, long long> extgcd(long long a, long long b)
      if (b == 0)
     if (b == 0)
    return {1, 0};
long long k = a / b;
pair<long long, long long> p = extgcd(b, a - k * b);
//cout << p.first << " " << p.second << endl;
//cout << "商數(k)= " << k << endl << endl;
return {p.second, p.first - k * p.second};</pre>
}
int main()
      int a, b;
      cin >> a >> b;
      return 0;
// ax + by = gcd(a,b) * r
/*find |x|+|y| -> min*/
int main()
      long long r, p, q; /*px+qy = r*/
      int cases;
cin >> cases;
      while (cases--)
            cin >> r >> p >> q;
            pair<long long, long long> xy = extgcd(q, p); //(x0,y0)
long long ans = 0, tmp = 0;
double k, k1;
long long s, s1;
k = 1 - (double)(r * xy.first) / p;
            s = round(k);
ans = llabs(r * xy.first + s * p) + llabs(r * xy.second
            - s * q);
k1 = -(double)(r * xy.first) / p;
            s1 = round(k1);
/*cout << k << endl << k1 << endl;
            cout << s << endl << s1 << endl;*/
tmp = llabs(r * xy.first + s1 * p) + llabs(r * xy.
    second - s1 * q);</pre>
            ans = min(ans, tmp);
            cout << ans << endl;</pre>
       return 0:
```

6.5 Fermat

- $a^{(p-1)} \equiv 1 \pmod{p} \iff a * a^{(p-2)} \equiv 1$ • $a^{(p-2)} \equiv 1/a$
- 同餘因數定理

$$\circ \ a \equiv b \ (mod \ p) \iff k|a-b|$$

• 同餘加法性質

o
$$a \equiv b \pmod{p}$$
 and $c \equiv d \pmod{p}$
<=> $a + c \equiv b + d \pmod{p}$

• 同餘相乘性質

$$\circ \ a \equiv b \pmod{p}$$
 and $c \equiv d \pmod{p}$
 $<=> ac \equiv bd \pmod{p}$

• 同餘次方件質

$$\circ \ \ a \equiv b \ (mod \ p) \iff a^n \equiv b^n \ (mod \ p)$$

• 同餘倍方性質

```
\circ \ a \equiv b \pmod{p} \iff am \equiv bm \pmod{p}
```

6.6 Hex to Dec

```
int HextoDec(string num) //16 to 10
{
    int base = 1;
    int temp = 0;
    for (int i = num.length() - 1; i >= 0; i--)
    {
        if (num[i] >= '0' && num[i] <= '9')
        {
            temp += (num[i] - 48) * base;
            base = base * 16;
        }
        else if (num[i] >= 'A' && num[i] <= 'F')
        {
            temp += (num[i] - 55) * base;
            base = base * 16;
        }
    }
    return temp;
}
void DecToHex(int p) //10 to 16
{
    char *l = new (char);
    sprintf(l, "%X", p);
    //int l_intResult = stoi(l);
    cout << l << "\n";
    //return l_intResult;
}</pre>
```

6.7 Log

6.8 Mod 性質

```
加法: (a+b) \mod p = (a \mod p + b \mod p) \mod p
減法: (a-b) \operatorname{mod} p = (a \operatorname{mod} p - b \operatorname{mod} p + p) \operatorname{mod} p
乘法: (a*b) \mod p = (a \mod p \cdot b \mod p) \mod p
次方: (a^b) \operatorname{mod} p = ((a \operatorname{mod} p)^b) \operatorname{mod} p
加法結合律: ((a+b) \operatorname{mod} p + c) \operatorname{mod} p = (a+(b+c)) \operatorname{mod} p
乘法結合律: ((a \cdot b) \mod p \cdot c) \mod p = (a \cdot (b \cdot c)) \mod p
加法交換律: (a+b) \mod p = (b+a) \mod p
乘法交換律: (a \cdot b) \mod p = (b \cdot a) \mod p
結合律: ((a+b) \operatorname{mod} p \cdot c) = ((a \cdot c) \operatorname{mod} p + (b \cdot c) \operatorname{mod} p) \operatorname{mod} p
如果 a \equiv b \pmod{m} ・我們會說 a, b 在模 m 下同餘。
以下為性質:
 ・ 整除性: a \equiv b \pmod{m} \Rightarrow c \cdot m = a - b, c \in \mathbb{Z}
              \Rightarrow a \equiv b \pmod{m} \Rightarrow m \mid a - b
  • 遞移性: 若a \equiv b \pmod{c}, b \equiv d \pmod{c}
               則 a \equiv d \pmod{c}

    保持基本運算:

