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1	Basic 1		9.4 分數	
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		l	/*at home directory*/ /* vi ~/.vimrc */	
3	Flow & matching 3.1 Dinic		syntax enable set smartindent	
	3.2 Edmonds_karp		set tabstop=4	
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			set relativenumber	
4	Geometry	5	1.3 Code Template	
	4.1 Circle Intersect	-	1.9 Code Template	
	4.3 Line	~	<pre>#include <bits stdc++.h=""> using namespace std;</bits></pre>	
	4.4 max_cover_rectangle	_	typedef long long 11;	
	4.6 Polygon	7	<pre>typedef unsigned long long ull; #define pb push_back</pre>	
	4.7 Triangle		<pre>#define len length()</pre>	
5	Graph 9		<pre>#define all(p) p.begin(), p.end() #define endl '\n'</pre>	
	5.1 Bellman-Ford	9	#define x first	
	5.3 DFS-rec	9	<pre>#define y second #define bug(k) cout << "value of " << #k << " is " << k << en</pre>	dl
	5.4 Dijkstra	9	;	
	5.6 Floyd-warshall	U	<pre>#define bugp(k) cout << "pair of " << #k << " is " << k.x << ' << k.y << endl;</pre>	
	5.7 Hamilton_cycle	0	<pre>#define bugarr(k) for(auto i : k) cout << i << ' '; cout << endl;</pre>	
	5.9 Minimum Weight Cycle	1	<pre>int main()</pre>	
	5.10 Prim		<pre>{ ios::sync_with_stdio(0);</pre>	
6	Mathematics 12	2	<pre>cin.tie(0); return 0;</pre>	
	6.1 Catalan		}	
	6.2 Combination	9	1.4. D. (I	
	6.4 Extended Euclidean		1.4 Python	
	6.5 Fermat		//輸入	
	6.7 Log	- 1	<pre>input()</pre>	
	6.8 Mod 性質		array = [0] * (N) //N個0	
	6.10 Pow_Mod	-	<pre>range(0, N) // 0 ~ N-1 line = input().split()</pre>	
	6.11 Prime table	- 1	D, R, N = map(int, line) // 分三個 int 變數	
	6.13 Round(小數)		// 才是 取除數	
	6.15 公式	. !	/ 是 小數運算	
	6.16 四則運算		pow(a, b, c) // a ^ b % c	
	6.18 數字乘法組合	4		
	6.19 數字加法組合 14 6.20 羅馬數字 14		print(*objects, sep = ' ', end = '\n') // objects 可以一次輸出多個對象	
	6.21 質因數分解	5	// sep 分開多個objects	
	6.22 質數數量	5	// end 默認值是\n	
7	Other 15 7.1 Binary search 三類變化 15	-	// EOF break	
	7.2 Heap sort		try: while True:	
	7.3 Josephus		<pre>//input someithing except EOFError:</pre>	
	7.5 Merge sort	6	pass	
	7.6 Quick sort	6	1 × D	
	7.8 Weighted Job Scheduling		1.5 Range data	
8	String 17	•	int (-2147483648 to 2147483647)	
	8.1 KMP	7	unsigned int(0 to 4294967295) long(-2147483648 to 2147483647)	
	8.3 Sliding window	7	unsigned long(0 to 4294967295) long long(-9223372036854775808 to 9223372036854775807)	
	8.4 Split		unsigned long long (0 to 18446744073709551615)	

1.6 Some Function

```
// 四捨五入
 round(double f);
                           // 進入
 ceil(double f);
                           // 捨去
 floor(double f);
  _builtin_popcount(<mark>int</mark> n); // 32bit有多少 1
to_string(int s);
                           // int to string
 cout << setprecision(位數) // cout 小數位設定
printf 型別
"%lf" // long double
"%lld" // long long int
 set_union(all(a), all(b), back_inserter(d)); // 聯集
 set_intersection(all(a), all(b), back_inserter(c)); //交集
 /** 全排列要先 sort !!! **/
 next_permutation(num.begin(), num.end());
 prev_permutation(num.begin(), num.end());
 //用binary search找第一個大於或等於val的位置
 vector<int>::iterator it = lower_bound(v.begin(), v.end(), val)
 //用binary search找第一個大於val的位置
 vector<int>::iterator it = upper_bound(v.begin(), v.end(), val)
 /*找到範圍裏面的最大元素*/
 max_element(n, n + len);
                                // n到n+len範圍內最大值
 max_element(v.begin(), v.end()); // vector 中最大值
 /*找到範圍裏面的最大元素*/
                                // n到n+len範圍內最小值
 min element(n, n + len);
 min_element(v.begin(), v.end()); // vector 中最小值
 /*queue*/
 queue<datatype> q;
front(); /*取出最前面的值(沒有移除掉)*/
back(); /*取出最後面的值(沒有移除掉)*/
pop(); /*移掉最前面的值*/
push(); /*新增值到最後面*/
empty(); /*回傳bool,檢查是不是空的queue*/
 size(); /*queue 的大小*/
 /*stack*/
 stack<datatype> s;
top(); /*取出最上面的值(沒有移除掉)*/
        /*移掉最上面的值*/
 pop();
 push(); /*新增值到最上面*/
empty(); /*bool 檢查是不是空*/
size(); /*stack 的大小*/
 /*unordered_set*/
 unordered_set<datatype> s;
 unordered_set<datatype> s(arr, arr + n);
 /*initial with array*/
 insert(); /*插入值*/
erase(); /*刪除值*/
empty(); /*bool 檢查是不是空*/
 count(); /*判斷元素存在回傳1 無則回傳0*/
 /*tuple*/
tuple<datatype,datatype,datatype> t;
std::get<0>(t) /*Get first element of tuple*/
std::get<1>(t) /*Get second element of tuple*/
 std::get<2>(t) /*Get third element of tuple*/
1.7 Time
cout << 1.0 * clock() / CLOCKS_PER_SEC << endl;</pre>
     DP
```

2.1 3 維 DP 思路

```
解題思路: dp[i][j][k]
i 跟 j 代表 range i ~ j 的 value
k在我的理解裡是視題目的要求而定的
像是 Remove Boxes 當中 k 代表的是在 i 之前還有多少個連續的箱子
所以每次區間消去的值就是(k+1) * (k+1)
換言之‧我認為可以理解成 k 的意義就是題目今天所關注的重點‧就是
老師說的題目所規定的運算
```

2.2 Knapsack Bounded

```
const int N = 100, W = 100000;
int cost[N], weight[N], number[N];
int c[W + 1];
void knapsack(int n, int w)
{
```

```
for (int i = 0; i < n; ++i)
        int num = min(number[i], w / weight[i]);
        for (int k = 1; num > 0; k *= 2)
            if (k > num)
                k = num;
            num -= k;
            }
    cout << "Max Prince" << c[w];</pre>
2.3 Knapsack sample
int Knapsack(vector<int> weight, vector<int> value, int
     bag Weight)
    // vector<int> weight = {1, 3, 4};
// vector<int> value = {15, 20, 30};
    // int bagWeight = 4;
    vector<vector<int>> dp(weight.size(), vector<int>(bagWeight
    + 1, 0));
for (int j = weight[0]; j <= bagWeight; j++)
dp[0][j] = value[0];
    // weight數組的大小就是物品個數
    for (int i = 1; i < weight.size(); i++)</pre>
```

2.4 Knapsack Unbounded

{ // 遍歷背包容量

{ // 遍歷物品

for (int j = 0; j <= bagWeight; j++)</pre>

weight[i]] + value[i]);

cout << dp[weight.size() - 1][bagWeight] << endl;</pre>

if (j < weight[i]) dp[i][j] = dp[i - 1][j];
else dp[i][j] = max(dp[i - 1][j], dp[i - 1][j - 1][j]</pre>

2.5 LCIS

```
int LCIS_len(vector<int> arr1, vetor<int> arr2)
     int n = arr1.size(), m = arr2.size();
     vector<int> table(m, 0);
     for (int j = 0; j < m; j++)
          table[j] = 0;
     for (int i = 0; i < n; i++)
         int current = 0;
for (int j = 0; j < m; j++)</pre>
              if (arr1[i] == arr2[j])
                   if (current + 1 > table[j])
  table[j] = current + 1;
              if (arr1[i] > arr2[j])
                   if (table[j] > current)
                        current = table[j];
         }
    int result = 0;
for (int i = 0; i < m; i++)</pre>
         if (table[i] > result)
              result = table[i];
     return result:
```

2.6 LCS

```
int LCS(vector<string> Ans, vector<string> num)
{
    int N = Ans.size(), M = num.size();
    vector<vector<int>> LCS(N + 1, vector<int>(M + 1, 0));
    for (int i = 1; i <= N; ++i)
    {
        for (int j = 1; j <= M; ++j)
    }
}</pre>
```

```
if (Ans[i - 1] == num[j - 1])
    LCS[i][j] = LCS[i - 1][j - 1] + 1;
             LCS[i][j] = max(LCS[i - 1][j], LCS[i][j - 1]);
    }
cout << LCS[N][M] << '\n';</pre>
//列印 LCS
int n = N, m = M;
vector<string> k;
while (n && m)
    if (LCS[n][m] != max(LCS[n - 1][m], LCS[n][m - 1]))
         k.push_back(Ans[n - 1]);
         n - - ;
    else if (LCS[n][m] == LCS[n - 1][m])
    n--;
else if (LCS[n][m] == LCS[n][m - 1])
reverse(k.begin(), k.end());
for (auto i : k)
    cout << i << " ";
cout << endl;</pre>
return LCS[N][M];
```

2.7 LIS O(Nlog(N))

2.8 LIS

```
vector<int> ans;
void LIS(vector<int> &arr)
     vector<int> dp(arr.size(), 1);
     vector<int> pos(arr.size(), -1);
     int res = INT_MIN, index = 0;
for (int i = 0; i < arr.size(); ++i)</pre>
          for (int j = i + 1; j < arr.size(); ++j)</pre>
               if (arr[j] > arr[i])
                     if (dp[i] + 1 > dp[j])
                          dp[j] = dp[i] + 1;
                          pos[j] = i;
                     }
               }
          if (dp[i] > res)
               res = dp[i];
               index = i;
     cout << res << endl; // length
printLIS(arr, pos, index);
for (int i = 0; i < ans.size(); i++)</pre>
          cout << ans[i];</pre>
          if (i != ans.size() - 1)
    cout << ' ';</pre>
     cout << '\n';
void printLIS(vector<int> &arr, vector<int> &pos, int index)
     if (pos[index] != -1)
```

```
printLIS(arr, pos, pos[index]);
ans.push_back(arr[index]);
2.9 LPS
void LPS(string s)
    int maxlen = 0, 1, r;
    int n = n;
    for (int i = 0; i < n; i++)
        while ((s[i - x] == s[i + x]) \&\& (i - x >= 0) \&\& (i + x)
               < n)) //odd length
             x++;
         if (2 * x + 1 > maxlen)
             maxlen = 2 * x + 1;
             l = i - x;
        }
         while ((s[i - x] == s[i + 1 + x]) \&\& (i - x >= 0) \&\& (i
              + 1 + x < n)) //even length
        if (2 * x > maxlen)
             maxlen = 2 * x;
             1 = i - x + 1;
             r = i + x;
    }
    cout << maxlen << '\n'; // 最後長度
cout << l + 1 << ' ' << r + 1 << '\n'; //頭到尾
2.10 Max_subarray
 *Kadane's algorithm*/
int maxSubArrav(vector<int>& nums) {
    int local_max = nums[0], global_max = nums[0];
for(int i = 1; i < nums.size(); i++){</pre>
        local_max = max(nums[i],nums[i]+local_max);
         global_max = max(local_max,global_max);
    return global_max;
2.11 Money problem
//能否湊得某個價位
```

```
void change(vector<int> price, int limit)
     vector<bool> c(limit + 1, 0);
     c[0] = true;
                                                           // 依序加入各種
     for (int i = 0; i < price.size(); ++i)</pre>
           面額
          for (int j = price[i]; j <= limit; ++j) // 由低價位逐步
                到高價位
     c[j] = c[j] | c[j - price[i]];
if (c[limit]) cout << "YES\n";
else cout << "NO\n";</pre>
                                                          // 湊、湊、湊
// 湊得某個價位的湊法總共幾種
void change(vector<int> price, int limit)
     vector<int> c(limit + 1, 0);
    for (int i = 0; i < price.size(); ++i)
    for (int j = price[i]; j <= limit; ++j)
        c[j] += c[j - price[i]];
cout << c[limit] << '\n';</pre>
// 湊得某個價位的最少錢幣用量
void change(vector<int> price, int limit)
     vector<int> c(limit + 1, 0);
     c[0] = true;
for (int i = 0; i < price.size(); ++i)</pre>
     for (int j = price[i]; j <= limit; ++j)
    c[j] = min(c[j], c[j - price[i]] + 1);
cout << c[limit] << '\n';</pre>
//湊得某個價位的錢幣用量,有哪幾種可能性
void change(vector<int> price, int limit)
     vector<int> c(limit + 1, 0);
     c[0] = true;
for (int i = 0; i < price.size(); ++i)</pre>
          for (int j = price[i]; j <= limit; ++j)</pre>
              c[j] |= c[j-price[i]] << 1; // 錢幣數量加一·每一種
                     可能性都加一。
```

