1 Basic

1.1 Code Template

```
1 #include <bits/stdc++.h>
  using namespace std;
  typedef long long 11;
4 typedef unsigned long long ull;
5 typedef pair<int, int> pii;
6 #define pb push back
  #define endl '\n'
  #define bug(x) cout << "value of x is " << x
        << endl:
9 #define bugarr(x)
      for (auto i : x)
           cout << i << ' '; \
      cout << endl;
13 #define x first
14 #define y second
  int main()
16
      ios::sync_with_stdio(0);
17
18
      cin.tie(0);
19
      return 0:
20 }
```

1.5 Range data

6 array = [0] * (N) //N個0

三個 int 變數

10 pow(a, b, c) // a ^ b % c

14 // sep -- 分開多個objects

15 // end -- 默認值是\n

 $8 \mid D$, R, N = map(int, line[:-1].split()) // %

12 print(*objects, sep = ' ', end = '\n')

13 // objects -- 可以一次輸出多個對象

7 range(0, N) // 0 ~ N-1

```
int (-2147483648 to 2147483647)
unsigned int(0 to 4294967295)
long(-2147483648 to 2147483647)
unsigned long(0 to 4294967295)
long long(-9223372036854775808 to 9223372036854775807)
unsigned long long (0 to 18446744073709551615)
```

1.2 Codeblock setting

```
Settings -> Editor -> Keyboard shortcuts -> Plugins -> Source code formatter (AStyle )

Settings -> Source Formatter -> Padding

Delete empty lines within a function or method

Insert space padding around operators

Insert space padding around parentheses on outside

Remove extra space padding around parentheses
```

1.3 IO fast

```
1 void io()
2 {
3     ios::sync_with_stdio(false);
4     cin.tie(nullptr);
5 }
```

1.4 Python

```
1 //輸入
2 import sys
3 line = sys.stdin.readline() // 會讀到換行
4 input().strip()
```

```
1.6 Some Function
```

```
// 四捨五入
1 | round(double f);
2 ceil(double f);
                           // 無條件捨去
3 | floor(double f);
                           //無條件進入
   builtin popcount(int n); // 32bit有多少 1
  to string(int s);
                           // int to string
  /** 全排列要先 sort !!! **/
  next permutation(num.begin(), num.end());
9 | prev_permutation(num.begin(), num.end());
10 | // 用 binary search 找 大 於 或 等 於 val 的 最 小 值 的 位
vector<int>::iterator it = lower bound(v.
       begin(), v.end(), val);
12 / /用binary search找大於val的最小值的位置
13 | vector<int>::iterator it = upper_bound(v.
       begin(), v.end(), val);
14 /*queue*/
16 queue < datatype > q;
17 | front(); /*取出最前面的值(沒有移除掉)*/
18 | back(); /*取出最後面的值(沒有移除掉)*/
19 | pop(); /*移掉最前面的值*/
20 | push(); /*新增值到最後面*/
21 empty(); /*回傳bool,檢查是不是空的queue*/
22 | size(); /*queue 的大小*/
24 /*stack*/
25 stack<datatype> s;
26 top(); /*取出最上面的值(沒有移除掉)*/
27 | pop(); /*移掉最上面的值*/
```

1.7 Time

```
1 cout << 1.0 * clock() / CLOCKS_PER_SEC << endl;</pre>
```

1.8 Vim setting

```
1  /*at home directory*/
2  /* vi ~/.vimrc */
3  syntax enable
4  set smartindent
5  set tabstop=4
6  set shiftwidth=4
7  set expandtab
8  set relativenumber
```

2 DP

2.1 3 維 DP 思路

```
      1 解題思路: dp[i][j][k]

      2 i 跟 j 代表 range i ~ j 的 value

      3 k在我的理解裡是視題目的要求而定的

      4 像是 Remove Boxes 當中 k 代表的是在 i 之前還 有多少個連續的箱子

      5 所以每次區間消去的值就是(k+1) * (k+1)

      6 换言之・我認為可以理解成 k 的意義就是題目今 天所關注的重點,就是老師說的題目所規定的 運算
```

2.2 Knapsack Bounded

```
const int N = 100, W = 100000;
int cost[N], weight[N], number[N];
int c[W + 1];
void knapsack(int n, int w)
```

```
for (int i = 0; i < n; ++i)
           int num = min(number[i], w / weight[
           for (int k = 1; num > 0; k *= 2)
               if (k > num)
11
12
                    k = num;
13
               num -= k;
14
               for (int j = w; j >= weight[i] *
                      k; --j)
1.5
                    c[j] = max(c[j], c[j -
                         weight[i] * k] + cost[i]
                          * k);
16
17
       cout << "Max Prince" << c[w];</pre>
18
19
```

2.3 Knapsack sample

```
1 int Knapsack(vector<int> weight, vector<int>
        value, int bag_Weight)
       // vector<int> weight = {1, 3, 4};
      // vector<int> value = {15, 20, 30};
      // int bagWeight = 4;
      vector<vector<int>> dp(weight.size(),
           vector<int>(bagWeight + 1, 0));
       for (int j = weight[0]; j <= bagWeight;</pre>
           i++)
          dp[0][j] = value[0];
       // weight數組的大小就是物品個數
       for (int i = 1; i < weight.size(); i++)</pre>
      { // 遍歷物品
           for (int j = 0; j <= bagWeight; j++)</pre>
           { // 遍歷背包容量
               if (j < weight[i]) dp[i][j] = dp</pre>
                    [i - 1][j];
               else dp[i][j] = max(dp[i - 1][j
                   ], dp[i - 1][j - weight[i]]
                   + value[i]);
16
      cout << dp[weight.size() - 1][bagWeight]</pre>
            << endl;
```

2.4 Knapsack Unbounded

```
const int N = 100, W = 100000;
int cost[N], weight[N];
int c[W + 1];
void knapsack(int n, int w)
{
    memset(c, 0, sizeof(c));
    for (int i = 0; i < n; ++i)
    for (int j = weight[i]; j <= w; ++j)</pre>
```

```
2.10 Money problem
               c[j] = max(c[j], c[j - weight[i
                                                        vector<string> k:
                                                                                                             if (i != ans.size() - 1)
                                                        while (n && m)
                                                                                                                  cout << ' ';
                    11 + cost[i]);
                                                 19
                                                                                                  39
       cout << "最高的價值為" << c[w];
                                                 20
                                                                                                   40
                                                            if (LCS[n][m] != max(LCS[n - 1][m],
                                                                                                         cout << '\n';
                                                 21
                                                                                                  41
11 }
                                                                 LCS[n][m - 1]))
                                                 22
                                                 23
                                                                k.push back(Ans[n - 1]);
                                                                                                                                                     1 / / 能否湊得某個價位
                                                 24
  2.5 LCIS
                                                                n--;
                                                                                                                                                     void change(vector<int> price, int limit)
                                                 25
                                                                                                     2.8 LPS
                                                 26
                                                                                                                                                           vector<bool> c(limit + 1, 0);
                                                 27
                                                            else if (LCS[n][m] == LCS[n - 1][m])
int LCIS len(vector<int> arr1, vetor<int>
                                                                                                                                                           c[0] = true;
                                                                                                   1 | void LPS(string s)
                                                                                                                                                           for (int i = 0; i < price.size(); ++i)</pre>
                                                            else if (LCS[n][m] == LCS[n][m - 1])
                                                 29
                                                                                                                                                                     // 依序加入各種面額
                                                 30
       int n = arr1.size(), m = arr2.size();
                                                                                                         int maxlen = 0, 1, r;
                                                                                                                                                               for (int j = price[i]; j <= limit;</pre>
                                                 31
       vector<int> table(m, 0);
                                                                                                         int n = n:
                                                 32
                                                        reverse(k.begin(), k.end());
                                                                                                                                                                    ++i) // 由低價位逐步到高價位
      for (int j = 0; j < m; j++)
                                                                                                         for (int i = 0; i < n; i++)
                                                        for (auto i : k)
                                                 33
                                                                                                                                                                   c[j] = c[j] | c[j - price[i]];
          table[j] = 0;
                                                            cout << i << " ":
                                                 34
                                                                                                                                                                            // 湊、湊、湊
       for (int i = 0; i < n; i++)
                                                                                                             int x = 0:
                                                        cout << endl:
                                                 35
                                                                                                                                                           if (c[limit]) cout << "YES\n";</pre>
                                                                                                              while ((s[i - x] == s[i + x]) \&\& (i
                                                        return LCS[N][M];
                                                 36
                                                                                                                                                           else cout << "NO\n";</pre>
           int current = 0;
                                                                                                                  -x >= 0) && (i + x < n)) //odd
           for (int j = 0; j < m; j++)
                                                                                                                  length
                                                                                                                                                    12 // 湊得某個價位的湊法總共幾種
                                                                                                                  x++;
                                                                                                                                                       void change(vector<int> price, int limit)
                                                                                                   10
               if (arr1[i] == arr2[j])
                                                                                                   11
                                                                                                              if (2 * x + 1 > maxlen)
                                                    2.7 LIS
                                                                                                                                                           vector<int> c(limit + 1, 0);
                   if (current + 1 > table[j])
                                                                                                   12
                                                                                                                                                           c[0] = true;
                       table[i] = current + 1:
                                                                                                   13
                                                                                                                  maxlen = 2 * x + 1;
                                                                                                                                                           for (int i = 0; i < price.size(); ++i)</pre>
                                                                                                                 l = i - x;
                                                  1 | vector<int> ans:
                                                                                                                                                               for (int j = price[i]; j <= limit;</pre>
               if (arr1[i] > arr2[j])
                                                                                                                  r = i + x:
                                                  void printLIS(vector<int> &arr, vector<int>
                   if (table[j] > current)
                                                                                                             }
                                                                                                   16
                                                         &pos, int index)
                                                                                                                                                                   c[j] += c[j - price[i]];
19
                       current = table[j];
                                                                                                   17
20
                                                                                                                                                           cout << c[limit] << '\n';</pre>
                                                                                                              while ((s[i - x] == s[i + 1 + x]) \&\&
                                                                                                   18
                                                        if (pos[index] != -1)
21
                                                                                                                   (i - x >= 0) \&\& (i + 1 + x < n)
                                                            printLIS(arr, pos, pos[index]);
                                                                                                                                                    22 // 湊得某個價位的最少錢幣用量
22
       int result = 0;
                                                                                                                  ) //even length
                                                        // printf("%d", arr[index]);
23
       for (int i = 0; i < m; i++)</pre>
                                                                                                                                                       void change(vector<int> price, int limit)
                                                                                                   19
                                                                                                                  x++;
                                                        ans.push_back(arr[index]);
24
          if (table[i] > result)
                                                                                                                                                    24
                                                                                                              if (2 * x > maxlen)
                                                                                                   20
              result = table[i];
25
                                                                                                                                                    25
                                                                                                                                                           vector<int> c(limit + 1, 0);
                                                                                                   21
                                                  9 void LIS(vector<int> &arr)
       return result:
26
                                                                                                                  maxlen = 2 * x;
                                                                                                                                                    26
                                                                                                                                                           c[0] = true;
                                                                                                   22
                                                 10
27 }
                                                                                                                                                    27
                                                                                                                                                           for (int i = 0; i < price.size(); ++i)</pre>
                                                                                                                  1 = i - x + 1;
                                                                                                   23
                                                 11
                                                        vector<int> dp(arr.size(), 1);
                                                                                                                                                               for (int j = price[i]; j <= limit;</pre>
                                                                                                                  r = i + x:
                                                                                                  24
                                                        vector<int> pos(arr.size(), -1);
                                                 12
                                                                                                                                                                    ++j)
                                                        int res = INT MIN, index = 0;
                                                                                                   25
                                                 13
                                                                                                                                                                   c[j] = min(c[j], c[j - price[i]]
                                                                                                   26
                                                        for (int i = 0; i < arr.size(); ++i)</pre>
                                                 14
  2.6 LCS
                                                                                                                                                                         + 1);
                                                                                                   27
                                                                                                         cout << maxlen << '\n'; // 最後長度
                                                 15
                                                                                                                                                           cout << c[limit] << '\n';</pre>
                                                                                                         cout << 1 + 1 << ' ' << r + 1 << '\n':
                                                            for (int j = i + 1; j < arr.size();</pre>
                                                                                                   28
                                                 16
                                                                                                                                                    31 }
                                                                                                              //頭到尾
                                                                 ++j)
                                                                                                                                                    32 | // 湊得某個價位的錢幣用量,有哪幾種可能性
1 int LCS(vector<string> Ans, vector<string>
                                                                                                                                                       void change(vector<int> price, int limit)
       num)
                                                                if (arr[j] > arr[i])
                                                 18
                                                                                                                                                    34
2
                                                 19
                                                                                                                                                           vector<int> c(limit + 1, 0);
       int N = Ans.size(), M = num.size();
                                                 20
                                                                    if (dp[i] + 1 > dp[j])
                                                                                                                                                           c[0] = true;
       vector<vector<int>> LCS(N + 1, vector
                                                 21
                                                                                                     2.9 Max subarray
                                                                                                                                                           for (int i = 0; i < price.size(); ++i)</pre>
            int>(M + 1, 0));
                                                                        dp[j] = dp[i] + 1;
                                                 22
                                                                                                                                                               for (int j = price[i]; j <= limit;</pre>
       for (int i = 1; i <= N; ++i)
                                                 23
                                                                        pos[j] = i;
                                                                                                                                                                   c[j] |= c[j-price[i]] << 1; //</pre>
                                                                                                   1 /*Kadane's algorithm*/
           for (int j = 1; j <= M; ++j)
                                                                                                                                                                        錢幣數量加一,每一種可能性都
                                                                                                     int maxSubArray(vector<int>& nums) {
               if (Ans[i - 1] == num[j - 1])
                                                                                                         int local max = nums[0], global max =
                                                            if (dp[i] > res)
                                                                                                                                                                        加一。
                                                 27
                   LCS[i][j] = LCS[i - 1][j -
                                                                                                               nums[0];
                       1] + 1;
                                                                                                         for(int i = 1; i < nums.size(); i++){</pre>
                                                                                                                                                           for (int i = 1; i <= 63; ++i)
                                                                res = dp[i];
                                                                                                                                                    41
                                                                                                              local max = max(nums[i],nums[i]+
               else
                                                                                                                                                               if (c[m] & (1 << i))
                                                                index = i;
                                                                                                                                                    42
                                                                                                                  _
local_max);
12
                   LCS[i][j] = max(LCS[i - 1][j]_{31}
                                                                                                                                                                   cout << "用" << i << "個錢幣可湊
                                                                                                                                                    43
                                                                                                              global max = max(local max,
                       ], LCS[i][j - 1]);
                                                 32
                                                                                                                                                                        得價位" << m;
                                                                                                                  global max);
13
                                                        cout << res << endl; // length
                                                                                                                                                    44 }
14
                                                        printLIS(arr, pos, index);
15
       cout << LCS[N][M] << '\n';</pre>
                                                                                                         return global max;
```

for (int i = 0; i < ans.size(); i++)</pre>

cout << ans[i];</pre>

36

//列印 LCS

int n = N, m = M;

