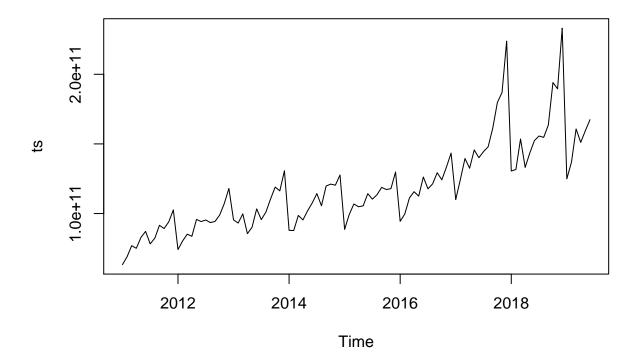
report_tsf_HW_ARIMA[1,1,1]

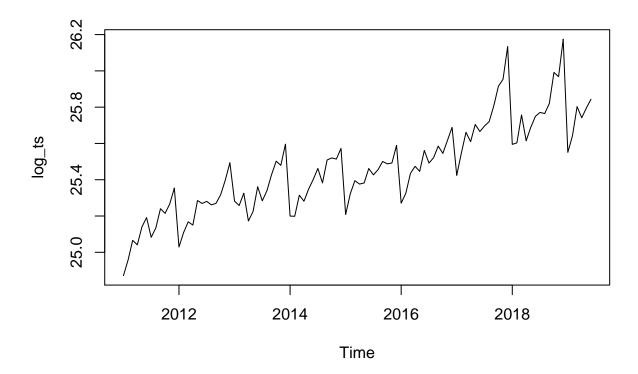
Kevork Sulahian September 6, 2019

```
library(readxl)
library(forecast)
df <- read_xls('economy.xls', sheet='2011-2019 NACE 2')</pre>
## New names:
## * `` -> ...2
## * `` -> ...3
## * `` -> ...4
## * `` -> ...5
## * `` -> ...6
## * ... and 99 more problems
df = df[4,]
df = df[-c(1,3)]
rownames(df) = df[1]
## Warning: Setting row names on a tibble is deprecated.
df = df[-1]
df = t(df)
df[] <- sapply(df[],function(x) as.numeric(as.character(x)))</pre>
df = as.numeric(df)
df= df * 1000000
ts = ts(df, start = c(2011,1), frequency = c(12))
```



In this case, it appears that an additive model is not appropriate for describing this time series, since the size of the seasonal fluctuations and random fluctuations seem to increase with the level of the time series. Thus, we may need to transform the time series in order to get a transformed time series that can be described using an additive model. For example, we can transform the time series by calculating the natural log of the original data:

```
log_ts <- log(ts)
plot.ts(log_ts)</pre>
```



Decomposing Time Series

Decomposing a time series means separating it into its constituent components, which are usually a trend component and an irregular component, and if it is a seasonal time series, a seasonal component.

Decomposing Seasonal Data

A seasonal time series consists of a trend component, a seasonal component and an irregular component. Decomposing the time series means separating the time series into these three components: that is, estimating these three components.

```
ts_components <- decompose(ts)
```

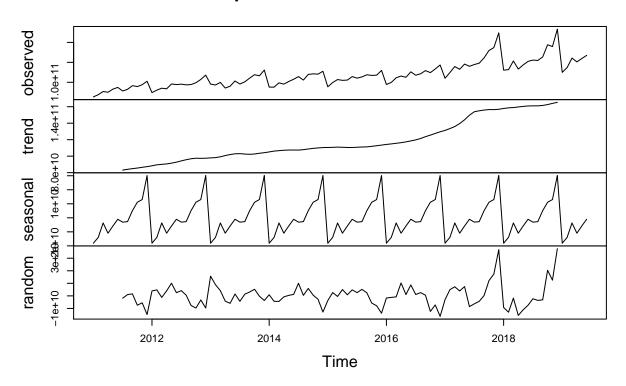
we can print out the estimated values of the seasonal component