         \left\{ \begin{aligned} a &\equiv b (\operatorname{mod} m) \\ c &\equiv d (\operatorname{mod} m) \end{aligned} \right. \Rightarrow \left\{ \begin{aligned} a &\pm c \equiv b \pm d (\operatorname{mod} m) \\ a \cdot c \equiv b \cdot d (\operatorname{mod} m) \end{aligned} \right.
      k \in \mathbb{Z}^+, a \equiv b \pmod{m} \Leftrightarrow k \cdot a \equiv k \cdot b \pmod{k \cdot m}
 模逆元是取模下的反元素,即為找到 a^{-1} 使得 aa^{-1}\equiv 1 \, \mathrm{mod} \, c 。
 整數 a \in \text{mod } c 下要有模反元素的充分必要條件為 a, c 互質。
 模逆元如果存在會有無限個,任意兩相鄰模逆元相差c。
 給定一個質數 p 及一個整數 a · 那麼: a^p \equiv a \pmod{p} 如果 \gcd(a,p) = 1 · 則:
 a^{p-1} \equiv 1 (\mod \, p)
 歐拉定理是比較 general 版本的費馬小定理。給定兩個整數 n 和 a · 如果 \gcd(a,n)=1 · 貝
 a^{\Phi(n)} \equiv 1 (\mod n) 如果 n 是質數 \cdot \Phi(n) = n-1 \cdot 也就是費馬小定理
 Wilson's theorem
 給定一個質數 p · 則 : (p-1)! \equiv -1 \pmod{p}
6.9 PI
#define PI acos(-1)
#define PI M PI
6.10 Pow Mod
int pow_mod(int a, int n, int m) // a ^ n mod m;
                                                             // a, n, m < 10 ^ 9
       if (n == 0)
              return 1;
       int x = pow_mid(a, n / 2, m);
long long ans = (long long)x * x % m;
if (n % 2 == 1)
    ans = ans * a % m;
return (int)ans;
int inv(int a, int n, int p) // n = p-2
       long long res = 1;
              (; n; n >>= 1, (a *= a) %= p)
if (n & 1)
                      (res *= a) %= p;
       return rès;
6.11 Prime table
const int maxn = 10e9:
vector<int> p;
bitset<maxn> is_notp;
void PrimeTable()
       is_notp.reset();
       is_notp[0] = is_notp[1] = 1;
for (int i = 2; i <= maxn; ++i)</pre>
```

if (!is_notp[i])

p.push_back(i);
for (int j = 0; j < (int)p.size(); ++j)</pre>

if (i * p[j] > maxn)
 break;
is_notp[i * p[j]] = 1;
if (i % p[j] == 0)

break;

```
}
```

6.12 Prime 判斷

```
typedef long long ll;
ll modmul(ll a, ll b, ll mod)
     11 ret = 0;
for (; b; b >>= 1, a = (a + a) % mod)
    if (b & 1)
               ret = (ret + a) % mod;
     return ret;
}
11 qpow(11 x, 11 u, 11 mod)
     ll ret = 111;
     for (; u; u >>= 1, x = modmul(x, x, mod))
    if (u & 1)
               ret = modmul(ret, x, mod);
     return ret;
ll gcd(ll a, ll b)
     return b ? gcd(b, a % b) : a;
11 Pollard_Rho(ll n, ll c)
     ll i = 1, j = 2, x = rand() % (n - 1) + 1, y = x;
     while (1)
          x = (modmul(x, x, n) + c) % n;
ll p = gcd((y - x + n) % n, n);
if (p != 1 && p != n)
               return p;
          if(y == x)
                return n;
          if (i == j)
               y = x;
j <<= 1;
          }
    }
bool Miller_Rabin(ll n)
     ll x, pre, u = n - 1;
int i, j, k = 0;
if (n == 2 || n == 3 || n == 5 || n == 7 || n == 11)
     return 1;

if (n == 1 || !(n % 2) || !(n % 3) || !(n % 5) || !(n % 7)

|| !(n % 11))
     while (!(u & 1))
          k++;
          u >>= 1;
     srand((long long)12234336);
for (i = 1; i <= 50; i++)</pre>
          x = rand() % (n - 2) + 2;
          if (!(n % x))
               return 0;
          x = qpow(x, u, n);
          pre = x;
for (j = 1; j <= k; j++)
               x = modmul(x, x, n);
if (x == 1 && pre != 1 && pre != n - 1)
                    return 0:
               pre = x;
          if (x != 1)
               return 0;
     return 1:
// if (Miller_Rabin(n)) puts("Prime");
```

6.13 Round(小數)

