Contents	8 String 8.1 KMP 8.2 Min Edit Dista
1 Basic 1	8.3 Sliding window 8.4 Split
1.1 Basic codeblock setting	8.4 Spiit
1.2 Basic vim setting	9 data structure
1.4 Python	9.1 Bigint
1.5 Range data       2         1.6 Some Function       2	9.2 DisjointSet . 9.3 Matirx
1.6 Some Function       2         1.7 Time       2	9.4 分數
2 DP 2	
2.1 3 維 DP 思路 2	
2.2 Knapsack Bounded       2         2.3 Knapsack sample       2	1 Basic
2.3 Knapsack sample       2         2.4 Knapsack Unbounded       2	
2.5 LCIS	1.1 D
2.6 LCS O(Nlog(N))	1.1 Basic co
2.8 LIS O(Nlog(N))	Settings -> Editor
2.9 LIS	code formatter
2.10 LPS	Settings -> Source
2.12 Money problem	Delete empty lines Insert space paddi
2.13 Palindromic Substrings count	Insert space paddin Remove extra space
3 Flow & matching 4	Remove extra space
3.1 Dinic	19 Dania
3.3 Hungarian	1.2 Basic vi
3.4 Independent set	/*at home directory
3.5 Maximum general weighted matching	/* vi ~/.vimrc */
3.7 Minimum cut	syntax enable
3.8 Model	set smartindent set tabstop=4
3.9 Stable matching 6	set shiftwidth=4
4 Geometry 7	set expandtab set relativenumber
4.1 Circle Intersect       7         4.2 Closest Pair       7	Jee relacivenamber
4.3 Line	19 Cala Ta
4.4 Max_cover_rectangle	1.3 Code Te
4.5 Point	#include <bits stde<="" td=""></bits>
4.7 Triangle	using namespace sto
5 Graph 10	typedef long long typedef unsigned lo
5.1 Bellman-Ford	#define pb push_ba
5.2 BFS-queue	#define len(k) (in
5.3 DFS-rec	<pre>#define all(p) p.bo #define endl '\n'</pre>
5.5 Euler circuit	#define x first
5.6 Floyd-warshall       11         5.7 Hamilton_cycle       11	<pre>#define y second #define bug(k) cour</pre>
5.8 Kruskal	;
5.9 LCA	#define bugp(k) con
5.10 Minimum Weight Cycle	' << k.y << er #define bugarr(k)
5.12 Union_find	endl;
6 Mathematics 13	<pre>int main() {</pre>
6.1 Catalan	ios::sync_with
6.2 Combination	<pre>cin.tie(0); return 0;</pre>
6.3 CRT	}
6.5 Fermat	
6.6 Hex to Dec	1.4 Python
6.7 Log	101
6.9 PI	//輸入
6.10 Pow_Mod	input()
6.12 Prime 判斷	array = [0] * (N)
6.13 Round(小數)	range(0, N) // 0 ~
6.14 二分逼近法	line = input().spl:
6.16 四則運算	D, R, N = map(int,
6.17 因數表	// 才是 取除數
6.18 數字乘法組合	/ 是 小數運算
6.20 羅馬數字	pow(a, b, c) // a
6.21 質因數分解	
	print(*objects, sep  // objects 可以
7 Other 17 7.1 Binary search 三類變化	// sep 分開多個
7.2 Heap sort	// end 默認值是
7.3 Josephus	// EOF break
7.4 Largest Multi-Interval	try:
7.6 Quick sort	while True: //input so
7.7 Sudoku solution	except EOEEnnon:

```
8 String
   19
   19
 19
```

# deblock setting

```
-> Keyboard shortcuts -> Plugins -> Source
r (AStýle)
Formatter -> Padding within a function or method
ng around operators
ng around parentheses on outside
padding around parentheses
```

## m setting

```
y*/
```

# emplate

```
c++.h>
:d;
11;
ong long ull;
t)k.length()
egin(), p.end()
t << "value of " << #k << " is " << k << endl
ut << "pair of " << #k << " is " << k.x << '
for(auto i : k) cout << i << ' '; cout <<</pre>
_stdio(0);
```

```
//N個0
                    N-1
                   it()
                    line) // 分三個 int 變數
                   ^ b % c
                   ep = ' ', end = '\n')
一次輸出多個對象
                   objects
         //input someithing
except EOFError:
    pass
```

```
1.5 Range data
int (-2147483648 to 2147483647)
unsigned int(0 to 4294967295)
long(-2147483648 to 2147483647)
unsigned long(0 to 4294967295)
long long(-9223372036854775808 to 9223372036854775807)
unsigned long long (0 to 18446744073709551615)
1.6 Some Function
round(double f);
                             // 四捨五入
ceil(double f);
                             // 進入
                             // 捨去
floor(double f);
 _builtin_popcount(int n); // 32bit有多少 1
to_string(int s);
                             // int to string
cout << setprecision(位數) // cout 小數位設定
```

printf 型別 "%lf" // long double "%lld" // long long int

```
| set_union(all(a), all(b), back_inserter(d)); // 聯集
| set_intersection(all(a), all(b), back_inserter(c)); //交集
| /** 全排列要先 sort !!! **/
| next_permutation(num.begin(), num.end());
| prev_permutation(num.begin(), num.end());
| //用binary search找第一個大於或等於val的位置
| vector<int>::iterator it = lower_bound(v.begin(), v.end(), val)
| ;
| //用binary search找第一個大於val的位置
| vector<int>::iterator it = upper_bound(v.begin(), v.end(), val)
| ;
| /*找到節團車面的最大元素*/
```

```
/*找到範圍裏面的最大元素*/
max_element(n, n + len); // n到n+len範圍內最大值
max_element(v.begin(), v.end()); // vector 中最大值
/*找到範圍裏面的最大元素*/
min_element(n, n + len); // n到n+len範圍內最小值
min_element(v.begin(), v.end()); // vector 中最小值
```

```
queue<datatype> q;
front(); /*取出最前面的值(沒有移除掉)*/
back(); /*取出最後面的值(沒有移除掉)*/
pop(); /*移掉最前面的值*/
push(); /*新增值到最後面*/
empty(); /*回傳bool,檢查是不是空的queue*/
size(); /*queue 的大小*/
/*stack*/
```

/ unordered\_set<datatype> s; unordered\_set<datatype> s(arr, arr + n); /\*initial with array\*/ insert(); /\*插入值\*/

erase(); /\*刪除值\*/ empty(); /\*bool 檢查是不是空\*/ count(); /\*判斷元素存在回傳1 無則回傳0\*/

# /\*tuple\*/ tuple<datatype,datatype,datatype> t;

stack<datatype> s;

std::get<0>(t) /\*Get first element of tuple\*/
std::get<1>(t) /\*Get second element of tuple\*/
std::get<2>(t) /\*Get third element of tuple\*/

#### 1.7 Time

 $\mid$  cout << 1.0 \* clock() / CLOCKS\_PER\_SEC << endl;

## 2 DP

#### 2.1 3 維 DP 思路

```
|解題思路: dp[i][j][k]
|i 跟 j 代表 range i ~ j 的 value
|k在我的理解裡是視題目的要求而定的
|像是 Remove Boxes 當中 k 代表的是在 i 之前還有多少個連續的箱子
|所以每次區間消去的值就是(k+1) * (k+1)
|換言之·我認為可以理解成 k 的意義就是題目今天所關注的重點·就是
老師說的題目所規定的運算
```

# 2.2 Knapsack Bounded

# 2.3 Knapsack sample

## 2.4 Knapsack Unbounded

```
| const int N = 100, W = 100000;
| int cost[N], weight[N];
| int c[W + 1];
| void knapsack(int n, int w) {
| memset(c, 0, sizeof(c));
| for (int i = 0; i < n; ++i)
| for (int j = weight[i]; j <= w; ++j)
| c[j] = max(c[j], c[j - weight[i]] + cost[i]);
| cout << "最高的價值為" << c[w]; }
```

#### 2.5 LCIS

# $2.6 \quad LCS O(Nlog(N))$

```
#define LEN 500004
int a[LEN], b[LEN];
int loc[LEN], n;
int LIS()
     for (int i = 1; i <= n; i++)
   loc[b[i]] = i;
for (int i = 1; i <= n; i++)</pre>
          b[i] = loc[a[i]];
     int k, l, r, mid;
a[1] = b[1], k = 1;
     for (int i = 2; i <= n; i++)
           if (a[k] < b[i])</pre>
                `a[++k] = b[i];
           else
                l = 1;
r = k;
while (1 <= r)</pre>
                      mid = (1 + r) / 2;
                      if (a[mid] < b[i])</pre>
                           l = mid + 1;
                      else
                           r = mid - 1;
                a[1] = b[i];
           }
     return k:
```

## 2.7 LCS

```
int LCS(vector<string> Ans, vector<string> num)
    int N = Ans.size(), M = num.size();
    vector<vector<int>> LCS(N + 1, vector<int>(M + 1, 0));
    for (int i = 1; i <= N; ++i)
         for (int j = 1; j <= M; ++j)
             if (Ans[i - 1] == num[j - 1])
    LCS[i][j] = LCS[i - 1][j - 1] + 1;
                  LCS[i][j] = max(LCS[i - 1][j], LCS[i][j - 1]);
    cout << LCS[N][M] << '\n';</pre>
    //列印 LCS
    int n = N, m = M;
    vector<string> k;
    while (n && m)
         if (LCS[n][m] != max(LCS[n - 1][m], LCS[n][m - 1]))
             k.push_back(Ans[n - 1]);
             n--;
         else if (LCS[n][m] == LCS[n - 1][m])
         else if (LCS[n][m] == LCS[n][m - 1])
             m - -;
    reverse(k.begin(), k.end());
    for (auto i : k)
    cout << i << " ";</pre>
    cout << endl;
return LCS[N][M];</pre>
```

# 2.8 LIS O(Nlog(N))

```
3
    return length;
2.9 LIS
vector<int> ans;
void LIS(vector<int> &arr)
    vector<int> dp(arr.size(), 1);
    vector<int> pos(arr.size(), -1);
    int res = INT_MIN, index = 0;
    for (int i = 0; i < arr.size(); ++i)</pre>
         for (int j = i + 1; j < arr.size(); ++j)</pre>
              if (arr[j] > arr[i])
                  if (dp[i] + 1 > dp[j])
                      dp[j] = dp[i] + 1;
                      pos[j] = i;
         if (dp[i] > res)
              res = dp[i];
              index = i;
         }
    cout << res << endl; // length</pre>
    printLIS(arr, pos, index);
for (int i = 0; i < ans.size(); i++)</pre>
         cout << ans[i];
         if (i != ans.size() - 1)
cout << ' ';
    cout << '\n':
void printLIS(vector<int> &arr, vector<int> &pos, int index)
    printLIS(arr, pos, pos[index]);
ans.push_back(arr[index]);
2.10 LPS
// manacher
void LPS(string s)
  int maxlen = 0, 1, r;
  int n = n;
  for (int i = 0; i < n; i++)
  {
    int x = 0;
    while ((s[i - x] == s[i + x]) \&\& (i - x >= 0) \&\& (i + x < n)
         )) //odd length
    if (2 * x + 1 > maxlen)
    {
      maxlen = 2 * x + 1;
      1 = i - x;
      r = i + x;
    }
    while ((s[i - x] == s[i + 1 + x]) \& (i - x >= 0) \& (i + 1)
           + x < n)) //even length
    x++;
if (2 * x > maxlen)
    {
      maxlen = 2 * x;
      1 = i - x + 1;
       r = i + x;
  }
  cout << maxlen << '\n';</pre>
                                              // 最後長度
  cout << l + 1 << ' ' << r + 1 << '\n'; //頭到尾
         Max subarray
/*Kadane's algorithm*/
int maxSubArray(vector<int>& nums) {
    int local_max = nums[0], global_max = nums[0];
for(int i = 1; i < nums.size(); i++){</pre>
```

local\_max = max(nums[i],nums[i]+local\_max);
global\_max = max(local\_max,global\_max);

return global\_max;