3 Flow & matching

3.1 Dinic

```
1 const long long INF = 1LL<<60;</pre>
   struct Dinic { //O(VVE), with minimum cut
       static const int MAXN = 5003;
       struct Edge{
           int u, v;
           long long cap, rest;
       int n, m, s, t, d[MAXN], cur[MAXN];
       vector<Edge> edges:
       vector<int> G[MAXN];
10
       void init(){
12
           edges.clear();
13
           for ( int i = 0 ; i < n ; i++ ) G[i]
                ].clear();
           n = 0:
15
       // min cut start
16
       bool side[MAXN];
       void cut(int u) {
           side[u] = 1;
19
           for ( int i : G[u] ) {
20
               if ( !side[ edges[i].v ] &&
                    edges[i].rest )
               cut(edges[i].v);
22
23
24
25
       // min cut end
26
       int add node(){
27
           return n++;
28
29
       void add edge(int u, int v, long long
           edges.push_back( {u, v, cap, cap} );
           edges.push_back( {v, u, 0, 0LL} );
           m = edges.size();
32
33
           G[u].push_back(m-2);
           G[v].push_back(m-1);
34
35
36
       bool bfs(){
           fill(d,d+n,-1);
           queue<int> que;
           que.push(s); d[s]=0;
39
           while (!que.empty()){
               int u = que.front(); que.pop();
               for (int ei : G[u]){
                   Edge &e = edges[ei];
                   if (d[e.v] < 0 && e.rest >
                       d[e.v] = d[u] + 1;
                       que.push(e.v);
           return d[t] >= 0;
       long long dfs(int u, long long a){
           if ( u == t || a == 0 ) return a;
           long long flow = 0, f;
```

```
for ( int \&i=cur[u]; i < (int)G[u].
               size(); i++) {
               Edge &e = edges[ G[u][i] ];
               if ( d[u] + 1 != d[e.v] )
               f = dfs(e.v, min(a, e.rest) );
               if (f > 0) {
               e.rest -= f;
               edges[ G[u][i]^1 ].rest += f;
              flow += f;
              a -= f;
               if ( a == 0 ) break;
           return flow:
       long long maxflow(int s, int t){
          s = _s, t = _t;
           long long flow = 0, mf;
           while ( bfs() ){
               fill(cur,cur+n,0);
               while ( (mf = dfs(s, INF)) )
                   flow += mf:
           return flow:
78 } dinic;
```

3.2 Edmonds karp

56

57

59

60

61

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63

64

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66

67

68

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70

71

72

76

77

10

11

14

15

21

22

23

```
1 | /*Flow - Edmonds-karp*/
2 /*Based on UVa820*/
3 #define inf 1000000
4 int getMaxFlow(vector<vector<int>> &capacity
      , int s, int t, int n){
    int ans = 0:
    vector<vector<int>> residual(n+1, vector
         int>(n+1, 0)); //residual network
    while(true){
      vector<int> bottleneck(n+1, 0);
      bottleneck[s] = inf;
      queue<int> q;
      q.push(s);
      vector<int> pre(n+1, 0);
      while(!q.empty() && bottleneck[t] == 0){
       int cur = q.front();
        q.pop();
        for(int i = 1; i <= n; i++){
          if(bottleneck[i] == 0 && capacity[
               cur][i] > residual[cur][i]){
            q.push(i);
            pre[i] = cur;
            bottleneck[i] = min(bottleneck[cur 16
                 ], capacity[cur][i] - residual 17
                 [cur][i]);
      if(bottleneck[t] == 0) break;
      for(int cur = t; cur != s; cur = pre[cur 23
          residual[pre[cur]][cur] +=
               bottleneck[t];
```

```
residual[cur][pre[cur]] -=
                bottleneck[t];
28
                                                    29
       ans += bottleneck[t];
29
                                                    31
30
31
     return ans;
                                                    32
32
                                                    33 } graph;
   int main(){
34
     int testcase = 1;
     int n;
36
     while(cin>>n){
       if(n == 0)
       vector<vector<int>> capacitv(n+1, vector
            <int>(n+1, 0));
       int s, t, c;
                                                     1 /*bipartite - maximum matching*/
       cin >> s >> t >> c:
41
                                                     2 bool dfs(vector<vector<bool>> res,int node,
       int a, b, bandwidth;
       for(int i = 0 ; i < c ; ++i){</pre>
         cin >> a >> b >> bandwidth;
45
         capacity[a][b] += bandwidth;
         capacity[b][a] += bandwidth;
46
47
       cout << "Network " << testcase++ << endl</pre>
       cout << "The bandwidth is " <<
            getMaxFlow(capacity, s, t, n) << "."</pre>
       cout << endl;</pre>
50
                                                    1.1
51
                                                    12
52
     return 0;
                                                    13
                                                    14
```

3.3 hungarian

```
1 /*bipartite - hungarian*/
2 struct Graph{
       static const int MAXN = 5003;
       vector<int> G[MAXN];
       int n, match[MAXN], vis[MAXN];
       void init(int n){
           for (int i=0; i<n; i++) G[i].clear()</pre>
       bool dfs(int u){
               for (int v:G[u]){
               if (vis[v]) continue;
               vis[v]=true;
               if (match[v]==-1 || dfs(match[v
                   match[v] = u;
                   match[u] = v;
                   return true;
19
           return false:
20
22
       int solve(){
           int res = 0:
           memset(match,-1,sizeof(match));
           for (int i=0; i<n; i++){</pre>
25
```

if (match[i]==-1){

3.4 Maximum matching

vector<int>& x, vector<int>& y, vector<</pre>

return res;

memset(vis,0,sizeof(vis));

if (dfs(i)) res++;

```
bool> pass){
       for (int i = 0; i < res[0].size(); i++){</pre>
           if(res[node][i] && !pass[i]){
               pass[i] = true;
               if(y[i] == -1 \mid | dfs(res,y[i],x,
                    v,pass)){
                   x[node] = i;
                   y[i] = node;
                   return true;
           }
       return false:
  int main(){
15
       int n,m,1;
       while(cin>>n>>m>>l){
           vector<vector<bool>> res(n, vector<</pre>
                bool>(m, false));
           for (int i = 0; i < 1; i++){
               int a, b;
               cin >> a >> b;
               res[a][b] = true;
           int ans = 0;
           vector<int> x(n, -1);
           vector<int> y(n, -1);
           for (int i = 0; i < n; i++){
               vector<bool> pass(n, false);
               if(dfs(res,i,x,y,pass))
                   ans += 1;
           cout << ans << endl;</pre>
       return 0;
35
36
37 input:
38 4 3 5 //n matching m, 1 links
39 0 0
40 0 2
41 1 0
42 2 1
43 3 1
44 answer is 3
```

17

20

21

22

23

24

28

29

30

31

32

```
1 typedef long long 11;
2 struct MF
3
       static const int N = 5000 + 5:
       static const int M = 60000 + 5;
       static const 11 oo = 100000000000000L;
       int n, m, s, t, tot, tim;
       int first[N], next[M];
       int u[M], v[M], cur[N], vi[N];
       11 cap[M], flow[M], dis[N];
12
       int que[N + N];
13
       void Clear()
14
15
16
           tot = 0:
           tim = 0:
17
18
           for (int i = 1; i <= n; ++i)
               first[i] = -1:
19
20
21
       void Add(int from, int to, ll cp, ll flw
22
23
           u[tot] = from;
24
           v[tot] = to:
25
           cap[tot] = cp;
26
           flow[tot] = flw;
27
           next[tot] = first[u[tot]];
28
           first[u[tot]] = tot;
29
           ++tot:
30
       bool bfs()
31
32
33
           ++tim;
34
           dis[s] = 0;
35
           vi[s] = tim;
36
           int head, tail:
           head = tail = 1:
           que[head] = s;
           while (head <= tail)
               for (int i = first[que[head]]; i
                     != -1; i = next[i])
                   if (vi[v[i]] != tim && cap[i
                        ] > flow[i])
                        vi[v[i]] = tim;
                        dis[v[i]] = dis[que[head
                            ]] + 1;
                        que[++tail] = v[i];
                   }
               ++head:
           return vi[t] == tim:
       11 dfs(int x, 11 a)
           if (x == t || a == 0)
               return a;
           11 \text{ flw} = 0, f;
```

MFlow Model

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87

```
int &i = cur[x]:
           for (i = first[x]; i != -1; i = next
                                                 16
               if (dis[x] + 1 == dis[v[i]] && (
                   f = dfs(v[i], min(a, cap[i]
                   - flow[i]))) > 0)
                                                 19
                                                 20
                   flow[i] += f;
                   flow[i ^ 1] -= f;
                   a -= f;
                                                 21
                   flw += f:
                   if (a == 0)
                                                 22
                       break:
                                                 23
           return flw:
       11 MaxFlow(int s, int t)
           this->s = s;
           this->t = t:
           11 \text{ flw} = 0:
           while (bfs())
               for (int i = 1; i <= n; ++i)
                   cur[i] = 0;
               flw += dfs(s, oo);
           return flw;
88 };
                                                 11
89 // MF Net:
                                                 12
90 // Net.n = n;
                                                 13
91 // Net.Clear();
92 // a 到 b (注意從1開始!!!!)
                                                 15
93 // Net.Add(a, b, w, 0);
94 // Net.MaxFlow(s, d)
                                                 16
95 // s 到 d 的 MF
                                                 17
                                                 18
                                                 19
                                                 20
  4 Geometry
                                                 21
                                                 22
                                                 23
   4.1 Closest Pair
                                                 ^{24}
                                                 25
                                                 26
 1 | //最近點對 (距離) //台大
 vector<pair<double, double>> p;
                                                 27
3 double closest_pair(int 1, int r)
                                                 28
                                                 29
      // p 要對 x 軸做 sort
                                                 30
       if (1 == r)
                                                 31
           return 1e9;
                                                 32
       if (r - 1 == 1)
                                                 33
                                                34
           return dist(p[l], p[r]); // 兩點距離
                                                 35
       int m = (1 + r) >> 1;
                                                 36
       double d = min(closest pair(1, m),
                                                 37
           closest pair(m + 1, r));
       vector<int> vec:
                                                 38
       for (int i = m; i >= 1 && fabs(p[m].x -
                                                 39
                                                 40
           p[i].x) < d; --i)
```

vec.push back(i);

```
for (int i = m + 1; i <= r && fabs(p[m]. 42|
          x - p[i].x) < d; ++i)
          vec.push back(i);
     sort(vec.begin(), vec.end(), [&](int a,
                                                43
           { return p[a].y < p[b].y; });
     for (int i = 0: i < vec.size(): ++i)</pre>
          for (int j = i + 1; j < vec.size()</pre>
              && fabs(p[vec[j]].y - p[vec[i]]. 47
              v) < d; ++i)
              d = min(d, dist(p[vec[i]], p[vec 48
                   [j]]));
     return d;
                                                50
                                                51
 4.2 Line
1 template <typename T>
2 struct line
                                                57
     line() {}
     point<T> p1, p2;
     T a, b, c; //ax+by+c=0
     line(const point<T> &x, const point<T> &
          y) : p1(x), p2(y) {}
     void pton()
                                                62
     { //轉成一般式
                                                63
         a = p1.y - p2.y;
                                                64
         b = p2.x - p1.x;
         c = -a * p1.x - b * p1.y;
     T ori(const point<T> &p) const
     { //點和有向直線的關係, >0左邊、=0在線上
          return (p2 - p1).cross(p - p1);
                                                69
     T btw(const point<T> &p) const
                                                70
     { //點投影落在線段上<=0
         return (p1 - p).dot(p2 - p);
     bool point on segment(const point<T> &p)
           const
     { //點是否在線段上
                                                74
          return ori(p) == 0 && btw(p) <= 0;</pre>
     T dis2(const point<T> &p, bool
          is_segment = 0) const
     { //點跟直線/線段的距離平方
                                                79
          point < T > v = p2 - p1, v1 = p - p1;
          if (is segment)
                                                81
              point < T > v2 = p - p2:
              if (v.dot(v1) <= 0)</pre>
                                                82
                  return v1.abs2();
              if(v.dot(v2) >= 0)
                                                83
                  return v2.abs2();
                                                84
         T tmp = v.cross(v1):
                                                85
          return tmp * tmp / v.abs2();
                                                86
     T seg_dis2(const line<T> &1) const
```