```
double myround(double number, unsigned int bits)
{
    LL integerPart = number;
    number -= integerPart;
    for (unsigned int i = 0; i < bits; ++i)
        number *= 10;
    number = (LL)(number + 0.5);
    for (unsigned int i = 0; i < bits; ++i)
        number /= 10;
    return integerPart + number;
}
//printf("%.1f\n", round(3.4515239, 1));</pre>
```

6.14 二分逼近法

```
#define eps 1e-14
void half_interval()
{

    double L = 0, R = /*區間*/, M;
    while (R - L >= eps)
    {

        M = (R + L) / 2;
        if (/*函數*/ > /*方程式目標*/)
            L = M;
        else
            R = M;
    }
    printf("%.31f\n", R);
}
```

6.15 公式

```
S_n = \frac{a(1-r^n)}{1-r} \ a_n = \frac{a_1+a_n}{2} \sum_{k=1}^n k = \frac{n(n+1)}{2} \sum_{k=1}^n k^2 = \frac{n(n+1)(2n+1)}{6}\sum_{k=1}^n k^3 = \left[\frac{n(n+1)}{2}\right]^2
```

6.16 四則運算

```
string s = ""; //開頭是負號要補0
long long int DFS(int le, int ri) // (0, string final index)
     for (int i = ri; i >= le; i--)
           if (s[i] == ')')
           if (s[i] == '(')
           if (s[i] == '+' && c == 0)
           return DFS(le, i - 1) + DFS(i + 1, ri);
if (s[i] == '-' && c == 0)
                return DFS(le, i - 1) - DFS(i + 1, ri);
     for (int i = ri; i >= le; i--)
           if (s[i] == ')')
           if (s[i] == '(')
           if (s[i] == '*' && c == 0)
    return DFS(le, i - 1) * DFS(i + 1, ri);
if (s[i] == '/' && c == 0)
           return DFS(le, i - 1) / DFS(i + 1, ri);
if (s[i] == '%' && c == 0)
return DFS(le, i - 1) % DFS(i + 1, ri);
     if ((s[le] == '(') && (s[ri] == ')'))
     return DFS(le + 1, ri - 1); //去除刮號
if (s[le] == ' ' && s[ri] == ' ')
     return DFS(le + 1, ri - 1); //去除左右兩邊空格
if (s[le] == ' ')
     return DFS(le + 1, ri); //去除左邊空格
if (s[ri] == ' ')
           return DFS(le, ri - 1); //去除右邊空格
     long long int num = 0;
     for (int i = le; i <= ri; i++)

num = num * 10 + s[i] - '0';
     return num;
```

6.17 因數表

```
| const int limit = 10000000;
| vector<vector<int>> arr(limit);
| for (int i = 1; i <= limit; i++)
| for (int j = i; j <= limit; j += i)
| arr[j].pb(i); // i 為因數
```

6.18 數字乘法組合

