

Part 1: (25%)

R05631027 楊皓文 image processing #3

330 (a) 具有 2 個梯形函數及 1 個三角函數

$$\Rightarrow \mu(z) = \begin{cases} 0.5 - \frac{(a-c)-z}{a-c}, & 0 \leq z \leq a-c \\ 0.5, & a-c \leq z \leq a-b \\ 1 - \frac{(a-z)}{b}, & a-b \leq z \leq a \\ 1 - \frac{(z-a)}{1}, & a \leq z \leq a+b \\ 0.5, & a+b \leq z \leq a+c \\ 0.5 - \frac{z-(a+c)}{a-c}, & a+c \leq z \leq 1 \end{cases}$$

(b) 具有 2 個梯形函數

$$\Rightarrow \mu(z) = \begin{cases} 0.5 - \frac{a+c-z}{c}, & a \leq z \leq a+c \\ 0.5, & a+c \leq z \leq b \\ 1 - \frac{b+c-z}{c}, & b \leq z \leq b+c \\ 1, & b+c \leq z \leq d \\ 0, & \text{otherwise} \end{cases}$$

(c) 具有 2 個三角函數

$$\Rightarrow \mu(z) = \begin{cases} 1 - \frac{a-b-z}{a-b}, & 0 \leq z \leq a-b \\ 1 - \frac{z-(a-b)}{b}, & a-b \leq z \leq a \\ 1 - \frac{a+b-z}{b}, & a \leq z \leq a+b \\ 1 - \frac{z-1}{1-(a+b)}, & a+b \leq z \leq 1 \end{cases} \quad \times$$

$$4.8 \quad F(u) = \sum_{x=0}^{M-1} f(x) e^{j2\pi ux/M}$$

$$f(x) = \frac{1}{M} \sum_{u=0}^{M-1} F(u) e^{j2\pi ux/M}$$

$$(a) \quad F(u) = \sum_{x=0}^{M-1} \left(\frac{1}{M} \sum_{u=0}^{M-1} F(u) e^{j2\pi ux/M} \right) e^{-j2\pi ux/M}$$

$$= \frac{1}{M} \sum_{x=0}^{M-1} \sum_{u=0}^{M-1} F(u) e^{j2\pi ux/M} e^{-j2\pi ux/M}$$

$$= \frac{1}{M} \times M \times F(u) = F(u)$$

$$f(x) = \frac{1}{M} \sum_{u=0}^{M-1} \left(\sum_{x=0}^{M-1} f(x) e^{-j2\pi ux/M} \right) e^{j2\pi ux/M}$$

$$= \frac{1}{M} \sum_{u=0}^{M-1} \sum_{x=0}^{M-1} f(x) e^{-j2\pi ux/M} e^{j2\pi ux/M}$$

$$= f(x)$$

$$(b) \quad F(u) = \sum_{x=0}^{M-1} \left[\frac{1}{M} \sum_{r=0}^{M-1} F(r) e^{-j2\pi rx/M} \right] e^{-j2\pi ux/M}$$

$$= \frac{1}{M} \sum_{r=0}^{M-1} F(r) \left[\sum_{x=0}^{M-1} e^{-j2\pi rx/M} e^{-j2\pi ux/M} \right]$$

$$= F(u) \quad \times$$

4.12

period = 2 mm

$$\Rightarrow \text{max frequency} = \frac{1}{\text{period}} = 0.5 \text{ cycles/mm}$$

c. 為避免 aliasing, 至少須高於 max frequency 的兩倍的 sampling rate

$$\Rightarrow 2 \cdot 0.5 = 1 \text{ sample/mm} \quad \times$$

4.16

$$\begin{aligned} (a) & F[f(x,y) e^{j2\pi(u_0x+v_0y)}] \\ &= \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} [f(x,y) e^{j2\pi(u_0x+v_0y)}] e^{-j2\pi(ux/M+vy/N)} \\ &= \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} f(x,y) e^{-j2\pi[(u-u_0)x/M+(v-v_0)y/N]} \\ &= F(u-u_0, v-v_0) \end{aligned}$$

$$\begin{aligned} (b) & F^{-1}[F(u,v) e^{-j2\pi(ux_0+vy_0)}] \\ &= \frac{1}{MN} \sum_{u=0}^{M-1} \sum_{v=0}^{N-1} [F(u,v) e^{-j2\pi(ux_0+vy_0)}] e^{j2\pi(ux/M+vy/N)} \\ &= \frac{1}{MN} \sum_{u=0}^{M-1} \sum_{v=0}^{N-1} F(u,v) e^{j2\pi[u(x-x_0)/M+v(y-y_0)/N]} \\ &= f(x-x_0, y-y_0) \quad \times \end{aligned}$$

4.21

需要進行 padding 的原因，最主要是因為要在 Discrete Fourier Transform 的 domain，建立一個 buffer。因此，不管什麼形式的 padding，應該都可達到相同效果。 \times

```

function varargout = HW02(varargin)

gui_Singleton = 1;
gui_State = struct('gui_Name',       mfilename, ...
                  'gui_Singleton',   gui_Singleton, ...
                  'gui_OpeningFcn',   @HW02_OpeningFcn, ...
                  'gui_OutputFcn',    @HW02_OutputFcn, ...
                  'gui_LayoutFcn',    [], ...
                  'gui_Callback',     []);
if nargin && ischar(varargin{1})
    gui_State.gui_Callback = str2func(varargin{1});
end

if nargout
    [varargout{1:nargout}] = gui_mainfcn(gui_State, varargin{:});
else
    gui_mainfcn(gui_State, varargin{:});
end


function HW02_OpeningFcn(hObject, eventdata, handles, varargin)

handles.w = 0;
w = num2str(handles.w);
set(handles.edit1,'string', w);
set(handles.edit1, 'Max', 9);

handles.output = hObject;
guidata(hObject, handles);


function varargout = HW02_OutputFcn(hObject, eventdata, handles)

varargout{1} = handles.output;


function pushbutton1_Callback(hObject, eventdata, handles)

filename = uigetfile({'*.jpg;*.tif;*.png;*.gif;*.bmp','All Image Files'});