{ //兩線段距離平方

```
return min({dis2(l.p1, 1), dis2(l.p2
        , 1), l.dis2(p1, 1), l.dis2(p2,
point<T> projection(const point<T> &p)
    const
{ //點對直線的投影
   point < T > n = (p2 - p1).normal();
   return p - n * (p - p1).dot(n) / n.
        abs2();
point<T> mirror(const point<T> &p) const
   //點對直線的鏡射,要先呼叫pton轉成一
        般式
   point<T> R:
   Td = a * a + b * b;
   R.x = (b * b * p.x - a * a * p.x - 2)
         * a * b * p.y - 2 * a * c) / d;
    R.v = (a * a * p.v - b * b * p.v - 2)
          * a * b * p.x - 2 * b * c) / d;
    return R:
bool equal(const line &1) const
{ //直線相等
   return ori(1.p1) == 0 && ori(1.p2)
        == 0:
bool parallel(const line &1) const
   return (p1 - p2).cross(l.p1 - l.p2)
        == 0;
bool cross seg(const line &1) const
    return (p2 - p1).cross(l.p1 - p1) *
        (p2 - p1).cross(1.p2 - p1) <= 0;
         //直線是否交線段
int line_intersect(const line &1) const
{ //直線相交情況·-1無限多點、1交於一
    點、0不相交
    return parallel(1) ? (ori(1.p1) == 0
         ? -1 : 0) : 1;
int seg_intersect(const line &1) const
   T c1 = ori(1.p1), c2 = ori(1.p2);
   T c3 = 1.ori(p1), c4 = 1.ori(p2);
   if (c1 == 0 && c2 == 0)
   { //共線
       bool b1 = btw(l.p1) \Rightarrow 0, b2 =
            btw(1.p2) >= 0;
       T = 3 = 1.btw(p1), a4 = 1.btw(p2)
       if (b1 && b2 && a3 == 0 && a4 >=
             0)
           return 2;
       if (b1 && b2 && a3 >= 0 && a4 ==
             0)
           return 3;
       if (b1 && b2 && a3 >= 0 && a4 >=
             0)
           return 0;
```

47

```
return -1; //無限交點
                                                 30
                                                         T cross(const point &b) const
                                                  31
           else if (c1 * c2 <= 0 && c3 * c4 <=
                                                  32
                                                                                                   29
                                                             return x * b.y - y * b.x;
                                                  33
               return 1;
                                                  34
                                                                                                   30
                                                         point normal() const
           return 0; //不相交
                                                  35
                                                                                                   31
92
                                                         { //求法向量
93
                                                  36
       point<T> line intersection(const line &l
                                                             return point(-y, x);
                                                                                                   32
94
            ) const
       { /*直線交點*/
                                                        T abs2() const
95
           point < T > a = p2 - p1, b = 1.p2 - 1.
                                                         { //向量長度的平方
                                                 40
                                                                                                   33
                p1, s = 1.p1 - p1;
                                                             return dot(*this);
                                                  41
                                                                                                   34
           //if(a.cross(b)==0)return INF;
                                                  42
           return p1 + a * (s.cross(b) / a.
                                                                                                   35
                                                        T rad(const point &b) const
98
                                                  43
                                                                                                   36
                cross(b));
                                                         { //兩向量的弧度
                                                             return fabs(atan2(fabs(cross(b)),
                                                                                                   37
100
       point<T> seg_intersection(const line &1)
                                                                  dot(b)));
                                                                                                   38
             const
                                                  46
                                                                                                   39
       { //線段交點
101
                                                  47
                                                        T getA() const
                                                                                                   40
           int res = seg intersect(1);
102
                                                                                //對x軸的弧度
                                                  48
           if (res <= 0)
103
                                                  49
                                                             T A = atan2(y, x); //超過180度會變負
104
               assert(0):
                                                                                                   42
105
           if (res == 2)
                                                  50
                                                             if (A <= -PI / 2)
106
               return p1;
                                                  51
                                                                 A += PI * 2:
           if (res == 3)
                                                                                                   43
107
                                                  52
                                                             return A;
108
               return p2;
                                                  53
           return line intersection(1):
                                                                                                   44
109
                                                                                                   45
110
111 };
                                                                                                   46
```

4.3 Point

```
1 template <typename T>
   struct point
3
      T x, y;
       point() {}
       point(const T &x, const T &y) : x(x), y(
       point operator+(const point &b) const
           return point(x + b.x, y + b.y);
                                                   11
                                                   12
       point operator-(const point &b) const
                                                  13
12
                                                  14
13
           return point(x - b.x, y - b.y);
                                                   15
14
                                                   16
       point operator*(const T &b) const
15
                                                   17
           return point(x * b, y * b);
                                                   18
                                                   19
       point operator/(const T &b) const
                                                  20
20
                                                  21
           return point(x / b, y / b);
                                                  22
22
                                                  23
23
       bool operator == (const point &b) const
24
                                                  24
25
           return x == b.x && y == b.y;
                                                  25
26
                                                  26
27
       T dot(const point &b) const
28
           return x * b.x + y * b.y;
```

4.4 Polygon

```
49
1 template <typename T>
                                               50
2 struct polygon
                                               51
                                               52
      polygon() {}
                                               53
     vector<point<T>> p: //逆時針順序
                                               54
     T area() const
                                               55
     { //面積
                                               56
          T ans = 0;
          for (int i = p.size() - 1, i = 0; i
              < (int)p.size(); i = j++)
              ans += p[i].cross(p[j]);
          return ans / 2;
                                               60
     point<T> center of mass() const
                                               61
      { //重心
                                               62
          T cx = 0, cy = 0, w = 0;
                                               63
          for (int i = p.size() - 1, j = 0; j
               < (int)p.size(); i = j++)
                                               64
             T = p[i].cross(p[i]);
              cx += (p[i].x + p[j].x) * a;
                                               66
              cy += (p[i].y + p[j].y) * a;
             w += a;
          return point\langle T \rangle (cx / 3 / w, cy / 3 / 67
               w);
                                                68
      char ahas(const point<T> &t) const
                                               69
      { //點是否在簡單多邊形內,是的話回傳1、
                                               70
           在邊上回傳-1、否則回傳0
          bool c = 0:
```

```
point on segment(t))
                                          74
            return -1;
        else if ((p[i].y > t.y) != (p[j
             1.y > t.y) &&
                 t.x < (p[j].x - p[i].x) 78
                       * (t.y - p[i].y) /
                       (p[j].y - p[i].y)
                     + p[i].x)
            c = !c:
    return c;
char point in convex(const point<T> &x)
    int l = 1, r = (int)p.size() - 2;
                                          83
    while (1 <= r)
   { //點是否在凸多邊形內,是的話回傳1
         、在邊上回傳-1、否則回傳0
        int mid = (1 + r) / 2;
       T a1 = (p[mid] - p[0]).cross(x - 87)
             p[0]);
       T = (p[mid + 1] - p[0]).cross 88
            (x - p[0]);
        if (a1 >= 0 && a2 <= 0)
            T res = (p[mid + 1] - p[mid
                ]).cross(x - p[mid]);
            return res > 0 ? 1 : (res >=
                 0 ? -1 : 0);
        else if (a1 < 0)
                                          95
           r = mid - 1;
        else
           l = mid + 1;
                                          97
    return 0;
vector<T> getA() const
{//凸包邊對x軸的夾角
    vector<T> res: //一定是遞增的
                                         100
    for (size_t i = 0; i < p.size(); ++i 101</pre>
                                         102
        res.push back((p[(i + 1) \% p.
             size()] - p[i]).getA());
                                         103
                                         104
bool line intersect(const vector<T> &A,
    const line<T> &1) const
                                         105
                                         106
    int f1 = upper_bound(A.begin(), A.
                                         107
        end(), (1.p1 - 1.p2).getA()) - A<sub>108</sub>
         .begin();
    int f2 = upper bound(A.begin(), A.
        end(), (1.p2 - 1.p1).getA()) - A<sup>109</sup>
         .begin();
   return 1.cross_seg(line<T>(p[f1], p[ 111
                                         112
        f2]));
                                         113
polygon cut(const line<T> &1) const
                                         114
                                        115
{ //凸包對直線切割,得到直線1左側的凸包
                                         116
    polygon ans:
                                         117
```