```
// ex tn = 2 * 2 * 3 => {2, 1}
              a.push back(num / i);
                                                                               {
                                                                                     // "2" 個 2, "1" 個 3
vector<int> fac;
              ans.push_back(a);
    }
                                                                                     for (auto pr : p)
vector<vector<int>> ans;
                                                                                          if (pr * pr > tn)
                                                                                               break;
vector<int> zero;
dfs(2, num, num, zero, ans);
/*/num 為 input 數字*/
                                                                                          if (tn % pr == 0)
for (int i = 0; i < ans.size(); i++)</pre>
                                                                                               int cc = 0;
                                                                                               while (tn \% pr == 0)
     for (int j = 0; j < ans[i].size() - 1; j++)
    cout << ans[i][j] << " ";</pre>
     cout << ans[i][ans[i].size() - 1] << endl;
                                                                                                   tn /= pr;
                                                                                               fac.push back(cc);
6.19 數字加法組合
                                                                                     if (tn > 1)
void recur(int i, int n, int m, vector<int> &out, vector<vector</pre>
                                                                                          fac.push_back(1);
     <int>> &ans)
                                                                                     return fac:
                                                                               }
     if (n == 0)
          for (int i : out)
                                                                                6.22 質數數量
              if (i > m)
                   return:
                                                                                // 10 ^ 11 左右
          ans.push_back(out);
                                                                                #define LL long long
                                                                                const int N = 5e6 + 2:
     for (int j = i; j <= n; j++)</pre>
                                                                                bool np[N];
          out.push_back(j);
                                                                                int prime[N], pi[N];
                                                                                int getprime()
          recur(j, n - j, m, out, ans);
out.pop_back();
                                                                                     int cnt = 0;
                                                                                     np[0] = np[1] = true;
pi[0] = pi[1] = 0;
for (int i = 2; i < N; ++i)</pre>
vector<vector<int>> ans:
vector<int> zero:
recur(1, num, num, zero, ans);
                                                                                          if (!np[i])
// num 為 input 數字
                                                                                              prime[++cnt] = i;
for (int i = 0; i < ans.size(); i++)</pre>
                                                                                          pi[i] = cnt;
                                                                                          for (int j = 1; j <= cnt && i * prime[j] < N; ++j)
     for (int j = 0; j < ans[i].size() - 1; j++)
    cout << ans[i][j] << " ";</pre>
     cout << ans[i][]] << " ";
cout << ans[i][ans[i].size() - 1] << endl;</pre>
                                                                                               np[i * prime[j]] = true;
                                                                                               if (i % prime[j] == 0)
}
                                                                                         }
6.20 羅馬數字
                                                                                     }
                                                                                     return cnt;
int romanToInt(string s)
                                                                                const int M = 7;
const int PM = 2 * 3 * 5 * 7 * 11 * 13 * 17;
     unordered_map<char, int> T;
     T['I'] = 1;
T['V'] = 5;
                                                                                int phi[PM + 1][M + 1], sz[M + 1];
                                                                                void init()
    T['V'] = 5;
T['X'] = 10;
T['L'] = 50;
T['C'] = 100;
T['D'] = 500;
                                                                                     getprime();
                                                                                     sz[0] = 1;
for (int i = 0; i <= PM; ++i)</pre>
     T['M'] = 1000;
                                                                                        phi[i][0] = i;
                                                                                     for (int i = 1; i <= M; ++i)
     int sum = T[s.back()];
                                                                                          sz[i] = prime[i] * sz[i - 1];
for (int j = 1; j <= PM; ++j)
    phi[j][i] = phi[j][i - 1] - phi[j / prime[i]][i -</pre>
     for (int i = s.length() - 2; i >= 0; --i)
          if (T[s[i]] < T[s[i + 1]])
              sum -= T[s[i]];
          else
                                                                                     }
              sum += T[s[i]];
                                                                                int sqrt2(LL x)
     return sum;
}
                                                                                     LL r = (LL) sqrt(x - 0.1);
                                                                                     while (r * r <= x)
          質因數分解
                                                                                         ++r;
6.21
                                                                                     return int(r - 1);
vector<int> primeFactorization(int tn) // 配合質數表
                                                                                int sqrt3(LL x)
                                               //重複 or 不重複擇一
{
     vector<int> f:
                                                                                     LL r = (LL)cbrt(x - 0.1);
while (r * r * r <= x)
     f.clear();
     int n = tn:
                                                                                         ++r;
     for (int i = 0; i < (int)p.size(); ++i)</pre>
                                                                                     return int(r - 1);
          if (p[i] * p[i] > n)
                                                                                LL getphi(LL x, int s)
          if (n % p[i])
                                                                                     if (s == 0)
              continue;
                                                                                          return x;
          // f.pb(p[i]); //不重複
                                                                                     if (s <= M)
          while (n \% p[i] == 0)
                                                                                     return phi[x % sz[s]][s] + (x / sz[s]) * phi[sz[s]][s];
if (x <= prime[s] * prime[s])
    return pi[x] - s + 1;</pre>
              n /= p[i];
              // f.pb(p[i]); //重複
                                                                                     if (x <= prime[s] * prime[s] * prime[s] && x < N)</pre>
                                                                                          int s2x = pi[sqrt2(x)];
                                                                                          LL ans = pi[x] - (s2x + s - 2) * (s2x - s + 1) / 2;
for (int i = s + 1; i <= s2x; ++i)
     if (n != 1)
          f.pb(n);
     return f;
                                                                                              ans += pi[x / prime[i]];
```

return ans;

| vector<int> factorcount(int tn) // 質因數個數

```
return getphi(x, s - 1) - getphi(x / prime[s], s - 1);
LL getpi(LL x)
     if(x < N)
          return pi[x];
     LL ans = getphi(x, pi[sqrt3(x)]) + pi[sqrt3(x)] - 1;
for (int i = pi[sqrt3(x)] + 1, ed = pi[sqrt2(x)]; i <= ed;
           ans -= getpi(x / prime[i]) - i + 1;
     return ans;
LL lehmer_pi(LL x)
     if(x < N)
          return pi[x];
     int a = (int)lehmer_pi(sqrt2(sqrt2(x)));
     int b = (int)lehmer_pi(sqrt2(x));
     int c = (int)lehmer_pi(sqrt3(x));
LL sum = getphi(x, a) + (LL)(b + a - 2) * (b - a + 1) / 2;
for (int i = a + 1; i <= b; i++)</pre>
          LL w = x / prime[i];
           sum -= lehmer_pi(w);
          if (i > c)
                continue:
          LL lim = lehmer_pi(sqrt2(w));
for (int j = i; j <= lim; j++)
                sum -= lehmer_pi(w / prime[j]) - (j - 1);
     return sum;
}
// lehmer_pi(n)
```

7 Other

7.1 Binary search 三類變化