```

```

handles.I = imread(filename);

[handles.row, handles.col, handles.lay] = size(handles.I);

if handles.lay == 1
    handles.I_gray = handles.I;
    fprintf('gray image\n');
elseif handles.lay == 3
    handles.R = uint8(handles.I(:, :, 1));
    handles.G = uint8(handles.I(:, :, 2));
    handles.B = uint8(handles.I(:, :, 3));
    handles.I_gray = 0.299*handles.R + 0.587*handles.G + 0.114*handles.B;
    fprintf('color image\n');
end

axes(handles.axes1);
imshow(handles.I_gray);

handles.output = hObject;
guidata(hObject, handles);

function radiobutton1_Callback(hObject, eventdata, handles)

set(handles.radiobutton1, 'Value', 1);
set(handles.radiobutton2, 'Value', 0);

w(hObject, eventdata, handles);

function radiobutton2_Callback(hObject, eventdata, handles)

set(handles.radiobutton1, 'Value', 0);
set(handles.radiobutton2, 'Value', 1);

w(hObject, eventdata, handles);

function radiobutton4_Callback(hObject, eventdata, handles)

```

```
set(handles.radiobutton4, 'Value', 1);
set(handles.radiobutton5, 'Value', 0);
set(handles.radiobutton6, 'Value', 0);
```

```
w(hObject, eventdata, handles);
```

```
function radiobutton5_Callback(hObject, eventdata, handles)
```

```
set(handles.radiobutton4, 'Value', 0);
set(handles.radiobutton5, 'Value', 1);
set(handles.radiobutton6, 'Value', 0);
```

```
w(hObject, eventdata, handles);
```

```
function radiobutton6_Callback(hObject, eventdata, handles)
```

```
set(handles.radiobutton4, 'Value', 0);
set(handles.radiobutton5, 'Value', 0);
set(handles.radiobutton6, 'Value', 1);
```

```
w(hObject, eventdata, handles);
```

```
function w(hObject, eventdata, handles)
```

```
% Laplacian 3x3
```

```
if handles.radiobutton1.Value == 1 && handles.radiobutton4.Value == 1
```

```
    handles.w = [0 1 0
                  1 -4 1
                  0 1 0];
```

```
% Sobel_x 3x3
```

```
elseif handles.radiobutton1.Value == 1 && handles.radiobutton5.Value == 1
```

```
    handles.w = [1 0 -1
                  2 0 -2
                  1 0 -1];
```

```
% Smoothing 3x3
```

```
elseif handles.radiobutton1.Value == 1 && handles.radiobutton6.Value == 1
```

```
    handles.w = [1 1 1
```

```

        1 1 1
        1 1 1];

% Laplacian 5x5
elseif handles.radiobutton2.Value == 1 && handles.radiobutton4.Value == 1
    handles.w = [0 0 1 0 0
        0 1 2 1 0
        1 2 -16 2 1
        0 1 2 1 0
        0 0 1 0 0];

% Sobel_x 5x5
elseif handles.radiobutton2.Value == 1 && handles.radiobutton5.Value == 1
    handles.w = [1 2 0 -2 -1
        4 8 0 -8 -4
        6 12 0 -12 -6
        4 8 0 -8 -4
        1 2 0 -2 -1];

% Smoothing 5x5
elseif handles.radiobutton2.Value == 1 && handles.radiobutton6.Value == 1
    handles.w = [1 1 1 1 1
        1 1 1 1 1
        1 1 1 1 1
        1 1 1 1 1];

end
w = num2str(handles.w);
set(handles.edit1,'String', w);

handles.output = hObject;
guidata(hObject, handles);

function edit1_Callback(hObject, eventdata, handles)

function edit1_CreateFcn(hObject, eventdata, handles)

if ispc && isequal(get(hObject,'BackgroundColor'), get(0,'defaultUicontrolBackgroundColor'))
    set(hObject,'BackgroundColor','white');
end

```

```

function pushbutton2_Callback(hObject, eventdata, handles)

handles.w = get(handles.edit1, 'String');
handles.w = str2num(handles.w);

% time start
timer1=tic;

% p 隨 mask 的大小改變，例如: 3x3 => p = 1, 5x5 => p = 2
p = ( size(handles.w, 1) - 1 ) / 2;

% smoothing 的分母
N = sum(sum(handles.w));
if N == 0
    N = 1;
end

I3 = double(zeros(handles.row+2*p, handles.col+2*p));
I3(1 + p:handles.row + p, 1 + p:handles.col + p) = handles.I_gray;
I4 = double(zeros(handles.row, handles.col));

for x = 1+p:handles.row+p
    for y = 1+p:handles.col+p
        a = 1;
        for m = x-p:x+p
            b = 1;
            for n = y-p:y+p
                % 將 mask 裡面的數全部加起來
                I4(x-p, y-p) = I4(x-p, y-p) + round( handles.w(a, b)*I3(m, n)/N );
                b = b+1;
            end
            a = a+1;
        end
    end
end

I4 = uint8(I4);
axes(handles.axes1); imshow(I4);

% time end

```



```
set(handles.text2, 'String', ['Overall time =', num2str( toc(timer1) ), ' sec'] );
```

```
handles.output = hObject;  
guidata(hObject, handles);
```