ts_components\$seasonal

```
##
                              Feb
                 Jan
                                           Mar
                                                         Apr
                                                                      May
## 2011 -18114721416 -13972761892
                                   -3652881535 -10968033321
                                                              -5840660702
## 2012 -18114721416 -13972761892
                                                              -5840660702
                                   -3652881535 -10968033321
## 2013 -18114721416 -13972761892
                                   -3652881535 -10968033321
                                                              -5840660702
## 2014 -18114721416 -13972761892
                                   -3652881535 -10968033321
                                                              -5840660702
## 2015 -18114721416 -13972761892 -3652881535 -10968033321
                                                              -5840660702
```

```
## 2016 -18114721416 -13972761892
                                     -3652881535 -10968033321
                                                                 -5840660702
  2017 -18114721416 -13972761892
                                     -3652881535 -10968033321
                                                                 -5840660702
   2018 -18114721416
                      -13972761892
                                     -3652881535
                                                 -10968033321
                                                                 -5840660702
##
   2019
        -18114721416
                      -13972761892
                                     -3652881535
                                                  -10968033321
                                                                 -5840660702
##
                  Jun
                                Jul
                                              Aug
                                                            Sep
                                                                         Oct
## 2011
         -1030591654
                                     -2737647830
                       -3088941580
                                                    5107804253
                                                                 11091117274
  2012
         -1030591654
                       -3088941580
                                     -2737647830
                                                    5107804253
                                                                 11091117274
## 2013
         -1030591654
                       -3088941580
                                     -2737647830
                                                    5107804253
                                                                 11091117274
##
  2014
         -1030591654
                       -3088941580
                                     -2737647830
                                                    5107804253
                                                                 11091117274
##
  2015
         -1030591654
                       -3088941580
                                     -2737647830
                                                    5107804253
                                                                 11091117274
   2016
         -1030591654
                       -3088941580
                                     -2737647830
                                                    5107804253
                                                                 11091117274
   2017
                       -3088941580
                                     -2737647830
##
         -1030591654
                                                    5107804253
                                                                 11091117274
##
   2018
         -1030591654
                       -3088941580
                                     -2737647830
                                                    5107804253
                                                                 11091117274
   2019
         -1030591654
##
##
                  Nov
                                Dec
##
  2011
         13028793837
                       30178524566
   2012
##
         13028793837
                       30178524566
  2013
         13028793837
                       30178524566
  2014
##
         13028793837
                       30178524566
   2015
         13028793837
                       30178524566
##
   2016
         13028793837
                       30178524566
  2017
         13028793837
                       30178524566
## 2018
         13028793837
                       30178524566
## 2019
```

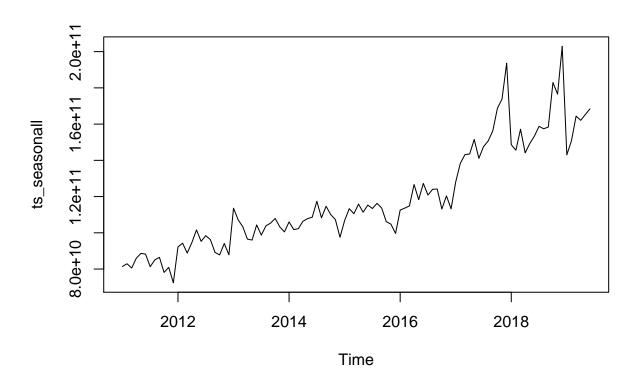
Decomposition of additive time series



The plot above shows the original time series (top), the estimated trend component (second from top), the estimated seasonal component (third from top), and the estimated irregular component (bottom)