```
// 查找和目標值完全相等的數
int find(vector<int> &nums, int target)
    int left = 0, right = nums.size() - 1;
   while (left < right)</pre>
        int mid = left + (right - left) / 2;
        if (nums[mid] == target)
            return mid;
        else if (nums[mid] < target)</pre>
           left = mid + 1;
        else
            right = mid;
   return -1;
// 找第一個不小於目標值的數 == 找最後一個小於目標值的數
/*(lower_bound)*/
int find(vector<int> &nums, int target)
   int left = 0, right = nums.size() - 1;
while (left < right)</pre>
        int mid = left + (right - left) / 2;
        if (nums[mid] < target)</pre>
            left = mid + 1;
        else
            right = mid;
   return right;
·
// 找第一個大於目標值的數 == 找最後一個不大於目標值的數
/*(upper_bound)*/
int find(vector<int> &nums, int target)
   int left = 0, right = nums.size() - 1;
   while (left < right)
    {
        int mid = left + (right - left) / 2;
        if (nums[mid] <= target)</pre>
           left = mid + 1;
        else
           right = mid;
   return right;
```

7.2 Heap sort

```
void MaxHeapify(vector<int> &array, int root, int length)
{
   int left = 2 * root, right = 2 * root + 1, largest;
   if (left <= length && array[left] > array[root])
        largest = left;
   else
        largest = root;
```

7.3 Josephus

```
/*n people kill k for each turn*/
int josephus(int n, int k)
{
    int s = 0;
    for (int i = 2; i <= n; i++)
    {
        s = (s + k) % i;
    }
    /*index start from 1 -> s+1*/
    return s + 1;
}

/*died at kth*/
int kth(int n, int m, int k)
{
    if (m == 1)
        return n - 1;
    for (k = k * m + m - 1; k >= n; k = k - n + (k - n) / (m - 1))
        ;
    return k;
}
```

7.4 Largest Multi-interval

7.5 Merge sort

```
long long merge(vector<int> &arr, int left, int mid, int right)
{
    int *tmp = new int[right - left + 1];
    long long sum = 0;
    int l = left, r = mid + 1, m = 0;
    while (l <= mid && r <= right)
    {
        if (arr[l] <= arr[r])
            tmp[m++] = arr[l++];
        else
        {
            tmp[m++] = arr[r++];
            sum += mid - l + 1;
        }
    }
    while (l <= mid)
        tmp[m++] = arr[l++];
    while (r <= right)
        tmp[m++] = arr[r++];
    for (int i = left; i <= right; ++i)
        arr[i] = tmp[i - left];</pre>
```

```
delete[] tmp;
    return sum;
}
long long mergesort(vector<int> &arr, int left, int right)
{
    long long sum = 0;
    // left = 0, right = P.size() - 1
    if (left < right)
    {
        int mid = (left + right) / 2;
        sum = mergesort(arr, left, mid);
        sum += mergesort(arr, mid + 1, right);
        sum += merge(arr, left, mid, right);
    }
    return sum; // 回傳為 swap 次數
}</pre>
```

7.6 Quick sort

```
int Partition(vector<int> &arr, int front, int end)
    int pivot = arr[end];
   int i = front -
    for (int j = front; j < end; j++)</pre>
        if (arr[j] < pivot)
            swap(arr[i], arr[j]);
        }
   i++;
   swap(arr[i], arr[end]);
void QuickSort(vector<int> &arr, int front, int end)
    // front = 0 , end = arr.size() - 1
   if (front < end)</pre>
   {
        int pivot = Partition(arr, front, end);
        QuickSort(arr, front, pivot - 1);
        QuickSort(arr, pivot + 1, end);
```

7.7 Sudoku solution