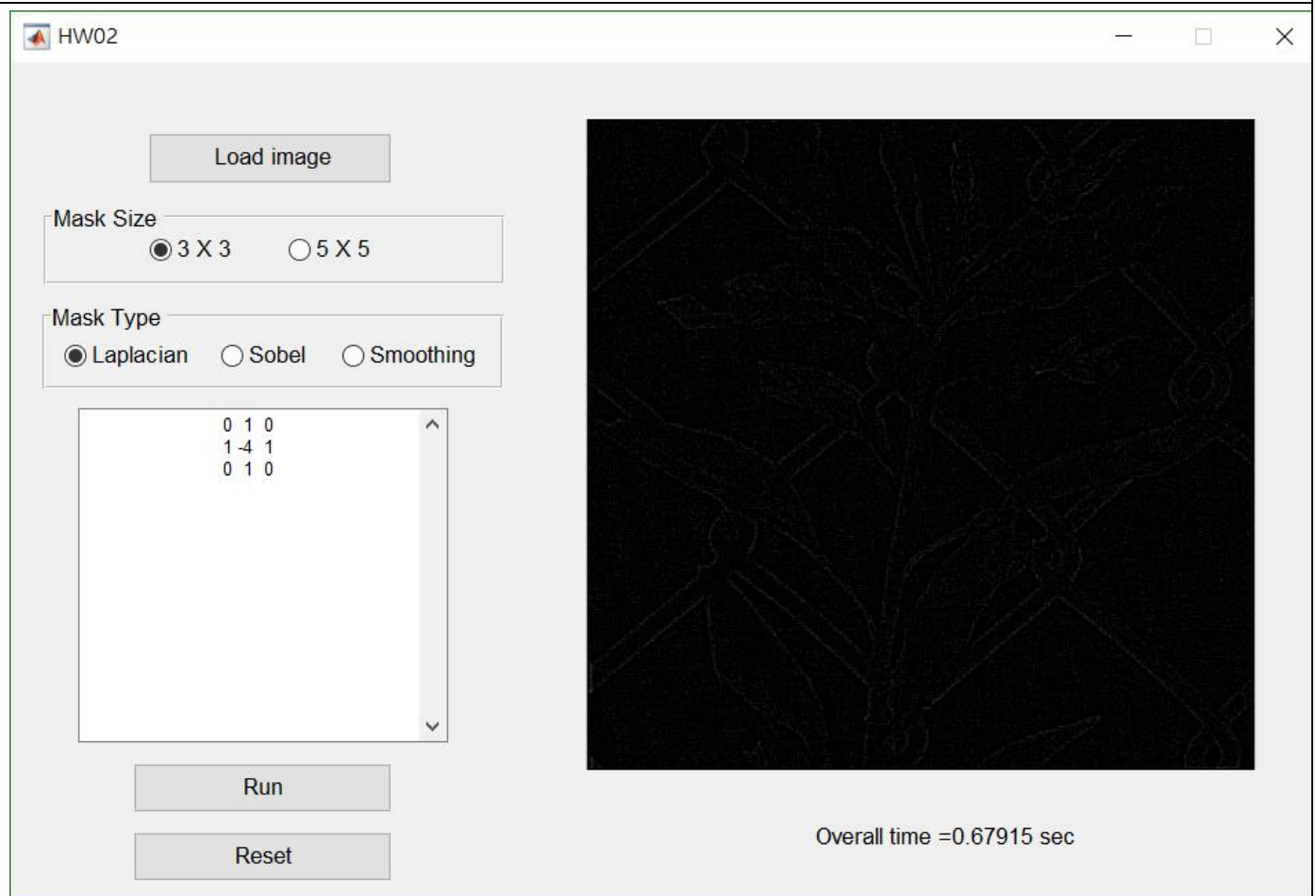
```
function pushbutton3_Callback(hObject, eventdata, handles)
```

```
set(handles radiobutton1, 'Value', 0);  
set(handles radiobutton2, 'Value', 0);  
set(handles radiobutton4, 'Value', 0);  
set(handles radiobutton5, 'Value', 0);  
set(handles radiobutton6, 'Value', 0);  
handles.w = 0;  
w(hObject, eventdata, handles);  
set(handles.text2, 'String', 'Overall time :' );
```


```
axes(handles.axes1);  
imshow(handles.I_gray);
```