for (int i = 0, j = p.size() - 1; i 72

73

 $\langle p.size(); j = i++ \rangle$

if (line<T>(p[i], p[j]).

```
for (int n = p.size(), i = n - 1, j
                         = 0; j < n; i = j++)
                       if (l.ori(p[i]) >= 0)
                                  ans.p.push back(p[i]);
                                  if (1.ori(p[i]) < 0)</pre>
                                              ans.p.push_back(1.
                                                           line intersection(
                                                           line<T>(p[i], p[j]))
                       else if (l.ori(p[j]) > 0)
                                  ans.p.push back(1.
                                                line intersection(line<T
                                                >(p[i], p[j])));
           return ans;
static bool graham cmp(const point<T> &a
              , const point<T> &b)
{ //凸包排序函數 // 起始點不同
           // return (a.x < b.x) || (a.x == b.x) || (a.
                            && a.v < b.v); //最左下角開始
           return (a.y < b.y) || (a.y == b.y &&
                           a.x < b.x); //Y最小開始
void graham(vector<point<T>> &s)
{ //凸包 Convexhull 2D
           sort(s.begin(), s.end(), graham_cmp)
           p.resize(s.size() + 1);
           int m = 0;
           // cross >= 0 順時針。cross <= 0 逆
           for (size_t i = 0; i < s.size(); ++i</pre>
                       while (m >= 2 \&\& (p[m - 1] - p[m
                                        - 2]).cross(s[i] - p[m -
                                    2]) <= 0)
                                  --m;
                       p[m++] = s[i];
           for (int i = s.size() - 2, t = m +
                         1; i >= 0; --i)
                       while (m >= t && (p[m - 1] - p[m
                                        - 2]).cross(s[i] - p[m -
                                    2]) <= 0)
                                  --m:
                       p[m++] = s[i];
           if (s.size() > 1) // 重複頭一次需扣
                       --m;
           p.resize(m);
T diam()
{ // 直徑
           int n = p.size(), t = 1;
           T ans = 0:
           p.push_back(p[0]);
            for (int i = 0; i < n; i++)
```

```
triangle(const point<T> &a, const point< 15
118
119
                point \langle T \rangle now = p[i + 1] - p[i]; 171
                                                           static char sign(const point<T> &t)
                                                                                                                    T> &b, const point\langle T \rangle &c): a(a), b( 16
                while (now.cross(p[t + 1] - p[i 172
                                                                                                                    b), c(c) {}
                                                                                                                                                                           }
120
                     ]) > now.cross(p[t] - p[i]))173
                                                                return (t.y == 0 ? t.x : t.y) < 0;
                                                                                                               T area() const
                                                                                                                                                            18
                                                                                                                                                                       }
                    t = (t + 1) \% n;
121
                                                   174
                                                                                                                                                            19
                                                                                                                   T t = (b - a).cross(c - a) / 2;
122
                ans = max(ans, (p[i] - p[t]).
                                                   175
                                                           static bool angle cmp(const line<T> &A,
                                                                                                                                                            20
                     abs2()):
                                                                const line<T> &B)
                                                                                                                    return t > 0 ? t : -t:
                                                                                                                                                            21
                                                                                                                                                                   for(int i = 0: i < node: i++) //</pre>
                                                                                                        10
                                                                                                                                                                        negative cycle detection
123
                                                   176
124
            return p.pop back(), ans;
                                                   177
                                                                point < T > a = A.p2 - A.p1, b = B.p2 -
                                                                                                       12
                                                                                                               point<T> barycenter() const
                                                                                                                                                            22
                                                                                                                                                                       for(int j = 0; j < node; j++)</pre>
                                                                                                                                                                           if(dist[i] + edges[i][j] < dist[</pre>
125
                                                                                                                                                            23
                                                                                                               { //重心
126
       T min cover rectangle()
                                                                return sign(a) < sign(b) || (sign(a)</pre>
                                                   178
                                                                                                                                                                                j])
                                                                                                       14
                                                                                                                    return (a + b + c) / 3;
                                                                      == sign(b) && a.cross(b) > 0); 15
        { //最小覆蓋矩形
127
                                                                                                                                                            24
                                                                                                                                                                                cout<<"Negative cycle!"<<</pre>
            int n = p.size(), t = 1, r = 1, 1;
                                                   179
                                                                                                               point<T> circumcenter() const
                                                                                                                                                            25
128
            if (n < 3)
                                                   180
                                                           int halfplane intersection(vector<line<T</pre>
                                                                                                                                                                                     endl:
129
                                                                                                               { //外心
                                                                >> &s)
                                                                                                                                                            26
                                                                                                                                                                                return:
                return 0; //也可以做最小周長矩形
130
                                                                                                                   static line<T> u, v;
                                                                                                        18
                                                           { //半平面交
                                                                                                                                                            27
                                                   181
            T ans = 1e99:
                                                                                                                   u.p1 = (a + b) / 2;
131
                                                                                                                                                            28
                                                                sort(s.begin(), s.end(), angle\_cmp); 20
                                                   182
132
            p.push_back(p[0]);
                                                                                                                   u.p2 = point < T > (u.p1.x - a.y + b.y,
                                                                                                                                                              int main(){
                                                                                                                                                            29
133
            for (int i = 0; i < n; i++)
                                                                      //線段左側為該線段半平面
                                                                                                                        u.p1.y + a.x - b.x;
                                                                                                                                                                   int node:
                                                                                                                                                            30
                                                                int L, R, n = s.size();
                                                                                                                    v.p1 = (a + c) / 2;
134
                                                   183
                                                                                                        21
                                                                                                                                                                   cin>>node:
                point < T > now = p[i + 1] - p[i];
                                                               vector<point<T>> px(n);
                                                                                                                   v.p2 = point < T > (v.p1.x - a.y + c.y,
135
                                                  184
                                                                                                        22
                                                                                                                                                            32
                                                                                                                                                                   edges.resize(node, vector<int>(node, inf))
                while (now.cross(p[t + 1] - p[i 185])
                                                               vector<line<T>> q(n);
136
                                                                                                                        v.p1.y + a.x - c.x);
                     ]) > now.cross(p[t] - p[i]))186
                                                                q[L = R = 0] = s[0];
                                                                                                                    return u.line_intersection(v);
                                                                                                        23
                                                                                                                                                                   dist.resize(node.inf):
                                                                                                                                                            33
                                                                for (int i = 1; i < n; ++i)
137
                    t = (t + 1) \% n;
                                                                                                        24
                                                                                                                                                                   ancestor.resize(node,-1);
                                                                                                                                                            34
                while (now.dot(p[r + 1] - p[i]) <sub>188</sub>
                                                                                                               point<T> incenter() const
138
                                                                                                        ^{25}
                                                                                                                                                            35
                                                                                                                                                                   int a,b,d;
                     > now.dot(p[r] - p[i]))
                                                   189
                                                                    while (L < R \&\& s[i].ori(px[R -
                                                                                                               { //內心
                                                                                                        26
                                                                                                                                                                   while(cin>>a>>b>>d){
                    r = (r + 1) \% n;
                                                                        1]) <= 0)
139
                                                                                                                   T A = sqrt((b - c).abs2()), B = sqrt
                                                                                                                                                                       /*input: source destination weight*/
                if (!i)
140
                                                   190
                                                                        --R;
                                                                                                                        ((a - c).abs2()), C = sqrt((a -
                                                                                                                                                                       if(a == -1 \&\& b == -1 \&\& d == -1)
                                                                    while (L < R \&\& s[i].ori(px[L])
141
                    1 = r:
                                                   191
                                                                                                                        b).abs2()):
                                                                                                                                                                           break;
                while (now.dot(p[l + 1] - p[i])
142
                                                                         <= 0)
                                                                                                                    return point<T>(A * a.x + B * b.x +
                                                                                                        28
                                                                                                                                                                       edges[a][b] = d;
                     <= now.dot(p[1] - p[i]))
                                                   192
                                                                        ++L;
                                                                                                                        C * c.x, A * a.y + B * b.y + C *
                                                                                                                                                            41
                    1 = (1 + 1) \% n;
                                                                    q[++R] = s[i];
143
                                                   193
                                                                                                                         c.v) / (A + B + C);
                                                                                                                                                                   int start;
                                                                                                                                                            42
144
                T d = now.abs2();
                                                   194
                                                                    if (q[R].parallel(q[R - 1]))
                                                                                                        29
                                                                                                                                                                   cin>>start:
                                                                                                                                                            43
145
                T \text{ tmp} = \text{now.cross}(p[t] - p[i]) * 195
                                                                                                        30
                                                                                                               point<T> perpencenter() const
                                                                                                                                                                   BellmanFord(start, node);
                                                                                                                                                            44
                      (now.dot(p[r] - p[i]) - now_{196}
                                                                                                               { //垂心
                                                                                                                                                                   return 0;
                                                                                                                                                            45
                                                                        if (q[R].ori(s[i].p1) > 0)
                      .dot(p[l] - p[i])) / d;
                                                   197
                                                                                                        32
                                                                                                                    return barycenter() * 3 -
146
                ans = min(ans, tmp);
                                                   198
                                                                            q[R] = s[i];
                                                                                                                        circumcenter() * 2;
147
                                                   199
                                                                                                        33
                                                                    if (L < R)
148
            return p.pop_back(), ans;
                                                   200
                                                                                                        34 };
                                                                        px[R - 1] = q[R - 1].
149
                                                   201
                                                                                                                                                               5.2 BFS-queue
150
       T dis2(polygon &pl)
                                                                             line intersection(q[R]);
        { //凸包最近距離平方
151
                                                                while (L < R \&\& q[L].ori(px[R - 1])
            vector<point<T>> &P = p, &Q = pl.p;
152
                                                                                                                                                            1 /*BFS - queue version*/
                                                                    <= 0)
                                                                                                                Graph
            int n = P.size(), m = Q.size(), l =
153
                                                                                                                                                            void BFS(vector<int> &result, vector<pair</pre>
                                                                    --R;
                                                   204
                 0, r = 0;
                                                                                                                                                                    int, int>> edges, int node, int start)
                                                                p.clear();
            for (int i = 0; i < n; ++i)</pre>
                                                   205
154
                                                   206
                                                                if (R - L <= 1)
155
                if (P[i].y < P[1].y)</pre>
                                                                                                           5.1 Bellman-Ford
                                                                                                                                                                   vector<int> pass(node, 0);
                                                                    return 0;
156
                                                   207
                    1 = i:
                                                                                                                                                                   queue<int> q;
            for (int i = 0; i < m; ++i)</pre>
                                                   208
                                                                px[R] = q[R].line intersection(q[L])
157
                                                                                                                                                                   queue<int> p;
                if (Q[i].y < Q[r].y)</pre>
158
                                                                                                         1 /*SPA - Bellman-Ford*/
                                                                                                                                                                   q.push(start);
                                                                for (int i = L; i \leftarrow R; ++i)
159
                    r = i;
                                                                                                         2 #define inf 99999 //define by you maximum
                                                                                                                                                                   int count = 1;
                                                                    p.push back(px[i]);
            P.push_back(P[0]), Q.push_back(Q[0])
                                                   210
160
                                                                                                                edges weight
                                                                                                                                                                   vector<pair<int, int>> newedges;
                                                                return R - L + 1;
                                                   211
                                                                                                                                                                   while (!q.empty())
                                                                                                         3 vector<vector<int> > edges;
                                                                                                                                                            10
                                                   212
161
            T ans = 1e99;
                                                                                                         4 vector<int> dist;
                                                                                                                                                            11
                                                   213 };
162
            for (int i = 0; i < n; ++i)
                                                                                                         5 vector<int> ancestor;
                                                                                                                                                            12
                                                                                                                                                                       pass[q.front()] = 1;
163
                                                                                                                                                                       for (int i = 0; i < edges.size(); i</pre>
                                                                                                         6 | void BellmanFord(int start, int node){
                                                                                                                                                            13
                while ((P[1] - P[1 + 1]).cross(Q
164
                                                                                                               dist[start] = 0;
                                                                                                                                                                             ++)
                     [r + 1] - Q[r] < 0
                                                                                                               for(int it = 0; it < node-1; it++){</pre>
                    r = (r + 1) \% m;
165
                                                       4.5 Triangle
                                                                                                                    for(int i = 0; i < node; i++){</pre>
                                                                                                                                                                           if (edges[i].first == q.front()
                ans = min(ans, line<T>(P[1], P[1
166
                                                                                                                        for(int j = 0; j < node; j++){</pre>
                                                                                                                                                                                 && pass[edges[i].second] ==
                      + 1]).seg dis2(line<T>(Q[r
                                                                                                        11
                                                                                                                            if(edges[i][j] != -1){
                     ], Q[r + 1])));
                                                     1 template <typename T>
                                                                                                        12
                                                                                                                                if(dist[i] + edges[i][j] 16
167
                l = (l + 1) \% n;
                                                     2 struct triangle
                                                                                                                                      < dist[j]){
                                                                                                                                                                                p.push(edges[i].second);
168
                                                     3 | {
                                                                                                        13
                                                                                                                                     dist[i] = dist[i] +
                                                                                                                                                                                result[edges[i].second] =
            return P.pop_back(), Q.pop_back(),
                                                           point<T> a, b, c;
                                                                                                                                          edges[i][j];
                                                                                                                                                                                     count;
                 ans;
                                                           triangle() {}
                                                                                                                                     ancestor[j] = i;
```

```
else if (edges[i].second == q.
                                                             else if((*iter).first.second ==
                                                                                                    32 // weight[a - 1].push back(pii(b - 1, w));
                                                                                                                                                                     break:
                                                                  start && (*iter).second == 0 && 33 // weight[b - 1].push back(pii(a - 1, w));
                    front() && pass[edges[i].
                                                                                                                                                                 distance[a][b] = d;
                                                                                                                                                      ^{24}
                                                                  pass[(*iter).first.first] == 0){ 34 // dist.resize(n, inf);
                    first] == 0)
                                                                                                                                                      25
                                                                                                                                                                 ancestor[a][b] = a;
                                                                 route.push back((*iter).first.
                                                                                                   35 // ancestor.resize(n, -1);
                                                                                                                                                      26
                   p.push(edges[i].first);
                                                                                                    36 // dist[0] = 0;
                                                                                                                                                      27
                                                                                                                                                             for (int i = 0; i < n; i++)
                   result[edges[i].first] =
                                                                 DFS((*iter).first.first);
                                                                                                    37 // dijkstra(0);
                                                                                                                                                                 distance[i][i] = 0;
                        count:
                                                  16
                                                                                                                                                             floyd warshall(distance, ancestor, n);
                                                                                                                                                             /*Negative cycle detection*/
                                                  17
                                                                                                                                                             for (int i = 0; i < n; i++){
               else
                                                  18
                                                                                                       5.5 Euler circuit
                   newedges.push_back(edges[i])
                                                 19 int main(){
                                                                                                                                                                 if(distance[i][i] < 0){</pre>
                                                  20
                                                         int node;
                                                                                                                                                                     cout << "Negative cycle!" <<</pre>
                                                         cin>>node:
                                                 21
           edges = newedges;
                                                         pass.resize(node,0);
                                                                                                     1 /* Euler circuit*/
                                                                                                                                                                     break;
                                                  22
                                                                                                                                                      34
                                                                                                     2 /*From NTU kiseki*/
           newedges.clear():
                                                         int a.b:
                                                                                                                                                      35
           q.pop();
                                                  24
                                                         while(cin>>a>>b){
                                                                                                     3 /*G is graph, vis is visited, la is path*/
                                                                                                                                                      36
           if (q.empty() == true)
                                                  25
                                                             if(a == -1 \&\& b == -1)
                                                                                                     4 bool vis[ N ]; size t la[ K ];
                                                                                                                                                      37
                                                                                                                                                             return 0;
32
                                                                                                      void dfs( int u, vector< int >& vec ) {
                                                  26
33
                                                 27
                                                             edges.insert(pair<pair<int,int>,int
                                                                                                           while ( la[ u ] < G[ u ].size() ) {</pre>
               q = p;
                                                                  >(pair<int,int>(a,b),0));
                                                                                                               if( vis[ G[ u ][ la[ u ] ].second ]
34
               queue<int> tmp;
               p = tmp;
                                                 28
                                                                                                                   ) {
                                                                                                                                                         5.7 Hamilton cycle
36
               count++;
                                                 29
                                                         int start;
                                                                                                               ++ la[ u ];
                                                         cin>>start:
37
                                                 30
                                                                                                               continue;
38
                                                 31
                                                         route.push back(start);
                                                                                                    10
39
                                                  32
                                                         DFS(start);
                                                                                                    11
                                                                                                           int v = G[ u ][ la[ u ] ].first;
                                                                                                                                                       1 /*find hamilton cycle*/
   int main()
                                                                                                           vis[ G[ u ][ la[ u ] ].second ] = true;
                                                                                                                                                       void hamilton(vector<vector<int>> gp, int k,
40
                                                  33
                                                         return 0;
                                                                                                    12
                                                  34 }
                                                                                                    13
                                                                                                           ++ la[ u ]; dfs( v, vec );
                                                                                                                                                               int cur, vector<int>& solution, vector<</pre>
41
                                                                                                    14
                                                                                                           vec.push back( v );
                                                                                                                                                              bool> pass,bool& flag){
42
       int node;
       cin >> node:
                                                                                                    15
                                                                                                                                                             if(k == gp.size()-1){
       vector<pair<int, int>> edges;
                                                                                                                                                                 if(gp[cur][1] == 1){
44
                                                     5.4 Dijkstra
45
       int a, b;
                                                                                                                                                                     cout << 1 << " ";
       while (cin >> a >> b)
                                                                                                                                                                     while(cur != 1){
                                                                                                                                                                         cout << cur << " ";
                                                                                                       5.6 Floyd-warshall
           /*a = b = -1 means input edges ended 1 /*SPA - Diikstra*/
                                                                                                                                                                         cur = solution[cur]:
                                                   _{2} const int MAXN = 1e5 + 3;
           if (a == -1 && b == -1)
                                                  3 const int inf = INT_MAX;
                                                                                                                                                                     cout << cur << endl;</pre>
                                                   4 typedef pair<int, int> pii;
                                                                                                     1 /*SPA - Floyd-Warshall*/
                                                                                                                                                                     flag = true;
               break;
                                                                                                                                                      11
           edges.push_back(pair<int, int>(a, b)
                                                  5 vector<vector<pii>>> weight;
                                                                                                     2 #define inf 99999
                                                                                                                                                      12
                                                                                                                                                                     return;
                                                   6 vector<int> isDone(MAXN, false), dist,
                                                                                                     3 void floyd_warshall(vector<vector<int>>&
                                                                                                                                                      13
52
                                                          ancestor:
                                                                                                            distance, vector<vector<int>>& ancestor, 14
53
       vector<int> result(node, -1);
                                                     void dijkstra(int s)
                                                                                                                                                             for (int i = 0; i < gp[cur].size() && !</pre>
       BFS(result, edges, node, 0);
                                                                                                           for (int k = 0; k < n; k++){
                                                                                                                                                                  flag; i++){
54
55
                                                         priority queue<pii, vector<pii>, greater
                                                                                                               for (int i = 0; i < n; i++){
                                                                                                                                                                 if(gp[cur][i] == 1 && !pass[i]){
                                                              <pii>>> pq;
                                                                                                                   for (int j = 0; j < n; j++){
56
       return 0;
                                                                                                                                                                     pass[i] = true;
                                                         pq.push(pii(0, s));
                                                                                                                       if(distance[i][k] + distance 18
                                                                                                                                                                     solution[i] = cur;
                                                  10
                                                                                                                                                                     hamilton(gp, k + 1, i, solution,
                                                         ancestor[s] = -1;
                                                  11
                                                                                                                            [k][j] < distance[i][j]) 19
                                                  12
                                                         while (!pq.empty())
                                                                                                                                                                           pass, flag);
                                                  13
                                                                                                                           distance[i][j] =
                                                                                                                                                                     pass[i] = false;
  5.3 DFS-rec
                                                  14
                                                             int u = pq.top().second;
                                                                                                                                distance[i][k] +
                                                                                                                                                      21
                                                                                                                                distance[k][j];
                                                  15
                                                             pq.pop();
                                                                                                                                                      22
                                                  16
                                                                                                                           ancestor[i][j] =
                                                                                                                                                      23
1 /*DFS - Recursive version*/
                                                             isDone[u] = true;
                                                                                                                                ancestor[k][j];
                                                                                                                                                      24 int main(){
                                                  17
2 map<pair<int,int>,int> edges;
                                                                                                                                                      25
                                                                                                                                                             int n;
3 vector<int> pass;
                                                             for (auto &pr : weight[u])
                                                                                                                   }
                                                                                                                                                      26
                                                                                                                                                             while(cin>>n){
                                                  19
4 vector<int> route;
                                                  20
                                                                                                                                                      27
                                                                                                                                                                 int a,b;
5 void DFS(int start){
                                                  21
                                                                 int v = pr.first, w = pr.second; 13
                                                                                                                                                      28
                                                                                                                                                                 bool end = false;
                                                                                                                                                                 vector<vector<int>> gp(n+1,vector<</pre>
       pass[start] = 1;
       map<pair<int,int>,int>::iterator iter;
                                                                 if (!isDone[v] && dist[u] + w <</pre>
                                                                                                   15 int main(){
                                                                                                                                                                      int>(n+1,0));
                                                                      dist[v])
       for(iter = edges.begin(); iter != edges.
                                                                                                           int n:
                                                                                                                                                                 while(cin>>a>>b){
                                                                                                                                                                     if(a == 0 && b == 0)
            end(); iter++){
                                                                                                           cin >> n;
                                                                                                                                                      31
           if((*iter).first.first == start &&
                                                                     dist[v] = dist[u] + w;
                                                                                                           int a, b, d;
                                                                                                                                                      32
                                                                                                                                                                         break:
                (*iter).second == 0 && pass[(*
                                                                     pq.push(pii(dist[v], v));
                                                                                                           vector<vector<int>> distance(n, vector
                                                                                                                                                                     gp[a][b] = 1;
                iter).first.second] == 0){
                                                  27
                                                                     ancestor[v] = u;
                                                                                                                int>(n,99999));
                                                                                                                                                                     gp[b][a] = 1;
               route.push back((*iter).first.
                                                                                                           vector<vector<int>> ancestor(n, vector
                    second);
                                                  29
                                                                                                                int>(n,-1));
                                                                                                                                                      36
                                                                                                                                                                 vector<int> solution(n + 1, -1);
               DFS((*iter).first.second);
                                                                                                           while(cin>>a>>b>>d){
                                                                                                                                                                 vector<bool> pass(n + 1, false);
                                                  30
                                                                                                    21
                                                                                                               if(a == -1 \&\& b == -1 \&\& d == -1)
                                                                                                                                                                 solution[1] = 0;
```

```
pass[1] = true;
                                                                                                                              tmp.weight = gp[cur.to][28]
                                                                                                                                                                vector<int> union set(node, 0);
                                                          if(edge < n-1)
           bool flag = false;
                                                                                                                                                                vector<int> rank(node, 0);
                                                                                                                                   il;
                                                                                                                                                                for (int i = 0; i < node; i++)
           hamilton(gp, 1,1 ,solution,pass,flag 39
                                                              cout << "No mst" << endl;</pre>
                                                                                                                              pq.push(tmp);
                                                                                                      36
                                                                                                                                                                    union set[i] = i;
                                                                                                      37
                                                                                                                                                         31
           if(!flag)
                                                              cout << cost << endl;</pre>
                                                   41
                                                                                                      38
               cout << "N" << endl;</pre>
                                                                                                                      pass[cur.to] = true;
                                                                                                                                                                cin >> edge; //Input Edge number
                                                  42 }
                                                                                                      39
44
                                                   43 int main(){
                                                                                                      40
                                                                                                                      edge += 1:
                                                                                                                                                                for (int i = 0; i < edge; i++)
       return 0;
                                                          int n;
                                                                                                                      cost += cur.weight;
                                                                                                                                                         35
45
                                                   44
                                                                                                      41
46
                                                   45
                                                          cin >> n;
                                                                                                      42
                                                                                                                                                         36
                                                                                                                                                                    int a, b;
                                                          int a, b, d;
                                                                                                                                                         37
                                                                                                                                                                    cin >> a >> b;
47
                                                   46
                                                                                                      43
48 4
                                                   47
                                                          priority queue<edges> pq;
                                                                                                      44
                                                                                                             if(edge < n-1)
                                                                                                                                                         38
                                                                                                                                                                    merge(a, b, union_set, rank);
                                                          while(cin>>a>>b>>d){
                                                                                                                 cout << "No mst" << endl:
                                                   48
                                                                                                      45
                                                                                                                                                         39
                                                              if(a == -1 \&\& b == -1 \&\& d == -1)
                                                                                                                                                                /*build party*/
                                                   49
                                                                                                      46
                                                                                                                                                         40
                                                                                                                                                                vector<vector<int>> party(node, vector
                                                   50
                                                                                                      47
                                                                                                                 cout << cost << endl:
                                                  51
                                                              edges tmp:
                                                                                                      48 }
                                                                                                                                                                     int>(0));
53 3 1
                                                  52
                                                              tmp.from = a;
                                                                                                      49 int main(){
                                                                                                                                                                for (int i = 0; i < node; i++)</pre>
54 0 0
                                                   53
                                                              tmp.to = b:
                                                                                                             int n:
                                                                                                                                                                    party[find(i, union set)].push back(
                                                                                                      50
55 output: 1 3 4 2 1
                                                  54
                                                              tmp.weight = d;
                                                                                                      51
                                                                                                             cin >> n;
                                                                                                             int a, b, d;
                                                   55
                                                              pq.push(tmp);
                                                                                                      52
                                                                                                             vector<vector<int>> gp(n,vector<int>(n,
                                                   56
                                                   57
                                                          kruskal(pq, n);
                                                          return 0:
                                                                                                             while(cin>>a>>b>>d){
                                                                                                      54
   5.8 Kruskal
                                                                                                      55
                                                                                                                 if(a == -1 \&\& b == -1 \&\& d == -1)
                                                                                                                                                                 Mathematics
                                                                                                      56
                                                                                                                     break:
                                                                                                                 if(gp[a][b] > d)
                                                                                                      57
1 /*mst - Kruskal*/
                                                                                                      58
                                                                                                                     gp[a][b] = d;
                                                                                                                                                            6.1 Catalan
  struct edges{
                                                                                                      59
                                                      5.9 Prim
       int from:
                                                                                                      60
                                                                                                             Prim(gp,n,0);
       int to;
                                                                                                      61
                                                                                                             return 0;
                                                                                                                                                            Catalan number
       int weight;
       friend bool operator < (edges a, edges b 1 /*mst - Prim*/
                                                                                                                                                              • 0~19項的catalan number
                                                    2 #define inf 99999
                                                                                                                                                                0 1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 16796, 58786,
           return a.weight > b.weight;
                                                   3 struct edges{
                                                                                                         5.10 Union find
                                                          int from;
                                                                                                                                                                  208012, 742900, 2674440, 9694845, 35357670, 129644790
9
                                                          int to;
   };
                                                                                                                                                                  477638700, 1767263190
   int find(int x, vector < int > & union set){
                                                          int weight;
                                                                                                                                                               • 公式: C_n = \frac{1}{n+1} {2n \choose n} = \frac{(2n)!}{(n+1)!n!}
       if(x != union_set[x])
                                                          friend bool operator < (edges a, edges b
                                                                                                       1 int find(int x, vector<int> &union_set)
           union_set[x] = find(union_set[x],
                union set);
                                                              return a.weight > b.weight;
                                                                                                             if (union_set[x] != x)
       return union_set[x];
                                                                                                                 union_set[x] = find(union_set[x],
                                                                                                                      union set); //compress path
14 }
                                                   10 };
                                                                                                                                                            6.2 Combination
                                                   11 void Prim(vector<vector<int>> gp,int n,int
void merge(int a,int b,vector<int>&
                                                                                                             return union set[x];
       union set){
                                                           start){
       int pa = find(a, union_set);
                                                          vector<bool> pass(n, false);
                                                                                                         void merge(int x, int y, vector<int> &
                                                                                                                                                          1 /*input type string or vector*/
       int pb = find(b, union_set);
                                                          int edge = 0;
                                                                                                              union_set, vector<int> &rank)
                                                   13
                                                                                                                                                          2 for (int i = 0; i < (1 << input.size()); ++i</pre>
                                                          int cost = 0; //evaluate cost of mst
       if(pa != pb)
           union set[pa] = pb;
                                                          priority_queue<edges> pq;
                                                                                                             int rx, ry;
19
                                                          for (int i = 0; i < n; i++){
                                                                                                             rx = find(x, union_set);
20 }
                                                   16
                                                                                                                                                                string testCase = "";
   void kruskal(priority_queue<edges> pq,int n)
                                                              if(gp[start][i] != inf){
                                                                                                             ry = find(y, union_set);
                                                                                                                                                                for (int j = 0; j < input.size(); ++j)</pre>
                                                                  edges tmp;
                                                                                                             if (rx == ry)
                                                                                                                                                                    if (i & (1 << j))
       vector<int> union_set(n, 0);
                                                                  tmp.from = start;
                                                   19
                                                                                                                                                                         testCase += input[j];
       for (int i = 0; i < n; i++)
                                                                                                             /*merge by rank -> always merge small
                                                   20
                                                                  tmp.to = i;
           union set[i] = i;
                                                                  tmp.weight = gp[start][i];
                                                                                                                  tree to big tree*/
       int edge = 0;
                                                                  pq.push(tmp);
                                                                                                             if (rank[rx] > rank[ry])
       int cost = 0; //evaluate cost of mst
                                                   23
                                                                                                      16
                                                                                                                 union set[ry] = rx;
       while(!pq.empty() && edge < n - 1){</pre>
                                                   24
                                                                                                      17
                                                                                                                                                            6.3 Extended Euclidean
           edges cur = pq.top();
                                                          pass[start] = true;
                                                                                                      18
           int from = find(cur.from, union set)
                                                          while(!pq.empty() && edge < n-1){</pre>
                                                                                                      19
                                                                                                                 union set[rx] = ry;
```