```
/*數獨解法*/
int getSquareIndex(int row, int column, int n)
    return row / n * n + column / n;
}
bool backtracking(vector<vector<int>> &board, vector<vector<</pre>
     bool>> &rows, vector<vector<bool>> &cols,
                   vector<vector<bool>> &boxs, int index, int n)
    int n2 = n * n:
    int rowNum = index / n2, colNum = index % n2;
    if (index >= n2 * n2)
        return true;
    if (board[rowNum][colNum] != 0)
        return backtracking(board, rows, cols, boxs, index + 1,
              n);
    for (int i = 1; i <= n2; i++)
        if (!rows[rowNum][i] && !cols[colNum][i] && !boxs[
             getSquareIndex(rowNum, colNum, n)][i])
            rows[rowNum][i] = true;
             cols[colNum][i] = true;
             boxs[getSquareIndex(rowNum, colNum, n)][i] = true;
             board[rowNum][colNum] = i;
             if (backtracking(board, rows, cols, boxs, index +
                 1, n))
                 return true:
            board[rowNum][colNum] = 0;
            rows[rowNum][i] = false;
cols[colNum][i] = false;
            boxs[getSquareIndex(rowNum, colNum, n)][i] = false;
        }
    return false;
/*用法 main*/
int n = sqrt(數獨邊長大小) /*e.g. 9*9 n=3*/
vector<vector<int>> board(n * n + 1, vector<int>(n * n + 1, 0))
vector<vector<bool>> isRow(n * n + 1, vector<bool>(n * n + 1,
     false));
vector<vector<bool>> isColumn(n * n + 1, vector<bool>(n * n +
     1, false));
```

7.8 Weighted Job Scheduling

```
struct Job
    int start, finish, profit;
bool jobComparataor(Job s1, Job s2)
    return (s1.finish < s2.finish);</pre>
int latestNonConflict(Job arr[], int i)
    for (int j = i - 1; j >= 0; j--)
         if (arr[j].finish <= arr[i].start)</pre>
             return j;
    return -1:
int findMaxProfit(Job arr[], int n)
    sort(arr, arr + n, jobComparataor);
int *table = new int[n];
    table[0] = arr[0].profit;
    for (int i = 1; i < n; i++)
         int inclProf = arr[i].profit;
         int l = latestNonConflict(arr, i);
if (l != -1)
             inclProf += table[1];
         table[i] = max(inclProf, table[i - 1]);
     int result = table[n - 1];
    delete[] table;
    return result;
```

8 String

8.1 KMP

```
// 用在在一個 S 內查找一個詞 W 的出現位置
void ComputePrefix(string s, int next[])
    int n = s.length();
    int q, k;
    next[0] = 0;
    for (k = 0, q = 1; q < n; q++)
        while (k > 0 \&\& s[k] != s[q])
               = next[k];
        if (s[k] == s[q])
            k++:
        next[q] = k;
    }
void KMPMatcher(string text, string pattern)
    int n = text.length();
    int m = pattern.length();
int next[pattern.length()];
    ComputePrefix(pattern, next);
    for (int i = 0, q = 0; i < n; i++)
        while (q > 0 && pattern[q] != text[i])
            q = next[q];
        if (pattern[q] == text[i])
            q++;
        if (q == m)
```

8.3 Sliding window

```
string minWindow(string s, string t)
     unordered_map<char, int> letterCnt;
     for (int i = 0; i < t.length(); i++)
         letterCnt[t[i]]++;
     int minLength = INT_MAX, minStart = -1;
    int left = 0, matchCnt = 0;
for (int i = 0; i < s.length(); i++)</pre>
         if (--letterCnt[s[i]] >= 0)
             matchCnt++;
         while (matchCnt == t.length())
              if (i - left + 1 < minLength)</pre>
             {
                  minLength = i - left + 1;
                  minStart = left;
              if (++letterCnt[s[left]] > 0)
                  matchCnt--;
             left++;
         }
     return minLength == INT_MAX ? "" : s.substr(minStart,
          minLength);
}
```

8.4 Split

```
vector<string> mysplit(const string& str, const string& delim)
    vector<string> res;
         "" == str)
    if ('
        return res;
    char *strs = new char[str.length() + 1];
    strcpy(strs, str.c_str());
    char *d = new char[delim.length() + 1];
    strcpy(d, delim.c_str());
    char *p = strtok(strs, d);
    while (p)
        string s = p;
        res.push_back(s);
        p = strtok(NULL, d);
    return res;
}
```

9 data structure

9.1 Bigint