結果呈現：

Laplacian 3x3



Sobel_x 3x3

 HW02

Load image


Mask Size
☒ 3 X 3 ☐ 5 X 5

Mask Type
☐ Laplacian ☒ Sobel ☐ Smoothing

1	0	-1
2	0	-2
1	0	-1


Run

Reset



Overall time =0.63852 sec

Smoothing 3x3

 HW02

Load image


Mask Size
☒ 3 X 3 ☐ 5 X 5

Mask Type
☐ Laplacian ☐ Sobel ☒ Smoothing

1	1	1
1	1	1
1	1	1

Run

Reset



Overall time =0.64351 sec

Laplacian 5x5

HW02

— □ ×

Load image


Mask Size
☐ 3 X 3 ☒ 5 X 5

Mask Type
☒ Laplacian ☐ Sobel ☐ Smoothing

0	0	1	0	0
0	1	2	1	0
1	2	-16	2	1
0	1	2	1	0
0	0	1	0	0

Run

Reset



Overall time = 1.5705 sec

Sobel_x 5x5

HW02

— □ ×

Load image


Mask Size
☐ 3 X 3 ☒ 5 X 5

Mask Type
☐ Laplacian ☒ Sobel ☐ Smoothing

1	2	0	-2	-1
4	8	0	-8	-4
6	12	0	-12	-6
4	8	0	-8	-4
1	2	0	-2	-1

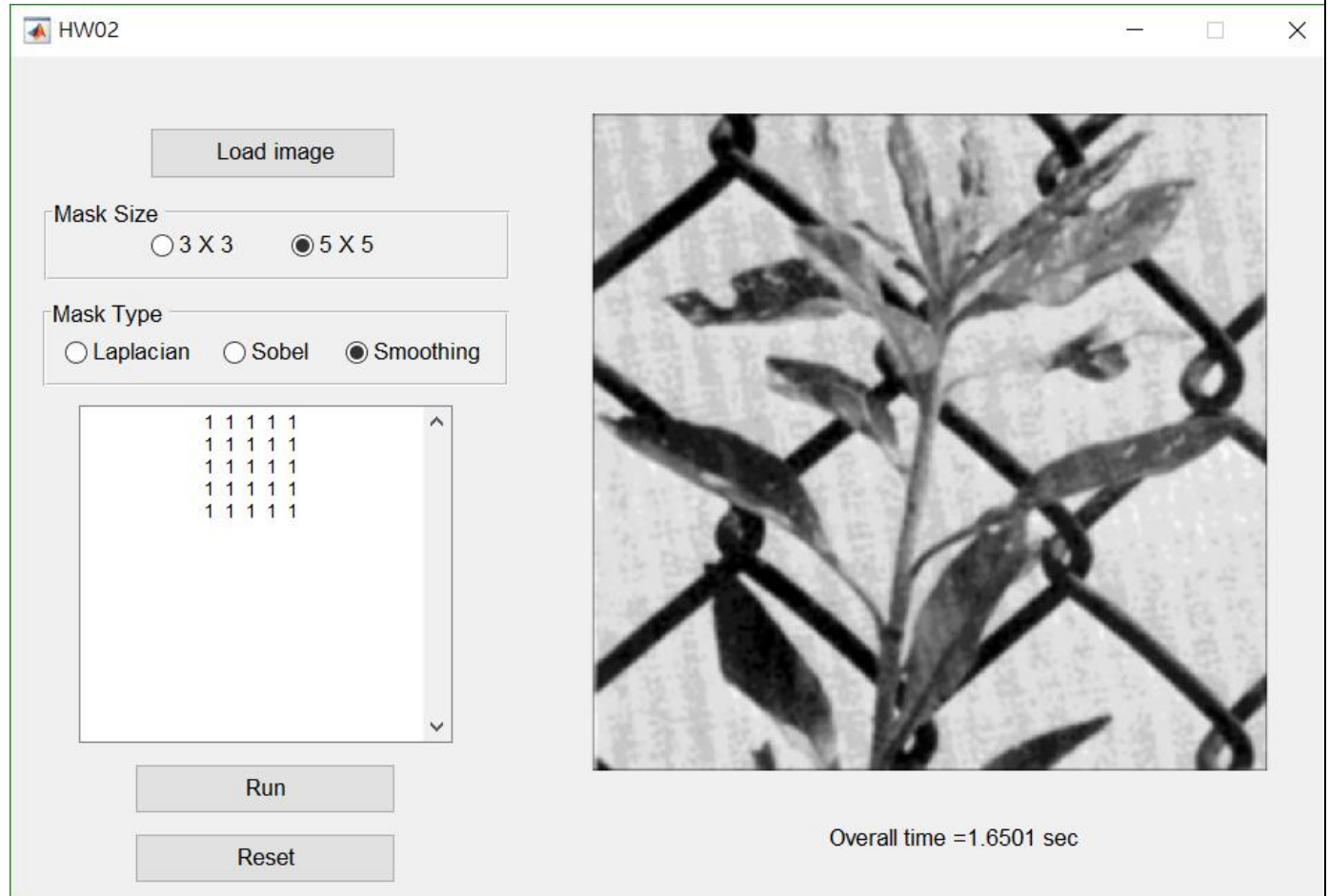
Run

Reset



Overall time = 1.5769 sec

Smoothing 5x5



結果討論：

Mask 的大小對於輸出的影像會有很大的影響，像是從 smoothing 就可以看出 5x5 較 3x3 模糊，而 Laplacian 和 Sobel 因為 5x5 沒有明確的定義，所以 weight 不太一樣，以至於輸出的影像也是大不相同。

至於計算時間的部分，我設計在 GUI 的右下角，可以看到 mask 的大小很明顯地影響計算速度，只要是 5x5 計算時間都大於 3x3，而不同 type 的 mask 大小相同的 mask，計算時間則差不多。

Part 3: (25%)

程式碼：

```
function varargout = HW03(varargin)
```

```
gui_Singleton = 1;
```

```
gui_State = struct('gui_Name',       mfilename, ...  
                  'gui_Singleton',   gui_Singleton, ...  
                  'gui_OpeningFcn', @HW03_OpeningFcn, ...  
                  'gui_OutputFcn',  @HW03_OutputFcn, ...  
                  'gui_LayoutFcn',  [], ...  
                  'gui_Callback',    []);
```

```
if nargin && ischar(varargin{1})
```

```
    gui_State.gui_Callback = str2func(varargin{1});
```

```
end
```

```
if nargin
    [varargout{1:nargout}] = gui_mainfcn(gui_State, varargin{:});
else
    gui_mainfcn(gui_State, varargin{:});
end
```

```
function HW03_OpeningFcn(hObject, eventdata, handles, varargin)
```

```
handles.output = hObject;
guidata(hObject, handles);
```

```
function varargout = HW03_OutputFcn(hObject, eventdata, handles)
```

```
varargout{1} = handles.output;
```

```
function pushbutton1_Callback(hObject, eventdata, handles)
```

```
% 原圖
```

```
filename = uigetfile({'*.jpg;*.tif;*.png;*.gif;*.bmp','All Image Files'});
handles.I = imread(filename);
```

```
[handles.row, handles.col, handles.lay] = size(handles.I);
```

```
if handles.lay == 1
```

```
    handles.I_gray = handles.I;
    fprintf('gray image\n');
```

```
elseif handles.lay == 3
```

```
    handles.R = uint8(handles.I(:, :, 1));
    handles.G = uint8(handles.I(:, :, 2));
    handles.B = uint8(handles.I(:, :, 3));
    handles.I_gray = 0.299*handles.R + 0.587*handles.G + 0.114*handles.B;
    fprintf('color image\n');
```

```
end
```

```
axes(handles.axes1);
```

```

imshow(handles.I_gray);

% Marr-Hildreth
handles.LoG = [0 0 -1 0 0
               0 -1 -2 -1 0
               -1 -2 16 -2 -1
               0 -1 -2 -1 0
               0 0 -1 0 0];

% p 隨 mask 的大小改變，例如: 3x3 => p = 1, 5x5 => p = 2
p = ( size(handles.LoG, 1) - 1 ) / 2;

I3 = double(zeros(handles.row+2*p, handles.col+2*p));
I3(1 + p:handles.row + p, 1 + p:handles.col + p) = handles.I_gray;
I4 = double(zeros(handles.row, handles.col));

for x = 1+p:handles.row+p
    for y = 1+p:handles.col+p
        a = 1;
        for m = x-p:x+p
            b = 1;
            for n = y-p:y+p
                % 將 mask 裡面的數全部加起來
                I4(x-p, y-p) = I4(x-p, y-p) + round( handles.LoG(a, b)*I3(m, n) );
                b = b+1;
            end
            a = a+1;
        end
    end
end

I4 = uint8(I4);
axes(handles.axes2); imshow(I4);

% Sobel_x
handles.Sx = [-1 0 1
               -2 0 2
               -1 0 1];

% p 隨 mask 的大小改變，例如: 3x3 => p = 1, 5x5 => p = 2
p = ( size(handles.Sx, 1) - 1 ) / 2;

I3 = double(zeros(handles.row+2*p, handles.col+2*p));