Seasonally Adjusting

```
ts_seasonall <- ts - ts_components$seasonal</pre>
```



Holt-Winters Exponential Smoothing

```
ts_forcaste <- HoltWinters(ts)</pre>
{\tt ts\_forcaste}
## Holt-Winters exponential smoothing with trend and additive seasonal component.
##
## Call:
## HoltWinters(x = ts)
##
## Smoothing parameters:
    alpha: 0.3841348
##
    beta : 0
##
##
    gamma: 1
##
## Coefficients:
##
                [,1]
## a
       166929650345
## b
          859005492
## s1
         2680812331
         1004407035
## s2
```

```
## s3
         9728353964
##
  s4
        31427608853
        23274665015
##
   s5
        56266579294
##
   s6
##
   s7
       -47717485979
       -33061264111
##
   s8
## s9
        -7294279687
## s10 -17388238299
## s11
        -7579809787
          458749655
## s12
```

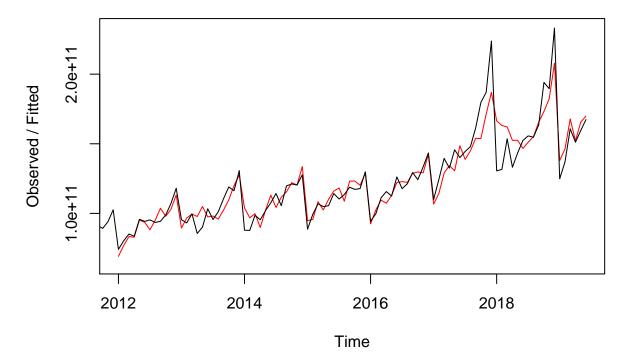
#

The value of alpha (0.41) is relatively low, indicating that the estimate of the level at the current time point is based upon both recent observations and some observations in the more distant past. The value of beta is 0.00, indicating that the estimate of the slope b of the trend component is not updated over the time series, and instead is set equal to its initial value. This makes good intuitive sense, as the level changes quite a bit over the time series, but the slope b of the trend component remains roughly the same. In contrast, the value of gamma (0.96) is high, indicating that the estimate of the seasonal component at the current time point is just based upon very recent observations

ts_forcaste\$SSE

[1] 9.131448e+21

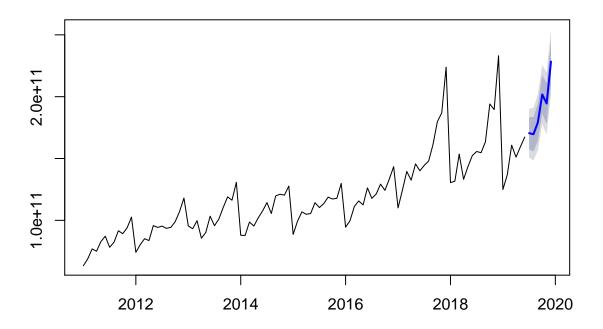
Holt-Winters filtering



```
ts_forcaste2 = forecast:::forecast.HoltWinters(ts_forcaste, h= 6)
(as.data.frame(ts_forcaste2))[1]
```

```
## Jul 2019 170469468169
## Aug 2019 169652068366
## Sep 2019 179235020787
## Oct 2019 201793281168
## Nov 2019 194499342823
## Dec 2019 228350262594
```

Forecasts from HoltWinters



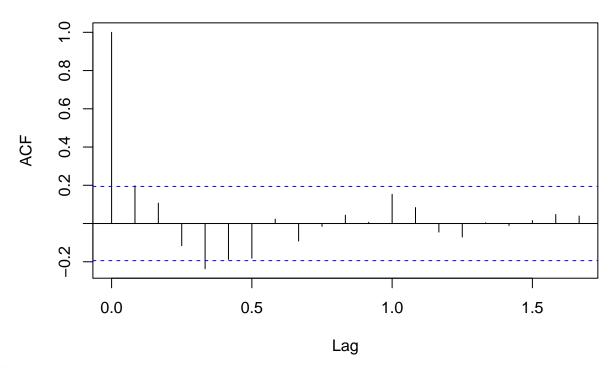
Growth

```
last_year <- window(ts, 2018, c(2018,12))
this_year <- window(ts, 2019)
this_year_predict_HW <- (as.data.frame(ts_forcaste2))[1]
growth_HW <- growth(sum(c(this_year,as.numeric(this_year_predict_HW$`Point Forecast`))), sum(last_year)
growth_HW</pre>
```