3 Flow & matching

3.1 Dinic

```
const long long INF = 1LL<<60;
struct Dinic { //O(VVE), with minimum cut
       static const int MAXN = 5003;
       struct Edge{
             int u, v;
             long long cap, rest;
       int n, m, s, t, d[MAXN], cur[MAXN];
       vector<Edge> edges
       vector<int> G[MAXN];
      void init(){
             edges.clear();
for ( int i = 0 ; i < n ; i++ ) G[i].clear();</pre>
       // min cut start
      bool side[MAXN];
      void cut(int u) {
    side[u] = 1;
    for ( int i : G[u] ) {
        if ( !side[ edges[i].v ] && edges[i].rest )
            cut(edges[i].v);
}
             }
       // min cut end
      int add_node(){
             return n++;
       void add_edge(int u, int v, long long cap){
  edges.push_back( {u, v, cap, cap} );
  edges.push_back( {v, u, 0, OLL} );
             m = edges.size();
             G[u].push_back(m-2);
             G[v].push_back(m-1);
      bool bfs(){
             fill(d,d+n,-1);
queue<int> que;
             que.push(s); d[s]=0;
while (!que.empty()){
                   int u = que.front(); que.pop();
                   for (int ei : G[u]){
    Edge &e = edges[ei];
    if (d[e.v] < 0 && e.rest > 0){
        d[e.v] = d[u] + 1;
}
                                que.push(e.v);
                         }
                   }
             return d[t] >= 0;
      long long dfs(int u, long long a){
   if ( u == t || a == 0 ) return a;
             long long flow = 0, f;
for ( int &i=cur[u]; i < (int)G[u].size() ; i++) {
    Edge &e = edges[ G[u][i] ];
    if ( d[u] + 1 != d[e.v] ) continue;</pre>
                   f = dfs(e.v, min(a, e.rest));
if (f > 0) {
                   e.rest -= f
                   edges[ G[u][i]^1 ].rest += f;
                   flow += f;
                   a -= f;
                   if ( a == 0 ) break;
             return flow;
       long long maxflow(int _s, int _t){
             s = _s, t = _t;
long long flow = 0, mf;
             while ( bfs() ){
                   fill(cur,cur+n,0);
while ( (mf = dfs(s, INF)) ) flow += mf;
             return flow;
} dinic;
```

3.2 Edmonds_karp

```
/*Flow - Edmonds-karp*/
/*Based on UVa820*/
#define inf 1000000
```

```
int getMaxFlow(vector<vector<int>> &capacity, int s, int t, int
       n){
   int ans = 0;
   vector<vector<int>> residual(n+1, vector<int>(n+1, 0)); //
        residual network
   while(true){
     vector<int> bottleneck(n+1, 0);
     bottleneck[s] = inf;
     queue<int> q;
     q.push(s);
     vector<int> pre(n+1, 0);
while(!q.empty() && bottleneck[t] == 0){
        int cur = q.front();
        q.pop();
for(int i = 1; i <= n ; i++){</pre>
          if(bottleneck[i] == 0 && capacity[cur][i] > residual[
                cur][i]){
             q.push(i);
             pre[i] = cur:
             bottleneck[i] = min(bottleneck[cur], capacity[cur][i]
                     - residual[cur][i]);
          }
       }
     if(bottleneck[t] == 0) break;
for(int cur = t; cur != s; cur = pre[cur]){
    residual[pre[cur]][cur] += bottleneck[t];
          residual[cur][pre[cur]] -= bottleneck[t];
     ans += bottleneck[t];
   return ans:
int main(){
   int testcase = 1;
   int n;
   while(cin>>n){
     if(n == 0)
        break:
      vector<vector<int>> capacity(n+1, vector<int>(n+1, 0));
     int s, t, c;
cin >> s >> t >> c
     int a, b, bandwidth;
for(int i = 0 ; i < c ; ++i){
   cin >> a >> b >> bandwidth;
        capacity[a][b] += bandwidth;
        capacity[b][a] += bandwidth;
     cout << "Network " << testcase++ << endl;
cout << "The bandwidth is " << getMaxFlow(capacity, s, t, n
    ) << "." << endl;</pre>
     cout << endl;</pre>
   return 0;
}
```

3.3 hungarian

```
*bipartite - hungarian*/
 struct Graph{
      static const int MAXN = 5003;
      vector<int> G[MAXN];
      int n, match[MAXN], vis[MAXN];
      void init(int _n){
           n = _n;
           for (int i=0; i<n; i++) G[i].clear();</pre>
      bool dfs(int u){
                for (int v:G[u]){
                if (vis[v]) continue;
                vis[v]=true:
                if (match[v]==-1 || dfs(match[v])){
    match[v] = u;
                     match[u] = v;
                     return true;
                }
           return false;
      int solve(){
           int res = 0;
           memset(match,-1,sizeof(match));
for (int i=0; i<n; i++){
    if (match[i]==-1){</pre>
                     memset(vis,0,sizeof(vis));
if ( dfs(i) ) res++;
                }
           }
           return res;
      }
} graph;
```

3.4 Maximum_matching

/*bipartite - maximum matching*/

```
bool dfs(vector<vector<bool>> res,int node,vector<int>& x,
    vector<int>& y, vector<bool> pass){
    for (int i = 0; i < res[0].size(); i++){</pre>
             if(res[node][i] && !pass[i]){
                   if(y[i] = true;
if(y[i] == -1 || dfs(res,y[i],x,y,pass)){
    x[node] = i;
    y[i] = node;
                          return true;
                   }
            }
      }
      return false:
int main(){
      while(cin>>n>>m>>l){
             vector<vector<bool>> res(n, vector<bool>(m, false));
for (int i = 0; i < 1; i++){</pre>
                   int a, b;
cin >> a >> b;
                   res[a][b] = true;
             int ans = 0;
            int ans = 0;
vector<int> x(n, -1);
vector<int> y(n, -1);
for (int i = 0; i < n; i++){
    vector<bool> pass(n, false);
}
                   if(dfs(res,i,x,y,pass))
                         ans += 1;
             cout << ans << endl;
      return 0;
input:
4 3 5 //n matching m, 1 links
0 0
1 0
2 1
3 1
answer is 3
```

3.5 MFlow Model

```
typedef long long 11;
struct MF
     static const int N = 5000 + 5;
     static const int M = 60000 + 5
     static const 11 oo = 100000000000000L;
     int n, m, s, t, tot, tim;
     int first[N], next[M];
int u[M], v[M], cur[N], vi[N];
ll cap[M], flow[M], dis[N];
     int que[N + N];
     void Clear()
     {
          tot = 0;
          tim = 0;
for (int i = 1; i <= n; ++i)
    first[i] = -1;
     void Add(int from, int to, ll cp, ll flw)
          u[tot] = from;
          v[tot] = to;
cap[tot] = cp;
flow[tot] = flw;
next[tot] = first[u[tot]];
          first[u[tot]] = tot;
          ++tot;
     bool bfs()
     {
          ++tim;
          dis[s] = 0;
          vi[s] = tim;
          int head, tail;
          head = tail = 1;
que[head] = s;
          while (head <= tail)</pre>
               for (int i = first[que[head]]; i != -1; i = next[i
                    if (vi[v[i]] != tim && cap[i] > flow[i])
                         vi[v[i]] = tim;
                         dis[v[i]] = dis[que[head]] + 1;
                         que[++tail] = v[i];
```

```
}
                 ++head;
           return vi[t] == tim;
      11 dfs(int x, 11 a)
           if (x == t || a == 0)
           return a;
11 flw = 0, f;
int &i = cur[x];
           for (i = first[x]; i != -1; i = next[i])
                if (dis[x] + 1 == dis[v[i]] && (f = dfs(v[i], min(a
        , cap[i] - flow[i]))) > 0)
                     flow[i] += f;
flow[i ^ 1] -= f;
                     a -= f;
flw += f;
                     if (a == 0)
                           break;
                }
           return flw;
      11 MaxFlow(int s, int t)
           this->s = s:
           this->t = t;
           11 \text{ flw} = 0;
           while (bfs())
                for (int i = 1; i <= n; ++i)
    cur[i] = 0;</pre>
                flw += dfs(s, oo);
           return flw;
     }
};
// MF Net;
// Net.n = n;
// Net.Clear();
// a 到 b (注意從1開始!!!!)
// Net.Add(a, b, w, 0);
// Net.MaxFlow(s, d)
// s 到 d 的 MF
```

4 Geometry

4.1 Circle Intersect

```
bool same(double a, double b)
{
         return abs(a - b) < 0;</pre>
}
struct P
       double x, y;
P() : x(0), y(0) {}
P(double x, double y) : x(x), y(y) {}
P operator+(P b) { return P(x + b.x, y + b.y); }
P operator-(P b) { return P(x - b.x, y - b.y); }
P operator*(double b) { return P(x * b, y * b); }
P operator/(double b) { return P(x / b, y / b); }
double operator*(P b) { return x * b.x + y * b.y; }
// double operator^(P b) { return x * b.y - y * b.x; }
double abs() { return hypot(x, y); }
        double abs() { return hypot(x, y); }
P unit() { return *this / abs(); }
        P rot(double o)
                 double c = cos(o), s = sin(o);
return P(c * x - s * y, s * x + c * y);
         double angle() { return atan2(y, x); }
};
struct C
{
        C(P c = P(0, 0), double r = 0) : c(c), r(r) {}
vector<P> Intersect(C a, C b)
         if(a.r > b.r)
        swap(a, b);
double d = (a.c - b.c).abs();
vector<P> p;
        if (same(a.r + b.r, d))
    p.pb(a.c + (b.c - a.c).unit() * a.r);
else if (a.r + b.r > d && d + a.r >= b.r)
                 double o = acos((sqrt(a.r) + sqrt(d) - sqrt(b.r)) / (2
    * a.r * d));
```