```
//台大 //非必要請用python
struct Bigint
    static const int LEN = 60;
                                         // maxLEN
    static const int BIGMOD = 10000; //10為正常位數
    int v1, v[LEN];
    // vector<int> v;
Bigint() : s(1) { vl = 0; }
    Bigint(long long a)
         v1 = 0;
        if (a < 0)
        {
             s = -1:
             a = -a;
         while (a)
             push_back(a % BIGMOD);
             a /= BIGMOD;
    Bigint(string str)
        s = 1:
        v1 = 0;
        int stPos = 0, num = 0;
         if (!str.empty() && str[0] == '-')
             stPos = 1;
             s = -1;
         for (int i = str.length() - 1, q = 1; i >= stPos; i--)
             num += (str[i] - '0') * q;
             if ((q *= 10) >= BIGMOD)
                 push_back(num);
                 num = 0;
                 q = 1;
             }
        if (num)
        push_back(num);
n();
    int len() const
        return vl; //return SZ(v);
    bool empty() const { return len() == 0; }
    void push_back(int x)
    {
        v[vl++] = x; //v.PB(x);
    }
    void pop_back()
        vl--; //v.pop_back();
    int back() const
    {
        return v[vl - 1]; //return v.back();
    void n()
         while (!empty() && !back())
             pop_back();
    void resize(int nl)
                               //v.resize(nl);
         fill(v, v + vl, 0); //fill(ALL(v), 0);
    void print() const
        if (empty())
        {
             putchar('0');
             return;
         if (s == -1)
        lf (s == -1)
    putchar('-');
printf("%d", back());
for (int i = len() - 2; i >= 0; i--)
    printf("%.4d", v[i]);
    friend std::ostream &operator<<(std::ostream &out, const
         Bigint &a)
        if (a.empty())
        {
             out << "0";
             return out;
         if (a.s == -1)
```

```
out << "-
    out << a.back();
     for (int i = a.len() - 2; i >= 0; i--)
         char str[10];
sprintf(str, 5, "%.4d", a.v[i]);
         out << str;
     return out:
int cp3(const Bigint &b) const
     if (s != b.s)
         return s - b.s;
     if (s == -1)
         return '-(-*this).cp3(-b);
     if (len() != b.len())
     return len() - b.len(); //int

for (int i = len() - 1; i >= 0; i--)

if (v[i] != b.v[i])
              return v[i] - b.v[i];
     return 0;
bool operator<(const Bigint &b) const</pre>
     return cp3(b) < 0;
bool operator<=(const Bigint &b) const
{
     return cp3(b) <= 0;</pre>
bool operator == (const Bigint &b) const
{
     return cp3(b) == 0;
bool operator!=(const Bigint &b) const
     return cp3(b) != 0:
bool operator>(const Bigint &b) const
{
     return cp3(b) > 0;
bool operator>=(const Bigint &b) const
{
     return cp3(b) >= 0;
Bigint operator-() const
     Bigint r = (*this);
    r.s = -r.s;
     return r;
Bigint operator+(const Bigint &b) const
     if (s == -1)
    return -(-(*this) + (-b));
if (b.s == -1)
         return (*this) - (-b);
    Bigint r;
     int nl = max(len(), b.len());
    r.resize(nl + 1);
for (int i = 0; i < nl; i++)
         if (i < len())</pre>
              r.v[i] += v[i];
         if (i < b.len())
    r.v[i] += b.v[i];</pre>
         if (r.v[i] >= BIGMOD)
         {
              r.v[i + 1] += r.v[i] / BIGMOD;
              r.v[i] %= BIGMOD;
         }
    }
    r.n();
    return r:
Bigint operator-(const Bigint &b) const
     if (s == -1)
    return -(-(*this) - (-b));
if (b.s == -1)
     return (*this) + (-b);
if ((*this) < b)
         return -(b - (*this));
     Bigint r;
    r.resize(len());
for (int i = 0; i < len(); i++)
         r.v[i] += v[i];
         if (i < b.len())</pre>
             r.v[i] -= b.v[i];
         if (r.v[i] < 0)</pre>
              r.v[i] += BIGMOD;
              r.v[i + 1]--;
```

```
r.n();
         return r;
     Bigint operator*(const Bigint &b)
         Bigint r;
         r.resize(len() + b.len() + 1);
         r.s = s * b.s;
         for (int i = 0; i < len(); i++)</pre>
              for (int j = 0; j < b.len(); j++)</pre>
                  r.v[i + j] += v[i] * b.v[j];
                   if (r.v[i + j] >= BIGMOD)
                       r.v[i + j + 1] += r.v[i + j] / BIGMOD;
r.v[i + j] %= BIGMOD;
              }
         r.n();
         return r;
     Bigint operator/(const Bigint &b)
         Bigint r;
         r.resize(max(1, len() - b.len() + 1));
         int oriS = s;
         Bigint b2 = \dot{b}; // b2 = abs(b)
         s = b2.s = r.s = 1;
for (int i = r.len() - 1; i >= 0; i--)
              int d = 0, u = BIGMOD - 1;
              while (d < u)
                  int m = (d + u + 1) >> 1;
r.v[i] = m;
if ((r * b2) > (*this))
                       ù = m - 1;
                  else
                       d = m;
              r.v[i] = d;
         }
         \dot{s} = oriS;
         r.s = s * b.s;
         r.n();
         return r;
     Bigint operator%(const Bigint &b)
         return (*this) - (*this) / b * b;
};
9.2 DisjointSet
```