[1] 0.05644614

We can investigate whether the predictive model can be improved upon by checking whether the in-sample forecast errors show non-zero autocorrelations at lags 1-20, by making a correlogram and carrying out the

Series ts_forcaste2\$residuals



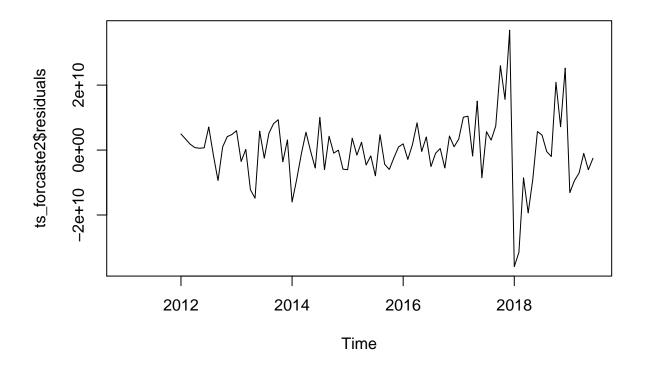
Ljung-Box test:

```
##
## Box-Ljung test
##
## data: ts_forcaste2$residuals
## X-squared = 23.626, df = 20, p-value = 0.2591
```

The correlogram shows that the autocorrelations for the in-sample forecast errors do not exceed the significance bounds for lags 1-20. Furthermore, the p-value for Ljung-Box test is 0.2, indicating that there is little evidence of non-zero autocorrelations at lags 1-20.

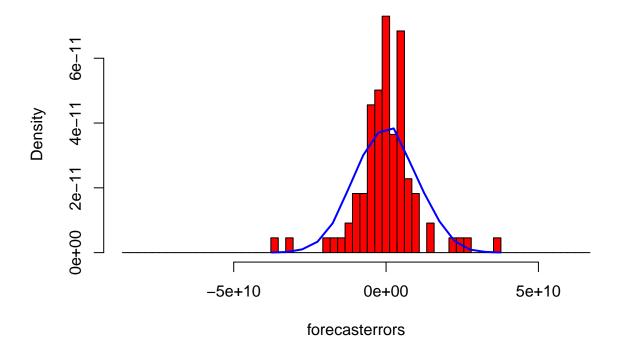
We can check whether the forecast errors have constant variance over time, and are normally distributed with mean zero, by making a time plot of the forecast errors and a histogram (with overlaid normal curve):

```
plot.ts(ts_forcaste2$residuals)
```



plotForecastErrors(ts_forcaste2\$residuals)