6

```
NCNU - No idea codebook
                                                                                R.y = (a * a * p.y - b * b * p.y - 2 * a * b * p.x - 2
        P i = (b.c - a.c).unit();
p.pb(a.c + i.rot(o) * a.r);
p.pb(a.c + i.rot(-o) * a.r);
                                                                                     * b * c) / d;
                                                                                return R;
    return p;
                                                                            bool equal(const line &1) const
                                                                            { //直線相等
                                                                                return ori(1.p1) == 0 && ori(1.p2) == 0;
4.2 Closest Pair
                                                                            bool parallel(const line &1) const
//最近點對 (距離) //台大
                                                                                return (p1 - p2).cross(l.p1 - l.p2) == 0;
vector<pair<double, double>> p;
double closest_pair(int 1, int r)
                                                                            bool cross_seg(const line &1) const
     // p 要對 x 軸做 sort
                                                                                return (p2 - p1).cross(l.p1 - p1) * (p2 - p1).cross(l.
    if (1 == r)
                                                                                      p2 - p1) <= 0; //直線是否交線段
         return 1e9;
    if (r - 1 == 1)
                                                                            int line_intersect(const line &1) const
        return dist(p[l], p[r]); // 兩點距離
                                                                            { //直線相交情況·-1無限多點、1交於一點、0不相交
     int m = (1 + r) >> 1;
                                                                                return parallel(1) ? (ori(1.p1) == 0 ? -1 : 0) : 1;
    double d = min(closest_pair(1, m), closest_pair(m + 1, r));
    for (int i = m; i >= 1 && fabs(p[m].x - p[i].x) < d; --i)</pre>
                                                                            int seg intersect(const line &1) const
         vec.push_back(i);
                                                                                T c1 = ori(1.p1), c2 = ori(1.p2);
     for (int i = m + 1; i <= r && fabs(p[m].x - p[i].x) < d; ++
                                                                                T c3 = 1.ori(p1), c4 = 1.ori(p2);
if (c1 == 0 && c2 == 0)
          i)
         vec.push_back(i);
                                                                                { //共線
    bool b1 = btw(1.p1) \Rightarrow= 0, b2 = btw(1.p2) \Rightarrow= 0;
                                                                                     T a3 = 1.btw(p1), a4 = 1.btw(p2);
if (b1 && b2 && a3 == 0 && a4 >= 0)
                                                                                         return 2;
                                                                                     if (b1 && b2 && a3 >= 0 && a4 == 0)
             d = min(d, dist(p[vec[i]], p[vec[j]]));
                                                                                         return 3;
    return d;
                                                                                     if (b1 && b2 && a3 >= 0 && a4 >= 0)
}
                                                                                         return 0;
                                                                                     return -1; //無限交點
4.3 Line
                                                                                else if (c1 * c2 <= 0 && c3 * c4 <= 0)
                                                                                     return 1;
template <typename T>
                                                                                return 0; //不相交
struct line
    line() {}
                                                                            point<T> line intersection(const line &1) const
                                                                            { /*直線交點*/
    point<T> p1, p2;
T a, b, c; //ax+by+c=0
line(const point<T> &x, const point<T> &y) : p1(x), p2(y)
                                                                                point<T> a = p2 - p1, b = l.p2 - l.p1, s = l.p1 - p1;
                                                                                // if (a.cross(b) == 0)
                                                                                        return INF;
         {}
    void pton()
                                                                                return p1 + a * (s.cross(b) / a.cross(b));
    { //轉成一般式
        a = p1.y - p2.y;
b = p2.x - p1.x;
c = -a * p1.x - b * p1.y;
                                                                            point<T> seg_intersection(const line &1) const
                                                                            { //線段交點
                                                                                int res = seg_intersect(1);
    }
T ori(const point<T> &p) const
                                                                                if (res <= 0)
                                                                                     assert(0);
    { //點和有向直線的關係 > 0左邊 、= 0在線上 < 0右邊
                                                                                if (res == 2)
                                                                                     return p1;
         return (p2 - p1).cross(p - p1);
                                                                                if (res == 3)
     T btw(const point<T> &p) const
                                                                                     return p2;
    { //點投影落在線段上<=0
                                                                                return line_intersection(1);
                                                                            }
         return (p1 - p).dot(p2 - p);
                                                                       };
     bool point_on_segment(const point<T> &p) const
    { //點是否在線段上
                                                                        4.4 max_cover_rectangle
         return ori(p) == 0 && btw(p) <= 0;</pre>
                                                                        const double PI = atan2(0.0, -1.0);
    T dis2(const point<T> &p, bool is_segment = 0) const
                                                                        const double eps = 1e-10;
    { //點跟直線/線段的距離平方
                                                                        typedef point<double> p; // data type 依照題目更改
         point<T> v = p2 - p1, v1 = p - p1;
                                                                        int mycmp(double a) { return fabs(a) < eps ? 0 : (a < 0 ? -1 :
         if (is_segment)
                                                                             1); }
                                                                        point<T> v2 = p - p2;
if (v.dot(v1) <= 0)</pre>
                 return v1.abs2();
                                                                        double angle(p a) { return atan2(a.y, a.x); }
                                                                        double angle(p a, p b) { return atan2(a.cy, a.x), }
double angle(p a, p b) { return atan2(a.cross(b), a.dot(b)); }
double turnAngle(p a, p b) { return mycmp(a.dot(b)) == 1 ?
    angle(a, b) : PI + angle(a, b); }
double distanceOfpAndLine(p a, p b, p c) { return fabs((b - a).
    cross(c - a) / Length(b - c)); }
             if (v.dot(v2) >= 0)
                 return v2.abs2();
         T \text{ tmp} = v.cross(v1);
        return tmp * tmp / v.abs2();
                                                                        double Area(int a, int b, int c, int d, p ab, p cd, polygon<
    T seg_dis2(const line<T> &1) const
                                                                             double> po)
    { //兩線段距離平方
         return min({dis2(1.p1, 1), dis2(1.p2, 1), 1.dis2(p1, 1)
                                                                            double h1 = distanceOfpAndLine(po.p[a], po.p[b], po.p[b] +
             , l.dis2(p2, 1)});
                                                                                 ab):
                                                                            double h2 = distanceOfpAndLine(po.p[c], po.p[d], po.p[d] +
    point<T> projection(const point<T> &p) const
                                                                                 cd);
                                                                            return h1 * h2;
     { //點對直線的投影
         point<T> n = (p2 - p1).normal();
```

double max_cover_rectangle(polygon<double> po)

return 0; // 沒凸包哪來外包矩形

double Minx = po.p[0].x, Miny = po.p[0].y, Maxx = po.p[0].x

po.p.pb(po.p[0]); int m = po.p.size();

double Max = -1;

, Maxy = po.p[0].y;

if (m < 3)

return p - n * (p - p1).dot(n) / n.abs2();

//點對直線的鏡射·要先呼叫pton轉成一般式

R.x = (b * b * p.x - a * a * p.x - 2 * a * b * p.y - 2 * a * c) / d;

point<T> mirror(const point<T> &p) const

point<T> R;

```
int p1 = 0, p2 = 0, p3 = 0, p4 = 0;
    p v1, v2, ori;
ori = v1 = p(1, 0);
     v2 = p(0, 1);
     for (int i = 1; i < m; i++)
         if (mycmp(Minx - po.p[i].x) == 1)
    Minx = po.p[i].x, p3 = i;
         if (mycmp(Maxx - po.p[i].x) == -1)
              Maxx = po.p[i].x, p4 = i;
         if (mycmp(Miny - po.p[i].y) == 1)
              Miny = po.p[i].y, p1 = i;
         if (mycmp(Maxy - po.p[i].y) == -1)
    Maxy = po.p[i].y, p2 = i;
     while (mycmp(ori.cross(v1)) >= 0)
         double minRad = 1e20;
minRad = min(minRad, turnAngle(v1, po.p[p1 + 1] - po.p[
              p1]));
         minRad = min(minRad, turnAngle(v1 * (-1), po.p[p2 + 1]
               - po.p[p2]));
         minRad = min(minRad, turnAngle(v2 * (-1), po.p[p3 + 1]
               - po.p[p3]));
         minRad = min(minRad, turnAngle(v2, po.p[p4 + 1] - po.p[
         p4]));
double 1 = 0, r = minRad;
         while (mycmp(l - r))
              double len = (r - 1) / 3;
double midl = 1 + len;
              double midr = r - len;
              r = midr;
              else
                  1 = midl;
         Max = max(Max, Area(p1, p2, p3, p4, Rotate(v1, 1),
              Rotate(v2, 1), po));
         v1 = Rotate(v1, minRad);
         v2 = Rotate(v2, minRad);
if (mycmp(angle(v1, po.p[p1 + 1] - po.p[p1])) == 0)
    p1 = (p1 + 1) % m;
         if (mycmp(angle(v1 * (-1), po.p[p2 + 1] - po.p[p2])) ==
         p2 = (p2 + 1) \% m;
if (mycmp(angle(v2 * (-1), po.p[p3 + 1] - po.p[p3])) ==
                0)
              p3 = (p3 + 1) \% m;
         if (mycmp(angle(v2, po.p[p4 + 1] - po.p[p4])) == 0)
    p4 = (p4 + 1) % m;
     return Max;
}
```

4.5 Point

```
const double PI = atan2(0.0, -1.0);
template <typename T>
struct point
    point() {}
    point(const T &x, const T &y) : x(x), y(y) {}
    point operator+(const point &b) const
        return point(x + b.x, y + b.y);
    point operator-(const point &b) const
        return point(x - b.x, y - b.y);
    point operator*(const T &b) const
        return point(x * b, y * b);
   point operator/(const T &b) const
        return point(x / b, y / b);
    bool operator==(const point &b) const
        return x == b.x && y == b.y;
     dot(const point &b) const
    {
        return x * b.x + y * b.y;
     cross(const point &b) const
        return x * b.y - y * b.x;
    point normal() const
```

```
7
    { //求法向量
        return point(-y, x);
    T abs2() const
    { //向量長度的平方
        return dot(*this);
    T rad(const point &b) const
    { //兩向量的弧度
        return fabs(atan2(fabs(cross(b)), dot(b)));
    T getA() const
                            //對x軸的弧度
        T A = atan2(y, x); //超過180度會變負的
if (A <= -PI / 2)
A += PI * 2;
        return A;
4.6 Polygon
template <tvpename T>
struct polygon
{
    polygon() {}
    vector<point<T>> p; //逆時針順序
    T area() const
    { //面積
        T ans = 0;
        for (int i = p.size() - 1, j = 0; j < (int)p.size(); i</pre>
             = j++)
            ans += p[i].cross(p[j]);
        return ans / 2;
    point<T> center_of_mass() const
    { //重心
        T cx = 0, cy = 0, w = 0;
for (int i = p.size() - 1, j = 0; j < (int)p.size(); i
             = j++)
            T a = p[i].cross(p[j]);
cx += (p[i].x + p[j].x)
            cy += (p[i].y + p[j].y) * a;
        return point<T>(cx / 3 / w, cy / 3 / w);
    char ahas(const point<T> &t) const
    { //點是否在簡單多邊形內,是的話回傳1、在邊上回傳-1、否則回
        bool c = 0;
        for (int i = 0, j = p.size() - 1; i < p.size(); j = i</pre>
             ++)
            if (line<T>(p[i], p[j]).point_on_segment(t))
                return -1
            c = !c;
        return c;
    char point_in_convex(const point<T> &x) const
        int 1 = 1, r = (int)p.size() - 2;
        while (1 <= r)
        { //點是否在凸多邊形內,是的話回傳1、在邊上回傳-1、否則
             回傳0
            int mid = (1 + r) / 2;
            T a1 = (p[mid] - p[0]).cross(x - p[0]);
T a2 = (p[mid + 1] - p[0]).cross(x - p[0]);
            if (a1 >= 0 && a2 <= 0)
                T res = (p[mid + 1] - p[mid]).cross(x - p[mid])
                return res > 0 ? 1 : (res >= 0 ? -1 : 0);
            else if (a1 < 0)
                r = mid - 1;
            else
                1 = mid + 1;
        return 0;
    vector<T> getA() const
{//凸包邊對x軸的夾角
        vector<T> res; //一定是遞增的
for (size_t i = 0; i < p.size(); ++i)
            res.push_back((p[(i + 1) % p.size()] - p[i]).getA()
        return res;
    bool line_intersect(const vector<T> &A, const line<T> &1)
```

