# Reverse Engineering Algorithmic Mechanism Behind WeChat Red Envelope

Qifan Zhang, 47422183, zhangqf@shanghaitech.edu.cn School of Information Science and Technology ShanghaiTech University

Abstract—WeChat Red Envelope is now becoming a fashion around. We always ask, is it fair for every one participating in this trying-luck game? This article will look into this problem taking the case that 5 people pick 10 yuan as an example.

## I. INTRODUCTION

I give out 10 yuan for 5 people each time. Priorly my classmates and I conduct 80 trials to get the prior distribution of money every one gets by sequence of picking red envelopes. Then I guess and build up our model based on the 80 prior trials. Finally, I will test my model by 100 posterior trials. All cell phones used in our experiments are conducted on

WeChat 6.6.1 on iOS. The main results and contributions of this report are summarized as follows:

- Modeling.
- Simulation Verification.
- Theoretical Analysis.

## II. MODEL AND ALGORITHMS

From 80 prior cases, we notice that the first participant will never get more than  $\frac{2}{5}$  of the total money (i.e. 4 yuan). The distribution and potential PMF curve are showing below: Define money gotten by the jth participant is  $X_i$ .

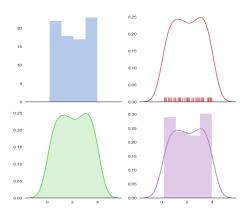


Fig. 1. Distribution of  $X_1$ 

We can see it clearly that no red envelop for the first participant is larger than 4 yuan, and from 0 to 4 yuan, it distributes nearly uniformly. Ie also found that in a 100-yuan red envelop, the first participant could get at most 40 yuan and in a 1-yuan red envelop, the first participant could get at most 0.4 yuan. According to facts above, I model that:

$$X_1 \sim Unif(0, \frac{2}{5} \times 10)$$

Then, we guess that every one except the last is following this rule, i.e.

$$X_j|X_1, X_2, ..., X_{j-1} \sim Unif(0, \frac{2}{5} \times (10 - \sum_{i=1}^{j-1} X_i)) \ (1 \le j \le 4)$$

$$X_5 = 10 - \sum_{i=1}^4 X_i$$

It does not fit the following prior distributions, but the shape is quite similar:

Therefore, we guess that it follows:

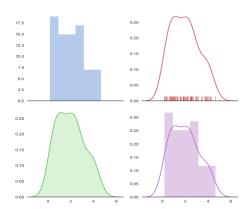


Fig. 2. Distribution of  $X_2$ 

$$X_j|X_1, X_2, ..., X_{j-1} \sim Unif(0, \frac{2}{6-i} \times (10 - \sum_{i=1}^{j-1} X_i)) \ (1 \le j \le 4)$$

$$X_5 = 10 - \sum_{i=1}^4 X_i$$
  
It works well.

Then we generalize the distribution, for a *n*-yuan red envelop for m participators:

$$X_{1} \sim Unif(0, \frac{2n}{m})$$

$$X_{j}|X_{1}, X_{2}, ..., X_{j-1} \sim Unif(0, \frac{2(n - \sum_{i=1}^{j-1} X_{i})}{m+1-j})$$

$$2 \leq j \leq m-1$$

$$X_{m} = n - \sum_{i=1}^{m} X_{i}$$

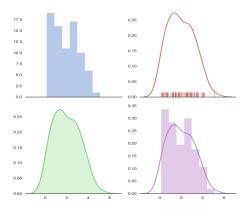


Fig. 3. Distribution of  $X_3$ 

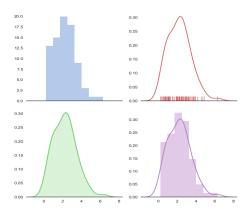


Fig. 4. Distribution of  $X_4$ 

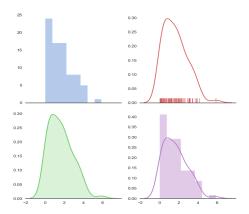


Fig. 5. Distribution of  $X_5$ 

# III. SIMULATION RESULTS

I use Python programming language for simulation:

```
import random
import sys

f = open("output.csv", "w")

def Rp(value, num):
   value_left = value
   result = []
   for i in range(num-1):
      now = random.uniform(0, (2/(num-i))*value_left)
      now = float('%.2f' %now)
```

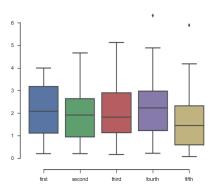


Fig. 6. Overall Distribution in one red envelop

```
result.append(now)
value_left = value_left - now
value_left = float('%.2f' %value_left)
result.append(float('%.2f' %value_left))
result_str = ''
for i in result:
    result_str = result_str + '%.2f,'%i
result_str = result_str.rstrip(',')
print(result_str, file = f)
```

I generate 100 cases for a 10-yuan red envelop for 5 participators. Results are below:

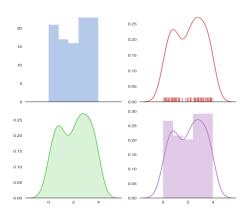


Fig. 7. Distribution of  $X_1$ 

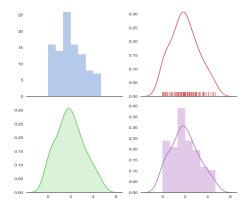


Fig. 8. Distribution of  $X_2$ 

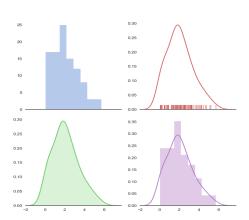


Fig. 9. Distribution of  $X_3$ 

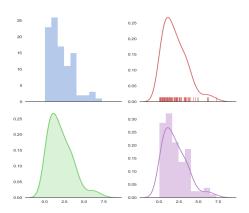


Fig. 10. Distribution of  $X_4$ 

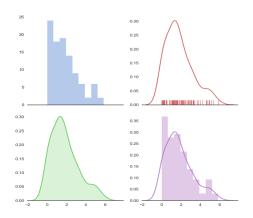


Fig. 11. Distribution of  $X_5$ 

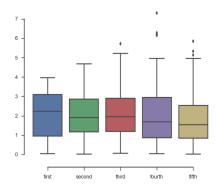


Fig. 12. Overall Distribution in one red envelop

# IV. RESULT ANALYSIS

In order to compare with my stimulation results with real ones, I do 20 more real trials combined with previous 80 trials as posterior verification.

The results are below: Intuitively, my model satisfies real

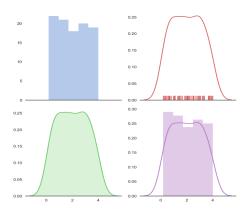


Fig. 13. Distribution of  $X_1$ 

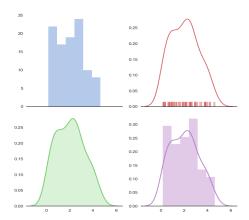


Fig. 14. Distribution of  $X_2$ 

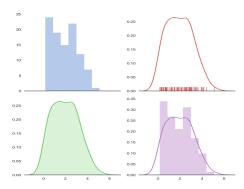


Fig. 15. Distribution of  $X_3$ 

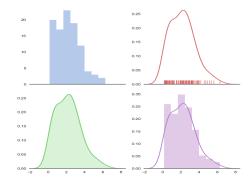


Fig. 16. Distribution of  $X_4$ 

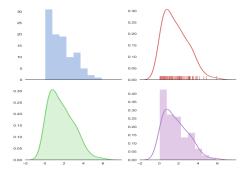


Fig. 17. Distribution of  $X_5$ 

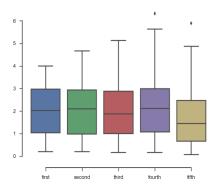


Fig. 18. Overall Distribution in one red envelop

trials very well.

Assuming that my model is right, I conduct 1 million times stimulation trials. Since 1 million is large, we see it as the whole of the distribution. **Fig.19** below shows its overall mean and variance.

It could be seen that the mean of money every one gets is 2

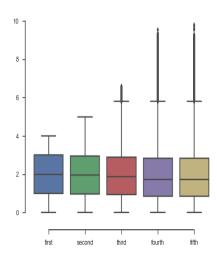


Fig. 19. Distribution of  $X_5$ 

with variance becoming larger and larger. From Standard Deviation of Probability Distribution:

$$\sigma_X = \sqrt{Var(X)}$$

$$= \lim_{n \to \infty} \sqrt{\frac{1}{N} \sum_{i=1}^n (X_i - \mu)}$$

$$S = \sqrt{\frac{1}{N-1} \sum_{i=1}^n (X_i - \mu)}$$

Compare the 1 million stimulation model with real trials, we could see that the third, fourth and fifth participants suffer more unstable distributions, which meets our expectation from the theory *Standard Deviation of Probability Distribution*. We can also see that the sharps of the distributions are quite similar

with the real ones. In all, it is a good model for red envelope distribution.

## V. CONCLUSIONS

Just like my model, define  $X_j$  as the money the jth participant gets for a n-yuan red envelop for m participators. The distribution is:

$$X_{1} \sim Unif(0, \frac{2n}{m})$$

$$X_{j}|X_{1}, X_{2}, ..., X_{j-1} \sim Unif(0, \frac{2(n - \sum_{i=1}^{j-1} X_{i})}{m+1-j}$$

$$2 \leq j \leq m-1$$

$$X_{m} = n - \sum_{i=1}^{m} X_{i}$$

Furthermore, from our model, we can learn that mean  $E(X_j)$  for each participator is the same. But variance  $Var(X_j)$  gets larger with serial numbers.

#### ACKNOWLEDGMENT

During this project, I collaborated and discussed with my classmates Cheng'an Wang, Huifan Zhang, and Letong Wang. Data of real trials are collected by Cheng'an Wang, Huifan Zhang and me. I got inspiration of *Uniform Distribution* from Zhihu[1] and Zybuluo.com[2]. I think the idea *Uniform Distribution* is quite excellent, but the author does not choose a right domain for it. All the resources of this report have been pushed to Github[3].

#### REFERENCE

- [1] https://www.zhihu.com/question/22625187/answer/85530416
- [2] "Brief Introduction to Framework Design of WeChat Red Envelope" https://www.zybuluo.com/yulin718/note/93148
- [3] https://github.com/KevinZhang199803/SI140\_Final\_Project