```
struct DisjointSet {
      int p[maxn], sz[maxn], n, cc;
vector<pair<int*, int>> his;
      vector<int> sh;
      void init(int _n) {
    n = _n; cc = n;
    for (int i = 0; i < n; ++i) sz[i] = 1, p[i] = i;</pre>
           sh.clear(); his.clear();
      void assign(int *k, int v) {
           his.emplace_back(k, *k);
            *k = v;
      void save() {
           sh.push_back((int)his.size());
      void undo() {
   int last = sh.back(); sh.pop_back();
   while (his.size() != last) {
                 int *k, v;
                 tie(k, v) = his.back(); his.pop_back();
           }
      int find(int x) {
           if (x == p[x]) return x;
            return find(p[x]);
      void merge(int x, int y) {
           x = find(x); y = find(y);
if (x == y) return;
if (sz[x] > sz[y]) swap(x, y);
assign(&sz[y], sz[x] + sz[y]);
            assign(&p[x], y);
            assign(&cc, cc - 1);
} ;
```

9.3 Matirx

```
template <tvpename T>
 struct Matrix
        using rt = std::vector<T>;
        using mt = std::vector<rt>;
        using matrix = Matrix<T>;
        int r, c; // [r][c]
        mt m:
        Matrix(int r, int c) : r(r), c(c), m(r, rt(c)) {}
Matrix(mt a) { m = a, r = a.size(), c = a[0].size(); }
rt & operator[](int i) { return m[i]; }
matrix operator+(const matrix &a)
               matrix rev(r, c);
for (int i = 0; i < r; ++i)
    for (int j = 0; j < c; ++j)
        rev[i][j] = m[i][j] + a.m[i][j];</pre>
               return rev;
        matrix operator-(const matrix &a)
               matrix rev(r, c);
for (int i = 0; i < r; ++i)
    for (int j = 0; j < c; ++j)</pre>
                            rev[i][j] = m[i][j] - a.m[i][j];
               return rev;
        matrix operator*(const matrix &a)
               matrix rev(r, a.c);
              matrix rev(r, a.c);
matrix tmp(a.c, a.r);
for (int i = 0; i < a.r; ++i)
    for (int j = 0; j < a.c; ++j)
        tmp[j][i] = a.m[i][j];
for (int i = 0; i < r; ++i)
    for (int j = 0; j < a.c; ++j)
        for (int k = 0; k < c; ++k)
        rev.m[i][j] += m[i][k] * tmp[j][k];
return rev:</pre>
               return rev:
        bool inverse() //逆矩陣判斷
               Matrix t(r, r + c);
for (int y = 0; y < r; y++)
                      t.m[y][c + y] = 1;
for (int x = 0; x < c; ++x)
    t.m[y][x] = m[y][x];</pre>
               if (!t.gas())
                       return false;
               for (int y = 0; y < r; y++)
    for (int x = 0; x < c; ++x)
        m[y][x] = t.m[y][c + x] / t.m[y][y];</pre>
               return true;
        T gas() //行列式
               vector<T> lazy(r, 1);
               bool sign = false;
               for (int i = 0; i < r; ++i)
                      if (m[i][i] == 0)
                             int j = i + 1;
while (j < r && !m[j][i])</pre>
                                   j++;
                              if (\bar{j} == r)
                                     continue:
                             m[i].swap(m[j]);
                             sign = !sign;
                       for (int j = 0; j < r; ++j)
                              if (i == j)
                             continue;
lazy[j] = lazy[j] * m[i][i];
                              T mx = m[j][i];
for (int k = 0; k < c; ++k)
    m[j][k] = m[j][k] * m[i][i] - m[i][k] * mx;</pre>
                      }
               T det = sign ? -1 : 1;
for (int i = 0; i < r; ++i)
                      det = det * m[i][i];
det = det / lazy[i];
for (auto &j : m[i])
                             j /= lazy[i];
               return det;
};
```

```
9.4 分數
 typedef long long 11;
 struct fraction
   11 n, d;
   fraction(const ll &_n = 0, const ll &_d = 1) : n(_n), d(_d)
   {
     11 t = __gcd(n, d);
n /= t, d /= t;
if (d < 0)</pre>
      n = -n, d = -d;
   fraction operator-() const
     return fraction(-n, d);
   fraction operator+(const fraction &b) const
     return fraction(n * b.d + b.n * d, d * b.d);
   fraction operator-(const fraction &b) const
     return fraction(n * b.d - b.n * d, d * b.d);
   fraction operator*(const fraction &b) const
     return fraction(n * b.n, d * b.d);
   fraction operator/(const fraction &b) const
     return fraction(n * b.d, d * b.n);
   void print()
     cout << n;
     if (d != 1)
cout << "/" << d;
};
```