{ //O(logN)

```
int f1 = upper_bound(A.begin(), A.end(), (1.p1 - 1.p2).
    getA()) - A.begin();
     int f2 = upper_bound(A.begin(), A.end(), (1.p2 - 1.p1).
          getA()) - A.begin();
     return 1.cross_seg(line<T>(p[f1], p[f2]));
polygon cut(const line<T> &1) const
{ //凸包對直線切割,得到直線1左側的凸包
    polygon ans;
     for (int n = p.size(), i = n - 1, j = 0; j < n; i = j
     {
         if (1.ori(p[i]) >= 0)
              ans.p.push_back(p[i]);
              if (1.ori(p[j]) < 0)
    ans.p.push_back(1.line_intersection(line<T</pre>
                       >(p[i], p[j])));
         else if (1.ori(p[j]) > 0)
    ans.p.push_back(1.line_intersection(line<T>(p[i
                   ], p[j])));
     return ans;
static bool Andrew_Monotone_Chain_angle(const point<T> &a,
const point<T> &b)
{ //凸包排序函數 // 起始點不同
     return (a.y < b.y) || (a.y == b.y && a.x < b.x); //Y最
          小開始
void Andrew_Monotone_Chain(vector<point<T>> &s)
{ // 凸包 Convexhull 2D
     sort(s.begin(), s.end(), Andrew_Monotone_Chain_angle);
     p.resize(s.size() + 1);
    int m = 0;
    // cross >= 0 順時針。cross <= 0 逆時針旋轉
for (size_t i = 0; i < s.size(); ++i)
         while (m >= 2 && (p[m - 1] - p[m - 2]).cross(s[i] - p[m - 2]) <= 0)
              --m;
         p[m++] = s[i];
     for (int i = s.size() - 2, t = m + 1; i >= 0; --i)
         while (m >= t \&\& (p[m - 1] - p[m - 2]).cross(s[i] -
              p[m - 2]) <= 0)
             --m;
         p[m++] = s[i];
     if (s.size() > 1) // 重複頭一次需扣掉
    p.resize(m);
     // p.pb(s[0]); // 需要頭在 pb 回去!!
}
T diam()
{ //直徑
    int n = p.size(), t = 1;
T ans = 0;
    p.push_back(p[0]);
     for (int i = 0; i < n; i++)
         \begin{array}{lll} point<T> \ now = p[i+1] - p[i]; \\ while \ (now.cross(p[t+1] - p[i]) > now.cross(p[t] \end{array}
             - p[i]))
t = (t + 1) % n;
         ans = max(ans, (p[i] - p[t]).abs2());
     return p.pop_back(), ans;
}
T min_cover_rectangle()
                                                                      };
{ // 先做凸包 //最小覆蓋矩形
     int n = p.size(), t = 1, r = 1, l;
     if (n < 3)
         return 0; //也可以做最小周長矩形
                                                                       template <typename T>
    T ans = 1e99;
    p.push_back(p[0]);
for (int i = 0; i < n; i++)
         point<T> now = p[i + 1] - p[i];
while (now.cross(p[t + 1] - p[i]) > now.cross(p[t])
              - p[i]))
             t = (t + 1) \% n;
         while (now.dot(p[r + 1] - p[i]) > now.dot(p[r] - p[
              i]))
             r = (r + 1) \% n;
         if (!i)
         1 = r;
while (now.dot(p[l + 1] - p[i]) <= now.dot(p[l] - p</pre>
                                                                            { //重心
              [i]))
             l = (l + 1) \% n;
         T d = now.abs2();
         T \ tmp = now.cross(p[t] - p[i]) * (now.dot(p[r] - p[
              i]) - now.dot(p[1] - p[i])) / d;
```

```
ans = min(ans, tmp);
    return p.pop_back(), ans;
T dis2(polygon &pl)
{ //凸包最近距離平方
    vector<point<T>> &P = p, &Q = pl.p;
    int n = P.size(), m = Q.size(), l = 0, r = 0;
for (int i = 0; i < n; ++i)
    if (P[i].y < P[l].y)</pre>
             l = i;
    for (int i = 0; i < m; ++i)
        if (Q[i].y < Q[r].y)</pre>
    P.push_back(P[0]), Q.push_back(Q[0]);
    T ans = 1e99;
for (int i = 0; i < n; ++i)
         while ((P[1] - P[1 + 1]).cross(Q[r + 1] - Q[r]) <
        0)
r = (r + 1) % m;
ans = min(ans, line<T>(P[1], P[1 + 1]).seg_dis2(
line<T>(Q[r], Q[r + 1])));
    return P.pop_back(), Q.pop_back(), ans;
static char sign(const point<T> &t)
    return (t.y == 0 ? t.x : t.y) < 0;</pre>
static bool angle_cmp(const line<T> &A, const line<T> &B)
    int halfplane_intersection(vector<line<T>> &s)
{ //半平面交
    sort(s.begin(), s.end(), angle_cmp); //線段左側為該線段
         半平面
    int L, R, n = s.size();
vector<point<T>> px(n);
    vector<line<T>> q(n);
    q[L = R = 0] = s[0];
     or (int i = 1; i < n; ++i)
         while (L < R \&\& s[i].ori(px[R - 1]) <= 0)
         while (\hat{L} < R \&\& s[i].ori(px[L]) <= 0)
         ++L;
q[++R] = s[i];
         if (q[R].parallel(q[R - 1]))
        {
             if (q[R].ori(s[i].p1) > 0)
                 q[R] = s[i];
         if (L < R)
             px[R - 1] = q[R - 1].line_intersection(q[R]);
    while (L < R \&\& q[L].ori(px[R - 1]) <= 0)
         - - R :
    p.clear();
    if (R - L <= 1)
    return 0;
px[R] = q[R].line_intersection(q[L]);
    for (int i = L; i <= R; ++i)
p.push_back(px[i]);
    return R - L + 1;
```

Triangle

```
struct triangle
    point<T> a, b, c;
    triangle() {{}
triangle(const point<T> &a, const point<T> &b, const point
          T> &c) : a(a), b(b), c(c) {}
    T area() const
         T t = (b - a).cross(c - a) / 2;
return t > 0 ? t : -t;
    point<T> barycenter() const
         return (a + b + c) / 3;
    point<T> circumcenter() const
    { //外心
         static line<T> u, v;
         u.p1 = (a + b) / 2;
```

5 Graph

5.1 Bellman-Ford

```
*SPA - Bellman-Ford*/
#define inf 99999 //define by you maximum edges weight
vector<vector<int> > edges;
vector<int> dist;
vector<int> ancestor;
if(dist[i] + edges[i][j] < dist[j]){
    dist[j] = dist[i] + edges[i][j];</pre>
                           ancestor[j] = i;
                       }
                  }
             }
         }
    }
    for(int i = 0; i < node; i++) //negative cycle detection</pre>
         for(int j = 0; j < node;</pre>
                                     j++)
             if(dist[i] + edges[i][j] < dist[j])</pre>
                  cout<<"Negative cycle!"<<endl;</pre>
                  return:
             }
int main(){
    int node;
    cin>>node:
    edges.resize(node, vector<int>(node,inf));
    dist.resize(node,inf);
    ancestor.resize(node,-1);
    int a,b,d;
    while(cin>>a>>b>>d){
         /*input: source destination weight*/
if(a == -1 && b == -1 && d == -1)
             break;
         edges[a][b] = d;
    int start;
    cin>>start:
    BellmanFord(start, node);
    return 0;
```

5.2 BFS-queue

```
void BFS(vector<int> &result, vector<pair<int, int>> edges, int
     node, int start)
   vector<int> pass(node, 0);
   queue<int> q;
    queue<int> p;
    q.push(start);
    int count = 1;
   vector<pair<int, int>> newedges;
   while (!q.empty())
        pass[q.front()] = 1;
        for (int i = 0; i < edges.size(); i++)
            if (edges[i].first == q.front() && pass[edges[i].
                 second] == 0)
                p.push(edges[i].second);
                result[edges[i].second] = count;
            }
```

```
else if (edges[i].second == q.front() && pass[edges
                 [i].first] == 0)
             {
                 p.push(edges[i].first);
                 result[edges[i].first] = count;
             else
                 newedges.push_back(edges[i]);
        edges = newedges;
        newedges.clear();
        q.pop();
        if (q.empty() == true)
             q = p;
             queue<int> tmp;
            p = tmp;
             count++;
    }
int main()
    int node;
    cin >> node:
    vector<pair<int, int>> edges;
    int a, b;
    while (cin >> a >> b)
        /*a = b = -1 means input edges ended*/
if (a == -1 && b == -1)
            break:
        edges.push_back(pair<int, int>(a, b));
    vector<int> result(node, -1);
    BFS(result, edges, node, 0);
    return 0:
```

5.3 DFS-rec

```
/*DFS - Recursive version*/
map<pair<int,int>,int> edges;
vector<int> pass;
vector<int> route;
void DFS(int start){
    pass[start] = 1;
map<pair<int,int>,int>::iterator iter;
     for(iter = edges.begin(); iter != edges.end(); iter++){
   if((*iter).first.first == start && (*iter).second == 0
              && pass[(*iter).first.second] == 0){
route.push_back((*iter).first.second);
              DFS((*iter).first.second);
         else if((*iter).first.second == start && (*iter).second
                == 0 && pass[(*iter).first.first] == 0){
               route.push_back((*iter).first.first);
              DFS((*iter).first.first);
         }
    }
int main(){
     cin>>node;
     pass.resize(node,0);
     int a,b;
     while(cin>>a>>b){
         if(a == -1 && b == -1)
break;
          edges.insert(pair<pair<int,int>,int>(pair<int,int>(a,b)
               ,0));
     int start:
     cin>>start;
     route.push_back(start);
     DFS(start);
    return 0;
```

5.4 Dijkstra

```
/*SPA - Dijkstra*/
const int MAXN = 1e5 + 3;
const int inf = INT_MAX;
typedef pair<int, int> pii;
vector<vector<pre>vectorvector<int> isDone(MAXN, false), dist, ancestor;
void dijkstra(int s)
{
    priority_queuevectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvectorvect
```

```
pq.pop();
    isDone[u] = true;

    for (auto &pr : weight[u])
    {
        int v = pr.first, w = pr.second;

        if (!isDone[v] && dist[u] + w < dist[v])
        {
            dist[v] = dist[u] + w;
            pq.push(pii(dist[v], v));
            ancestor[v] = u;
        }
    }
}
// weight[a - 1].push_back(pii(b - 1, w));
// weight[b - 1].push_back(pii(a - 1, w));
// dist.resize(n, inf);
// ancestor.resize(n, -1);
// dist[0] = 0;
// dijkstra(0);</pre>
```