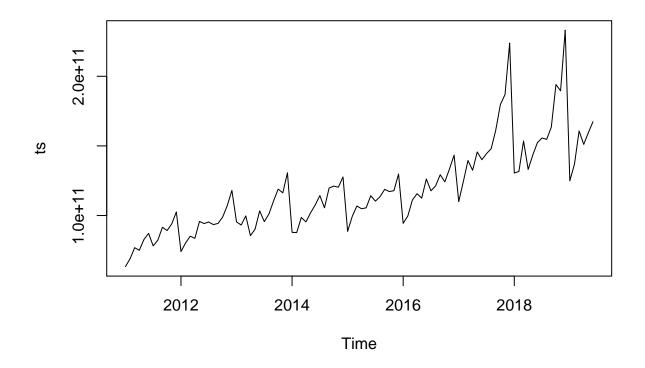
Histogram of forecasterrors



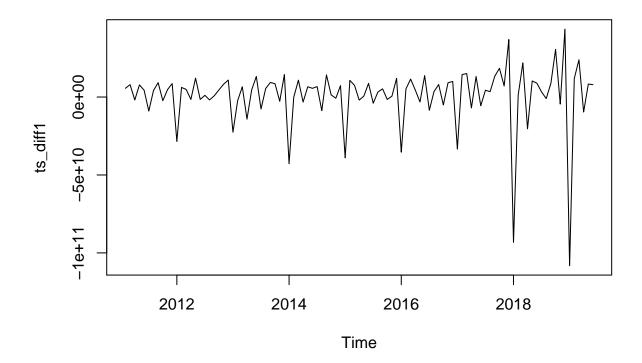
From the time plot, it appears plausible that the forecast errors have constant variance over time. From the histogram of forecast errors, it seems plausible that the forecast errors are normally distributed with mean zero

Thus, there is little evidence of autocorrelation at lags 1-20 for the forecast errors, and the forecast errors appear to be normally distributed with mean zero and constant variance over time. This suggests that Holt-Winters exponential smoothing provides an adequate predictive model of the log of total productivity, which probably cannot be improved upon. Furthermore, the assumptions upon which the prediction intervals were based are probably valid.

plot.ts(ts)



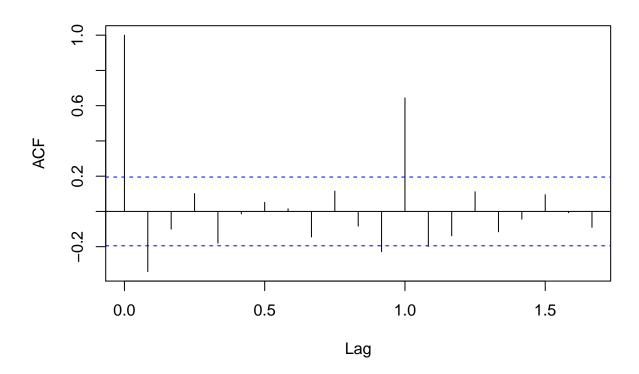
```
ts_diff1 <- diff(ts, differences = 1)
plot.ts(ts_diff1)</pre>
```



The time series of differences (above) does appear to be stationary in mean and variance, as the level of the series stays roughly constant over time, and the variance of the series appears roughly constant over time

acf(ts_diff1, lag.max=20) # plot a correlogram

Series ts_diff1



We see from the correlogram that the autocorrelation exceeds the significance bound 3 times but all the others do not exceed

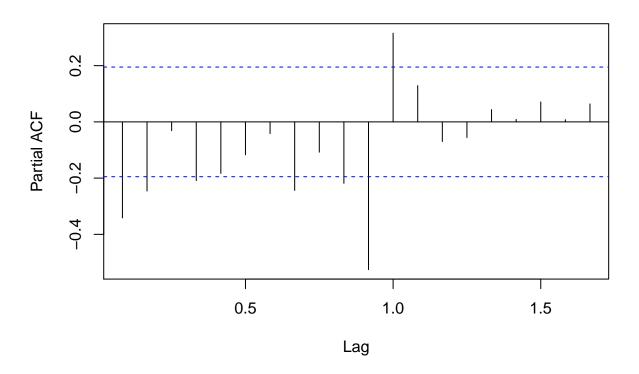
```
acf(ts_diff1, lag.max=20, plot=FALSE) # get the autocorrelation values
```

```
## ## Autocorrelations of series 'ts_diff1', by lag
##

## 0.0000 0.0833 0.1667 0.2500 0.3333 0.4167 0.5000 0.5833 0.6667 0.7500
## 1.000 -0.342 -0.101 0.101 -0.180 -0.014 0.051 0.015 -0.145 0.115
## 0.8333 0.9167 1.0000 1.0833 1.1667 1.2500 1.3333 1.4167 1.5000 1.5833
## -0.083 -0.228 0.644 -0.199 -0.138 0.112 -0.116 -0.044 0.095 -0.007
## 1.6667
## -0.090
```

pacf(ts_diff1, lag.max=20) # plot a partial correlogram

Series ts_diff1



```
pacf(ts_diff1, lag.max=20, plot=FALSE) # get the partial autocorrelation values
```