20

21

22

23 }

25 | {

26

24 int main()

if (rank[rx] == rank[ry])

cin >> node; //Input Node number

1 // ax + by = gcd(a,b)

if (b == 0)

a, long long b)

return {1, 0};

long long k = a / b;

pair<long long, long long> extgcd(long long

++rank[ry];

edges cur = pq.top();

for (int i = 0; i < n; i++){

edges tmp;

tmp.to = i;

if(gp[cur.to][i] != inf){

tmp.from = cur.to;

if(!pass[cur.to]){

pq.pop();

29

30

31

32

33

int to = find(cur.to, union set);

cost += cur.weight;

merge(from, to, union_set);

if(from != to){

pq.pop();

edge += 1;

```
pair<long long, long long> p = extgcd(b,
             a - k * b;
       //cout << p.first << " " << p.second <<
       //cout << "商數(k)= " << k << endl <<
       return {p.second, p.first - k * p.second
11
12
   int main()
       int a, b;
       cin >> a >> b;
       pair<long long, long long> xy = extgcd(a
            , b); //(x0,y0)
       cout << xy.first << " " << xy.second <<
       cout << xy.first << " * " << a << " + "
            << xy.second << " * " << b << endl;
       return 0;
20
21
   // ax + by = gcd(a,b) * r
   /*find |x|+|y| \rightarrow min*/
   int main()
25
       long long r, p, q; /*px+qy = r*/
27
       int cases;
28
       cin >> cases;
       while (cases--)
30
31
           cin >> r >> p >> q;
           pair<long long, long long> xy =
32
                extgcd(q, p); //(x0,y0)
           long long ans = 0, tmp = 0;
           double k, k1;
           long long s, s1;
           k = 1 - (double)(r * xy.first) / p;
           s = round(k);
           ans = llabs(r * xy.first + s * p) +
                llabs(r * xy.second - s * q);
           k1 = -(double)(r * xy.first) / p;
           s1 = round(k1);
           /*cout << k << endl << k1 << endl;
               cout << s << endl << s1 << endl;</pre>
42
           tmp = llabs(r * xy.first + s1 * p) +
                 llabs(r * xy.second - s1 * q);
           ans = min(ans, tmp);
45
           cout << ans << endl;</pre>
47
48
       return 0;
```

6.4 Fermat

• $a^{(p-1)} \equiv 1 \pmod{p} \iff a * a^{(p-2)} \equiv 1$ $a^{(p-2)} \equiv 1/a$