5.5 Euler circuit

```
/*Euler circuit*/
/*From NTU kiseki*/
/*G is graph, vis is visited, la is path*/
bool vis[N];
size_t la[K];
void dfs(int u, vector<int> &vec)
{
    while (la[u] < G[u].size())
    {
        if (vis[G[u][la[u]].second])
        {
            ++la[u];
            continue;
        }
        int v = G[u][la[u]].first;
        vis[G[u][la[u]].second] = true;
        ++la[u];
        dfs(v, vec);
        vec.push_back(v);
    }
}</pre>
```

5.6 Floyd-warshall

```
/*SPA - Floyd-Warshall*/
// 有向圖,正邊
                    O(V^3)
// 有向圖,無負環
                    O(V3)
// 有向圖,有負環
                    不適用
// 無向圖,正邊
// 無向圖,無負環
                    不適用
// 無向圖,有負環
                   不適用
/*Find min weight cycle*/
#define inf 99999
void floyd_warshall(vector<vector<int>> &distance, vector<</pre>
     vector<int>> &ancestor, int n)
    for (int k = 0; k < n; k++)
         for (int i = 0; i < n; i++)
             for (int j = 0; j < n; j++)
                 if (distance[i][k] + distance[k][j] < distance[</pre>
                      i][j])
                 {
                     distance[i][j] = distance[i][k] + distance[
                          k][j];
                     ancestor[i][j] = ancestor[k][j];
                 }
            }
        }
    }
vector<vector<int>> distance(n, vector<int>(n, inf));
vector<vector<int>> ancestor(n, vector<int>(n, -1));
distance[a][b] = w;
ancestor[a][b] = w;
floyd_warshall(distance, ancestor, n);
/*Negative cycle detection*
for (int i = 0; i < n; i++)</pre>
    if (distance[i][i] < 0)</pre>
         cout << "Negative cycle!" << endl;</pre>
}
```

5.7 Hamilton_cycle

```
/*find hamilton cycle*/
cout << cur << " "
                  cur = solution[cur];
              cout << cur << endl;
              flag = true;
              return;
         }
     for (int i = 0; i < gp[cur].size() && !flag; i++){
   if(gp[cur][i] == 1 && !pass[i]){
     pass[i] = true;</pre>
              solution[i] = cur;
              hamilton(gp, k + 1, i, solution, pass,flag);
pass[i] = false;
    }
int main(){
     int n;
     while(cin>>n){
         int a,b;
bool end = false;
vector<vector<int>> gp(n+1,vector<int>(n+1,0));
         while(cin>>a>>b){
              if(a == 0 \&\& b == 0)
              break;
gp[a][b] = 1;
              gp[b][a] = 1;
         vector<int> solution(n + 1, -1);
         vector<bool> pass(n + 1, false);
         solution[1] = 0;
         pass[1] = true;
bool flag = false;
         hamilton(gp, 1,1 ,solution,pass,flag);
         if(!flag)
              cout << "N" << endl;</pre>
     return 0;
}
/*
1 2
2
  3
2 4
3 4
3 1
output: 1 3 4 2 1
```

5.8 Kruskal

```
struct edges{
      int from;
      int to:
     int weight;
friend bool operator < (edges a, edges b){</pre>
           return a.weight > b.weight;
int find(int x,vector<int>& union_set){
     if(x != union_set[x])
    union_set[x] = find(union_set[x], union_set);
return union_set[x];
void merge(int a,int b,vector<int>& union_set){
     int pa = find(a, union_set);
int pb = find(b, union_set);
      if(pa != pb)
           union set[pa] = pb;
void kruskal(priority_queue<edges> pq,int n){
      vector<int> union_set(n, 0);
for (int i = 0; i < n; i++)</pre>
      union_set[i] = i;
int edge = 0;
int cost = 0; //evaluate cost of mst
     while(!pq.empty() && edge < n - 1){
  edges cur = pq.top();
  int from = find(cur.from, union_set);
  int to = find(cur.to, union_set);</pre>
           if(from != to){
                  merge(from, to, union_set);
                  edge += 1;
                  cost += cur.weight;
```

```
pq.pop();
    if(edge < n-1)</pre>
         cout << "No mst" << endl;
         cout << cost << endl:
int main(){
    int n;
    cin >> n;
    int a, b, d;
    priority_queue<edges> pq;
    while(cin>>a>>b>>d){
    if(a == -1 && b == -1 && d == -1)
             break;
         edges tmp;
         tmp.from = a;
         tmp.to = b;
tmp.weight = d;
         pq.push(tmp);
     kruskal(pq, n);
    return 0;
}
```

5.9 Minimum Weight Cycle

```
// 最小環
// 圖上無負環!!!!
#define INF 99999
vector<vector<int>> w, d, p;
vector<int> cycle;
int c = 0;
void trace(int i, int j)
    cycle[c++] = i;
    if (i != j)
        trace(p[i][j], j);
void init(int n)
    for (int i = 0; i < n; ++i)</pre>
        d[i][i] = 0;
void minimum_cycle(int n)
    int weight = 1e9;
    for (int k = 0; k < n; ++k)
    {
         for (int i = 0; i < k; ++i)
             for (int j = 0; j < k; ++j)
if (i != j)
                      if (w[k][i] + d[i][j] + w[j][k] < weight)
                          weight = w[k][i] + d[i][j] + w[j][k];
                          c = 0:
                          trace(i, j);
                          cycle[c++] = k;
                      }
         for (int i = 0; i < n; ++i)
             for (int j = 0; j < n; ++j)</pre>
                 if (d[i][k] + d[k][j] < d[i][j])</pre>
                      d[i][j] = d[i][k] + d[k][j];
                     p[i][j] = p[i][k];
            }
        }
    if (weight == 1e9)
    cout << "No exist";</pre>
    {
        bug(weight);
        bug(c);
        bugarr(cycle);
void simple_minimum_cycle(int n) // No use vector p
    int weight = INF;
    for (int k = 0; k < n; ++k)
    {
         for (int i = 0; i < k; ++i)
             for (int j = 0; j < k; ++j)
if (i != j)
                     weight = min(mp[k][i] + d[i][j] + mp[j][k],
                            weight);
         for (int i = 0; i < n; ++i)</pre>
             for (int j = 0; j < n; ++j)
                 d[i][j] = min(d[i][k] + d[k][j], d[i][j]);
```

```
if (weight == INF)
          cout << "Back to jail\n";
          cout << weight << endl;</pre>
w.resize(n, vector<int>(n, INF));
d.resize(n, vector<int>(n, INF));
p.resize(n, vector<int>(n));
cycle.resize(n);
//Edge input
w[a][b] = w;
d[a][b] = w;
p[a][b] = b;
init(n);
minimum_cycle(n);
5.10 Prim
 *mst - Prim*,
#define inf 99999
struct edges
     int from:
     int to:
     int weight;
friend bool operator<(edges a, edges b)</pre>
          return a.weight > b.weight;
void Prim(vector<vector<int>> gp, int n, int start)
{
     vector<bool> pass(n, false);
     int edge = 0;
int cost = 0; //evaluate cost of mst
     priority_queue<edges> pq;
for (int i = 0; i < n; i++)</pre>
          if (gp[start][i] != inf)
               edges tmp;
               tmp.from = start;
tmp.to = i;
tmp.weight = gp[start][i];
               pq.push(tmp);
     pass[start] = true;
     while (!pq.empty() && edge < n - 1)</pre>
          edges cur = pq.top();
          pq.pop();
          if (!pass[cur.to])
               for (int i = 0; i < n; i++)
                    if (gp[cur.to][i] != inf)
                    {
                         edges tmp;
                         tmp.from = cur.to;
tmp.to = i;
tmp.weight = gp[cur.to][i];
                         pq.push(tmp);
               pass[cur.to] = true;
               edge += 1;
cost += cur.weight;
     if (edge < n - 1)
cout << "No mst" << endl;
     else
          cout << cost << endl;</pre>
int main()
     int n;
     cin >> n;
     int a, b, d;
     vector<vector<int>> gp(n, vector<int>(n, inf));
while (cin >> a >> b >> d)
          if (a == -1 && b == -1 && d == -1)
          break;
if (gp[a][b] > d)
               gp[a][b] = d;
     Prim(gp, n, 0);
     return 0;
5.11 Union_find
```

```
// union_find from 台大
vector<int> father;
```

```
vector<int> people:
void init(int n)
    for (int i = 0; i < n; i++)</pre>
        father[i] = i:
        people[i] = 1;
int Find(int x)
    if (x != father[x])
        father[x] = Find(father[x]);
    return father[x];
void Union(int x, int y)
    int m = Find(x):
    int n = Find(y);
    if (m != n)
        father[n] = m;
        people[m] += people[n];
}
```

6 Mathematics

6.1 Catalan

Catalan number

```
• 0~19項的catalan number \circ 1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 16796, 58786, \\ 208012, 742900, 2674440, 9694845, 35357670, 129644790, \\ 477638700, 1767263190 \\ \circ 公式: <math>C_n = \frac{1}{n+1} \binom{2n}{n} = \frac{(2n)!}{(n+1)!n!}
```

6.2 Combination

6.3 CRT

```
// 中國剩餘定理
template <typename T>
tuple<T, T, T> extgcd(T a, T b)
         return make_tuple(a, 1, 0);
    T d, x, y;
    tie(d, x, y) = extgcd(b, a % b);
    return make_tuple(d, y, x - (a / b) * y);
long long crt(vector<int> mod, vector<int> a)
{ // \times \% \text{ mod}[i] = a[i] }
    long long mult = mod[0];
    int n = (int)mod.size();
long long res = a[0];
for (int i = 1; i < n; ++i)</pre>
          long long d, x, y;
tie(d, x, y) = extgcd(mult, mod[i] * 111);
if ((a[i] - res) % d)
               return -1:
          long long new_mult = mult / __gcd(mult, 1ll * mod[i]) *
                 mod[i];
          res += x * ((a[i] - res) / d) % new_mult * mult %
               new_mult;
          mult = new_mult;
          ((res %= mult) += mult) %= mult;
     return res;
```

6.4 Extended Euclidean

```
// ax + by = gcd(a,b)
pair<long long, long long> extgcd(long long a, long long b)
{
   if (b == 0)
```

```
return \{1, \emptyset\};
long long k = a / b;
pair<long long, long long> p = extgcd(b, a - k * b);
//cout << p.first << " " << p.second << endl;
//cout << "商數(k)= " << k << endl << endl;
return \{p.second, p.first - k * p.second\};
}
int main()
      int a, b;
      cin >> a >> b;
      return 0;
// ax + by = gcd(a,b) * r
/*find |x|+|y| -> min*/
int main()
      long long r, p, q; /*px+qy = r*/
      int cases;
      cin >> cases;
      while (cases--)
            cin >> r >> p >> q;
pair<long long, long long> xy = extgcd(q, p); //(x0,y0)
long long ans = 0, tmp = 0;
             double k, k1;
            long long s, s1;
k = 1 - (double)(r * xy.first) / p;
            s = round(k);
ans = llabs(r * xy.first + s * p) + llabs(r * xy.second
                        s * q);
            k1 = -(double)(r * xy.first) / p;
             s1 = round(k1);
            /*cout << k << endl << k1 << endl;
cout << s << endl << s1 << endl;*/
tmp = llabs(r * xy.first + s1 * p) + llabs(r * xy.
second - s1 * q);
             ans = min(ans, tmp);
            cout << ans << endl;</pre>
      return 0:
```