}

# 2.12 Money problem

```
//能否湊得某個價位
void change(vector<int> price, int limit)
    vector<bool> c(limit + 1, 0);
    c[0] = true;
    for (int i = 0; i < price.size(); ++i)</pre>
                                                      // 依序加入各種
         for (int j = price[i]; j <= limit; ++j) // 由低價位逐步
              到高價位
             c[j] = c[j] | c[j - price[i]];
    if (c[limit]) cout << "YES\n";
else cout << "NO\n";</pre>
// 湊得某個價位的湊法總共幾種
void change(vector<int> price, int limit)
    vector<int> c(limit + 1, 0);
    c[0] = true;
    for (int i = 0; i < price.size(); ++i)</pre>
    // 湊得某個價位的最少錢幣用量
void change(vector<int> price, int limit)
    vector<int> c(limit + 1, 0);
    c[0] = true;
    for (int i = 0; i < price.size(); ++i)
    for (int j = price[i]; j <= limit; ++j)
        c[j] = min(c[j], c[j - price[i]] + 1);
cout << c[limit] << '\n';</pre>
    cout << c[limit] <<
·
//湊得某個價位的錢幣用量,有哪幾種可能性
void change(vector<int> price, int limit)
    vector<int> c(limit + 1, 0);
    c[0] = true;
for (int i = 0; i < price.size(); ++i)</pre>
        for (int j = price[i]; j <= limit; ++j)
c[j] |= c[j-price[i]] << 1; // 錢幣數量加一、每一種
                   可能性都加一
    for (int i = 1; i <= 63; ++i)
    if (c[m] & (1 << i))</pre>
             cout << "用" << i << "個錢幣可湊得價位" << m;
}
```

#### 2.13 Palindromic Substrings count

# 3 Flow & matching

#### 3.1 Dinic

```
const long long INF = 1LL<<60;
struct Dinic { //O(VVE), with minimum cut
    static const int MAXN = 5003;
    struct Edge{
        int u, v;
        long long cap, rest;
    };
    int n, m, s, t, d[MAXN], cur[MAXN];
    vector<Edge> edges;
    vector<int> G[MAXN];
    void init(){
        edges.clear();
        for ( int i = 0 ; i < n ; i++ ) G[i].clear();
        n = 0;
    }
    // min cut start
    bool side[MAXN];
    void cut(int u) {</pre>
```

```
side[u] = 1;
for ( int i : G[u] ) {
    if ( !side[ edges[i].v ] && edges[i].rest )
      // min cut end
      int add_node(){
            return n++;
      void add_edge(int u, int v, long long cap){
  edges.push_back( {u, v, cap, cap} );
  edges.push_back( {v, u, 0, 0LL} );
  m = edges.size();
            G[u].push_back(m-2);
G[v].push_back(m-1);
      bool bfs(){
    fill(d,d+n,-1);
            queue<int> que;
            que.push(s); d[s]=0;
            while (!que.empty()){
                 int u = que.front(); que.pop();
                  for (int ei : G[u]){
    Edge &e = edges[ei];
    if (d[e.v] < 0 && e.rest > 0){
        d[e.v] = d[u] + 1;
                               que.push(e.v);
                  }
            return d[t] >= 0;
      long long dfs(int u, long long a){
            if ( u == t || a == 0 ) return a;
            long long flow = 0, f;
for ( int &i=cur[u]; i < (int)G[u].size() ; i++) {
    Edge &e = edges[ G[u][i] ];
    if ( d[u] + 1 != d[e.v] ) continue;</pre>
                   f = dfs(e.v, min(a, e.rest) );
                   if (f > 0 ) {
                   e.rest -= f
                   edges[ G[u][i]^1 ].rest += f;
                   flow += f;
                   a -= f;
                   if ( a == 0 ) break;
            return flow:
      long long maxflow(int _s, int _t){
            s = _s, t = _t;
long long flow = 0, mf;
while ( bfs() ){
                  fill(cur,cur+n,0);
                  while ( (mf = dfs(s, INF)) ) flow += mf;
            return flow;
} dinic;
```

# 3.2 Edmonds\_karp

```
/*Flow - Edmonds-karp*/
/*Based on UVa820*/
#define inf 1000000
int getMaxFlow(vector<vector<int>> &capacity, int s, int t, int
       n){
   int ans = 0;
   vector<vector<int>> residual(n+1, vector<int>(n+1, 0)); //
        residual network
   while(true){
     vector<int> bottleneck(n+1, 0);
     bottleneck[s] = inf;
     queue<int> q;
     q.push(s);
     vector<int> pre(n+1, 0);
while(!q.empty() && bottleneck[t] == 0){
        int cur = q.front();
        q.pop();
for(int i = 1; i <= n ; i++){
   if(bottleneck[i] == 0 && capacity[cur][i] > residual[
                cur][i]){
             q.push(i);
             pre[i] = cur;
bottleneck[i] = min(bottleneck[cur], capacity[cur][i]
                     - residual[cur][i]);
          }
       }
     if(bottleneck[t] == 0) break;
     for(int cur = t; cur != s; cur = pre[cur]){
    residual[pre[cur]][cur] += bottleneck[t];
    residual[cur][pre[cur]] -= bottleneck[t];
     ans += bottleneck[t];
```

# 3.3 Hungarian

```
/*bipartite - hungarian*/
/*Based on 2017 ICPC Taiwan regional final Problem I*/
bool dfs(vector<vector<bool>> mp, vector<bool> pass, vector<int</pre>
      >& pre,int cur){
     for(int i = 0;i < mp[cur].size(); i++){
    if(mp[cur][i] && !pass[i]){
        pass[i] = true;
        if(pre[i] == -1 || dfs(mp,pass,pre,pre[i])){</pre>
                    pre[i] = cur;
                     return true;
          }
     return false:
int hungarian(vector<vector<bool>> mp,int n,int m){
     int ans = 0;
     vector<int> pre(m,-1);
for(int i = 0;i < n; i++){
    vector<bool> pass(m,false);
          if(dfs(mp,pass,pre,i))
               ans += 1;
     return ans;
int main(){
     int m,n,e;
     while(cin>>n){
          if(n == 0) break;
          cin>>m>>e;
          int a,b;
          vector<vector<bool>> mp(n,vector<bool>(m,false));
          for(int i = 0;i < e; i++){
               cin>>a>>b;
               mp[a][b] = true;
          cout<<hungarian(mp,n,m)<<endl;</pre>
     return 0;
```

## 3.4 Independent set

```
int mp[30][30];
int vis[30];
int n, m;
int dfs(int now){
   for(int i = 0;i < now; i++){</pre>
        if(mp[now][i]&&(vis[now] == vis[i]))//與now相鄰的結點與
            now有相同的頻率
            return 0;
    if(now == n - 1){//遍歷結束
        return 1;
   for(int i = 1;i <= 3; i++){//選顏色
vis[now+1] = i;
        if(dfs(now+1))
            return 1;
   return 0:
int main(){
   int t;
    cin >> t:
    while(t--){
```

memset(vis,0,sizeof(vis));

```
memset(mp,0,sizeof(mp));
cin >> n >> m;
while(m--){
    int a, b;
    cin >> a >> b;
    mp[a][b] = 1;
    mp[b][a] = 1;
}
vis[0] = 1;//第一個節點任意選一種顏色
if(dfs(0))
    cout <<"Y"<<endl;
else
    cout <<"N"<<endl;
//print vis = print result of combinaton
}
return 0;
```

## 3.5 Maximum general weighted matching

```
From NCTU codebook
 // Minimum Weight Perfect Matching (Perfect Match)
 struct Graph {
       static const int MAXN = 105;
      int n, e[MAXN][MAXN];
int match[MAXN], d[MAXN], onstk[MAXN];
       void init(int _n) {
            n = _n;
for( int i = 0 ; i < n ; i ++ )
for( int j = 0 ; j < n ; j ++ )</pre>
                  e[i][j] = 0;
       void add_edge(int u, int v, int w) {
            e[u][v] = e[v][u] = w;
      bool SPFA(int u){
    if (onstk[u]) return true;
            stk.push_back(u);
            for ( int v = 0 ; v < n ; v++ ) {
   if (u != v && match[u] != v && !onstk[v] ){</pre>
                        int m = match[v];
                        if ( d[m] > d[u] - e[v][m] + e[u][v] ){
   d[m] = d[u] - e[v][m] + e[u][v];
   onstk[v] = 1;
                             stk.push_back(v);
                             if (SPFA(m)) return true;
stk.pop_back();
onstk[v] = 0;
                        }
                 }
            onstk[u] = 0;
            stk.pop_back();
return false;
       int solve() {
            for ( int i = 0 ; i < n ; i += 2 ) {
                  match[i] = i+1;
match[i+1] = i;
            while (true){
                 fe (true);
int found = 0;
for ( int i = 0 ; i < n ; i++ )
    onstk[ i ] = d[ i ] = 0;
for ( int i = 0 ; i < n ; i++ ) {</pre>
                        stk.clear();
                        if ( !onstk[i] && SPFA(i) ) {
                             found = 1;
while ( stk.size() >= 2 ) {
                                   int u = stk.back(); stk.
                                   pop_back();
                                   int v = stk.back(); stk.
                                   pop_back();
                                   match[u] = v;
match[v] = u;
                             }
                        }
                  }
if (!found) break;
             int ret = 0;
            for ( int i = 0 ; i < n ; i++ )
                 ret += e[i][match[i]];
            ret /= 2;
            return ret;
} graph;
```

#### 3.6 Maximum matching

```
/*bipartite - maximum matching*/
bool dfs(vector<vector<bool>> res,int node,vector<int>& x,
    vector<int>& y, vector<bool> pass){
    for (int i = 0; i < res[0].size(); i++){</pre>
```

```
if(res[node][i] && !pass[i]){
                pass[i] = true;
if(y[i] == -1 || dfs(res,y[i],x,y,pass)){
                     x[node] = i;
                     y[i] = node;
return true;
                }
          }
     return false;
int main(){
     int n,m,1;
     while(cin>>n>>m>>l){
           vector<vector<bool>> res(n, vector<bool>(m, false));
           for (int i = 0; i < 1; i++){
                int a, b;
cin >> a >> b;
res[a][b] = true;
           int ans = 0;
           vector < int > x(n, -1);
          vector<int> y(n, -1);
for (int i = 0; i < n; i++){
    vector<bool> pass(n, false);
    if(dfs(res,i,x,y,pass))
                     ans += 1;
           cout << ans << endl;
     return 0:
}
/*
input:
4 3 5 //n matching m, 1 links
0 0
0 2
1 0
2 1
answer is 3
```

#### 3.8 Model

- Theorem
  - 最大匹配 + 最小邊覆蓋 = V
  - 最大獨立集 + 最小點覆蓋 = V
  - 最大匹配 = 最小點覆蓋
  - 最小路徑覆蓋數 = V 最大匹配數
  - o maximum flow minimum cut
    - 找到一個最大流 = 至少產生一個最小割
    - 找最大流的bottleneck就可以找到最小割
- Maximum Independent Set
  - o General: [NPC] maximum clique of complement of G
  - o Bipartite Graph: [P] Maximum Cardinality Bipartite Matching
  - o Tree: [P] dp
- Minimum Dominating Set
  - o General: [NPC] backtracking
  - o Bipartite Graph: [NPC] backtracking
  - o Tree: [P] DP
- Minimum Vertex Cover
  - o General: [NPC] (?)maximum clique of complement of G
  - o Bipartite Graph: [P] Maximum Cardinality Bipartite Matching
  - o Tree: [P] Greedy, from leaf to root
- Minimum Edge Cover
  - o General: [P] V Maximum Matching
  - o Bipartite Graph: [P] Greedy, strategy: cover small degree node first
  - o (Min/Max)Weighted: [P]: Minimum/Maximum Weight Matching

# 3.7 Minimum cut

```
/*from 演算法筆記*/
typedef int Graph[9][9];
                          // adiacency matrix
Graph C, F, R;
                          // 分別是容量上限、流量、剩餘容量
bool visit[9];
void DFS(int i)
   visit[i] = true;
    for (int j=0; j<9; ++j)
    if (!visit[j] && F[i][j] < C[i][j])</pre>
           DFS(j);
}
void minimum_s_t_cut(int s, int t)
    // 求一個最大源匯流,源點為s點,匯點為t點。
   Edmonds_Karp(s, t);
    // 從源點開始遍歷,找出流量瓶頸。
   memset(visit, false, sizeof(visit));
    // 找出其中一個最小源匯割,會是源點側點數最少的最小源匯割。
   for (int i=0; i<9; ++i)
                                 // 窮舉源點側的點
       if (visit[i])
           for (int j=0; j<9; ++j) // 窮舉匯點側的點
if (!visit[j])
                  if (C[i][j] > 0)
                                     // 要確定有邊
                      cout << "割上的邊有"
                          << "曲" << i << "到" << j;
```