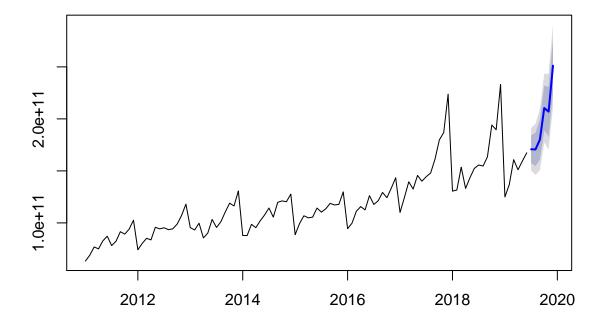
```
##
## Partial autocorrelations of series 'ts_diff1', by lag
##
## 0.0833 0.1667 0.2500 0.3333 0.4167 0.5000 0.5833 0.6667 0.7500 0.8333
## -0.342 -0.246 -0.031 -0.209 -0.183 -0.117 -0.041 -0.244 -0.108 -0.219
## 0.9167 1.0000 1.0833 1.1667 1.2500 1.3333 1.4167 1.5000 1.5833 1.6667
## -0.525 0.315 0.129 -0.070 -0.056 0.044 0.009 0.071 0.008 0.064
```

Arima, 1,1,1

```
ts_arima = Arima(ts, order=c(1,1,1),seasonal = list(order = c(1,1,1)))
ts_arima
## Series: ts
## ARIMA(1,1,1)(1,1,1)[12]
##
## Coefficients:
##
             ar1
                     ma1
                              sar1
                                      sma1
##
         -0.3595
                  0.0227
                          -0.5334
                                   0.4228
## s.e.
          0.3126 0.3363
                           1.1785
                                   1.2365
```

```
##
## sigma^2 estimated as 1.087e+20: log likelihood=-2177.43
## AIC=4364.86
                AICc=4365.58
                               BIC=4377.3
ts_arima_forecast = forecast(ts_arima,h = 6)
ts_arima_forecast
                                  Lo 80
##
                                               Hi 80
            Point Forecast
                                                             Lo 95
## Jul 2019
              170788319965 157428067448 184148572483 150355576982
              170645005267 154613295424 186676715109 146126620875
## Aug 2019
              180021974811 160869582624 199174366999 150730918630
## Sep 2019
## Oct 2019
              210457121225 188898689473 232015552977 177486345071
## Nov 2019
              206924998308 183115365432 230734631185 170511307141
## Dec 2019
              251110539040 225274163882 276946914198 211597213035
##
                   Hi 95
## Jul 2019 191221062948
## Aug 2019 195163389659
## Sep 2019 209313030992
## Oct 2019 243427897379
## Nov 2019 243338689476
## Dec 2019 290623865044
forecast:::plot.forecast(ts_arima_forecast)
```

Forecasts from ARIMA(1,1,1)(1,1,1)[12]



Growth

```
this_year_predict_ARIMA <- (as.data.frame(ts_arima_forecast))[1]
growth_ARIMA <- growth(sum(c(this_year,as.numeric(this_year_predict_ARIMA$^Point Forecast^))), sum(last growth_ARIMA</pre>
```