6.5 Fermat

- $a^{(p-1)} \equiv 1 \pmod{p} \iff a * a^{(p-2)} \equiv 1$ • $a^{(p-2)} \equiv 1/a$
- 同餘因數定理
 - $\circ \ a \equiv b \ (mod \ p) \iff k|a-b|$
- 同餘加法性質
 - $\circ \ a \equiv b \ (mod \ p) \ \text{and} \ c \equiv d \ (mod \ p)$ $<=> \ a+c \equiv b+d \ (mod \ p)$
- 同餘相乘性質
 - $\circ \ a \equiv b \ (mod \ p) \ \text{and} \ c \equiv d \ (mod \ p)$ $<=> \ ac \equiv bd \ (mod \ p)$
- 同餘次方性質
 - $\circ \ a \equiv b \ (mod \ p) <=> \ a^n \equiv b^n \ (mod \ p)$
- 同餘倍方性質
 - $\circ \ a \equiv b \ (mod \ p) <=> \ am \equiv bm \ (mod \ p)$

6.6 Hex to Dec

```
int HextoDec(string num) //16 to 10
{
   int base = 1;
   int temp = 0;
   for (int i = num.length() - 1; i >= 0; i--)
   {
      if (num[i] >= '0' && num[i] <= '9')
      {
        temp += (num[i] - 48) * base;
        base = base * 16;
      }
   else if (num[i] >= 'A' && num[i] <= 'F')
      {
        temp += (num[i] - 55) * base;
        base = base * 16;
   }
}</pre>
```

```
}
return temp;
}
void DecToHex(int p) //10 to 16
{
    char *l = new (char);
    sprintf(l, "%X", p);
    //int l_intResult = stoi(l);
    cout << l << "\n";
    //return l_intResult;
}</pre>
```

$6.7 \quad \text{Log}$

```
| double mylog(double a, double base)
|{
| //a 的對數底數 b = 自然對數 (a) / 自然對數 (b)。
| return log(a) / log(base);
|}
```

6.8 Mod 性質

```
加法: (a+b) \mod p = (a \mod p + b \mod p) \mod p
減法: (a-b) \mod p = (a \mod p - b \mod p + p) \mod p
乘法: (a * b) \mod p = (a \mod p \cdot b \mod p) \mod p
次方: (a^b) \operatorname{mod} p = ((a \operatorname{mod} p)^b) \operatorname{mod} p
加法結合律: ((a+b) \operatorname{mod} p + c) \operatorname{mod} p = (a+(b+c)) \operatorname{mod} p
乘法結合律: ((a \cdot b) \operatorname{mod} p \cdot c) \operatorname{mod} p = (a \cdot (b \cdot c)) \operatorname{mod} p
加法交換律: (a+b) \mod p = (b+a) \mod p
乘法交換律: (a \cdot b) \mod p = (b \cdot a) \mod p
結合律: ((a+b) \operatorname{mod} p \cdot c) = ((a \cdot c) \operatorname{mod} p + (b \cdot c) \operatorname{mod} p) \operatorname{mod} p
如果 a \equiv b \pmod{m} ・我們會說 a, b 在模 m 下同餘。
以下為件質:
 • 整除性:a \equiv b \pmod{m} \Rightarrow c \cdot m = a - b, c \in \mathbb{Z}
               \Rightarrow a \equiv b \pmod{m} \Rightarrow m \mid a - b
 • 遞移性: 若a \equiv b \pmod{c}, b \equiv d \pmod{c}
                 則 a \equiv d \pmod{c}
           \left\{ \begin{array}{l} a \equiv b (\operatorname{mod} m) \\ c \equiv d (\operatorname{mod} m) \end{array} \right. \Rightarrow \left\{ \begin{array}{l} a \pm c \equiv b \pm d (\operatorname{mod} m) \\ a \cdot c \equiv b \cdot d (\operatorname{mod} m) \end{array} \right.

    放大縮小模數:

      k \in \mathbb{Z}^+, a \equiv b \pmod{m} \Leftrightarrow k \cdot a \equiv k \cdot b \pmod{k \cdot m}
 模逆元是取模下的反元素,即為找到 a^{-1} 使得 aa^{-1} \equiv 1 \, \mathrm{mod} \, c 。
 整數 a \in \operatorname{mod} c 下要有模反元素的充分必要條件為 a,c 互質。
 模逆元如果存在會有無限個,任意兩相鄰模逆元相差c。
 給定一個質數 p 及一個整數 a · 那麽: a^p \equiv a \pmod{p} 如果 \gcd(a,p) = 1 · 則:
 a^{p-1} \equiv 1 \pmod{p}
 歐拉定理是比較 general 版本的費馬小定理。給定兩個整數 n 和 a · 如果 gcd(a,n)=1 · \emptyset
 a^{\Phi(n)} \equiv 1 \pmod{n} 如果 n 是質數 \cdot \Phi(n) = n-1 \cdot 也就是費馬小定理 \cdot
 Wilson's theorem
 給定一個質數 p \cdot \mathbb{N} : (p-1)! \equiv -1 \pmod{p}
```

6.9 PI

```
#define PI acos(-1)
#define PI M_PI
```

6.10 Pow_Mod

6.11 Prime table

```
6.12 Prime 判斷
typedef long long ll;
ll modmul(ll a, ll b, ll mod)
     11 \text{ ret} = 0;
     for (; b; b >>= 1, a = (a + a) % mod)
if (b & 1)
              ret = (ret + a) % mod;
     return ret;
11 qpow(11 x, 11 u, 11 mod)
     ll ret = 111;
     for (; u; u >>= 1, x = modmul(x, x, mod))
    if (u & 1)
              ret = modmul(ret, x, mod);
     return ret;
}
ll gcd(ll a, ll b)
     return b ? gcd(b, a % b) : a;
11 Pollard Rho(11 n, 11 c)
     ll i = 1, j = 2, x = rand() % (n - 1) + 1, <math>y = x;
     while (1)
         x = (modmul(x, x, n) + c) % n;
ll p = gcd((y - x + n) % n, n);
if (p != 1 && p != n)
              return p;
          if (y == x)
               return n;
         if (i == j)
         {
              y = x;
              j <<= 1;
    }
bool Miller_Rabin(ll n)
     11 x, pre, u = n - 1;
     int i, j, k = 0;
if (n == 2 || n == 3 || n == 5 || n == 7 || n == 11)
          return 1
     return 1;
if (n == 1 || !(n % 2) || !(n % 3) || !(n % 5) || !(n % 7)
          || !(n % 11))
          return 0;
     while (!(u & 1))
         k++;
         u >>= 1;
     srand((long long)12234336);
     for (i = 1; i <= 50; i++)
          x = rand() % (n - 2) + 2;
         if (!(n % x))
              return 0:
          x = qpow(x, u, n);
         pre = x;
          for (j = 1; j <= k; j++)
              x = modmul(x, x, n);
if (x == 1 && pre != 1 && pre != n - 1)
                   return 0;
              pre = x;
          if (x != 1)
               return 0;
```

```
return 1;
}
// if (Miller_Rabin(n)) puts("Prime");
```

6.13 Round(小數)

```
double myround(double number, unsigned int bits)
{
    LL integerPart = number;
    number -= integerPart;
    for (unsigned int i = 0; i < bits; ++i)
        number *= 10;
    number = (LL)(number + 0.5);
    for (unsigned int i = 0; i < bits; ++i)
        number /= 10;
    return integerPart + number;
}
//printf("%.1f\n", round(3.4515239, 1));</pre>
```

6.14 二分逼近法

```
#define eps 1e-14
void half_interval()
{

    double L = 0, R = /*區間*/, M;
    while (R - L >= eps)
    {

        M = (R + L) / 2;
        if (/*函數*/ > /*方程式目標*/)
            L = M;
        else
            R = M;
    }
    printf("%.3lf\n", R);
}
```

6.15 公式

```
S_n = \frac{a(1-r^n)}{1-r} \ a_n = \frac{a_1 + a_n}{2} \sum_{k=1}^n k = \frac{n(n+1)}{2} \sum_{k=1}^n k^2 = \frac{n(n+1)(2n+1)}{6}\sum_{k=1}^n k^3 = \left[\frac{n(n+1)}{2}\right]^2
```

6.16 四則運算

```
string s = ""; //開頭是負號要補0
long long int DFS(int le, int ri) // (0, string final index)
     int c = 0:
     for (int i = ri; i >= le; i--)
           if (s[i] == ')')
           if (s[i] == '(')
           if (s[i] == '+' && c == 0)
    return DFS(le, i - 1) + DFS(i + 1, ri);
if (s[i] == '-' && c == 0)
                return DFS(le, i - 1) - DFS(i + 1, ri);
     for (int i = ri; i >= le; i--)
           if (s[i] == ')')
                c++;
           if (s[i] == '(')
          c--;
if (s[i] == '*' && c == 0)
    return DFS(le, i - 1) * DFS(i + 1, ri);
if (s[i] == '/' && c == 0)
    return DFS(le, i - 1) / DFS(i + 1, ri);
if (s[i] == '%' && c == 0)
                return DFS(le, i - 1) % DFS(i + 1, ri);
     if ((s[le] == '(') && (s[ri] == ')'))
     return DFS(le + 1, ri - 1); //去除刮號
if (s[le] == ' ' && s[ri] == ' ')
         return DFS(le + 1, ri - 1); //去除左右兩邊空格(s[le] == ' ')
           return DFS(le + 1, ri); //去除左邊空格
     if (s[ri] == '
     return DFS(le, ri - 1); //去除右邊空格
long long int num = 0;
for (int i = le; i <= ri; i++)
           num = num * 10 + s[i] - '0';
     return num;
```

6.17 因數表

```
const int limit = 10000000;
vector<vector<int>> arr(limit);
for (int i = 1; i <= limit; i++)
{
    for (int j = i; j <= limit; j += i)
        arr[j].pb(i); // i 為因數
}</pre>
```

6.18 數字乘法組合

```
void dfs(int j, int old, int num, vector<int> com, vector<</pre>
       vector<int>> &ans)
      for (int i = j; i <= sqrt(num); i++)</pre>
           if (old == num)
                 com.clear();
           if (num % i == 0)
                 vector<int> a;
                 a = com;
                 a.push_back(i);
finds(i, old, num / i, a, ans);
a.push_back(num / i);
                 ans.push_back(a);
     }
vector<vector<int>> ans;
vector<int> zero;
dfs(2, num, num, zero, ans);
/*/num 為 input 數字*/
for (int i = 0; i < ans.size(); i++)</pre>
     for (int j = 0; j < ans[i].size() - 1; j++)
    cout << ans[i][j] << " ";
cout << ans[i][ans[i].size() - 1] << endl;</pre>
```

6.19 數字加法組合

```
void recur(int i, int n, int m, vector<int> &out, vector<vector</pre>
     <int>> &ans)
    if (n == 0)
         for (int i : out)
             if (i > m)
         ans.push back(out);
    for (int j = i; j \leftarrow n; j++)
         out.push_back(j);
         recur(j, n - j, m, out, ans);
out.pop_back();
    }
vector<vector<int>> ans;
vector<int> zero;
recur(1, num, num, zero, ans);
// num 為 input 數字
for (int i = 0; i < ans.size(); i++)
    for (int j = 0; j < ans[i].size() - 1; j++)
        cout << ans[i][j] <<
    cout << ans[i][ans[i].size() - 1] << endl;</pre>
```