## 3.9 Stable matching

```
/*based on UVa1175*/
/*stable marriage problem*/
void engage(vector<int>& bm, vector<int>& gm, int a, int b,
      queue<int>& q){
     int tmp = gm[b];
     if(tmp != -1){
bm[tmp] = -1;
         q.push(tmp);
     bm[a] = b;
    gm[b] = a;
int main(){
    int cases;
bool blank = false;
     cin>>cases;
     while(cases--){
         if(blank) cout<<endl;</pre>
         int n,a;
         cin>>n;
         queue<int> q; // proposal
vector<vector<int>> boy(n+1,vector<int>(n+1,0)),girl(n
               +1, vector<int>(n+1,0));
         vector<int> p(n+1,1);
for(int i = 1;i <= n; i++){
    for(int j = 1;j <= n; j++){</pre>
                   cin>>a:
                   boy[i][j] = a;
               q.push(i);
          for(int i = 1;i <= n; i++){
               for(int j = 1; j <= n; j++){</pre>
                   cin>>a;
                   girl[i][a] = j;
          vector<int> bm(n+1,-1),gm(n+1,-1);
```

# 4 Geometry

#### 4.1 Circle Intersect

```
bool same(double a, double b)
       return abs(a - b) < 0;</pre>
struct P
      double x, y;
P() : x(0), y(0) {}
P(double x, double y) : x(x), y(y) {}
P operator+(P b) { return P(x + b.x, y + b.y); }
P operator-(P b) { return P(x - b.x, y - b.y); }
P operator*(double b) { return P(x * b, y * b); }
P operator*(double b) { return P(x / b, y / b); }
double operator*(P b) { return x * b.x + y * b.y; }
// double operator^(P b) { return x * b.y - y * b.double abs() { return hypot(x, y); }
       double abs() { return hypot(x, y); }
       P unit() { return *this / abs();
       P rot(double o)
              double c = cos(o), s = sin(o);
return P(c * x - s * y, s * x + c * y);
       double angle() { return atan2(y, x); }
struct C
       C(P \ c = P(0, 0), double \ r = 0) : c(c), r(r) \{\}
vector<P> Intersect(C a, C b)
       if (a.r > b.r)
               swap(a, b);
       double d = (a.c - b.c).abs();
       vector<P> p;
       if (same(a.r + b.r, d))
    p.pb(a.c + (b.c - a.c).unit() * a.r);
else if (a.r + b.r > d && d + a.r >= b.r)
               double o = acos((sqrt(a.r) + sqrt(d) - sqrt(b.r)) / (2
                      * a.r * d));
              P i = (b.c - a.c).unit();
p.pb(a.c + i.rot(o) * a.r);
p.pb(a.c + i.rot(-o) * a.r);
       return p;
```

#### 4.2 Closest Pair

```
d = min(d, dist(p[vec[i]], p[vec[j]]));
    return d;
4.3 Line
template <typename T>
struct line
    line() {}
    point<T> p1, p2;
T a, b, c; //ax+by+c=0
line(const point<T> &x, const point<T> &y) : p1(x), p2(y)
         {}
    void pton()
    { //轉成一般式
        a = p1.y - p2.y;
b = p2.x - p1.x;
        c = -a * p1.x - b * p1.y;
    T ori(const point<T> &p) const { //點和有向直線的關係·>0左邊、=0在線上<0右邊
        return (p2 - p1).cross(p - p1);
    T btw(const point<T> &p) const
    { //點投影落在線段上<=0
        return (p1 - p).dot(p2 - p);
    bool point_on_segment(const point<T> &p) const
    { //點是否在線段上
        return ori(p) == 0 && btw(p) <= 0;</pre>
    T dis2(const point<T> &p, bool is_segment = 0) const
    { //點跟直線/線段的距離平方
        point < T > v = p2 - p1, v1 = p - p1;
        if (is_segment)
            point<T> v2 = p - p2;
if (v.dot(v1) <= 0)</pre>
                 return v1.abs2();
             if (v.dot(v2) >= 0)
                 return v2.abs2();
        T tmp = v.cross(v1);
        return tmp * tmp / v.abs2();
    T seg_dis2(const line<T> &1) const
    { //兩線段距離平方
        return min({dis2(l.p1, 1), dis2(l.p2, 1), l.dis2(p1, 1)
             , l.dis2(p2, 1)});
    point<T> projection(const point<T> &p) const
    { //點對直線的投影
        point<T> n = (p2 - p1).normal();
return p - n * (p - p1).dot(n) / n.abs2();
    point<T> mirror(const point<T> &p) const
        //點對直線的鏡射,要先呼叫pton轉成一般式
        point<T> R:
        T d = a * a + b * b;
        R.x = (b * b * p.x - a * a * p.x - 2 * a * b * p.y - 2

* a * c) / d;

R.y = (a * a * p.y - b * b * p.y - 2 * a * b * p.x - 2

* b * c) / d;
        return R;
    bool equal(const line &1) const
    { //直線相等
        return ori(1.p1) == 0 && ori(1.p2) == 0;
    bool parallel(const line &1) const
        return (p1 - p2).cross(l.p1 - l.p2) == 0;
    bool cross_seg(const line &1) const
        return (p2 - p1).cross(l.p1 - p1) * (p2 - p1).cross(l.
             p2 - p1) <= 0; //直線是否交線段
    int line_intersect(const line &1) const
    { //直線相交情況,-1無限多點、1交於一點、0不相交
        return parallel(1) ? (ori(1.p1) == 0 ? -1 : 0) : 1;
    int seg_intersect(const line &1) const
        T c1 = ori(l.p1), c2 = ori(l.p2);
T c3 = l.ori(p1), c4 = l.ori(p2);
        if (c1 == 0 \&\& c2 == 0)
        { //共線
            bool b1 = btw(1.p1) >= 0, b2 = btw(1.p2) >= 0;
            T a3 = 1.btw(p1), a4 = 1.btw(p2);
             if (b1 && b2 && a3 == 0 && a4 >= 0)
```

```
return 2:
                                                                                         double midr = r - len:
             if (b1 && b2 && a3 >= 0 && a4 == 0)
                                                                                         if (b1 && b2 && a3 >= 0 && a4 >= 0)
                  return 0;
                                                                                               Rotate(v1, midr), Rotate(v2, midr), po)) == 1)
             return -1; //無限交點
                                                                                              r = midr:
                                                                                         else
                                                                                              1 = midl;
         else if (c1 * c2 <= 0 && c3 * c4 <= 0)
             return 1;
                                                                                    Max = max(Max, Area(p1, p2, p3, p4, Rotate(v1, 1),
         return 0; //不相交
                                                                                          Rotate(v2, 1), po));
                                                                                    v1 = Rotate(v1, minRad);
    point<T> line intersection(const line &1) const
                                                                                    v2 = Rotate(v2, minRad);
if (mycmp(angle(v1, po.p[p1 + 1] - po.p[p1])) == 0)
    p1 = (p1 + 1) % m;
     { /*直線交點*/
         point < T > a = p2 - p1, b = 1.p2 - 1.p1, s = 1.p1 - p1;
         // if (a.cross(b) == 0)
// return INF;
                                                                                     if (mycmp(angle(v1 * (-1), po.p[p2 + 1] - po.p[p2])) ==
         return p1 + a * (s.cross(b) / a.cross(b));
                                                                                    p2 = (p2 + 1) % m;
if (mycmp(angle(v2 * (-1), po.p[p3 + 1] - po.p[p3])) ==
    point<T> seg_intersection(const line &1) const
                                                                                           0)
    { //線段交點
                                                                                         p3 = (p3 + 1) \% m;
         int res = seg_intersect(1);
                                                                                    if (mycmp(angle(v2, po.p[p4 + 1] - po.p[p4])) == 0)
p4 = (p4 + 1) % m;
         if (res <= 0)
             assert(0);
         if (res == 2)
                                                                                return Max:
             return p1;
                                                                           }
         if (res == 3)
              return p2;
                                                                           4.5 Point
         return line_intersection(1);
                                                                            const double PI = atan2(0.0, -1.0);
};
                                                                            template <typename T>
                                                                           struct point
4.4 Max_cover_rectangle
                                                                                Тх,
const double PI = atan2(0.0, -1.0);
const double eps = 1e-10;
                                                                                point() {}
                                                                                point(const T &x, const T &y) : x(x), y(y) {}
typedef point<double> p; // data type 依照題目更改
                                                                                point operator+(const point &b) const
int mycmp(double a) { return fabs(a) < eps ? 0 : (a < 0 ? -1 :</pre>
1); }
double Length(p a) { return sqrt(a.dot(a)); }
p Rotate(p a, double rad) { return p(a.x * cos(rad) - a.y * sin (rad), a.x * sin(rad) + a.y * cos(rad)); }
                                                                                     return point(x + b.x, y + b.y);
                                                                                point operator-(const point &b) const
double angle(p a) { return atan2(a.y, a.x); }
                                                                                     return point(x - b.x, y - b.y);
double angle(p a, p b) { return atan2(a.cross(b), a.dot(b)); }
double turnAngle(p a, p b) { return mycmp(a.dot(b)) == 1 ?
    angle(a, b) : PI + angle(a, b); }
double distanceOfpAndLine(p a, p b, p c) { return fabs((b - a).
    cross(c - a) / Length(b - c)); }
                                                                                point operator*(const T &b) const
                                                                                     return point(x * b, y * b);
double Area(int a, int b, int c, int d, p ab, p cd, polygon<
                                                                                point operator/(const T &b) const
     double> po)
                                                                                     return point(x / b, y / b);
    double h1 = distanceOfpAndLine(po.p[a], po.p[b], po.p[b] +
         ab);
                                                                                bool operator==(const point &b) const
    double h2 = distanceOfpAndLine(po.p[c], po.p[d], po.p[d] +
                                                                                    return x == b.x \&\& v == b.v:
    return h1 * h2;
                                                                                  dot(const point &b) const
double max_cover_rectangle(polygon<double> po)
                                                                                    return x * b.x + y * b.y;
    po.p.pb(po.p[0]);
     int m = po.p.size();
                                                                                T cross(const point &b) const
    if (m < 3)
         return 0; // 沒凸包哪來外包矩形
                                                                                    return x * b.y - y * b.x;
     double Max = -1;
    double Minx = po.p[0].x, Miny = po.p[0].y, Maxx = po.p[0].x
                                                                                point normal() const
    , Maxy = po.p[0].y;
int p1 = 0, p2 = 0, p3 = 0, p4 = 0;
                                                                                { //求法向量
                                                                                    return point(-y, x);
    p v1, v2, ori;
ori = v1 = p(1, 0);
v2 = p(0, 1);
                                                                                T abs2() const
                                                                                { //向量長度的平方
     for (int i = 1; i < m; i++)
                                                                                     return dot(*this);
         if (mycmp(Minx - po.p[i].x) == 1)
    Minx = po.p[i].x, p3 = i;
if (mycmp(Maxx - po.p[i].x) == -1)
                                                                                T rad(const point &b) const
                                                                                { //兩向量的弧度
             Maxx = po.p[i].x, p4 = i;
mycmp(Miny - po.p[i].y) == 1)
                                                                                    return fabs(atan2(fabs(cross(b)), dot(b)));
         if (mycmp(Miny
                                                                                T getA() const
             Miny = po.p[i].y, p1 = i;
                                                                                                          //對x軸的弧度
         if (mycmp(Maxy - po.p[i].y) == -1)
             Maxy = po.p[i].y, p2 = i;
                                                                                    T A = atan2(y, x); //超過180度會變負的
if (A <= -PI / 2)
A += PI * 2;
    while (mycmp(ori.cross(v1)) >= 0)
                                                                                    return A;
         double minRad = 1e20;
         minRad = min(minRad, turnAngle(v1, po.p[p1 + 1] - po.p[
              p1]));
         minRad = min(minRad, turnAngle(v1 * (-1), po.p[p2 + 1]
                                                                           4.6 Polygon
                po.p[p2]));
         minRad = min(minRad, turnAngle(v2 * (-1), po.p[p3 + 1]
                                                                           template <typename T>
               - po.p[p3]));
                                                                            struct polygon
         minRad = min(minRad, turnAngle(v2, po.p[p4 + 1] - po.p[
         p4]));
double 1 = 0, r = minRad;
```

polygon() {}

T area() const { //面積

T ans = 0;

vector<point<T>> p; //逆時針順序

while (mycmp(1 - r))