- 同餘因數定理
 - $\circ \ a \equiv b \pmod{p} \iff k|a-b|$
- 同餘加法性質
 - $\circ \ a \equiv b \pmod{p}$ and $c \equiv d \pmod{p}$ $\langle = \rangle a + c \equiv b + d \pmod{p}$
- 同餘相乘性質
 - $\circ \ a \equiv b \pmod{p}$ and $c \equiv d \pmod{p}$ $\langle = \rangle \ ac \equiv bd \ (mod \ p)$
- 同餘次方件質
 - $\circ a \equiv b \pmod{p} \iff a^n \equiv b^n \pmod{p}$
- 同餘倍方件質
 - $\circ \ a \equiv b \pmod{p} \iff am \equiv bm \pmod{p}$

6.5 Hex to Dec

13

14

15

17 18

24

27 }

```
1 int HextoDec(string num) //16 to 10
       int base = 1;
       int temp = 0;
       for (int i = num.length() - 1; i >= 0; i
           if (num[i] >= '0' && num[i] <= '9')</pre>
               temp += (num[i] - 48) * base;
               base = base * 16;
           else if (num[i] >= 'A' && num[i] <=</pre>
               temp += (num[i] - 55) * base;
               base = base * 16;
16
       return temp;
                                                   13
19 }
                                                   14
20 void DecToHex(int p) //10 to 16
                                                   15
21
                                                   16
22
       char *1 = new (char);
                                                   17
       sprintf(l, "%X", p);
23
                                                   18 }
       //int l_intResult = stoi(1);
       cout << 1 << "\n";
25
26
       //return l_intResult;
```

6.6 Log

```
1 double mylog(double a, double base)
     //a 的對數底數 b = 自然對數 (a) / 自然對
          數 (b)。
     return log(a) / log(base);
```

6.7 Mod

```
1 int pow mod(int a, int n, int m) // a ^ n
       mod m;
                                   // a, n, m
       < 10 ^ 9
      if (n == 0)
          return 1;
      int x = pow mid(a, n / 2, m);
      long long ans = (long long)x * x % m;
      if (n % 2 == 1)
          ans = ans * a % m;
      return (int)ans;
int inv(int a, int n, int p) // n = p-2
      long long res = 1;
      for (; n; n >>= 1, (a *= a) %= p)
          if (n & 1)
              (res *= a) %= p;
      return res;
```

6.8 Mod 性質

```
加法: (a+b) \mod p = (a \mod p + b \mod p) \mod p
減法: (a-b) \mod p = (a \mod p - b \mod p + p) \mod p
乘法: (a * b) \mod p = (a \mod p \cdot b \mod p) \mod p
次方: (a^b) \mod p = ((a \mod p)^b) \mod p
加法結合律: ((a+b) \mod p + c) \mod p = (a+(b+c)) \mod p
乘法結合律: ((a \cdot b) \mod p \cdot c) \mod p = (a \cdot (b \cdot c)) \mod p
加法交換律: (a+b) \mod p = (b+a) \mod p
乘法交換律: (a \cdot b) \mod p = (b \cdot a) \mod p
結合律: ((a+b) \bmod p \cdot c) = ((a \cdot c) \bmod p + (b \cdot c) \bmod p) \bmod p
如果 a \equiv b \pmod{m} · 我們會說 a, b 在模 m 下同餘
以下為性質·
 • 整除性: a \equiv b \pmod{m} \Rightarrow c \cdot m = a - b, c \in \mathbb{Z}
           \Rightarrow a \equiv b \pmod{m} \Rightarrow m \mid a - b
 • 源移性: 若a \equiv b \pmod{c}, b \equiv d \pmod{c}
             則 a \equiv d \pmod{c}

    保持基本運算:

        \int a \equiv b \pmod{m} \xrightarrow{} \int a \pm c \equiv b \pm d \pmod{m}
        c \equiv d \pmod{m} \Rightarrow a \cdot c \equiv b \cdot d \pmod{m}

    放大縮小模數:

     k \in \mathbb{Z}^+, a \equiv b \pmod{m} \Leftrightarrow k \cdot a \equiv k \cdot b \pmod{k \cdot m}
 模逆元是取模下的反元素、即為找到 a^{-1} 使得 aa^{-1} \equiv 1 \mod c
 整數 a \in \text{mod } c 下要有模反元素的充分必要條件為 a, c 互質
 模逆元如果存在會有無限個,任意兩相鄰模逆元相差 c
 費馬小定理
給定一個質數 p 及一個整數 a · 那麼 : a^p \equiv a \pmod{p} 如果 \gcd(a,p) = 1 · 則 :
a^{p-1} \equiv 1 \pmod{p}
 歐拉定理
 歐拉定理是比較 general 版本的費馬小定理。給定兩個整數 n 和 a · 如果 gcd(a,n)=1 · 貝
a^{\Phi(n)} \equiv 1 \pmod{n} 如果 n 是質數 \Phi(n) = n - 1 · 也就是費馬小定理
```

Wilson's theorem

給定一個質數 $p \cdot \mathbb{H} : (p-1)! \equiv -1 \pmod{p}$

6.9 PI

```
1 #define PI acos(-1)
2 #define PI M PI
3 const double PI = atan2(0.0, -1.0);
```

6.10 Prime table

```
1 const int maxn = sqrt(INT MAX);
```

```
2 vector<int> p;
3 bitset<maxn> is notp;
   void PrimeTable()
       is notp.reset();
       is notp[0] = is notp[1] = 1;
       for (int i = 2; i <= maxn; ++i)</pre>
           if (!is notp[i])
               p.push_back(i);
           for (int j = 0; j < (int)p.size();</pre>
12
               if (i * p[j] > maxn)
                    break;
               is_notp[i * p[j]] = 1;
               if (i % p[j] == 0)
18
                    break;
19
20
```

6.11 Prime 判斷

```
ı // n < 4759123141
                         chk = [2, 7, 61]
2 // n < 1122004669633 chk = [2, 13, 23,
       1662803]
  // n < 2^64
                         chk = [2, 325, 9375,
       28178, 450775, 9780504, 1795265022]
4 vector<long long> chk = {};
  long long fmul(long long a, long long n,
       long long mod)
      long long ret = 0;
       for (; n; n >>= 1)
           if (n & 1)
               (ret += a) %= mod;
           (a += a) \% = mod;
       return ret;
15
   long long fpow(long long a, long long n,
       long long mod)
      long long ret = 1LL;
       for (; n; n >>= 1)
           if (n & 1)
               ret = fmul(ret, a, mod);
           a = fmul(a, a, mod);
26
       return ret;
27
   bool check(long long a, long long u, long
       long n, int t)
29
30
      a = fpow(a, u, n);
       if (a == 0)
           return true;
       if (a == 1 || a == n - 1)
           return true;
```

```
for (int i = 0; i < t; ++i)
36
            a = fmul(a, a, n);
37
38
            if (a == 1)
               return false;
39
           if (a == n - 1)
40
41
               return true:
42
43
       return false;
44 }
45 bool is prime(long long n)
46
47
       if (n < 2)
48
           return false:
49
       if (n % 2 == 0)
           return n == 2;
50
       long long u = n - 1:
51
52
       int t = 0;
       for (; u & 1; u >>= 1, ++t)
53
54
55
       for (long long i : chk)
56
57
            if (!check(i, u, n, t))
               return false;
58
59
60
       return true;
61
63 // if (is_prime(int num)) // true == prime
```

6.12 Round(小數)

```
double myround(double number, unsigned int
   bits)

{
   LL integerPart = number;
   number -= integerPart;
   for (unsigned int i = 0; i < bits; ++i)
        number *= 10;
   number = (LL)(number + 0.5);
   for (unsigned int i = 0; i < bits; ++i)
        number /= 10;
   return integerPart + number;

//printf("%.1f\n", round(3.4515239, 1));</pre>
```

6.13 二分逼近法

```
11 R = M;
12 }
13 printf("%.31f\n", R);
14 }
```

6.14 公式

```
S_n = \frac{a(1-r^n)}{1-r} \quad a_n = \frac{a_1 + a_n}{2} \quad \sum_{k=1}^n k = \frac{n(n+1)}{2}\sum_{k=1}^n k^2 = \frac{n(n+1)(2n+1)}{6} \sum_{k=1}^n k^3 = \left[\frac{n(n+1)}{2}\right]^2
```

6.15 四則運算

1 string s = ""; //開頭是負號要補0

```
2 long long int DFS(int le, int ri) // (0,
       string final index)
       int c = 0;
       for (int i = ri; i >= le; i--)
          if (s[i] == ')')
              C++;
          if (s[i] == '(')
           if (s[i] == '+' && c == 0)
               return DFS(le, i - 1) + DFS(i +
                   1, ri);
           if (s[i] == '-' && c == 0)
14
               return DFS(le, i - 1) - DFS(i +
                   1, ri);
       for (int i = ri; i >= le; i--)
16
           if (s[i] == ')')
              c++:
          if (s[i] == '(')
21
           if (s[i] == '*' && c == 0)
               return DFS(le, i - 1) * DFS(i +
                   1, ri);
           if (s[i] == '/' && c == 0)
               return DFS(le, i - 1) / DFS(i +
                   1, ri);
           if (s[i] == '%' && c == 0)
26
27
               return DFS(le, i - 1) % DFS(i +
                   1, ri);
28
       if ((s[le] == '(') && (s[ri] == ')'))
29
           return DFS(le + 1, ri - 1); //去除刮
       if (s[le] == ' ' && s[ri] == ' ')
           return DFS(le + 1, ri - 1); //去除左
32
                右兩邊空格
       if (s[le] == ' ')
33
34
           return DFS(le + 1, ri); //去除左邊空
       if (s[ri] == ' ')
```

```
return DFS(le, ri - 1); //去除右邊空
格
long long int num = 0;
for (int i = le; i <= ri; i++)
num = num * 10 + s[i] - '0';
return num;
```

6.16 因數表

```
1 | vector<vector<int>> arr(10000000);
2 | const int limit = 10e7;
3 | for (int i = 1; i <= limit; i++) | {
5 | for (int j = i; j <= limit; j += i) | arr[j].pb(i); // i 為因數
7 | }
```

6.17 數字乘法組合

```
1 | void dfs(int j, int old, int num, vector<int
        > com, vector<vector<int>> &ans)
       for (int i = j; i <= sqrt(num); i++)
           if (old == num)
               com.clear();
           if (num % i == 0)
               vector<int> a:
               a = com;
               a.push_back(i);
               finds(i, old, num / i, a, ans);
               a.push_back(num / i);
               ans.push_back(a);
  vector<vector<int>> ans;
19 vector<int> zero;
20 dfs(2, num, num, zero, ans);
  /*/num 為 input 數字*/
   for (int i = 0; i < ans.size(); i++)</pre>
23
       for (int j = 0; j < ans[i].size() - 1; j</pre>
24
           cout << ans[i][j] << " ";</pre>
       cout << ans[i][ans[i].size() - 1] <<</pre>
```

6.18 數字加法組合

44

45

```
if (n == 0)
           for (int i : out)
                if (i > m)
                    return;
           ans.push back(out);
       for (int j = i; j <= n; j++)</pre>
12
           out.push_back(j);
13
           recur(j, n - j, m, out, ans);
           out.pop back();
14
15
16
   vector<vector<int>> ans:
   vector<int> zero;
19 recur(1, num, num, zero, ans);
   // num 為 input 數字
   for (int i = 0; i < ans.size(); i++)</pre>
       for (int j = 0; j < ans[i].size() - 1; j</pre>
           cout << ans[i][j] << " ";</pre>
       cout << ans[i][ans[i].size() - 1] <<</pre>
            endl;
```

6.19 羅馬數字

```
1 int romanToInt(string s)
2
       unordered map<char, int> T;
       T['I'] = 1;
       T['V'] = 5;
       T['X'] = 10;
       T['L'] = 50:
       T['C'] = 100;
       T['D'] = 500;
       T['M'] = 1000;
       int sum = T[s.back()];
       for (int i = s.length() - 2; i >= 0; --i
15
           if (T[s[i]] < T[s[i + 1]])</pre>
               sum -= T[s[i]];
           else
               sum += T[s[i]];
20
       return sum:
```

6.20 質因數分解

7 Other

1 / / 查找和目標值完全相等的數

11

12

13

14

15

7.1 binary search 三類變化

```
2 int find(vector<int> &nums, int target)
       int left = 0, right = nums.size();
       while (left < right)</pre>
           int mid = left + (right - left) / 2;
           if (nums[mid] == target)
               return mid;
           else if (nums[mid] < target)</pre>
              left = mid + 1;
12
13
               right = mid;
14
       return -1;
16 }
17 // 找第一個不小於目標值的數 == 找最後一個小
        於目標值的數
18 /*(lower bound)*/
int find(vector<int> &nums, int target)
20 {
21
       int left = 0, right = nums.size();
       while (left < right)</pre>
22
           int mid = left + (right - left) / 2;
24
           if (nums[mid] < target)</pre>
25
               left = mid + 1;
26
27
           else
28
               right = mid;
29
30
       return right;
31
32 // 找第一個大於目標值的數 == 找最後一個不大
        於目標值的數
   /*(upper bound)*/
34 int find(vector<int> &nums, int target)
35
       int left = 0, right = nums.size();
       while (left < right)</pre>
           int mid = left + (right - left) / 2;
           if (nums[mid] <= target)</pre>
40
               left = mid + 1;
41
```

7.2 heap sort

, int length)

int left = 2 * root.

return right;

right = mid;

1 | void MaxHeapify(vector<int> &array, int root

right = 2 * root + 1.

```
largest;
       if (left <= length && arrav[left] >
            array[root])
           largest = left;
       else
           largest = root;
       if (right <= length && array[right] >
            array[largest])
           largest = right;
11
       if (largest != root)
12
13
           swap(array[largest], array[root]);
14
           MaxHeapify(array, largest, length);
15
16
17
  void HeapSort(vector<int> &array)
18
19
20
       array.insert(array.begin(), 0);
       for (int i = (int)array.size() / 2; i >=
21
            1; i--)
           MaxHeapify(array, i, (int)array.size
22
                () - 1);
       int size = (int)array.size() - 1;
       for (int i = (int)array.size() - 1; i >=
            2; i--)
25
26
           swap(array[1], array[i]);
27
           size--;
28
           MaxHeapify(array, 1, size);
29
       array.erase(array.begin());
```