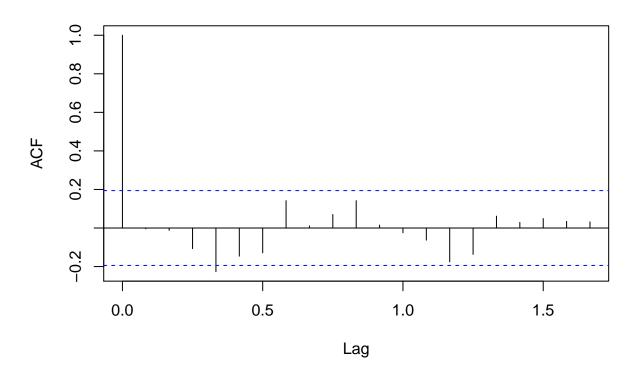
[1] 0.08018893

As in the case of exponential smoothing models, it is a good idea to investigate whether the forecast errors of an ARIMA model are normally distributed with mean zero and constant variance, and whether the are correlations between successive forecast errors.

For example, we can make a correlogram of the forecast errors for our ARIMA(0,1,1) model, and perform the Ljung-Box test for lags 1-20, by typing:

```
acf(ts_arima_forecast$residuals, lag.max=20)
```

Series ts_arima_forecast\$residuals

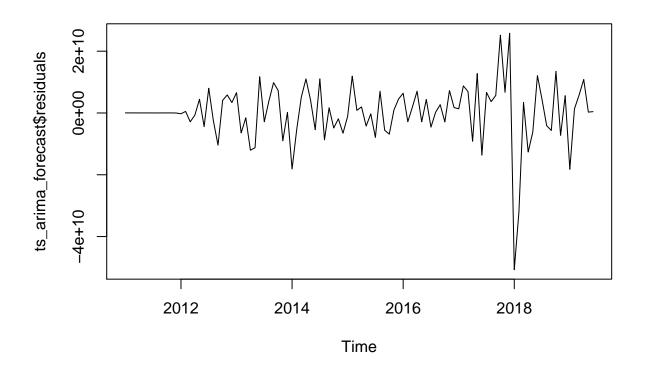


```
Box.test(ts_arima_forecast$residuals, lag=20, type="Ljung-Box")
```

```
##
## Box-Ljung test
##
## data: ts_arima_forecast$residuals
## X-squared = 23.833, df = 20, p-value = 0.2498
```

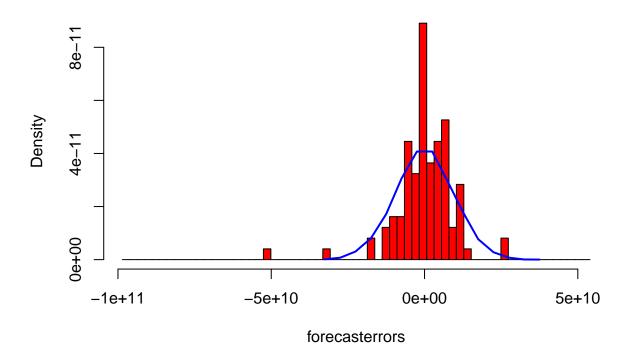
plot.ts(ts_arima_forecast\$residuals)

make time plot of forecast errors



plotForecastErrors(ts_arima_forecast\$residuals)

Histogram of forecasterrors



Since successive forecast errors do not seem to be correlated, and the forecast errors seem to be normally distributed with mean zero and constant variance, the ARIMA(0,1,1) does seem to provide an adequate predictive model

testing best arima

```
# library(forecast)
# modelAIC <- data.frame()</pre>
# for(d in 0:1){
    for(p in 0:9){
      for(q in 0:9){
#
        fit=Arima(mid.ts, order=c(p,d,q))
#
        modelAIC \leftarrow rbind(modelAIC, c(d,p,q,AIC(fit))) #
#
#
#
# }
# names(modelAIC) <- c("d", "p", "q", "AIC")
# rowNum <- which(modelAIC$AIC==max(modelAIC$AIC))</pre>
# modelAIC[rowNum,]#Required model parameters
```