double len = (r - 1) / 3;double midl = l + len;

```
for (int i = p.size() - 1, j = 0; j < (int)p.size(); i</pre>
         = i++)
        ans += p[i].cross(p[j]);
    return ans / 2;
point<T> center of mass() const
{ //重心
    T cx = 0, cy = 0, w = 0;
for (int i = p.size() - 1, j = 0; j < (int)p.size(); i
         `= j++)
        T a = p[i].cross(p[j]);
        cx += (p[i].x + p[j].x) * a;

cy += (p[i].y + p[j].y) * a;
        w += a:
    return point<T>(cx / 3 / w, cy / 3 / w);
char ahas(const point<T> &t) const
{ //點是否在簡單多邊形內·是的話回傳1、在邊上回傳-1、否則回
    bool c = 0:
    for (int i = 0, j = p.size() - 1; i < p.size(); j = i</pre>
        if (line<T>(p[i], p[j]).point_on_segment(t))
             return -1
        return c;
char point in convex(const point<T> &x) const
    int 1 = 1, r = (int)p.size() - 2;
    while (1 <= r)
    { //點是否在凸多邊形內,是的話回傳1、在邊上回傳-1、否則
         回傳0
        int mid = (1 + r) / 2;
        T a1 = (p[mid] - p[0]).cross(x - p[0]);
T a2 = (p[mid + 1] - p[0]).cross(x - p[if (a1 >= 0 && a2 <= 0)
             T res = (p[mid + 1] - p[mid]).cross(x - p[mid])
             return res > 0 ? 1 : (res >= 0 ? -1 : 0);
        else if (a1 < 0)
            r = mid - 1;
        else
             1 = mid + 1:
    return 0;
vector<T> getA() const
{//凸包邊對x軸的夾角
    vector<T> res; //一定是遞增的
for (size_t i = 0; i < p.size(); ++i)
    res.push_back((p[(i + 1) % p.size()] - p[i]).getA()
    return res;
bool line intersect(const vector<T> &A, const line<T> &1)
     const
{ //O(logN)
    int f1 = upper_bound(A.begin(), A.end(), (1.p1 - 1.p2).
         getA()) - A.begin();
    int f2 = upper_bound(A.begin(), A.end(), (1.p2 - 1.p1).
    getA()) - A.begin();
return 1.cross_seg(line<T>(p[f1], p[f2]));
polygon cut(const line<T> &1) const
{ //凸包對直線切割,得到直線1左側的凸包
    polygon ans;
    for (int n = p.size(), i = n - 1, j = 0; j < n; i = j
        if (l.ori(p[i]) >= 0)
             ans.p.push_back(p[i]);
             if (l.ori(p[j]) < 0)
                 ans.p.push_back(l.line_intersection(line<T
                      >(p[i], p[j])));
        else if (l.ori(p[j]) > 0)
             ans.p.push_back(1.line_intersection(line<T>(p[i
                  ], p[j])));
    return ans;
static bool Andrew_Monotone_Chain_angle(const point<T> &a,
     const point<T> &b)
{ //凸包排序函數 // 起始點不同
    return (a.y < b.y) || (a.y == b.y && a.x < b.x); //Y最
```

```
void Andrew_Monotone_Chain(vector<point<T>> &s)
{ //凸包 Convexhull 2D sort(s.begin(), s.end(), Andrew_Monotone_Chain_angle); p.resize(s.size() + 1);
    int m = 0;
    // cross >= 0 順時針。cross <= 0 逆時針旋轉
    for (size_t i = 0; i < s.size(); ++i)</pre>
         while (m \ge 2 \&\& (p[m - 1] - p[m - 2]).cross(s[i] -
              p[m - 2]) <= 0)
             --m;
        p[m++] = s[i];
    for (int i = s.size() - 2, t = m + 1; i >= 0; --i)
         while (m \ge t \&\& (p[m - 1] - p[m - 2]).cross(s[i] - p[m - 2])
              p[m - 2]) <= 0)
              - - m;
        p[m++] = s[i];
    if (s.size() > 1) // 重複頭一次需扣掉
    p.resize(m);
    // p.pb(s[0]); // 需要頭在 pb 回去!!
T diam()
{ //直徑
    int n = p.size(), t = 1;
    T ans = 0;
    p.push_back(p[0]);
    for (int i = 0; i < n; i++)
         point < T > now = p[i + 1] - p[i];
         while (now.cross(p[t + 1] - p[i]) > now.cross(p[t]
              - p[i]))
             t = (t + 1) \% n;
        ans = max(ans, (p[i] - p[t]).abs2());
    return p.pop back(), ans;
T min_cover_rectangle()
{ // 先做凸包 //最小覆蓋矩形
    int n = p.size(), t = 1, r = 1, l;
    if (n < 3)
        return 0; //也可以做最小周長矩形
    T ans = 1e99;
    p.push_back(p[0]);
    for (int i = 0; i < n; i++)
        point<T> now = p[i + 1] - p[i];
         while (now.cross(p[t + 1] - p[i]) > now.cross(p[t])
              - p[i]))
             t = (t + 1) % n;
         while (now.dot(p[r + 1] - p[i]) > now.dot(p[r] - p[
             i]))
        r = (r + 1) \% n;
if (!i)
             1 = r;
         while (now.dot(p[1 + 1] - p[i]) \le now.dot(p[1] - p
              [i]))
             1 = (1 + 1) \% n;
         T d = now.abs2();
        t u = now.abs2(),
T tmp = now.coss(p[t] - p[i]) * (now.dot(p[r] - p[i]) - now.dot(p[l] - p[i])) / d;
         ans = min(ans, tmp);
    return p.pop_back(), ans;
T dis2(polygon &pl)
{ //凸包最近距離平方
    vector<point<7>> &P = p, &Q = pl.p;
int n = P.size(), m = Q.size(), l = 0, r = 0;
for (int i = 0; i < n; ++i)</pre>
         if (P[i].y < P[1].y)
             1 = i
    for (int i = 0; i < m; ++i)
        if (Q[i].y < Q[r].y)</pre>
    P.push_back(P[0]), Q.push_back(Q[0]);
    T ans = 1e99;
    for (int i = 0; i < n; ++i)</pre>
         while ((P[1] - P[1 + 1]).cross(Q[r + 1] - Q[r]) <
             0) r = (r + 1) \% m;
        ans = min(ans, line<T>(P[1], P[1 + 1]).seg_dis2( line<T>(Q[r], Q[r + 1])));
        1 = (1 + 1) \% n;
    return P.pop_back(), Q.pop_back(), ans;
static char sign(const point<T> &t)
    return (t.y == 0 ? t.x : t.y) < 0;</pre>
```

```
static bool angle_cmp(const line<T> &A, const line<T> &B)
         point<T> a = A.p2 - A.p1, b = B.p2 - B.p1;
         return sign(a) < sign(b) || (sign(a) == sign(b) && a.
    cross(b) > 0);
    int halfplane_intersection(vector<line<T>> &s)
     { //半平面交
         sort(s.begin(), s.end(), angle_cmp); //線段左側為該線段
              半平面
         int L, R, n = s.size();
         vector<point<T>> px(n);
         vector<line<T>> q(n);
         q[L = R = 0] = s[0];
for (int i = 1; i < n; ++i)</pre>
              while (L < R \&\& s[i].ori(px[R - 1]) <= 0)
              while (\dot{L} < R \&\& s[i].ori(px[L]) <= 0)
              ++L;
q[++R] = s[i];
              if (q[R].parallel(q[R - 1]))
                  if (q[R].ori(s[i].p1) > 0)
                       q[R] = s[i];
              if (L < R)
                  px[R - 1] = q[R - 1].line_intersection(q[R]);
         while (L < R && q[L].ori(px[R - 1]) <= 0)
              --R:
         p.clear();
         if (R - L <= 1)
              return 0;
         px[R] = q[R].line_intersection(q[L]);
for (int i = L; i <= R; ++i)</pre>
              p.push_back(px[i]);
         return R - L + 1;
};
```

# 4.7 Triangle

```
template <typename T>
struct triangle
    point<T> a, b, c;
triangle() {}
    triangle(const point<T> &a, const point<T> &b, const point<</pre>
         T > &c) : a(a), b(b), c(c) {}
     T area() const
         T t = (b - a).cross(c - a) / 2;
         return t > 0 ? t : -t;
    point<T> barycenter() const
    { //重心
         return (a + b + c) / 3;
    point<T> circumcenter() const
    { //外心
         static line<T> u, v;
u.p1 = (a + b) / 2;
         u.p2 = point(T)(u.p1.x - a.y + b.y, u.p1.y + a.x - b.x)
         v.p1 = (a + c) / 2;
         v.p2 = point<T>(v.p1.x - a.y + c.y, v.p1.y + a.x - c.x)
         return u.line_intersection(v);
    point<T> incenter() const
    { //內心
         T A = sqrt((b - c).abs2()), B = sqrt((a - c).abs2()), C
         = sqrt((a - b).abs2());
return point<T>(A * a.x + B * b.x + C * c.x, A * a.y +
B * b.y + C * c.y) / (A + B + C);
    point<T> perpencenter() const
    { //垂心
         return barycenter() * 3 - circumcenter() * 2;
};
```

# 5 Graph

#### 5.1 Bellman-Ford

```
/*SPA - Bellman-Ford*/
#define inf 99999 //define by you maximum edges weight
vector<vector<int> > edges;
vector<int> dist;
vector<int> ancestor;
```

```
void BellmanFord(int start.int node){
    dist[start] = 0;
for(int it = 0; it < node-1; it++){
    for(int i = 0; i < node; i++){</pre>
              ancestor[j] = i;
                   }
              }
         }
    }
     for(int i = 0; i < node; i++) //negative cycle detection</pre>
         for(int j = 0; j < node; j++)
    if(dist[i] + edges[i][j] < dist[j])</pre>
                   cout<<"Negative cycle!"<<endl;</pre>
                   return;
int main(){
     int node;
     cin>>node;
     edges.resize(node, vector<int>(node, inf));
     dist.resize(node,inf);
     ancestor.resize(node,-1);
     int a,b,d;
     while(cin>>a>>b>>d){
         /*input: source destination weight*/
if(a == -1 && b == -1 && d == -1)
         edges[a][b] = d;
     int start;
     cin>>start:
     BellmanFord(start, node);
     return 0;
```

# 5.2 BFS-queue

```
void BFS(vector<int> &result, vector<pair<int, int>> edges, int
      node, int start)
{
    vector<int> pass(node, 0);
    queue<int> q;
    queue<int> p;
    q.push(start);
    int count = 1;
    vector<pair<int,
                     int>> newedges;
    while (!q.empty())
        pass[q.front()] = 1;
         for (int i = 0; i < edges.size(); i++)
             if (edges[i].first == q.front() && pass[edges[i].
                 second] == 0)
             {
                 p.push(edges[i].second);
                 result[edges[i].second] = count;
             else if (edges[i].second == q.front() && pass[edges
                 [i].first] == 0)
             {
                 p.push(edges[i].first);
                 result[edges[i].first] = count;
             else
                 newedges.push_back(edges[i]);
        edges = newedges;
        newedges.clear();
        q.pop();
        if (q.empty() == true)
            q = p;
queue<int> tmp;
            p = tmp;
             count++;
    }
int main()
    cin >> node;
    vector<pair<int, int>> edges;
    int a, b;
while (cin >> a >> b)
          a = b = -1 means input edges ended*/
        if (a == -1 && b == -1)
            break;
```

```
edges.push_back(pair<int, int>(a, b));
}
vector<int> result(node, -1);
BFS(result, edges, node, 0);
return 0;
}
```

#### 5.3 DFS-rec

```
/*DFS - Recursive version*/
map<pair<int,int>,int> edges;
vector<int> pass;
vector<int> route;
void DFS(int start){
    pass[start] = 1;
     map<pair<int,int>,int>::iterator iter;
     for(iter = edges.begin(); iter != edges.end(); iter++){
   if((*iter).first.first == start && (*iter).second == 0
        && pass[(*iter).first.second] == 0){
               route.push_back((*iter).first.second);
               DFS((*iter).first.second);
          else if((*iter).first.second == start && (*iter).second
               == 0 && pass[(*iter).first.first] == 0){
route.push_back((*iter).first.first);
               DFS((*iter).first.first);
          }
    }
int main(){
    int node;
    cin>>node:
    pass.resize(node,0);
     int a,b;
     while(cin>>a>>b){
          if(a == -1 && b == -1)
              break:
          edges.insert(pair<pair<int,int>,int>(pair<int,int>(a,b)
                ,0));
    int start;
    cin>>start;
     route.push_back(start);
     DFS(start);
    return 0;
```