6.20 羅馬數字

```
int romanToInt(string s)
{
    unordered_map<char, int> T;
    T['I'] = 1;
    T['Y'] = 5;
    T['X'] = 10;
    T['L'] = 50;
    T['C'] = 100;
    T['D'] = 500;
    T['M'] = 1000;

    int sum = T[s.back()];
    for (int i = s.length() - 2; i >= 0; --i)
    {
        if (T[s[i]] < T[s[i + 1]])
            sum -= T[s[i]];
        else
            sum += T[s[i]];
    }
    return sum;</pre>
```

6.21 質因數分解

```
質數數量
6.22
// 10 ^ 11 左右
#define LL long long
const int N = 5e6 + 2;
bool np[N];
int prime[N], pi[N];
int getprime()
     int cnt = 0:
     np[0] = np[1] = true;
pi[0] = pi[1] = 0;
for (int i = 2; i < N; ++i)</pre>
           if (!np[i])
                 prime[++cnt] = i;
           pi[i] = cnt;
for (int j = 1; j <= cnt && i * prime[j] < N; ++j)</pre>
                 np[i * prime[j]] = true;
                    (i % prime[j] == 0)
                      break;
           }
     return cnt;
const int M = 7;
const int PM = 2 * 3 * 5 * 7 * 11 * 13 * 17;
int phi[PM + 1][M + 1], sz[M + 1];
void init()
{
     getprime();
      sz[0] = 1;
     for (int i = 0; i <= PM; ++i)
    phi[i][0] = i;
for (int i = 1; i <= M; ++i)</pre>
           sz[i] = prime[i] * sz[i - 1];
for (int j = 1; j <= PM; ++j)
    phi[j][i] = phi[j][i - 1] - phi[j / prime[i]][i -</pre>
     }
int sqrt2(LL x)
     LL r = (LL) sqrt(x - 0.1);
     while (r * r <= x)
          ++r:
     return int(r - 1);
int sqrt3(LL x)
     LL r = (LL)cbrt(x - 0.1);
     while (r * r * r <= x)
           ++r;
     return int(r - 1);
LL getphi(LL x, int s)
     if (s == 0)
           return x;
     if (s <= M)
     return phi[x % sz[s]][s] + (x / sz[s]) * phi[sz[s]][s];
if (x <= prime[s] * prime[s])
    return pi[x] - s + 1;
if (x <= prime[s] * prime[s] * prime[s] && x < N)
           int s2x = pi[sqrt2(x)];
           LL ans = pi[x] - (s2x + s - 2) * (s2x - s + 1) / 2;
for (int i = s + 1; i <= s2x; ++i)
                ans += pi[x / prime[i]];
           return ans;
     return getphi(x, s - 1) - getphi(x / prime[s], s - 1);
LL getpi(LL x)
     if (x < N)
```

```
return pi[x];
     LL ans = getphi(x, pi[sqrt3(x)]) + pi[sqrt3(x)] - 1;
     for (int i = pi[sqrt3(x)] + 1, ed = pi[sqrt2(x)]; i <= ed;
          ++i)
         ans -= getpi(x / prime[i]) - i + 1;
     return ans:
LL lehmer_pi(LL x)
     if(x < N)
         return pi[x];
     int a = (int)lehmer_pi(sqrt2(sqrt2(x)));
     int b = (int)lehmer_pi(sqrt2(x));
int c = (int)lehmer_pi(sqrt3(x));
LL sum = getphi(x, a) + (LL)(b + a - 2) * (b - a + 1) / 2;
     for (int i = a + 1; i <= b; i++)
         LL w = x / prime[i];
sum -= lehmer_pi(w);
         if(i > c)
              continue;
         LL lim = lehmer_pi(sqrt2(w));
         for (int j = i; j <= lim; j++)</pre>
              sum -= lehmer_pi(w / prime[j]) - (j - 1);
     return sum;
// lehmer_pi(n)
```

7 Other

7.1 Binary search 三類變化

```
// 查找和目標值完全相等的數
int find(vector<int> &nums, int target)
    int left = 0, right = nums.size() - 1;
while (left < right)</pre>
         int mid = left + (right - left) / 2;
         if (nums[mid] == target)
             return mid;
        else if (nums[mid] < target)
   left = mid + 1;</pre>
         else
             right = mid;
    return -1;
}
// 找第一個不小於目標值的數 == 找最後一個小於目標值的數
/*(lower_bound)*/
int find(vector<int> &nums, int target)
    int left = 0, right = nums.size() - 1;
    while (left < right)
         int mid = left + (right - left) / 2;
        if (nums[mid] < target)
   left = mid + 1;</pre>
             right = mid;
    return right;
// 找第一個大於目標值的數 == 找最後一個不大於目標值的數
/*(upper_bound)*/
int find(vector<int> &nums, int target)
    int left = 0, right = nums.size() - 1;
    while (left < right)
        int mid = left + (right - left) / 2;
if (nums[mid] <= target)
   left = mid + 1;</pre>
        else
             right = mid;
    return right;
7.2 Heap sort
```

```
void MaxHeapify(vector<int> &array, int root, int length)
{
    int left = 2 * root, right = 2 * root + 1, largest;
    if (left <= length && array[left] > array[root])
        largest = left;
    else
        largest = root;
    if (right <= length && array[right] > array[largest])
        largest = right;
    if (largest != root)
    {
        swap(array[largest], array[root]);
    }
}
```

7.3 Josephus

```
/*n people kill k for each turn*/
int josephus(int n, int k)
{
    int s = 0;
    for (int i = 2; i <= n; i++)
    {
        s = (s + k) % i;
    }
    /*index start from 1 -> s+1*/
    return s + 1;
}
/*died at kth*/
int kth(int n, int m, int k)
{
    if (m == 1)
        return n - 1;
    for (k = k * m + m - 1; k >= n; k = k - n + (k - n) / (m - 1))
        return k;
}
```

7.4 Largest Multi-interval

```
/*多區間算最大值*/
bool name(pii a, pii b)
{ return b.first > a.first;}
vector<pii> data;
data.pb(pii(a, c)); // 區間 a 到 c
sort(data.begin(), data.end(), name); // pair first 從 小 到 大
int 1 = data[0].x, r = data[0].y, res = 0;
for (int i = 1; i < data.size(); i++)</pre>
     if (data[i].x <= r)</pre>
    {
         if (r < data[i].y)</pre>
              r = data[i].y;
    else
    {
         res += r - 1;
          1 = data[i].x;
          r = data[i].y;
    }
res += r - 1; // 最大段落不重疊
```

7.5 Merge sort

```
long long merge(vector<int> &arr, int left, int mid, int right)
     int *tmp = new int[right - left + 1];
     long long sum = 0;
int l = left, r = mid + 1, m = 0;
     while (1 <= mid && r <= right)
           if (arr[1] <= arr[r])
    tmp[m++] = arr[1++];</pre>
           else
           {
                tmp[m++] = arr[r++];
                sum += mid - 1 + 1;
          }
     while (1 <= mid)
           tmp[m++] = arr[1++];
     tmp[m++j - a:,[...,]
while (r <= right)
    tmp[m++] = arr[r++];
for (int i = left; i <= right; ++i)
    arr[i] = tmp[i - left];</pre>
     delete[] tmp;
     return sum:
long long mergesort(vector<int> &arr, int left, int right)
```

```
long long sum = 0;
// left = 0, right = P.size() - 1
if (left < right)
{
    int mid = (left + right) / 2;
    sum = mergesort(arr, left, mid);
    sum += mergesort(arr, mid + 1, right);
    sum += merge(arr, left, mid, right);
}
return sum; // 回傳為 swap 次數</pre>
```

7.6 Quick sort

```
int Partition(vector<int> &arr, int front, int end)
     int pivot = arr[end];
     int i = front -
     for (int j = front; j < end; j++)</pre>
         if (arr[j] < pivot)</pre>
         {
             i++;
             swap(arr[i], arr[j]);
     i++:
     swap(arr[i], arr[end]);
     return i:
void QuickSort(vector<int> &arr, int front, int end)
     // front = 0 , end = arr.size() - 1
     if (front < end)</pre>
         int pivot = Partition(arr, front, end);
         QuickSort(arr, front, pivot - 1);
QuickSort(arr, pivot + 1, end);
}
```

7.7 Sudoku solution

```
int getSquareIndex(int row, int column, int n)
{
    return row / n * n + column / n;
}
bool backtracking(vector<vector<int>> &board, vector<vector<</pre>
     bool>> &rows, vector<vector<bool>> &cols,
                  vector<vector<bool>> &boxs, int index, int n)
    int n2 = n * n;
    int rowNum = index / n2, colNum = index % n2;
    if (index >= n2 * n2)
        return true;
    if (board[rowNum][colNum] != 0)
        return backtracking(board, rows, cols, boxs, index + 1,
    for (int i = 1; i <= n2; i++)
        if (!rows[rowNum][i] && !cols[colNum][i] && !boxs[
             getSquareIndex(rowNum, colNum, n)][i])
            rows[rowNum][i] = true;
            cols[colNum][i] = true;
            boxs[getSquareIndex(rowNum, colNum, n)][i] = true;
            board[rowNum][colNum] = i;
            if (backtracking(board, rows, cols, boxs, index +
                1, n))
return true;
            board[rowNum][colNum] = 0;
            rows[rowNum][i] = false;
            cols[colNum][i] = false;
            boxs[getSquareIndex(rowNum, colNum, n)][i] = false;
        }
    }
    return false;
/*用法 main*/
int n = sqrt(數獨邊長大小) /*e.g. 9*9 n=3*/
vector<vector<int>> board(n * n + 1, vector<int>(n * n + 1, 0))
vector<vector<bool>> isRow(n * n + 1, vector<bool>(n * n + 1,
     false));
vector<vector<bool>> isColumn(n * n + 1, vector<bool>(n * n +
    1, false));
vector<vector<bool>> isSquare(n * n + 1, vector<bool>(n * n +
     1, false));
for (int i = 0; i < n * n; ++i)</pre>
    for (int j = 0; j < n * n; ++j)
```

```
{
    int number;
    cin >> number;
    board[i][j] = number;
    if (number == 0)
        continue;
    isRow[i][number] = true;
    isColumn[j][number] = true;
    isSquare[getSquareIndex(i, j, n)][number] = true;
}

}

if (backtracking(board, isRow, isColumn, isSquare, 0, n))

/*有解答*/
else
/*解答*/
```

7.8 Weighted Job Scheduling

```
struct Job
     int start, finish, profit;
bool jobComparataor(Job s1, Job s2)
     return (s1.finish < s2.finish);</pre>
int latestNonConflict(Job arr[], int i)
     for (int j = i - 1; j >= 0; j--)
          if (arr[j].finish <= arr[i].start)</pre>
               return j;
     return -1:
int findMaxProfit(Job arr[], int n)
{
     sort(arr, arr + n, jobComparataor);
     int *table = new int[n];
table[0] = arr[0].profit;
for (int i = 1; i < n; i++)</pre>
          int inclProf = arr[i].profit;
          int l = latestNonConflict(arr, i);
if (l != -1)
          inclProf += table[1];
table[i] = max(inclProf, table[i - 1]);
     int result = table[n - 1];
     delete[] table;
     return result;
}
```