7.3 Merge sort

```
15
               idxLeft++:
16
           else
               arr[i] = RightSub[idxRight];
                idxRight++:
21
22
23
  void MergeSort(vector<int> &arr, int front,
25
       // front = 0 , end = arr.size() - 1
26
       if (front < end)</pre>
27
28
           int mid = (front + end) / 2:
29
30
           MergeSort(arr, front, mid):
```

MergeSort(arr, mid + 1, end);

Merge(arr, front, mid, end);

idxRight])

if (LeftSub[idxLeft] <= RightSub[</pre>

arr[i] = LeftSub[idxLeft];

7.4 Quick

11

13

12

31

32

33

```
i int Partition(vector<int> &arr, int front,
        int end)
       int pivot = arr[end];
       int i = front - 1:
       for (int j = front; j < end; j++)</pre>
           if (arr[j] < pivot)</pre>
               i++:
               swap(arr[i], arr[j]);
13
       swap(arr[i], arr[end]);
14
15
       return i:
16
void QuickSort(vector<int> &arr, int front,
        int end)
18 {
       // front = 0 , end = arr.size() - 1
       if (front < end)</pre>
           int pivot = Partition(arr, front,
           QuickSort(arr, front, pivot - 1);
^{24}
           QuickSort(arr, pivot + 1, end);
25
```

for (int i = 1; i <= n2; i++)

return true:

18

20

21 22

24

25

26

27

28

29

30

31

32

33

44

45

46

47

48

49

50

54

55

58 else

34 }

return false:

int>(n * n + 1, 0));

for (int i = 0; i < n * n; ++i)

int number;

isSquare, 0, n))

cin >> number;

if (number == 0)continue;

board[i][j] = number;

isRow[i][number] = true;

number] = true;

<bool>(n * n + 1, false));

35 | /*用法 main*/

7.5 Weighted Job Scheduling

```
1 struct Job
       int start, finish, profit;
5 bool jobComparataor(Job s1, Job s2)
       return (s1.finish < s2.finish);</pre>
   int latestNonConflict(Job arr[], int i)
       for (int j = i - 1; j >= 0; j--)
           if (arr[j].finish <= arr[i].start)</pre>
               return j;
       return -1;
   int findMaxProfit(Job arr[], int n)
       sort(arr, arr + n, jobComparataor);
       int *table = new int[n];
       table[0] = arr[0].profit;
       for (int i = 1; i < n; i++)
25
           int inclProf = arr[i].profit;
           int 1 = latestNonConflict(arr, i);
26
           if (1 != -1)
               inclProf += table[1];
29
           table[i] = max(inclProf, table[i -
30
       int result = table[n - 1];
31
32
       delete[] table:
33
34
       return result;
```

7.6 數獨解法

```
int getSquareIndex(int row, int column, int
      return row / n * n + column / n;
  bool backtracking(vector<vector<int>> &board
       , vector<vector<bool>> &rows, vector<</pre>
       vector<bool>> &cols,
                     vector<vector<bool>> &boxs
                          , int index, int n)
      int n2 = n * n;
       int rowNum = index / n2, colNum = index
           % n2:
      if (index >= n2 * n2)
12
           return true;
      if (board[rowNum][colNum] != 0)
           return backtracking(board, rows,
               cols, boxs, index + 1, n);
```

String

/*有解答*/

/*解答*/

8.1 KMP

```
if (!rows[rowNum][i] && !cols[colNum
                ][i] && !boxs[getSquareIndex(
                rowNum, colNum, n)][i])
               rows[rowNum][i] = true;
               cols[colNum][i] = true;
               boxs[getSquareIndex(rowNum,
                                                 10
                    colNum, n)][i] = true;
                                                 11
               board[rowNum][colNum] = i;
                                                 12
               if (backtracking(board, rows,
                                                 13
                    cols, boxs, index + 1, n)
                                                 14
                                                 15 }
               board[rowNum][colNum] = 0;
               rows[rowNum][i] = false;
                                                 17
               cols[colNum][i] = false;
                                                 18
               boxs[getSquareIndex(rowNum,
                                                 19
                    colNum, n)][i] = false;
                                                 20
                                                 21
                                                 22
                                                 23
                                                 24
36 | int n = sqrt(數獨邊長大小) /*e.g. 9*9 n=3*/
   vector<vector<int>> board(n * n + 1, vector< 26
38 vector<vector<bool>> isRow(n * n + 1, vector
                                                 29
39 vector<vector<bool>> isColumn(n * n + 1,
                                                 31
       vector<bool>(n * n + 1, false));
40 vector<vector<bool>> isSquare(n * n + 1,
       vector<bool>(n * n + 1, false));
                                                 32
                                                 33
                                                 34
                                                 35
       for (int j = 0; j < n * n; ++j)
                                                    // string s = "abcdabcdebcd";
                                                    // string p = "bcd";
                                                 38 // KMPMatcher(s, p);
                                                 39 // cout << endl;
           isColumn[j][number] = true;
           isSquare[getSquareIndex(i, j, n)][
56 if (backtracking(board, isRow, isColumn,
                                                  11
                                                 12
                                                 13
                                                 14
                                                 15
```

```
1 // 用在在一個 S 內查找一個詞 W 的出現位置
2 void ComputePrefix(string s, int next[])
      int n = s.length();
                                                       return dp[m][n];
      int q, k;
      next[0] = 0;
      for (k = 0, q = 1; q < n; q++)
          while (k > 0 \&\& s[k] != s[q])
              k = next[k];
          if (s[k] == s[q])
              k++;
          next[q] = k;
16 void KMPMatcher(string text, string pattern)
      int n = text.length();
      int m = pattern.length();
      int next[pattern.length()];
      ComputePrefix(pattern, next);
      for (int i = 0, q = 0; i < n; i++)
          while (q > 0 && pattern[q] != text[i
               ])
              q = next[q];
          if (pattern[q] == text[i])
                                                16
                                                17
              q++;
          if (q == m)
              cout << "Pattern occurs with
                   shift " << i - m + 1 << endl 21
                                                23
                                                24
```

8.3 Sliding window

```
1 | string minWindow(string s, string t)
      unordered map<char, int> letterCnt;
      for (int i = 0; i < t.length(); i++)</pre>
          letterCnt[t[i]]++;
      int minLength = INT_MAX, minStart = -1;
      int left = 0, matchCnt = 0;
      for (int i = 0; i < s.length(); i++)</pre>
          if (--letterCnt[s[i]] >= 0)
          while (matchCnt == t.length())
              if (i - left + 1 < minLength)</pre>
                  minLength = i - left + 1;
                  minStart = left;
              if (++letterCnt[s[left]] > 0)
                  matchCnt--;
              left++;
      return minLength == INT MAX ? "" : s.
           substr(minStart, minLength);
```

dp[i - 1][j - 1]);

8.2 Min Edit Distance

```
int EditDistance(string a, string b)
     vector<vector<int>> dp(a.size() + 1,
          vector<int>(b.size() + 1, 0));
     int m = a.length(), n = b.length();
     for (int i = 0; i < m + 1; i++)
          for (int j = 0; j < n + 1; j++)
              if (i == 0)
                  dp[i][j] = j;
              else if (j == 0)
                  dp[i][j] = i;
              else if (a[i - 1] == b[i - 1])
                  dp[i][j] = dp[i - 1][j - 1];
                  dp[i][j] = 1 + min(min(dp[i
                       - 1][j], dp[i][j - 1]),
```

8.4 Split

```
1 | vector<string> mysplit(const string &str,
        const string &delim)
       vector<string> res;
       if ("" == str)
           return res;
       char *strs = new char[str.length() + 1];
       char *d = new char[delim.length() + 1];
       strcpy(strs, str.c str());
       strcpy(d, delim.c str());
11
       char *p = strtok(strs, d);
12
       while (p)
13
14
           string s = p:
15
           res.push back(s);
           p = strtok(NULL, d);
16
17
       return res;
```