# 5.4 Dijkstra

```
/*SPA - Dijkstra*/
const int MAXN = 1e5 + 3;
const int inf = INT_MAX;
typedef pair<int, int> pii;
vector<vector<pii>>> weight(MAXN);
vector<int> isDone(MAXN, false), dist, ancestor;
void dijkstra(int s)
    priority_queue<pii, vector<pii>> pq;
pq.push(pii(0, s));
ancestor[s] = -1;
     while (!pq.empty())
          int u = pq.top().second;
          pq.pop();
          isDone[u] = true;
          for (auto &pr : weight[u])
               int v = pr.first, w = pr.second;
               if (!isDone[v] && dist[u] + w < dist[v])</pre>
               {
                    dist[v] = dist[u] + w;
                    pq.push(pii(dist[v], v));
                    ancestor[v] = u;
               }
          }
    }
// weight[a - 1].push_back(pii(b - 1, w));
// weight[b - 1].push_back(pii(a - 1, w));
// dist.resize(n, inf);
// ancestor.resize(n, -1);
// dist[0] = 0;
// dijkstra(0);
```

## 5.5 Euler circuit

```
/*Euler circuit*/
/*From NTU kiseki*/
/*G is graph, vis is visited, la is path*/
bool vis[N];
size_t la[K];
```

```
void dfs(int u, vector<int> &vec)
{
    while (la[u] < G[u].size())
    {
        if (vis[G[u][la[u]].second])
        {
            ++la[u];
            continue;
        }
        int v = G[u][la[u]].first;
        vis[G[u][la[u]].second] = true;
        ++la[u];
        dfs(v, vec);
        vec.push_back(v);
    }
}</pre>
```

## 5.6 Floyd-warshall

```
/*SPA - Floyd-Warshall*/
// 有向圖,正邊
                   O(V3)
// 有向圖,無負環
                   O(V<sup>3</sup>)
// 有向圖,有負環
                   不適用
// 無向圖,正邊
// 無向圖,無負環
                  不適用
// 無向圖·有負環 不適用
/*Find min weight cycle*/
#define inf 99999
void floyd_warshall(vector<vector<int>> &distance, vector<</pre>
     vector<int>> &ancestor, int n)
    for (int k = 0; k < n; k++)
        for (int i = 0; i < n; i++)</pre>
             for (int j = 0; j < n; j++)
                if (distance[i][k] + distance[k][j] < distance[</pre>
                     i][j])
                {
                     distance[i][j] = distance[i][k] + distance[
                          k][j]
                     ancestor[i][j] = ancestor[k][j];
            }
        }
    }
}
vector<vector<int>> distance(n, vector<int>(n, inf));
vector<vector<int>> ancestor(n, vector<int>(n, -1));
distance[a][b] = w;
ancestor[a][b] = w;
floyd_warshall(distance, ancestor, n);
/*Negative cycle detection*,
for (int i = 0; i < n; i++)
    if (distance[i][i] < 0)</pre>
        cout << "Negative cycle!" << endl;</pre>
        break:
```

# 5.7 Hamilton\_cycle

}

```
/*find hamilton cycle*/
void hamilton(vector<vector<int>>> gp, int k, int cur, vector<</pre>
      int>& solution,vector<bool> pass,bool& flag){
     if(k == gp.size()-1){
         if(gp[cur][1] == 1){
    cout << 1 << " ";
               while(cur != 1){
                   cout << cur`<< "
                   cur = solution[cur];
               cout << cur << endl;
               flag = true;
              return;
     for (int i = 0; i < gp[cur].size() && !flag; i++){
   if(gp[cur][i] == 1 && !pass[i]){
      pass[i] = true;</pre>
               hamilton(gp, k + 1, i, solution, pass,flag);
               pass[i] = false;
         }
    }
int main(){
     int n;
     while(cin>>n){
         int a,b;
```

```
bool end = false;
         vector<vector<int>>> gp(n+1,vector<int>(n+1,0));
         while(cin>>a>>b){
              if(a == 0 && b == 0)
              break;
gp[a][b] = 1;
              gp[b][a] = 1;
         vector<int> solution(n + 1, -1);
         vector<bool> pass(n + 1, false);
         solution[1] = 0;
         pass[1] = true;
bool flag = false;
hamilton(gp, 1,1 ,solution,pass,flag);
         if(!flag)
              cout << "N" << endl;
     return 0;
}
/*
3 4
3 1
output: 1 3 4 2 1
```

#### 5.8 Kruskal

```
/*mst - Kruskal*/
struct edges{
     int from:
     int to;
      int weight;
     friend bool operator < (edges a, edges b){</pre>
           return a.weight > b.weight;
int find(int x,vector<int>& union_set){
   if(x != union_set[x])
      union_set[x] = find(union_set[x], union_set);
      return union_set[x];
void merge(int a,int b,vector<int>& union_set){
  int pa = find(a, union_set);
  int pb = find(b, union_set);
     if(pa != pb)
           union_set[pa] = pb;
void kruskal(priority_queue<edges> pq,int n){
     vector<int> union_set(n, 0);
for (int i = 0; i < n; i++)</pre>
           union_set[i] = i;
     int edge = 0;
int cost = 0; //evaluate cost of mst
     while(!pq.empty() && edge < n - 1){
           edges cur = pq.top();
int from = find(cur.from, union_set);
int to = find(cur.to, union_set);
           if(from != to){
                merge(from, to, union_set);
                edge += 1;
cost += cur.weight;
           pq.pop();
     if(edge < n-1)</pre>
           cout << "No mst" << endl;</pre>
     else
           cout << cost << endl:
int main(){
     int n;
     cin >> n;
     int a, b, d;
     priority_queue<edges> pq;
      while(cin>>a>>b>>d){
           if(a == -1 && b == -1 && d == -1)
                break;
           edges tmp;
           tmp.from = a;
tmp.to = b;
tmp.weight = d;
           pq.push(tmp);
      kruskal(pq, n);
     return 0;
}
```

#### 5.9 LCA

```
|bool adj[9][9]; // adjacency matrix
|bool visit[9]; // DFS當下已經拜訪過的點
```

```
int lca[9][9]; // 所有兩點之間的LCA
                // Disjoint-sets Forest
int p[9];
// 最多兩步
int find(int x)
{
    return x == p[x] ? x : (p[x] = find(p[x]));
int DFS(int x)
    if (visit[x])
        return;
    visit[x] = true;
    // 計算LCA
    for (int y = 0; y < 9; ++y)
        if (visit[y])
            lca[x][y] = lca[y][x] = find(y);
    // DES
    for (int y = 0; y < 9; ++y)
        if (adj[x][y])
        {
           DFS(y);
            p[y] = x; // merge(y, x)·並讓x是樹根。
}
void demo()
    for (int i = 0; i < 9; ++i)
    p[i] = i;
for (int i = 0; i < 9; ++i)
        visit[i] = false;
    DFS(0); // 假設樹根為0
    int x, y;
while (cin >> x >> y)
        cout << "x點與y點的LCA是" << lca[x][y];
```

# 5.10 Minimum Weight Cycle

```
// 最小環
// 圖上無負環!!!!
#define INF 99999
vector<vector<int>> w, d, p;
vector<int> cycle;
int c = 0;
void trace(int i, int j)
     cycle[c++] = i;
     if (i != j)
         trace(p[i][j], j);
void init(int n)
     for (int i = 0; i < n; ++i)</pre>
         d[i][i] = 0;
void minimum_cycle(int n)
     int weight = 1e9;
for (int k = 0; k < n; ++k)</pre>
          for (int i = 0; i < k; ++i)</pre>
              for (int j = 0; j < k; ++j)
if (i != j)
                       if (w[k][i] + d[i][j] + w[j][k] < weight)
                           weight = w[k][i] + d[i][j] + w[j][k];
                           trace(i, j);
                           cycle[c++] = k;
         for (int i = 0; i < n; ++i)
              for (int j = 0; j < n; ++j)
                  if (d[i][k] + d[k][j] < d[i][j])</pre>
                       d[i][j] = d[i][k] + d[k][j];
                      p[i][j] = p[i][k];
              }
     if (weight == 1e9)
         cout << "No exist";
     else
         bug(weight);
         bug(c);
         bugarr(cycle);
 void simple_minimum_cycle(int n) // No use vector p
     int weight = INF;
```

```
for (int k = 0; k < n; ++k)
                                                                                             if (gp[a][b] > d)
                                                                                                  gp[a][b] = d;
          for (int i = 0; i < k; ++i)
               for (int j = 0; j < k; ++j)
if (i != j)
                                                                                        Prim(gp, n, 0);
                                                                                        return 0;
                         weight = min(mp[k][i] + d[i][j] + mp[j][k],
                                weight);
                                                                                   5.12 Union_find
          for (int i = 0; i < n; ++i)
    for (int j = 0; j < n; ++j)
        d[i][j] = min(d[i][k] + d[k][j], d[i][j]);</pre>
                                                                                   // union_find from 台大
                                                                                   vector<int> father:
                                                                                   vector<int> people;
     if (weight == INF)
    cout << "Back to jail\n";</pre>
                                                                                   void init(int n)
                                                                                        father.clear();
          cout << weight << endl;</pre>
                                                                                        people.clear();
                                                                                        father.resize(n);
w.resize(n, vector<int>(n, INF));
d.resize(n, vector<int>(n, INF));
p.resize(n, vector<int>(n));
cycle.resize(n);
                                                                                        people.resize(n);
                                                                                        for (int i = 0; i < n; i++)
                                                                                             father[i] = i;
//Edge input
                                                                                             people[i] = 1;
w[a][b] = w;
d[a][b] = w;
p[a][b] = b;
                                                                                   }
int Find(int x)
init(n);
                                                                                   {
minimum_cycle(n);
                                                                                        if (x != father[x])
                                                                                             father[x] = Find(father[x]);
5.11 Prim
                                                                                        return father[x];
  *mst - Prim*,
#define inf 99999
                                                                                   void Union(int x, int y)
struct edges
                                                                                        int m = Find(x);
                                                                                        int n = Find(y);
     int from;
     int to;
int weight;
                                                                                        if (m != n)
     friend bool operator<(edges a, edges b)</pre>
                                                                                             father[n] = m;
                                                                                             people[m] += people[n];
          return a.weight > b.weight;
void Prim(vector<vector<int>> gp, int n, int start)
                                                                                         Mathematics
     vector<bool> pass(n, false);
     int edge = 0;
int cost = 0; //evaluate cost of mst
                                                                                   6.1
                                                                                            Catalan
     priority_queue<edges> pq;
     for (int i = 0; i < n; i++)
     {
                                                                                   Catalan number
          if (gp[start][i] != inf)
          {
                                                                                     • 0~19項的catalan number
               edges tmp;
                                                                                         0 1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 16796, 58786,
               tmp.from = start;
tmp.to = i;
                                                                                          208012, 742900, 2674440, 9694845, 35357670, 129644790,
               tmp.weight = gp[start][i];
                                                                                          477638700, 1767263190
               pq.push(tmp);
                                                                                       。 公武: C_n=rac{1}{n+1}inom{2n}{n}=rac{(2n)!}{(n+1)!n!}
     pass[start] = true;
     while (!pq.empty() && edge < n - 1)</pre>
                                                                                   6.2 Combination
          edges cur = pq.top();
                                                                                   /*input type string or vector*/
for (int i = 0; i < (1 << input.size()); ++i)</pre>
          pq.pop();
          if (!pass[cur.to])
                                                                                        string testCase = "";
               for (int i = 0; i < n; i++)
                                                                                        for (int j = 0; j < input.size(); ++j)
    if (i & (1 << j))
                    if (gp[cur.to][i] != inf)
                                                                                                  testCase += input[j];
                         edges tmp;
                         tmp.from = cur.to;
tmp.to = i;
                                                                                   6.3 CRT
                         tmp.weight = gp[cur.to][i];
                                                                                   // 中國剩餘定理
                         pq.push(tmp);
                    }
                                                                                   template <typename T>
                                                                                   tuple<T, T, T> extgcd(T a, T b)
               pass[cur.to] = true;
               edge += 1;
cost += cur.weight;
                                                                                        if (!b)
                                                                                        return make_tuple(a, 1, 0);
T d, x, y;
tie(d, x, y) = extgcd(b, a % b);
     if (edge < n - 1)
cout << "No mst" << endl;
                                                                                        return make_tuple(d, y, x - (a / b) * y);
     else
                                                                                   long long crt(vector<int> mod, vector<int> a)
                                                                                   { // x % mod[i] = a[i]
    long long mult = mod[0];
    int n = (int)mod.size();
          cout << cost << endl;</pre>
int main()
                                                                                        long long res = a[0];
     int n;
                                                                                        for (int i = 1; i < n; ++i)
     cin >> n;
     int a, b, d;
vector<vector<int>> gp(n, vector<int>(n, inf));
while (cin >> a >> b >> d)
                                                                                             long long d, x, y;
tie(d, x, y) = extgcd(mult, mod[i] * 111);
if ((a[i] - res) % d)
     {
                                                                                                  return -1;
          if (a == -1 && b == -1 && d == -1)
                                                                                             long long new_mult = mult / __gcd(mult, 111 * mod[i]) *
```

mod[i];

break;