8 String

8.1 KMP

```
// 用在在一個 S 內查找一個詞 W 的出現位置
void ComputePrefix(string s, int next[])
    int n = s.length();
   int q, k;
next[0] = 0;
    for (k = 0, q = 1; q < n; q++)
        while (k > 0 \&\& s[k] != s[q])
            k = next[k];
        if (s[k] == s[q])
            k++;
        next[q] = k;
void KMPMatcher(string text, string pattern)
    int n = text.length();
    int m = pattern.length();
    int next[pattern.length()];
   ComputePrefix(pattern, next);
    for (int i = 0, q = 0; i < n; i++)
        while (q > 0 && pattern[q] != text[i])
            q = next[q];
        if (pattern[q] == text[i])
            q++;
        if (q == m)
            cout << "Pattern occurs with shift " << i - m + 1</pre>
                 << endl;
       }
   }
```

```
// string s = "abcdabcdebcd";
// string p = "bcd";
// KMPMatcher(s, p);
// cout << end1;</pre>
```

8.2 Min Edit Distance

8.3 Sliding window

```
string minWindow(string s, string t)
     unordered_map<char, int> letterCnt;
     for (int \bar{i} = 0; i < t.length(); i++)
          letterCnt[t[i]]++
     int minLength = INT_MAX, minStart = -1;
int left = 0, matchCnt = 0;
for (int i = 0; i < s.length(); i++)</pre>
          if (--letterCnt[s[i]] >= 0)
               matchCnt++;
          while (matchCnt == t.length())
          {
               if (i - left + 1 < minLength)</pre>
               {
                    minLength = i - left + 1;
minStart = left;
               if (++letterCnt[s[left]] > 0)
                    matchCnt - -;
     return minLength == INT_MAX ? "" : s.substr(minStart,
           minLength);
```

8.4 Split

```
vector<string> mysplit(string s, string d)
{
    int ps = 0, pe, dl = d.length();
    string token;
    vector<string> res;
    while ((pe = s.find(d, ps)) != string::npos)
    {
        token = s.substr(ps, pe - ps);
        ps = pe + dl;
        res.push_back(token);
    }
    res.push_back(s.substr(ps));
    return res;
}
```

9 data structure

9.1 Bigint

```
if (a < 0)
         s = -1;
    while (a)
    {
         push_back(a % BIGMOD);
         a /= BIGMOD;
Bigint(string str)
    s = 1;
    v1 = 0;
    int stPos = 0, num = 0;
    if (!str.empty() && str[0] == '-')
         stPos = 1:
        s = -1;
    for (int i = str.length() - 1, q = 1; i >= stPos; i--)
        num += (str[i] - '0') * q;
if ((q *= 10) >= BIGMOD)
             push_back(num);
             q = 1;
         }
    if (num)
        push_back(num);
    n();
int len() const
    return vl; //return SZ(v);
bool empty() const { return len() == 0; }
void push_back(int x)
    v[vl++] = x; //v.PB(x);
void pop_back()
    vl--; //v.pop_back();
int back() const
    return v[vl - 1]; //return v.back();
void n()
    while (!empty() && !back())
        pop_back();
void resize(int nl)
                           //v.resize(nl);
    fill(v, v + vl, 0); //fill(ALL(v), 0);
void print() const
    if (empty())
    {
         putchar('0');
         return;
    if (s == -1)
        `putchar('-');
    printf("%d", back());
for (int i = len() - 2; i >= 0; i--)
    printf("%.4d", v[i]);
}
friend std::ostream &operator<<(std::ostream &out, const</pre>
     Bigint &a)
{
    if (a.empty())
         out << "0";
         return out;
    if (a.s == -1)
        out << "-
    out << a.back();
    for (int i = a.len() - 2; i >= 0; i--)
         char str[10];
snprintf(str, 5, "%.4d", a.v[i]);
         out << str;
    return out;
int cp3(const Bigint &b) const
    if (s != b.s)
```

```
return s - b.s:
    if (s == -1)
         return -(-*this).cp3(-b);
    if (len() != b.len())
    return len() - b.len(); //int
for (int i = len() - 1; i >= 0; i--)
   if (v[i] != b.v[i])
              return v[i] - b.v[i];
bool operator<(const Bigint &b) const
    return cp3(b) < 0;
bool operator<=(const Bigint &b) const
    return cp3(b) <= 0;</pre>
bool operator == (const Bigint &b) const
    return cp3(b) == 0;
bool operator!=(const Bigint &b) const
    return cp3(b) != 0;
bool operator>(const Bigint &b) const
    return cp3(b) > 0;
bool operator>=(const Bigint &b) const
    return cp3(b) >= 0;
Bigint operator-() const
    Bigint r = (*this);
    r.s = -r.s;
    return r;
Bigint operator+(const Bigint &b) const
    if (s == -1)
    return -(-(*this) + (-b));
if (b.s == -1)
         return (*this) - (-b);
    Bigint r;
int nl = max(len(), b.len());
    r.resize(nl + 1);
for (int i = 0; i < nl; i++)</pre>
         if (i < len())
              r.v[i] +=
         if (i < b.len())</pre>
         r.v[i] += b.v[i];
if (r.v[i] >= BIGMOD)
              r.v[i + 1] += r.v[i] / BIGMOD;
              r.v[i] %= BIGMOD;
    r.n();
    return r:
Bigint operator-(const Bigint &b) const
    if (s == -1)
    return -(-(*this) - (-b));
if (b.s == -1)
         return (*this) + (-b);
    if ((*this) < b)</pre>
         return -(b - (*this));
    Bigint r;
    r.resize(len());
    for (int i = 0; i < len(); i++)</pre>
         r.v[i] += v[i];
         if (i < b.len())</pre>
         r.v[i] -= b.v[i];
if (r.v[i] < 0)
             r.v[i] += BIGMOD;
r.v[i + 1]--;
    r.n();
    return r;
Bigint operator*(const Bigint &b)
    r.resize(len() + b.len() + 1);
r.s = s * b.s;
    for (int i = 0; i < len(); i++)</pre>
         for (int j = 0; j < b.len(); j++)</pre>
```

```
r.v[i + j] += v[i] * b.v[j];
if (r.v[i + j] >= BIGMOD)
                         r.v[i + j + 1] += r.v[i + j] / BIGMOD;
r.v[i + j] %= BIGMOD;
              }
          }
          r.n();
          return r;
     Bigint operator/(const Bigint &b)
          Bigint r;
          r.resize(max(1, len() - b.len() + 1));
          int oriS = s;
          Bigint b2 = b; // b2 = abs(b)
          s = b2.s = r.s = 1;
for (int i = r.len() - 1; i >= 0; i--)
               int d = 0, u = BIGMOD - 1;
               while (d < u)
                    int m = (d + u + 1) >> 1;
r.v[i] = m;
if ((r * b2) > (*this))
                         u = m - 1;
                         d = m;
               r.v[i] = d;
          s = oriS;
r.s = s * b.s;
          r.n();
          return r;
     Bigint operator%(const Bigint &b)
     {
          return (*this) - (*this) / b * b;
};
```

9.2 DisjointSet

```
struct DisjointSet {
      int p[maxn], sz[maxn], n, cc;
vector<pair<int*, int>> his;
       vector<int> sh;
       void init(int _n) {
    n = _n; cc = n;
    for (int i = 0; i < n; ++i) sz[i] = 1, p[i] = i;</pre>
              sh.clear(); his.clear();
       void assign(int *k, int v) {
    his.emplace_back(k, *k);
              *k = v;
       void save() {
              sh.push_back((int)his.size());
      void undo() {
   int last = sh.back(); sh.pop_back();
   while (his.size() != last) {
                    int *k, v;
                     tie(k, v) = his.back(); his.pop_back();
                     *k = v:
             }
       int find(int x) {
   if (x == p[x]) return x;
   return find(p[x]);
      void merge(int x, int y) {
    x = find(x); y = find(y);
    if (x == y) return;
    if (sz[x] > sz[y]) swap(x, y);
    assign(&sz[y], sz[x] + sz[y]);
    assign(**[y], y);
              assign(&p[x], y);
              assign(&cc, cc - 1);
```

9.3 Matirx

```
template <typename T>
struct Matrix
         using rt = std::vector<T>;
using mt = std::vector<rt>;
using matrix = Matrix<T>;
int r, c; // [r][c]
         Matrix(int r, int c) : r(r), c(c), m(r, rt(c)) {}
Matrix(mt a) { m = a, r = a.size(), c = a[0].size(); }
rt & operator[](int i) { return m[i]; }
```

```
matrix operator+(const matrix &a)
            matrix rev(r, c);
            for (int i = 0; i < r; ++i)
    for (int j = 0; j < c; ++j)
        rev[i][j] = m[i][j] + a.m[i][j];</pre>
            return rev;
      matrix operator-(const matrix &a)
           matrix rev(r, c);
for (int i = 0; i < r; ++i)
    for (int j = 0; j < c; ++j)
        rev[i][j] = m[i][j] - a.m[i][j];</pre>
      matrix operator*(const matrix &a)
            matrix rev(r, a.c);
           rev.m[i][j] += m[i][k] * tmp[j][k];
      bool inverse() //逆矩陣判斷
            Matrix t(r, r + c);
for (int y = 0; y < r; y++)
                 t.m[y][c + y] = 1;
for (int x = 0; x < c; ++x)
                       \dot{t}.m[y][x] = m[y][x];
            if (!t.gas())
                  return false;
            for (int y = 0; y < r; y++)
  for (int x = 0; x < c; ++x)
        m[y][x] = t.m[y][c + x] / t.m[y][y];</pre>
      T gas() //行列式
            vector<T> lazy(r, 1);
            bool sign = false;
for (int i = 0; i < r; ++i)</pre>
                  if (m[i][i] == 0)
                 {
                       int j = i + 1;
while (j < r && !m[j][i])</pre>
                           i++;
                       if (j == r)
                            continue
                       m[i].swap(m[j]);
                       sign = !sign;
                  for (int j = 0; j < r; ++j)
                       if (i == j)
                            continue;
                       lazy[j] = lazy[j] * m[i][i];
                       T mx = m[j][i];
for (int k = 0; k < c; ++k)
    m[j][k] = m[j][k] * m[i][i] - m[i][k] * mx;</pre>
                 }
            T det = sign ? -1 : 1;
            for (int i = 0; i < r; ++i)
                  det = det * m[i][i];
                 det = det / lazy[i];
for (auto &j : m[i])
                       j /= lazy[i];
            return det;
      }
};
 9.4 分數
```

```
typedef long long 11;
struct fraction
{
  11 n, d;
  fraction(const ll \&_n = 0, const ll \&_d = 1) : n(n), d(d)
    11 t = __gcd(n, d);
n /= t, d /= t;
    if (d < 0)
     n = -n, d = -d;
```

```
fraction operator-() const
{
    return fraction(-n, d);
}
fraction operator+(const fraction &b) const
{
    return fraction(n * b.d + b.n * d, d * b.d);
}
fraction operator-(const fraction &b) const
{
    return fraction(n * b.d - b.n * d, d * b.d);
}
fraction operator*(const fraction &b) const
{
    return fraction(n * b.n, d * b.d);
}
fraction operator/(const fraction &b) const
{
    return fraction(n * b.d, d * b.n);
}
void print()
{
    cout << n;
    if (d != 1)
        cout << "/" << d;
}
};</pre>
```