```

```

I3(1 + p:handles.row + p, 1 + p:handles.col + p) = handles.I_gray;
I4 = double(zeros(handles.row, handles.col));

for x = 1+p:handles.row+p
    for y = 1+p:handles.col+p
        a = 1;
        for m = x-p:x+p
            b = 1;
            for n = y-p:y+p
                % 將 mask 裡面的數全部加起來
                I4(x-p, y-p) = I4(x-p, y-p) + round( handles.Sx(a, b)*I3(m, n) );
                b = b+1;
            end
            a = a+1;
        end
    end
end
I5 = uint8(I4);

% Sobel_y
handles.Sy = [-1 -2 -1
               0 0 0
               1 2 1];

% p 隨 mask 的大小改變，例如: 3x3 => p = 1, 5x5 => p = 2
p = ( size(handles.Sy, 1) - 1 ) / 2;

I3 = double(zeros(handles.row+2*p, handles.col+2*p));
I3(1 + p:handles.row + p, 1 + p:handles.col + p) = handles.I_gray;
I4 = double(zeros(handles.row, handles.col));

for x = 1+p:handles.row+p
    for y = 1+p:handles.col+p
        a = 1;
        for m = x-p:x+p
            b = 1;
            for n = y-p:y+p
                % 將 mask 裡面的數全部加起來
                I4(x-p, y-p) = I4(x-p, y-p) + round( handles.Sy(a, b)*I3(m, n) );
                b = b+1;
            end
            a = a+1;
        end
    end
end