#### 6.4 Extended Euclidean

```
// ax + by = gcd(a,b)
pair<long long, long long> extgcd(long long a, long long b)
          return {1, 0};
     long long k = a / b;
pair<long long, long long> p = extgcd(b, a - k * b);
//cout << p.first << " " << p.second << endl;
//cout << "蔥數(k)= " << k << endl << endl;

b * p.second}:
     return {p.second, p.first - k * p.second};
}
int main()
     int a, b;
cin >> a >> b;
     return 0;
// ax + by = gcd(a,b) * r
/*find |x|+|y| -> min*/
int main()
     long long r, p, q; /*px+qy = r*/
     int cases;
cin >> cases;
     while (cases--)
           cin >> r >> p >> q;
pair<long long, long long> xy = extgcd(q, p); //(x0,y0)
           long long ans = 0, tmp = 0;
double k, k1;
long long s, s1;
           k = 1 - (double)(r * xy.first) / p;
           ans = llabs(r * xy.first + s * p) + llabs(r * xy.second
- s * q);
k1 - - (double)
           k1 = -(double)(r * xy.first) / p;
           s1 = round(k1);
           /*cout << k << endl << k1 << endl;
           cout << s << endl << s1 << endl;*/
tmp = llabs(r * xy.first + s1 * p) + llabs(r * xy.
    second - s1 * q);</pre>
           ans = min(ans, tmp);
           cout << ans << endl;</pre>
     return 0;
```

#### 6.5 Fermat

- $a^{(p-1)} \equiv 1 \pmod{p} \iff a * a^{(p-2)} \equiv 1$ •  $a^{(p-2)} \equiv 1/a$
- 同餘因數定理
  - $\circ \ a \equiv b \pmod{p} \iff k|a-b|$
- 同餘加法性質
  - $\circ \ a \equiv b \ (mod \ p) \ \text{and} \ c \equiv d \ (mod \ p)$  $<=> a+c \equiv b+d \ (mod \ p)$
- 同餘相乘性質
  - $\circ \ a \equiv b \ (mod \ p) \ \text{and} \ c \equiv d \ (mod \ p)$   $<=> ac \equiv bd \ (mod \ p)$
- 同餘次方性質
  - $\circ \ a \equiv b \pmod{p} \iff a^n \equiv b^n \pmod{p}$
- 同餘倍方性質
  - $\circ \ a \equiv b \pmod{p} \iff am \equiv bm \pmod{p}$

# 6.6 Hex to Dec

```
int HextoDec(string num) //16 to 10
        int base = 1;
        int temp = 0;
        for (int i = num.length() - 1; i >= 0; i--)
               if (num[i] >= '0' && num[i] <= '9')</pre>
                      temp += (num[i] - 48) * base;
base = base * 16;
               else if (num[i] >= 'A' && num[i] <= 'F')
                      temp += (num[i] - 55) * base;
base = base * 16;
        return temp;
void DecToHex(int p) //10 to 16
        char *1 = new (char);
sprintf(1, "%X", p);
        //int l_intResult = stoi(1);
cout << 1 << "\n";</pre>
        //return l_intResult;
6.7 \quad \text{Log}
double mylog(double a, double base)
        //a 的對數底數 b = 自然對數 (a) / 自然對數 (b)。
        return log(a) / log(base);
}
6.8 Mod 性質
 加法: (a+b) \operatorname{mod} p = (a \operatorname{mod} p + b \operatorname{mod} p) \operatorname{mod} p
 減法: (a-b) \operatorname{mod} p = (a \operatorname{mod} p - b \operatorname{mod} p + p) \operatorname{mod} p
 乘法: (a*b) \mod p = (a \mod p \cdot b \mod p) \mod p
 次方: (a^b) \mod p = ((a \mod p)^b) \mod p
 加法結合律: ((a+b) \operatorname{mod} p + c) \operatorname{mod} p = (a+(b+c)) \operatorname{mod} p
 乘法結合律: ((a \cdot b) \bmod p \cdot c) \bmod p = (a \cdot (b \cdot c)) \bmod p
 加法交換律: (a+b) \mod p = (b+a) \mod p
 乘法交換律: (a \cdot b) \mod p = (b \cdot a) \mod p
 結合律: ((a+b) \operatorname{mod} p \cdot c) = ((a \cdot c) \operatorname{mod} p + (b \cdot c) \operatorname{mod} p) \operatorname{mod} p
 如果 a \equiv b \pmod{m} · 我們會說 a, b 在模 m 下同餘。
  • 整除性: a \equiv b \pmod{m} \Rightarrow c \cdot m = a - b, c \in \mathbb{Z}
              \Rightarrow a \equiv b \pmod{m} \Rightarrow m \mid a - b
  • 遞移性: 若a \equiv b \pmod{c}, b \equiv d \pmod{c}
              則 a \equiv d \pmod{c}

    保持基本運算:

          \left\{ \begin{aligned} a &\equiv b (\operatorname{mod} m) \\ c &\equiv d (\operatorname{mod} m) \end{aligned} \right. \Rightarrow \left\{ \begin{aligned} a &\pm c \equiv b \pm d (\operatorname{mod} m) \\ a \cdot c \equiv b \cdot d (\operatorname{mod} m) \end{aligned} \right.

    放大縮小模數:

      k \in \mathbb{Z}^+, a \equiv b \pmod{m} \Leftrightarrow k \cdot a \equiv k \cdot b \pmod{k \cdot m}
  模逆元是取模下的反元素 · 即為找到 a^{-1} 使得 aa^{-1} \equiv 1 \, \mathrm{mod} \, c 。
  整數 a \leftarrow \mod c 下要有模反元素的充分必要條件為 a, c 互質
```

模逆元如果存在會有無限個,任意兩相鄰模逆元相差c

給定一個質數  $p \cdot \mathbb{H} : (p-1)! \equiv -1 \pmod{p}$ 

給定一個質數 p 及一個整數 a · 那麼 :  $a^p \equiv a \pmod{p}$  如果  $\gcd(a,p) = 1$  · 則 :

歐拉定理是比較 general 版本的費馬小定理。給定兩個整數 n 和 a · 如果 gcd(a,n)=1 · 貝

 $a^{\Phi(n)} \equiv 1 \pmod{n}$  如果 n 是質數  $\cdot$   $\Phi(n) = n-1$   $\cdot$  也就是費馬小定理

費馬小定理

 $a^{p-1} \equiv 1 (\mod \ p)$ 

Wilson's theorem

6.9 PI

#define PI acos(-1)

6.10 Pow Mod

#define PI M\_PI

}

#### 6.11 Prime table

## 6.12 Prime 判斷

```
typedef long long ll;
ll modmul(ll a, ll b, ll mod)
    11 \text{ ret} = 0;
    for (; b; b >>= 1, a = (a + a) % mod)
if (b & 1)
              ret = (ret + a) \% mod;
    return ret;
11 qpow(11 x, 11 u, 11 mod)
    ll ret = 111;
     for (; u; u >>= 1, x = modmul(x, x, mod))
   if (u & 1)
              ret = modmul(ret, x, mod);
    return ret;
ll gcd(ll a, ll b)
    return b ? gcd(b, a % b) : a;
11 Pollard_Rho(11 n, 11 c)
    ll i = 1, j = 2, x = rand() \% (n - 1) + 1, y = x;
    while (1)
         i++;
         x = (modmul(x, x, n) + c) % n;
ll p = gcd((y - x + n) % n, n);
         if (p != 1 && p != n)
              return p;
         if (y == x)
              return n;
         if (i == j)
              y = x;
j <<= 1;
    }
bool Miller_Rabin(ll n)
    11 x, pre, u = n - 1;
    int i, j, k = 0;
if (n == 2 || n == 3 || n == 5 || n == 7 || n == 11)
    return 1;
if (n == 1 || !(n % 2) || !(n % 3) || !(n % 5) || !(n % 7)
          || !(n % 11))
         return 0;
    while (!(u & 1))
```

```
k++;
          u >>= 1;
     srand((long long)12234336);
for (i = 1; i <= 50; i++)</pre>
          x = rand() % (n - 2) + 2;
if (!(n % x))
              return 0:
           x = qpow(x, u, n);
          pre = x;
for (j = 1; j <= k; j++)
                x = modmul(x, x, n);
if (x == 1 && pre != 1 && pre != n - 1)
                     return 0;
                pre = x;
          if (x != 1)
                return 0:
     return 1;
// if (Miller_Rabin(n)) puts("Prime");
6.13 Round(小數)
double myround(double number, unsigned int bits)
     LL integerPart = number:
     number -= integerPart;
     for (unsigned int i = 0; i < bits; ++i)
          number *= 10;
     number = (LL)(number + 0.5);
     for (unsigned int i = 0; i < bits; ++i)
number /= 10;
     return integerPart + number;
//printf("%.1f\n", round(3.4515239, 1));
6.14 二分逼近法
#define eps 1e-14
void half_interval()
     double L = 0, R = /*區間*/, M;
     while (R - L >= eps)
          M = (R + L) / 2;
          if (/*函數*/ > /*方程式目標*/)
L = M;
          else
               R = M;
     printf("%.31f\n", R);
6.15 公式
S_n = \frac{a(1-r^n)}{1-r} \ a_n = \frac{a_1 + a_n}{2} \sum_{k=1}^n k = \frac{n(n+1)}{2} \sum_{k=1}^n k^2 = \frac{n(n+1)(2n+1)}{6}
\sum_{k=1}^{n} k^3 = \left[ \frac{n(n+1)}{2} \right]^2
6.16 四則運算
string s = ""; //開頭是負號要補0
long long int DFS(int le, int ri) // (0, string final index)
     int c = 0;
for (int i = ri; i >= le; i--)
          if (s[i] == ')')
          if (s[i] == '(')
          if (s[i] == '+' && c == 0)
    return DFS(le, i - 1) + DFS(i + 1, ri);
if (s[i] == '-' && c == 0)
    return DFS(le, i - 1) - DFS(i + 1, ri);
     for (int i = ri; i >= le; i--)
          if (s[i] == ')')
          if (s[i] == '(')
          c--;
if (s[i] == '*' && c == 0)
    return DFS(le, i - 1) * DFS(i + 1, ri);
if (s[i] == '/' && c == 0)
    return DFS(le, i - 1) / DFS(i + 1, ri);
if (s[i] == '%' && c == 0)
                return DFS(le, i - 1) % DFS(i + 1, ri);
```

```
if ((s[le] == '(') && (s[ri] == ')'))
    return DFS(le + 1, ri - 1); //去除刮號
    if (s[le] == ' ' && s[ri] == ' ')
        return DFS(le + 1, ri - 1); //去除左右兩邊空格
    if (s[le] == ' ')
        return DFS(le + 1, ri); //去除左邊空格
    if (s[ri] == ' ')
        return DFS(le, ri - 1); //去除右邊空格
    long long int num = 0;
    for (int i = le; i <= ri; i++)
        num = num * 10 + s[i] - '0';
    return num;
}

6.17 因數表
```

```
| const int limit = 10000000;
| vector<vector<int>> arr(limit);
| for (int i = 1; i <= limit; i++) {
| for (int j = i; j <= limit; j += i) |
| arr[j].pb(i); // i 為因數
```

## 6.18 數字乘法組合

```
void dfs(int j, int old, int num, vector<int> com, vector<</pre>
     vector<int>> &ans)
     for (int i = j; i <= sqrt(num); i++)</pre>
          if (old == num)
               com.clear();
          if (num % i == 0)
               vector<int> a;
               a = com;
               a.push_back(i);
              finds(i, old, num / i, a, ans);
a.push_back(num / i);
               ans.push_back(a);
         }
    }
vector<vector<int>> ans;
vector<int> zero;
dfs(2, num, num, zero, ans); /*/num 為 input 數字*/
for (int i = 0; i < ans.size(); i++)</pre>
    for (int j = 0; j < ans[i].size() - 1; j++)
    cout << ans[i][j] << " ";</pre>
    cout << ans[i][ans[i].size() - 1] << endl;</pre>
}
```