9 data structure

56

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9.1 Bigint

```
1 | // 台大 // 非必要請用python
2 struct Bigint
3
       static const int LEN = 60:
       static const int BIGMOD = 10000; //10為
            正常位數
       int s;
       int v1, v[LEN];
       // vector<int> v;
       Bigint() : s(1) \{ vl = 0; \}
       Bigint(long long a)
10
11
12
           s = 1;
13
           v1 = 0:
14
           if (a < 0)
15
16
               s = -1:
               a = -a;
           while (a)
19
20
               push_back(a % BIGMOD);
21
               a /= BIGMOD:
22
23
24
25
       Bigint(string str)
26
27
           s = 1:
           v1 = 0;
28
29
           int stPos = 0, num = 0;
           if (!str.empty() && str[0] == '-')
30
               stPos = 1;
32
33
               s = -1;
34
           for (int i = str.length() - 1, q =
                1; i >= stPos; i--)
               num += (str[i] - '0') * q;
37
               if ((q *= 10) >= BIGMOD)
38
                    push back(num);
                    num = 0;
42
                   q = 1;
           if (num)
               push_back(num);
           n();
49
       int len() const
50
51
           return v1; //return SZ(v);
52
       bool empty() const { return len() == 0;
       void push_back(int x)
```

```
v[v]++] = x; //v.PB(x);
                                            118
                                            119
void pop_back()
                                            120
                                             121
    vl--; //v.pop_back();
                                            122
                                             123
int back() const
                                             124
                                             125
    return v[vl - 1]; //return v.back(); 126
                                             127
void n()
                                             128
                                             129
    while (!empty() && !back())
                                            130
        pop_back();
                                             131
                                             132
void resize(int nl)
                                             133
                                             134
    v1 = n1:
                          //v.resize(nl);
                                            135
    fill(v, v + vl, 0); //fill(ALL(v),
                                            136
                                             137
                                             138
void print() const
                                             139
                                            140
    if (empty())
                                            141
                                            142
        putchar('0');
                                            143
        return:
                                            144
                                            145
    if (s == -1)
                                            146
        putchar('-');
                                            147
    printf("%d", back());
                                             148
    for (int i = len() - 2; i >= 0; i--) 149
        printf("%.4d", v[i]);
                                            150
                                             151
friend std::ostream &operator<<(std::</pre>
                                            152
     ostream &out, const Bigint &a)
                                            153
                                             154
    if (a.empty())
                                             155
                                             156
        out << "0";
                                             157
        return out;
                                             158
                                             159
    if (a.s == -1)
                                             160
        out << "-"
                                             161
    out << a.back();
                                             162
    for (int i = a.len() - 2; i >= 0; i
         --)
                                             164
                                             165
        char str[10];
                                             166
        snprintf(str, 5, "%.4d", a.v[i]) 167
        out << str;
                                             168
                                             169
    return out;
                                             170
                                             171
int cp3(const Bigint &b) const
                                             172
                                             173
    if (s != b.s)
                                             174
        return s - b.s;
                                             175
    if (s == -1)
                                             176
        return -(-*this).cp3(-b);
    if (len() != b.len())
                                            178
        return len() - b.len(); //int
    for (int i = len() - 1; i >= 0; i--) 180
        if (v[i] != b.v[i])
                                             181
             return v[i] - b.v[i];
```

```
return 0;
                                             183
                                             184
bool operator < (const Bigint &b) const
                                             185
                                             186
    return cp3(b) < 0;
                                             187
                                             188
bool operator <= (const Bigint &b) const
                                             189
                                             190
    return cp3(b) <= 0;
                                             191
                                             192
bool operator == (const Bigint &b) const
                                             193
                                             194
    return cp3(b) == 0;
                                             195
                                             196
bool operator!=(const Bigint &b) const
                                             197
                                             198
    return cp3(b) != 0;
                                             199
                                             200
bool operator>(const Bigint &b) const
                                             201
                                             202
    return cp3(b) > 0;
                                             203
                                             204
bool operator>=(const Bigint &b) const
                                             205
    return cp3(b) >= 0;
                                             206
                                             207
Bigint operator-() const
                                             208
                                             209
    Bigint r = (*this);
                                             210
    r.s = -r.s;
    return r;
                                             211
                                             212
Bigint operator+(const Bigint &b) const
                                             213
                                             214
    if (s == -1)
                                             215
         return -(-(*this) + (-b));
                                             216
    if (b.s == -1)
                                             217
         return (*this) - (-b);
                                             218
    Bigint r;
                                             219
    int nl = max(len(), b.len());
                                             220
    r.resize(nl + 1);
                                             221
    for (int i = 0; i < nl; i++)</pre>
                                             222
         if (i < len())</pre>
                                             223
             r.v[i] += v[i];
                                             224
         if (i < b.len())</pre>
                                             225
             r.v[i] += b.v[i];
         if (r.v[i] >= BIGMOD)
                                             226
                                             227
             r.v[i + 1] += r.v[i] /
                                             228
                  BIGMOD;
                                             229
             r.v[i] %= BIGMOD;
                                             230
                                             231
                                             232
    r.n();
                                             233
Bigint operator-(const Bigint &b) const
                                             237
    if (s == -1)
         return -(-(*this) - (-b));
                                             239
    if (b.s == -1)
                                             240
         return (*this) + (-b);
                                             241
    if ((*this) < b)
                                             242
         return -(b - (*this));
                                             243
    Bigint r;
```

```
r.resize(len());
    for (int i = 0; i < len(); i++)
        r.v[i] += v[i];
        if (i < b.len())</pre>
            r.v[i] -= b.v[i];
        if (r.v[i] < 0)</pre>
            r.v[i] += BIGMOD;
            r.v[i + 1]--;
    r.n();
    return r:
Bigint operator*(const Bigint &b)
    Bigint r;
    r.resize(len() + b.len() + 1);
    r.s = s * b.s;
    for (int i = 0; i < len(); i++)
        for (int j = 0; j < b.len(); j</pre>
             ++)
            r.v[i + j] += v[i] * b.v[j];
            if (r.v[i + j] >= BIGMOD)
                r.v[i + j + 1] += r.v[i
                     + j] / BIGMOD;
                r.v[i + j] \% = BIGMOD;
    r.n();
    return r;
Bigint operator/(const Bigint &b)
    Bigint r;
    r.resize(max(1, len() - b.len() + 1)
         );
    int oriS = s;
    Bigint b2 = b; // b2 = abs(b)
    s = b2.s = r.s = 1;
    for (int i = r.len() - 1; i >= 0; i
        int d = 0, u = BIGMOD - 1;
        while (d < u)
            int m = (d + u + 1) >> 1;
            r.v[i] = m;
            if ((r * b2) > (*this))
                u = m - 1;
            else
        r.v[i] = d;
    s = oriS;
    r.s = s * b.s;
    r.n();
    return r;
Bigint operator%(const Bigint &b)
```

```
for (int y = 0; y < r; y++)
                                                                                                                                                                        sz = 1:
                                                    52
            return (*this) - (*this) / b * b;
                                                                                                               BigInteger operator = (const string& str
246
                                                    53
                                                                    for (int x = 0; x < c; ++x)
                                                                                                                                                            75
                                                                        m[y][x] = t.m[y][c + x] / t.
                                                                                                                                                                   void insert(BigInteger x, int v){
247
                                                    54
                                                                                                                                                            76
248 };
                                                                              m[y][y];
                                                                                                        18
                                                                                                                    s.clear();
                                                                                                                                                            77
                                                                                                                                                                        int u = 0:
                                                                                                                                                                        int max_len_count = 0;
                                                                return true;
                                                                                                                    int x, len = (str.length() - 1) /
                                                    55
                                                                                                        19
                                                                                                                                                            78
                                                                                                                                                                        int firstNum = x.s.back();
                                                    56
                                                                                                                         WIDTH + 1;
                                                                                                        20
                                                                                                                    for(int i = 0: i < len:i++){</pre>
                                                                                                                                                                        char firstBuf[20];
                                                    57
                                                             gas() //行列式
          Matirx
                                                                                                                        int end = str.length() - i*WIDTH
                                                                                                                                                                        sprintf(firstBuf, "%d", firstNum);
                                                                                                        21
                                                    58
                                                                                                                                                                        for(int j = 0; j < strlen(firstBuf);</pre>
                                                    59
                                                                vector<T> lazy(r, 1);
                                                                                                                        int start = max(0, end-WIDTH);
                                                                                                                                                                             i++){
                                                                                                        22
                                                    60
                                                                bool sign = false;
 1 template <typename T>
                                                                                                        23
                                                                                                                        sscanf(str.substr(start, end-
                                                                                                                                                                            int index = getIndex(firstBuf[j
                                                                for (int i = 0; i < r; ++i)
                                                                                                                                                            83
                                                    61
 2 struct Matrix
                                                                                                                             start).c str(), "%d", &x);
                                                                                                                                                                                 1);
                                                    62
 3
                                                                                                                                                                            if(!c[u][index]){
                                                                                                                        s.push_back(x);
                                                    63
                                                                    if (m[i][i] == 0)
                                                                                                        24
        using rt = std::vector<T>;
                                                                                                                                                                                memset(c[sz], 0 , sizeof(c[
                                                                                                        25
                                                    64
        using mt = std::vector<rt>;
                                                                                                        26
                                                                                                                    return *this:
                                                                                                                                                                                     sz]));
                                                    65
                                                                         int j = i + 1;
       using matrix = Matrix<T>;
                                                                                                        27
                                                                                                               }
                                                                                                                                                                                val[sz] = v;
                                                    66
                                                                        while (j < r && !m[j][i])</pre>
       int r, c; // [r][c]
                                                                                                                                                                                c[u][index] = sz++;
                                                                                                        28
                                                    67
                                                                            j++;
       mt m;
                                                                                                               BigInteger operator + (const BigInteger&
                                                                                                        29
                                                                        if (j == r)
       Matrix(int r, int c) : r(r), c(c), m(r,
                                                                                                                     b) const{
                                                                                                                                                                            u = c[u][index];
                                                                                                                                                            89
                                                                             continue:
             rt(c)) {}
                                                                                                                    BigInteger c;
                                                                                                        30
                                                                                                                                                            90
                                                                                                                                                                            max len count++;
                                                                        m[i].swap(m[j]);
       Matrix(mt a) \{ m = a, r = a.size(), c =
                                                                                                        31
                                                                                                                    c.s.clear();
                                                                        sign = !sign;
                                                                                                                                                            91
             a[0].size(); }
                                                                                                                    for(int i = 0, g = 0;;i++){
                                                                                                                                                                        for(int i = x.s.size()-2; i >= 0; i >= 0
                                                                                                        32
                                                                                                                                                            92
                                                    72
        rt &operator[](int i) { return m[i]; }
11
                                                                                                        33
                                                                                                                        if(g == 0 \&\& i >= s.size() \&\& i
                                                                                                                                                                             --){
                                                                    for (int j = 0; j < r; ++j)
                                                    73
        matrix operator+(const matrix &a)
                                                                                                                                                                            char buf[20];
12
                                                                                                                             >= b.s.size()) break;
                                                    74
                                                                                                                                                            93
13
                                                                                                                        int x = g;
                                                                                                                                                                            sprintf(buf, "%08d", x.s[i]);
                                                                        if (i == j)
                                                                                                        34
                                                                                                                                                            94
                                                    75
            matrix rev(r, c);
14
                                                                                                                        if(i < s.size()) x+=s[i];</pre>
                                                                                                                                                            95
                                                                                                                                                                            for(int j = 0; j < strlen(buf)</pre>
                                                                             continue;
                                                                                                        35
                                                    76
15
            for (int i = 0; i < r; ++i)
                                                                                                                        if(i < b.s.size()) x+=b.s[i];</pre>
                                                                                                                                                                                 && max_len_count < 50; j++){
                                                    77
                                                                        lazy[j] = lazy[j] * m[i][i];
                                                                                                        36
                for (int j = 0; j < c; ++j)
                                                                                                                        c.s.push back(x % BASE);
                                                                                                                                                                                int index = getIndex(buf[j])
                                                    78
                                                                        T mx = m[j][i];
                                                                                                        37
                                                                                                                                                            96
                    rev[i][j] = m[i][j] + a.m[i
                                                                                                                        g = x / \overline{BASE};
                                                                        for (int k = 0; k < c; ++k)
                         ][j];
                                                                                                                                                                                if(!c[u][index]){
                                                    80
                                                                             m[j][k] = m[j][k] * m[i]
                                                                                                        39
                                                                                                                                                            97
            return rev;
                                                                                  ][i] - m[i][k] * mx; 40
                                                                                                                    return c;
                                                                                                                                                            98
                                                                                                                                                                                     memset(c[sz], 0 , sizeof
19
                                                                                                                                                                                          (c[sz]));
                                                                                                        41
                                                    81
20
        matrix operator-(const matrix &a)
                                                                                                                                                                                     val[sz] = v;
                                                                                                        42
                                                                                                           };
                                                                                                                                                            99
                                                    82
21
                                                                                                                                                                                     c[u][index] = sz++;
                                                                                                        43
                                                                                                                                                           100
                                                    83
                                                                T det = sign ? -1 : 1;
22
            matrix rev(r, c);
                                                                                                           ostream& operator << (ostream &out, const
                                                                                                        44
                                                    84
                                                                for (int i = 0; i < r; ++i)
                                                                                                                                                           101
23
            for (int i = 0; i < r; ++i)
                                                                                                                BigInteger& x){
                                                                                                                                                                                u = c[u][index];
                                                                                                                                                           102
                                                    85
                for (int j = 0; j < c; ++j)
                                                                                                               out << x.s.back();</pre>
                                                                                                                                                                                max_len_count++;
                                                    86
                                                                    det = det * m[i][i];
                                                                                                        45
                                                                                                                                                           103
                    rev[i][j] = m[i][j] - a.m[i]
                                                                    det = det / lazy[i];
                                                                                                        46
                                                                                                               for(int i = x.s.size()-2; i >= 0;i--){
                                                                                                                                                           104
                                                    87
                         ][j];
                                                                                                        47
                                                                                                                    char buf[20];
                                                                                                                                                                            if(max len count >= 50){
                                                                                                                                                           105
                                                    88
                                                                    for (auto &i : m[i])
26
            return rev:
                                                                                                                    sprintf(buf, "%08d", x.s[i]);
                                                                                                                                                                                break:
                                                                                                        48
                                                                                                                                                           106
                                                    89
                                                                        i /= lazv[i]:
27
                                                                                                                    for(int j = 0; j< strlen(buf); j++){</pre>
                                                                                                        49
                                                                                                                                                           107
                                                    90
28
        matrix operator*(const matrix &a)
                                                                                                                        out << buf[j];</pre>
                                                                                                        50
                                                    91
                                                                return det;
                                                                                                                                                           108
29
                                                                                                        51
                                                                                                                                                           109
                                                    92
            matrix rev(r, a.c);
30
                                                                                                                                                                   int find(const char* s){
                                                                                                        52
                                                    93 };
                                                                                                                                                           110
31
            matrix tmp(a.c, a.r);
                                                                                                        53
                                                                                                                                                                        int u = 0;
                                                                                                               return out;
                                                                                                                                                           111
            for (int i = 0; i < a.r; ++i)</pre>
32
                                                                                                        54
                                                                                                                                                           112
                                                                                                                                                                        int n = strlen(s);
                for (int j = 0; j < a.c; ++j)
33
                                                                                                        55
                                                                                                                                                                        for(int i = 0; i < n; ++i)
                                                                                                                                                           113
34
                     tmp[j][i] = a.m[i][j];
                                                                                                        56
                                                                                                           istream& operator >> (istream &in,
                                                                                                                                                           114
                                                       9.3
                                                              Trie
35
            for (int i = 0; i < r; ++i)</pre>
                                                                                                                BigInteger& x){
                                                                                                                                                           115
                                                                                                                                                                            int index = getIndex(s[i]);
                for (int j = 0; j < a.c; ++j)</pre>
                                                                                                        57
                                                                                                               string s;
                                                                                                                                                           116
                                                                                                                                                                            if(!c[u][index]){
                     for (int k = 0; k < c; ++k)
37
                                                                                                        58
                                                                                                               if(!(in >> s))
                                                                                                                                                           117
                                                                                                                                                                                return -1;
                         rev.m[i][j] += m[i][k] *
38
                                                     1 // biginter字典數
                                                                                                        59
                                                                                                                    return in;
                                                                                                                                                           118
                               tmp[j][k];
                                                     2 struct BigInteger{
                                                                                                                                                                            u = c[u][index];
                                                                                                               x = s;
                                                                                                                                                           119
            return rev:
39
                                                            static const int BASE = 100000000;
                                                                                                        61
                                                                                                               return in;
                                                                                                                                                           120
40
                                                            static const int WIDTH = 8;
                                                                                                        62
                                                                                                                                                           121
                                                                                                                                                                        return val[u];
       bool inverse() //逆矩陣判斷
                                                            vector<int> s;
                                                                                                        63
                                                                                                                                                           122
                                                            BigInteger(long long num = 0){
                                                                                                           struct Trie{
                                                                                                                                                           123 }
42
                                                                                                               int c[5000005][10];
            Matrix t(r, r + c);
                                                                *this = num:
            for (int y = 0; y < r; y++)
                                                                                                               int val[5000005];
                                                           BigInteger operator = (long long num){
                                                                                                               int sz:
                                                                                                                                                               9.4 分數
                t.m[y][c + y] = 1;
                                                    10
                                                                s.clear();
                                                                                                        68
                                                                                                               int getIndex(char c){
                for (int x = 0; x < c; ++x)
                                                    11
                                                                                                        69
                                                                                                                    return c - '0';
                    t.m[y][x] = m[y][x];
                                                    12
                                                                    s.push back(num % BASE);
                                                                                                        70
                                                    13
                                                                    num /= BASE;
                                                                                                        71
                                                                                                               void init(){
                                                                                                                                                             1 typedef long long 11;
            if (!t.gas())
                                                                }while(num > 0);
                                                                                                                    memset(c[0], 0, sizeof(c[0]));
                                                                                                                                                             2 struct fraction
50
                                                    14
                                                                                                        72
                return false;
                                                                return *this;
                                                                                                                    memset(val, -1, sizeof(val));
```

```
11 n, d;
     fraction(const 11 &_n = 0, const 11 &_d =
         1) : n(_n), d(_d)
      11 t = __gcd(n, d);
n /= t, d /= t;
      if (d < 0)
10
         n = -n, d = -d;
11
12
     fraction operator-() const
13
14
       return fraction(-n, d);
15
     fraction operator+(const fraction &b)
16
17
       return fraction(n * b.d + b.n * d, d * b
18
19
     fraction operator-(const fraction &b)
20
21
       return fraction(n * b.d - b.n * d, d * b
22
23
     fraction operator*(const fraction &b)
24
25
       return fraction(n * b.n, d * b.d);
26
27
     fraction operator/(const fraction &b)
28
29
       return fraction(n * b.d, d * b.n);
30
31
     void print()
32
33
       cout << n;
34
      if (d != 1)
35
36
         cout << "/" << d;
37
38 };
```

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