```

```

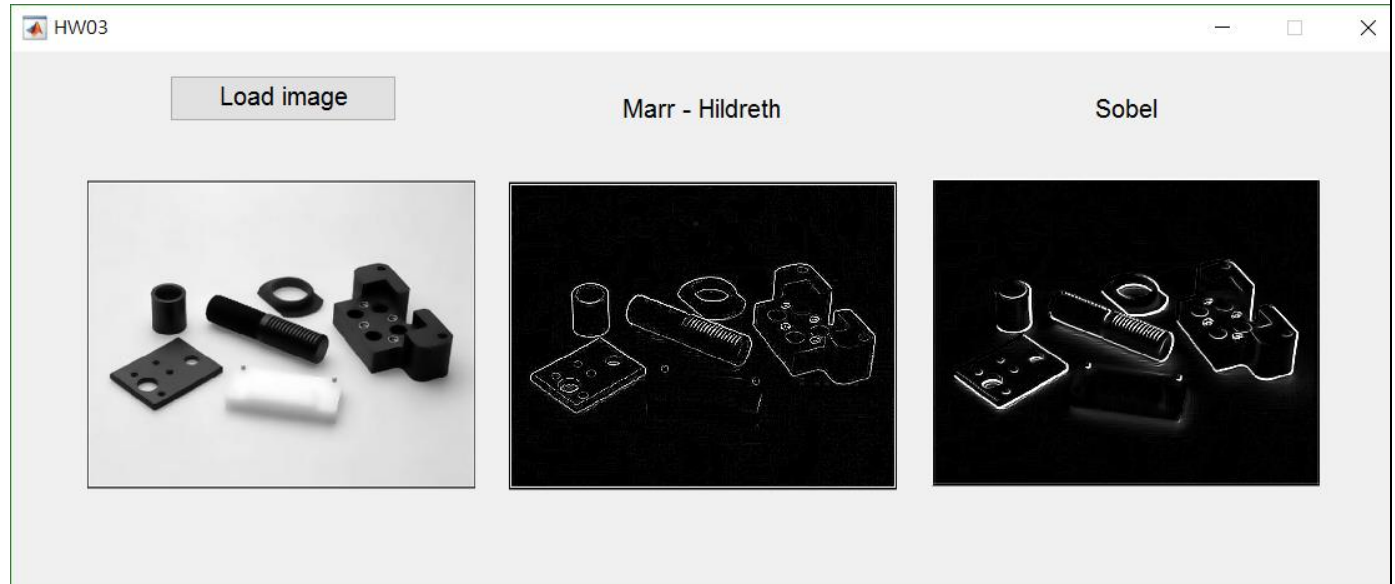
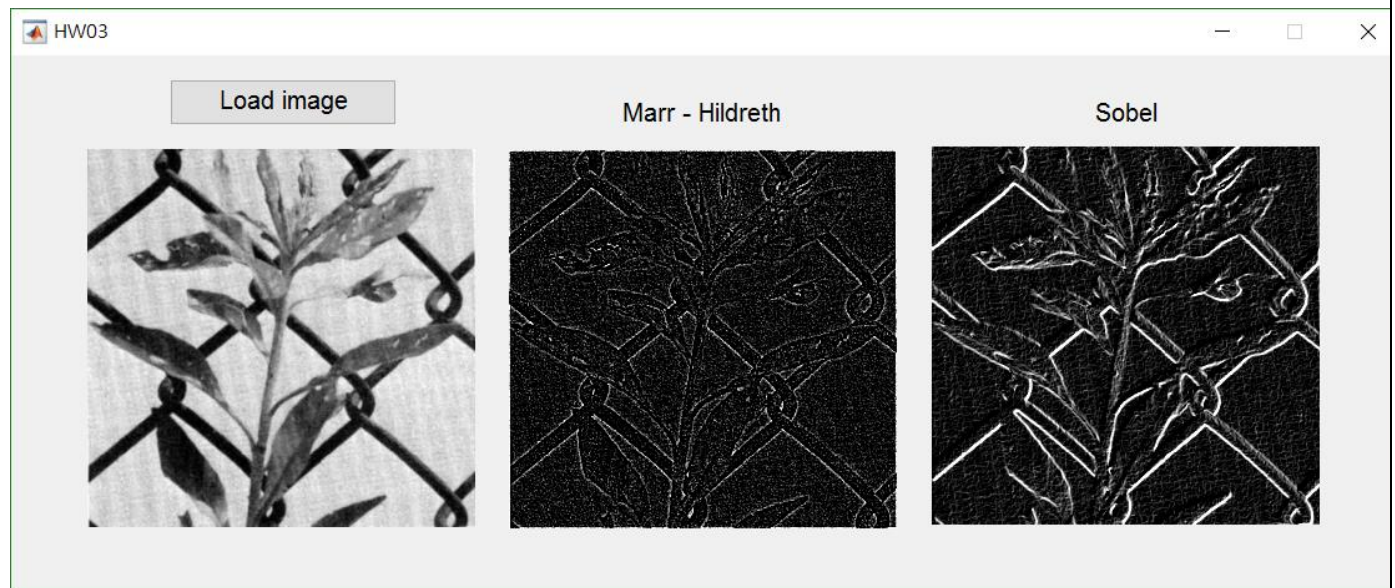
end
end
I6 = uint8(I4);

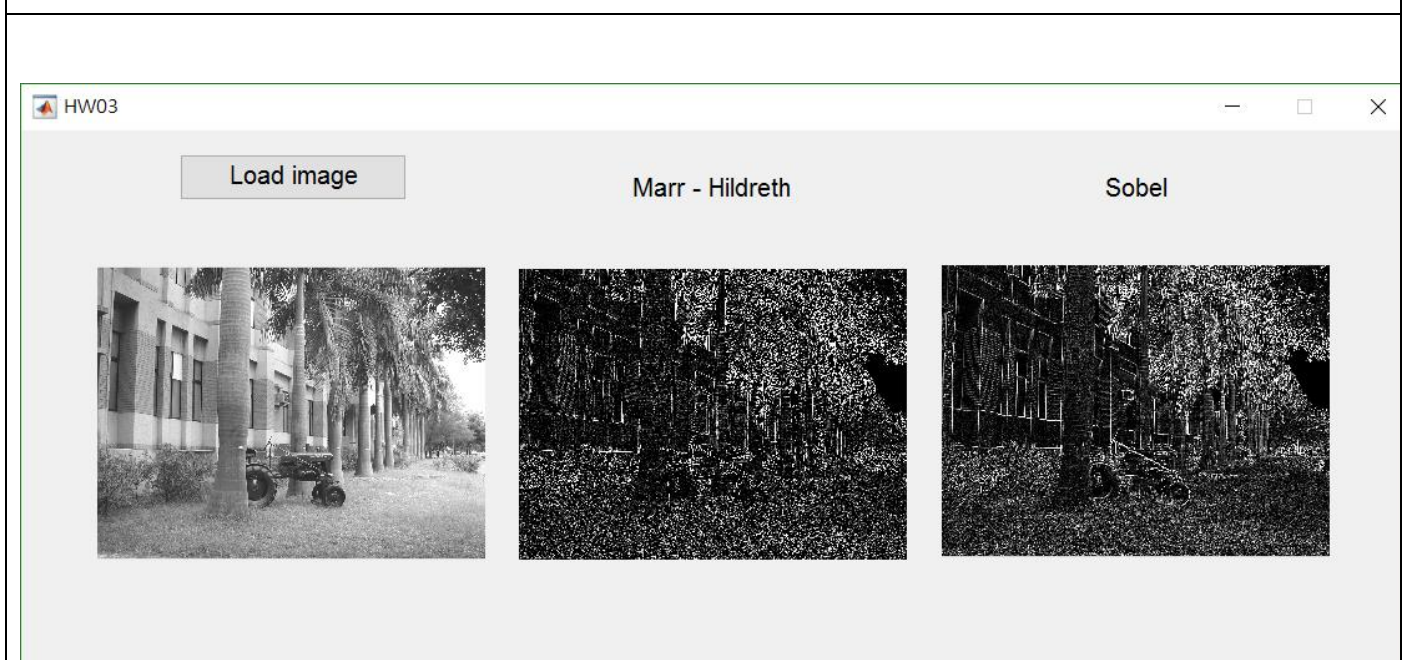
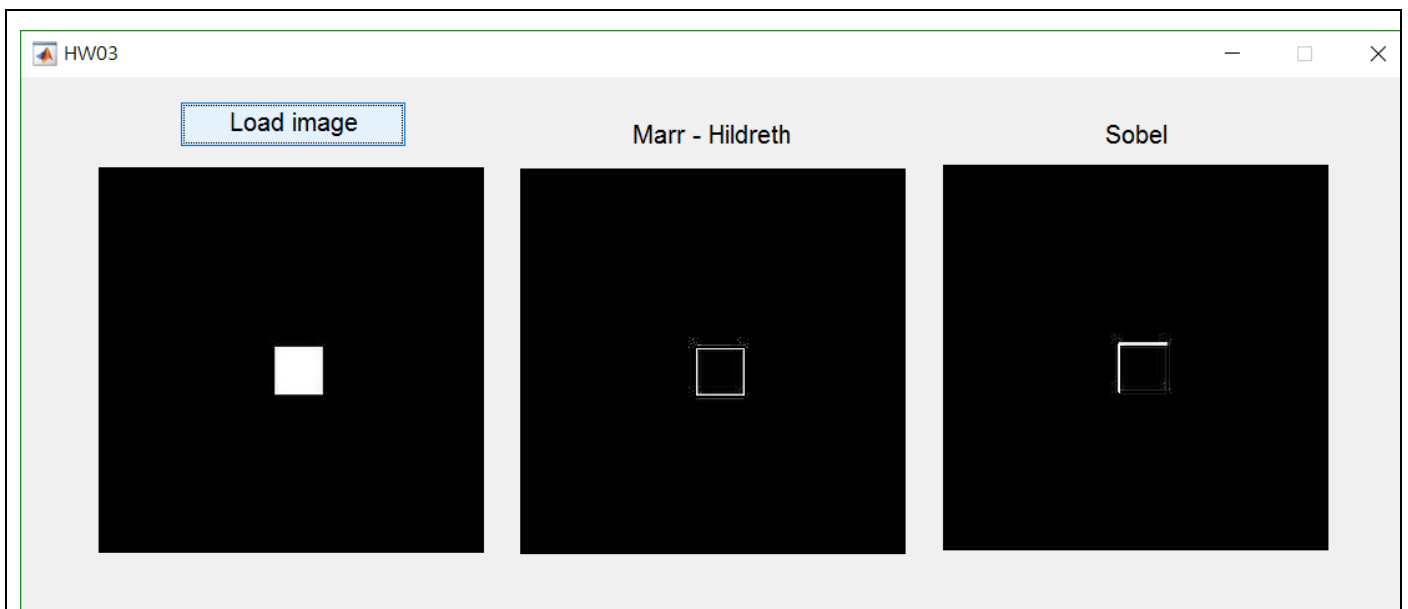
% Sobel_x + Sobel_y
axes(handles.axes3); imshow(I5+I6);

handles.output = hObject;
guidata(hObject, handles);