#### **6.19** 數字加法組合

```
void recur(int i, int n, int m, vector<int> &out, vector<vector</pre>
    <int>> &ans)
    if (n == 0)
    {
        for (int i : out)
            if (i > m)
                return:
        ans.push_back(out);
    for (int j = i; j <= n; j++)
        out.push_back(j);
        recur(j, n - j, m, out, ans);
        out.pop_back();
   }
vector<vector<int>> ans;
vector<int> zero;
recur(1, num, num, zero, ans);
// num 為 input 數字
for (int i = 0; i < ans.size(); i++)</pre>
    for (int j = 0; j < ans[i].size() - 1; j++)
        cout << ans[i][j] <<</pre>
    cout << ans[i][ans[i].size() - 1] << endl;</pre>
```

# 6.20 羅馬數字

```
int romanToInt(string s)
{
    unordered_map<char, int> T;
    T['I'] = 1;
    T['V'] = 5;
    T['X'] = 10;
    T['L'] = 50;
```

```
T['C'] = 100;
T['D'] = 500;
T['M'] = 1000;

int sum = T[s.back()];
for (int i = s.length() - 2; i >= 0; --i)
{
    if (T[s[i]] < T[s[i + 1]])
        sum -= T[s[i]];
    else
        sum += T[s[i]];
}
return sum;
}</pre>
```

## 6.21 質因數分解

```
vector<int> primeFactorization(int tn) // 配合質數表
                                         //重複 or 不重複擇一
{
    vector<int> f;
    f.clear();
    int n = tn;
for (int i = 0; i < (int)p.size(); ++i)</pre>
        if (p[i] * p[i] > n)
        if (n % p[i])
            continue;
        // f.pb(p[i]); //不重複
        while (n \% p[i] == 0)
            n /= p[i];
            // f.pb(p[i]); //重複
    if (n != 1)
        f.pb(n);
    return f;
}
vector<int> factorcount(int tn) // 質因數個數
{ // ex tn = 2 * 2 * 3 => {2, 1}
// "2" 個 2, "1" 個 3
    vector<int> fac;
    for (auto pr : p)
        if (pr * pr > tn)
            break:
        if (tn % pr == 0)
             int cc = 0;
            while (tn \% pr == 0)
                 cc++;
                tn /= pr;
            fac.push_back(cc);
        }
    if (tn > 1)
        fac.push_back(1);
```

## 6.22 質數數量

```
// 10 ^ 11 左右
#define LL long long
const int N = 5e6 + 2;
bool np[N];
int prime[N], pi[N];
int getprime()
{
     int cnt = 0;
    np[0] = np[1] = true;
pi[0] = pi[1] = 0;
     for (int i = 2; i < N; ++i)
         if (!np[i])
              prime[++cnt] = i;
         pi[i] = cnt;
          for (int j = 1; j <= cnt && i * prime[j] < N; ++j)
              np[i * prime[j]] = true;
if (i % prime[j] == 0)
    break;
         }
    return cnt;
const int M = 7;
const int PM = 2 * 3 * 5 * 7 * 11 * 13 * 17;
int phi[PM + 1][M + 1], sz[M + 1];
void init()
     getprime();
```

```
sz[0] = 1;
     for (int i = 0; i <= PM; ++i)
          phi[i][0] = i;
     for (int i = 1; i <= M; ++i)
           sz[i] = prime[i] * sz[i - 1];
          for (int j = 1; j <= PM; ++j)
    phi[j][i] = phi[j][i - 1] - phi[j / prime[i]][i -
                      1];
     }
int sqrt2(LL x)
     LL r = (LL) sqrt(x - 0.1);
     while (r * r <= x)
     return int(r - 1);
int sqrt3(LL x)
     LL r = (LL)cbrt(x - 0.1);
     while (r * r * r <= x)
     return int(r - 1);
LL getphi(LL x, int s)
     if (s == 0)
           return
     if (s <= M)
     return phi[x % sz[s]][s] + (x / sz[s]) * phi[sz[s]][s];
if (x <= prime[s] * prime[s])
    return pi[x] - s + 1;</pre>
     if (x <= prime[s] * prime[s] * prime[s] && x < N)</pre>
           int s2x = pi[sqrt2(x)];
          LL ans = pi[x] - (s2x + s - 2) * (s2x - s + 1) / 2;
for (int i = s + 1; i <= s2x; ++i)
                ans += pi[x / prime[i]];
          return ans;
     return getphi(x, s - 1) - getphi(x / prime[s], s - 1);
LL getpi(LL x)
     if(x < N)
          return pi[x];
     LL ans = getphi(x, pi[sqrt3(x)]) + pi[sqrt3(x)] - 1;
for (int i = pi[sqrt3(x)] + 1, ed = pi[sqrt2(x)]; i <= ed;
            ++i)
          ans -= getpi(x / prime[i]) - i + 1;
     return ans;
LL lehmer_pi(LL x)
     if (x < N)
          return pi[x];
     int a = (int)lehmer_pi(sqrt2(sqrt2(x)));
int b = (int)lehmer_pi(sqrt2(x));
int c = (int)lehmer_pi(sqrt3(x));
LL sum = getphi(x, a) + (LL)(b + a - 2) * (b - a + 1) / 2;
for (int i = a + 1; i <= b; i++)</pre>
           LL w = x / prime[i];
           sum -= lehmer_pi(w);
           if (i > c)
                continue;
          LL lim = lehmer_pi(sqrt2(w));
for (int j = i; j <= lim; j++)
                sum -= lehmer_pi(w / prime[j]) - (j - 1);
     return sum;
// lehmer_pi(n)
```

# 7 Other

# 7.1 Binary search 三類變化

```
// 查找和目標值完全相等的數
int find(vector<int> &nums, int target)
{
    int left = 0, right = nums.size() - 1;
    while (left < right)
    {
        int mid = left + (right - left) / 2;
        if (nums[mid] == target)
            return mid;
        else if (nums[mid] < target)
            left = mid + 1;
        else
            right = mid;
    }
    return -1;
}</pre>
```

```
找第一個不小於目標值的數 == 找最後一個小於目標值的數
/*(lower_bound)*/
int find(vector<int> &nums, int target)
    int left = 0, right = nums.size() - 1;
    while (left < right)
        int mid = left + (right - left) / 2;
        if (nums[mid] < target)</pre>
             left = mid + 1;
            right = mid;
    return right;
}
// 找第一個大於目標值的數 == 找最後一個不大於目標值的數
/*(upper_bound)*/
int find(vector<int> &nums, int target)
    int left = 0, right = nums.size() - 1;
    while (left < right)
        int mid = left + (right - left) / 2;
        if (nums[mid] <= target)</pre>
            left = mid + 1;
            right = mid;
    return right;
     Heap sort
void MaxHeapify(vector<int> &array, int root, int length)
    int left = 2 * root, right = 2 * root + 1, largest;
    if (left <= length && array[left] > array[root])
        largest = left;
    else
        largest = root;
    if (right <= length && array[right] > array[largest])
        largest = right;
    if (largest != root)
        swap(array[largest], array[root]);
        MaxHeapify(array, largest, length);
void HeapSort(vector<int> &array)
    array.insert(array.begin(), 0);
for (int i = (int)array.size() / 2; i >= 1; i--)
    MaxHeapify(array, i, (int)array.size() - 1);
    int size = (int)array.size() - 1;
    for (int i = (int)array.size() - 1; i >= 2; i--)
        swap(array[1], array[i]);
        size--;
        MaxHeapify(array, 1, size);
    array.erase(array.begin());
7.3 Josephus
/*n people kill k for each turn*/
int josephus(int n, int k)
    int s = 0;
    for (int i = 2; i <= n; i++)
        s = (s + k) \% i;
    /*index start from 1 -> s+1*/
    return s + 1;
/*died at kth*/
int kth(int n, int m, int k)
    if (m == 1)
        return n - 1;
    for (k = k * m + m - 1; k >= n; k = k - n + (k - n) / (m - n)
         1))
    return k;
}
```

7.4 Largest Multi-interval

data.pb(pii(a, c)); // 區間 a 到 c

| sort(data.begin(), data.end(), name); // pair first 從 小 到 大

/\*多區間算最大值\*/

vector<pii> data;

bool name(pii a, pii b)
{ return b.first > a.first;}

## 7.5 Merge sort

```
long long merge(vector<int> &arr, int left, int mid, int right)
     int *tmp = new int[right - left + 1];
     long long sum = 0;
int l = left, r = mid + 1, m = 0;
     while (1 <= mid && r <= right)</pre>
          if (arr[1] <= arr[r])</pre>
               tmp[m++] = arr[1++];
               tmp[m++] = arr[r++];
sum += mid - l + 1;
          }
     while (1 <= mid)
          tmp[m++] = arr[1++];
     while (r <= right)</pre>
     tmp[m++] = arr[r++];
for (int i = left; i <= right; ++i)
    arr[i] = tmp[i - left];</pre>
     delete[] tmp;
     return sum;
}
long long mergesort(vector<int> &arr, int left, int right)
     long long sum = 0;
// left = 0, right = P.size() - 1
     if (left < right)</pre>
          int mid = (left + right) / 2;
          sum = mergesort(arr, left, mid);
sum += mergesort(arr, mid + 1, right);
          sum += merge(arr, left, mid, right);
     return sum; // 回傳為 swap 次數
```

#### 7.6 Quick sort

```
int Partition(vector<int> &arr, int front, int end)
{
    int pivot = arr[end];
    int i = front -
    for (int j = front; j < end; j++)</pre>
         if (arr[j] < pivot)</pre>
         {
             swap(arr[i], arr[j]);
        }
    i++:
    swap(arr[i], arr[end]);
void QuickSort(vector<int> &arr, int front, int end)
    // front = 0 , end = arr.size() - 1
    if (front < end)</pre>
         int pivot = Partition(arr, front, end);
         QuickSort(arr, front, pivot - 1);
QuickSort(arr, pivot + 1, end);
```

#### 7.7 Sudoku solution

```
/*數獨解法*/
int getSquareIndex(int row, int column, int n)
{
    return row / n * n + column / n;
}
bool backtracking(vector<vector<int>> &board, vector<vector<br/>bool>> &rows, vector<vector<br/>color>> &cols,
```

```
vector<vector<bool>> &boxs, int index, int n)
           int n2 = n * n;
           int rowNum = index / n2, colNum = index % n2;
           if (index >= n2 * n2)
                     return true:
           if (board[rowNum][colNum] != 0)
                    return backtracking(board, rows, cols, boxs, index + 1,
           for (int i = 1; i <= n2; i++)
                     if (!rows[rowNum][i] && !cols[colNum][i] && !boxs[
                                 getSquareIndex(rowNum, colNum, n)][i])
                               rows[rowNum][i] = true;
                               cols[colNum][i] = true;
                               boxs[getSquareIndex(rowNum, colNum, n)][i] = true;
                               board[rowNum][colNum] = i:
                               if (backtracking(board, rows, cols, boxs, index +
                                          1, n))
                                         return true;
                               board[rowNum][colNum] = 0;
                               rows[rowNum][i] = false;
cols[colNum][i] = false;
                               boxs[getSquareIndex(rowNum, colNum, n)][i] = false;
                    }
           return false;
/*用法 main*/
int n = sqrt(數獨邊長大小) /*e.g. 9*9 n=3*/
vector<vector<int>> board(n * n + 1, vector<int>(n * n + 1, 0))
vector < vector < bool >> isRow(n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool > (n * n + 1, vector < bool
            false));
vector<vector<bool>> isColumn(n * n + 1, vector<bool>(n * n +
           1, false));
vector<vector<bool>> isSquare(n * n + 1, vector<bool>(n * n +
            1, false));
for (int i = 0; i < n * n; ++i)</pre>
           for (int j = 0; j < n * n; ++j)</pre>
                    int number;
                     cin >> number;
                    board[i][j] = number;
                     if (number == 0)
                               continue;
                     isRow[i][number] = true;
                     isColumn[j][number] = true;
                     isSquare[getSquareIndex(i, j, n)][number] = true;
if (backtracking(board, isRow, isColumn, isSquare, 0, n))
           /*有解答*/
else
           /*無解答*/
```

# 7.8 Weighted Job Scheduling

```
struct Job
    int start, finish, profit;
bool jobComparataor(Job s1, Job s2)
     return (s1.finish < s2.finish);</pre>
int latestNonConflict(Job arr[], int i)
     for (int j = i - 1; j >= 0; j--)
          if (arr[j].finish <= arr[i].start)</pre>
               return j;
     return -1;
int findMaxProfit(Job arr[], int n)
     sort(arr, arr + n, jobComparataor);
int *table = new int[n];
table[0] = arr[0].profit;
for (int i = 1; i < n; i++)</pre>
          int inclProf = arr[i].profit;
          int l = latestNonConflict(arr, i);
if (l != -1)
               inclProf += table[1];
          table[i] = max(inclProf, table[i - 1]);
     int result = table[n - 1];
     delete[] table;
```

```
|}
```

return result:

String

#### 8.1 KMP

8

```
// 用在在一個 S 內查找一個詞 W 的出現位置
void ComputePrefix(string s, int next[])
    int n = s.length();
int q, k;
next[0] = 0;
    for (k = 0, q = 1; q < n; q++)
         while (k > 0 && s[k] != s[q])
    k = next[k];
         if (s[k] == \overline{s[q]})
             k++;
         next[q] = k;
    }
void KMPMatcher(string text, string pattern)
    int n = text.length();
    int m = pattern.length();
    int next[pattern.length()];
    ComputePrefix(pattern, next);
    for (int i = 0, q = 0; i < n; i++)
         while (q > 0 && pattern[q] != text[i])
             q = next[q];
         if (pattern[q] == text[i])
             q++;
         if (q == m)
         {
             cout << "Pattern occurs with shift " << i - m + 1</pre>
                   << endl;
             q = 0;
         }
    }
// string s = "abcdabcdebcd";
// string p = "bcd";
// KMPMatcher(s, p);
// cout << endl;</pre>
```

#### 8.2 Min Edit Distance

## 8.3 Sliding window

# 8.4 Split

```
vector<string> mysplit(const string& str, const string& delim)
{
   vector<string> res;
   if ("" == str)
        return res;

   char *strs = new char[str.length() + 1];
   strcpy(strs, str.c_str());

   char *d = new char[delim.length() + 1];
   strcpy(d, delim.c_str());

   char *p = strtok(strs, d);
   while (p)
   {
      string s = p;
      res.push_back(s);
      p = strtok(NULL, d);
   }
   return res;
}
```

## 9 data structure

## 9.1 Bigint

```
//台大 //非必要請用python
struct Bigint
    static const int LEN = 60;
                                       // maxLEN
    static const int BIGMOD = 10000; //10為正常位數
    int v1, v[LEN];
    // vector<int> v;
Bigint() : s(1) { vl = 0; }
    Bigint(long long a)
        v1 = 0;
        if (a < 0)
             s = -1;
             a = -a;
         while (a)
             push_back(a % BIGMOD);
             a /= BIGMOD;
        }
    Bigint(string str)
        v1 = 0:
        int stPos = 0, num = 0;
        if (!str.empty() && str[0] == '-')
             stPos = 1;
             s = -1;
         for (int i = str.length() - 1, q = 1; i >= stPos; i--)
             num += (str[i] - '0') * q;
if ((q *= 10) >= BIGMOD)
                 push_back(num);
                 num = 0;
                 q = 1;
             }
        push_back(num);
n();
        if (num)
    int len() const
        return vl; //return SZ(v);
    bool empty() const { return len() == 0; }
    void push_back(int x)
        v[vl++] = x; //v.PB(x);
    void pop_back()
```

```
return (*this) - (-b);
                                                                                   Bigint r;
int nl = max(len(), b.len());
    vl--; //v.pop_back();
int back() const
                                                                                   r.resize(nl + 1);
                                                                                   for (int i = 0; i < nl; i++)</pre>
{
    return v[vl - 1]; //return v.back();
                                                                                        if (i < len())
    r.v[i] += v[i];</pre>
void n()
                                                                                        if (i < b.len())</pre>
     while (!empty() && !back())
                                                                                             r.v[i] += b.v[i];
                                                                                        if (r.v[i] >= BIGMOD)
         pop_back();
                                                                                             r.v[i + 1] += r.v[i] / BIGMOD;
r.v[i] %= BIGMOD;
void resize(int nl)
     v1 = n1;
                            //v.resize(nl);
     fill(v, v + vl, 0); //fill(ALL(v), 0);
                                                                                   r.n();
void print() const
                                                                                   return r;
    if (empty())
                                                                              Bigint operator-(const Bigint &b) const
    {
         putchar('0');
                                                                                   if (s == -1)
                                                                                        return -(-(*this) - (-b));
                                                                                   if (b.s == -1)
                                                                                        return (*this) + (-b);
     if (s == -1)
         putchar('-');
                                                                                   if ((*this) < b)</pre>
    printf("%d", back());
for (int i = len() - 2; i >= 0; i--)
    printf("%.4d", v[i]);
                                                                                        return - (b - (*this));
                                                                                   Bigint r;
                                                                                   r.resize(len());
                                                                                   for (int i = 0; i < len(); i++)</pre>
}
friend std::ostream &operator<<(std::ostream &out, const</pre>
                                                                                        r.v[i] += v[i];
if (i < b.len())</pre>
     Bigint &a)
                                                                                        r.v[i] -= b.v[i];
if (r.v[i] < 0)
     if (a.empty())
         out << "0";
                                                                                             r.v[i] += BIGMOD;
         return out;
                                                                                             r.v[i + 1]--;
    if (a.s == -1)
out << "-"
     out << a.back();
                                                                                   r.n();
     for (int i = a.len() - 2; i >= 0; i--)
                                                                                   return r;
         char str[10];
sprintf(str, 5, "%.4d", a.v[i]);
                                                                              Bigint operator*(const Bigint &b)
         out << str;
                                                                                   Bigint r;
                                                                                   r.resize(len() + b.len() + 1);
     return out;
}
int cp3(const Bigint &b) const
                                                                                   for (int i = 0; i < len(); i++)</pre>
                                                                                        for (int j = 0; j < b.len(); j++)</pre>
     if (s != b.s)
         return s - b.s;
                                                                                             r.v[i + j] += v[i] * b.v[j];
    if (s == -1)
                                                                                             if (r.v[i + j] >= BIGMOD)
         return -(-*this).cp3(-b);
    if (len() != b.len())
  return len() - b.len(); //int
for (int i = len() - 1; i >= 0; i--)
  if (v[i] != b.v[i])
                                                                                                 r.v[i + j + 1] += r.v[i + j] / BIGMOD;
r.v[i + j] %= BIGMOD;
                                                                                       }
              return v[i] - b.v[i];
     return 0:
                                                                                   r.n();
                                                                                   return r;
bool operator<(const Bigint &b) const
                                                                              Bigint operator/(const Bigint &b)
     return cp3(b) < 0;
bool operator<=(const Bigint &b) const
                                                                                   r.resize(max(1, len() - b.len() + 1));
                                                                                   int oriS = s;
Bigint b2 = b; // b2 = abs(b)
     return cp3(b) <= 0;
                                                                                   s = b2.s = r.s = 1;
for (int i = r.len() - 1; i >= 0; i--)
bool operator==(const Bigint &b) const
{
     return cp3(b) == 0;
                                                                                        int d = 0, u = BIGMOD - 1;
                                                                                        while (d < u)
bool operator!=(const Bigint &b) const
                                                                                             int m = (d + u + 1) >> 1;
{
                                                                                             r.v[i] = m;
if ((r * b2) > (*this))
     return cp3(b) != 0;
bool operator>(const Bigint &b) const
                                                                                                 u = m -
                                                                                             else
                                                                                                 d = m;
     return cp3(b) > 0;
bool operator>=(const Bigint &b) const
                                                                                        r.v[i] = d;
                                                                                   s = oris;
r.s = s * b.s;
     return cp3(b) >= 0;
                                                                                   r.n();
Bigint operator-() const
                                                                                   return r;
     Bigint r = (*this);
     r.\bar{s} = -r.s;
                                                                              Bigint operator%(const Bigint &b)
                                                                                   return (*this) - (*this) / b * b;
Bigint operator+(const Bigint &b) const
                                                                         };
     if (s == -1)
         return -(-(*this) + (-b));
```

if (b.s == -1)

#### 9.2 DisjointSet

```
struct DisjointSet {
      int p[maxn], sz[maxn], n, cc;
      vector<pair<int*, int>> his;
      vector<int> sh;
      void init(int _n) {
    n = _n; cc = n;
    for (int i = 0; i < n; ++i) sz[i] = 1, p[i] = i;</pre>
             sh.clear(); his.clear();
       void assign(int *k, int v) {
    his.emplace_back(k, *k);
             *k = v;
      void save() {
             sh.push_back((int)his.size());
       void undo() {
             int last = sh.back(); sh.pop_back();
while (his.size() != last) {
                   int *k, v;
                   tie(k, v) = his.back(); his.pop_back();
            }
      int find(int x) {
   if (x == p[x]) return x;
             return find(p[x]);
       void merge(int x, int y) {
            u merge(int x, int y) {
x = find(x); y = find(y);
if (x == y) return;
if (sz[x] > sz[y]) swap(x, y);
assign(&sz[y], sz[x] + sz[y]);
assign(&p[x], y);
assign(&cc, cc - 1);
} ;
```

## 9.3 Matirx

```
template <typename T>
struct Matrix
       using rt = std::vector<T>;
using mt = std::vector<rt>;
       using matrix = Matrix<T>;
        int r, c; // [r][c]
       Matrix(int r, int c) : r(r), c(c), m(r, rt(c)) {}
Matrix(mt a) { m = a, r = a.size(), c = a[0].size(); }
rt & operator[](int i) { return m[i]; }
       matrix operator+(const matrix &a)
               matrix rev(r, c);
for (int i = 0; i < r; ++i)
    for (int j = 0; j < c; ++j)
        rev[i][j] = m[i][j] + a.m[i][j];</pre>
               return rev;
       matrix operator-(const matrix &a)
              matrix rev(r, c);
for (int i = 0; i < r; ++i)
    for (int j = 0; j < c; ++j)
        rev[i][j] = m[i][j] - a.m[i][j];</pre>
       matrix operator*(const matrix &a)
               matrix rev(r, a.c);
               matrix tmp(a.c, a.r);
for (int i = 0; i < a.r; ++i)
               for (int i = 0; i < a.r, ++i)
    for (int j = 0; j < a.c; ++j)
        tmp[j][i] = a.m[i][j];
for (int i = 0; i < r; ++i)
    for (int j = 0; j < a.c; ++j)
    for (int k = 0; k < c; ++k)</pre>
                                     rev.m[i][j] += m[i][k] * tmp[j][k];
               return rev;
       bool inverse() //逆矩陣判斷
               Matrix t(r, r + c);
for (int y = 0; y < r; y++)</pre>
                       t.m[y][c + y] = 1;
for (int x = 0; x < c; ++x)
    t.m[y][x] = m[y][x];</pre>
               if (!t.gas())
                       return false;
               for (int y = 0; y < r; y++)
    for (int x = 0; x < c; ++x)
        m[y][x] = t.m[y][c + x] / t.m[y][y];</pre>
```

```
T gas() //行列式
            vector<T> lazy(r, 1);
            bool sign = false;
            for (int i = 0; i < r; ++i)
                 if (m[i][i] == 0)
                      int j = i + 1;
                      while (j < r && !m[j][i])
                           j++;
                      if (j == r)
                            continue
                      m[i].swap(m[j]);
                      sign = !sign;
                 for (int j = 0; j < r; ++j)
                      if (i == j)
                            continue:
                      continue;
lazy[j] = lazy[j] * m[i][i];
T mx = m[j][i];
for (int k = 0; k < c; ++k)
    m[j][k] = m[j][k] * m[i][i] - m[i][k] * mx;</pre>
                 }
            T det = sign ? -1 : 1;
            for (int i = 0; i < r; ++i)
                 det = det * m[i][i];
det = det / lazy[i];
for (auto &j : m[i])
                      j /= lazy[i];
            return det;
};
```

## 9.4 分數

```
typedef long long 11;
struct fraction
   fraction(const ll \&_n = 0, const ll \&_d = 1) : n(n), d(d)
    ll t = __gcd(n, d);
n /= t, d /= t;
if (d < 0)</pre>
       n = -n, d = -d;
   fraction operator-() const
     return fraction(-n, d);
   fraction operator+(const fraction &b) const
     return fraction(n * b.d + b.n * d, d * b.d);
   fraction operator-(const fraction &b) const
     return fraction(n * b.d - b.n * d, d * b.d);
   fraction operator*(const fraction &b) const
     return fraction(n * b.n. d * b.d):
   fraction operator/(const fraction &b) const
     return fraction(n * b.d, d * b.n);
   void print()
   {
     cout << n;
     if (d != 1)
       cout << "/" << d;
};
```