```

結果呈現：





結果討論：

由上面四種不同圖片可以發現，Marr – Hildreth 整體的輪廓較 Sobel 均勻，因為 Sobel 是利用 x 方向和 y 方向的一階導數相加，但是由於微分的方向不同，因此出來的圖片輪廓，總是會有某個方向不太完整；而 Marr – Hildreth 就沒有這個問題，他是使用 Laplacian of Gaussian 的 mask 來對圖片 convolution，而這個 mask 的特點之一就是上下左右對稱，因此運算出來的輪廓在四個方向較均勻。

Part 4: (25%)

程式碼：

```
function varargout = HW04(varargin)
```

```
gui_Singleton = 1;
```

```
gui_State = struct('gui_Name',       mfilename, ...
                  'gui_Singleton',   gui_Singleton, ...
                  'gui_OpeningFcn', @HW04_OpeningFcn, ...
```

```

        'gui_OutputFcn', @HW04_OutputFcn, ...
        'gui_LayoutFcn', [] , ...
        'gui_Callback', []);
if nargin && ischar(varargin{1})
    gui_State.gui_Callback = str2func(varargin{1});
end

if nargin
    [varargout{1:nargout}] = gui_mainfcn(gui_State, varargin{:});
else
    gui_mainfcn(gui_State, varargin{:});
end

function HW04_OpeningFcn(hObject, eventdata, handles, varargin)

handles.output = hObject;
guidata(hObject, handles);

function varargout = HW04_OutputFcn(hObject, eventdata, handles)

varargout{1} = handles.output;

function pushbutton1_Callback(hObject, eventdata, handles)

% 原圖
filename = uigetfile({'*.jpg;*.tif;*.png;*.gif;*.bmp','All Image Files'});
handles.I = imread(filename);

[handles.row, handles.col, handles.lay] = size(handles.I);

if handles.lay == 1
    handles.I_gray = handles.I;
    fprintf('gray image\n');
elseif handles.lay == 3
    handles.R = uint8(handles.I(:, :, 1));
    handles.G = uint8(handles.I(:, :, 2));

```

```

handles.B = uint8(handles.I(:, :, 3));
handles.I_gray = 0.299*handles.R + 0.587*handles.G + 0.114*handles.B;
fprintf('color image\n');
end

axes(handles.axes1);
imshow(handles.I_gray);

% Sobel_x
handles.Sx = [-1 0 1
              -2 0 2
              -1 0 1];

% p 隨 mask 的大小改變，例如: 3x3 => p = 1, 5x5 => p = 2
p = ( size(handles.Sx, 1) - 1 ) / 2;

I3 = double(zeros(handles.row+2*p, handles.col+2*p));
I3(1 + p:handles.row + p, 1 + p:handles.col + p) = handles.I_gray;
I4 = double(zeros(handles.row, handles.col));

for x = 1+p:handles.row+p
    for y = 1+p:handles.col+p
        a = 1;
        for m = x-p:x+p
            b = 1;
            for n = y-p:y+p
                % 將 mask 裡面的數全部加起來
                I4(x-p, y-p) = I4(x-p, y-p) + round( handles.Sx(a, b)*I3(m, n) );
                b = b+1;
            end
            a = a+1;
        end
    end
end

I5 = uint8(I4);

% Sobel_y
handles.Sy = [-1 -2 -1
              0 0 0
              1 2 1];

% p 隨 mask 的大小改變，例如: 3x3 => p = 1, 5x5 => p = 2
p = ( size(handles.Sy, 1) - 1 ) / 2;

```

```

I3 = double(zeros(handles.row+2*p, handles.col+2*p));
I3(1 + p:handles.row + p, 1 + p:handles.col + p) = handles.I_gray;
I4 = double(zeros(handles.row, handles.col));

for x = 1+p:handles.row+p
    for y = 1+p:handles.col+p
        a = 1;
        for m = x-p:x+p
            b = 1;
            for n = y-p:y+p
                % 將 mask 裡面的數全部加起來
                I4(x-p, y-p) = I4(x-p, y-p) + round( handles.Sy(a, b)*I3(m, n) );
                b = b+1;
            end
            a = a+1;
        end
    end
end
end
I6 = uint8(I4);

% Sobel_x + Sobel_y
axes(handles.axes3); imshow(I5+I6);

% Fuzzy sets
I7 = double(zeros(handles.row, handles.col));
for x = 1+p:handles.row+p
    for y = 1+p:handles.col+p
        d = zeros(3);
        a = 1;
        for m = x-p:x+p
            b = 1;
            for n = y-p:y+p
                % intensity difference
                d(a, b) = I3(m, n) - I3(x, y);
                b = b + 1;
            end
            a = a + 1;
        end
    end

    if abs( d(1, 2) ) <= 10 && abs( d(2, 3) ) <= 10
        I7(x-p, y-p) = 0;
    end
end

```

```
elseif abs( d(2, 3) ) <= 10 && abs( d(3, 2) ) <= 10
```

```
    I7(x-p, y-p) = 0;
```

```
elseif abs( d(3, 2) ) <= 10 && abs( d(2, 1) ) <= 10
```

```
    I7(x-p, y-p) = 0;
```

```
elseif abs( d(2, 1) ) <= 10 && abs( d(1, 2) ) <= 10
```

```
    I7(x-p, y-p) = 0;
```

```
else
```

```
    I7(x-p, y-p) = 255;
```

```
end
```

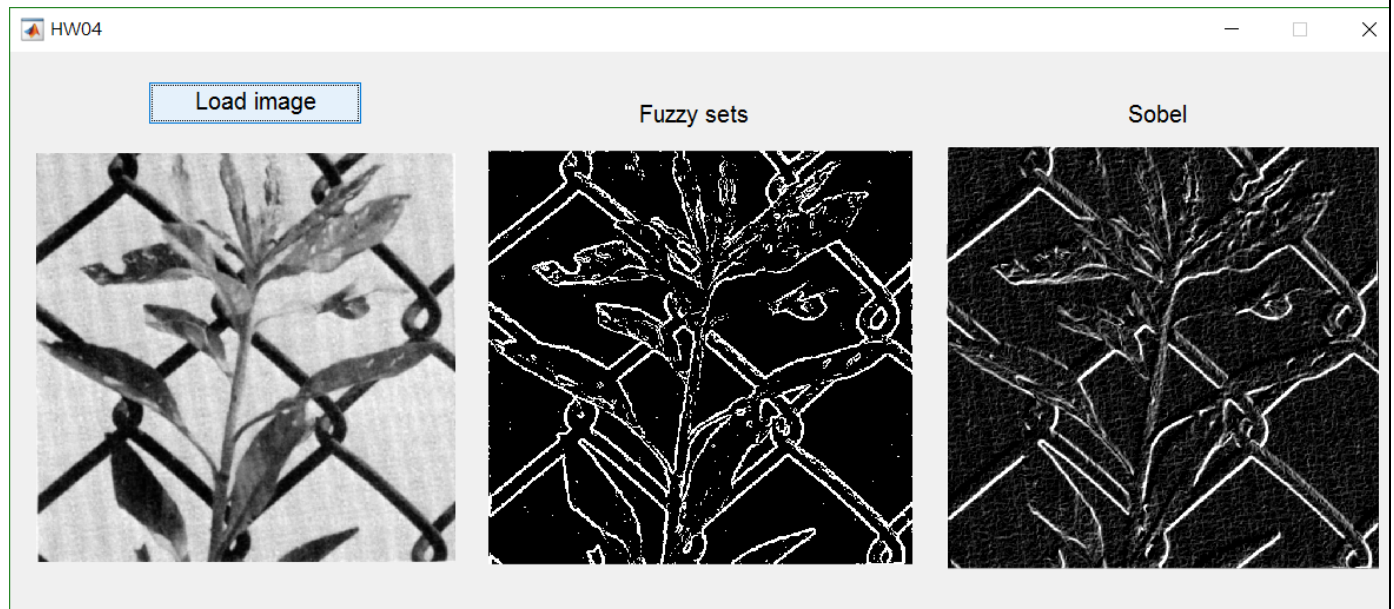
```
end
```

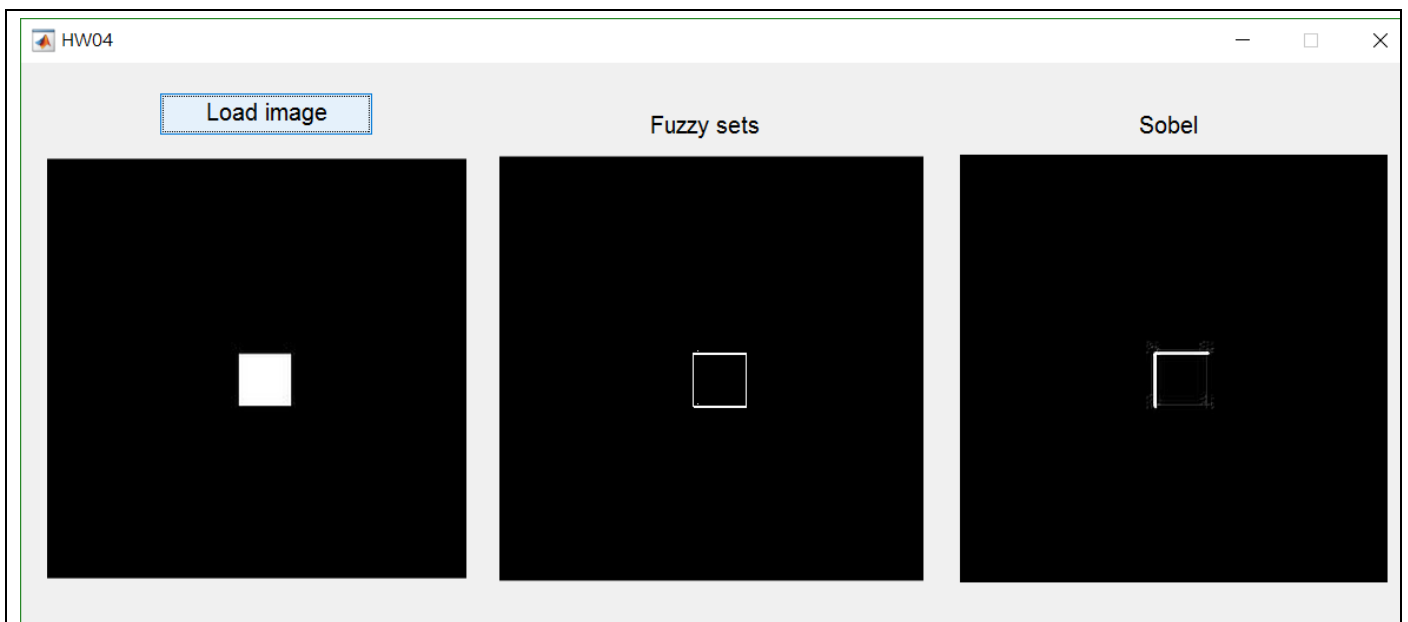
```
end
```

```
I7 = uint8(I7);
```

```
axes(handles.axes2); imshow(I7);
```

結果呈現：





結果討論：

相較於 Sobel 總是會有某個方向不太完整，Fuzzy sets 因為可以自己決定上下左右各種組合的 **intensity difference** 小於正負多少就會變成黑色，像我就設定若上下左右各種組合的 **intensity difference** 若絕對值小於 10，則該 **pixel** 就設定為黑色，其他則為白色，因此可以看到較無梯度變化的地方都是黑色，而有明顯梯度變化的地方則為白色。另一方面，由於影像只有黑白，因此輸出的影像輪廓對比又更清楚。