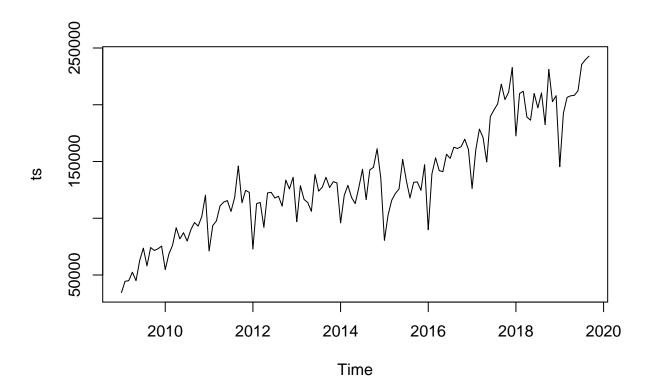
# $tsf\_export$

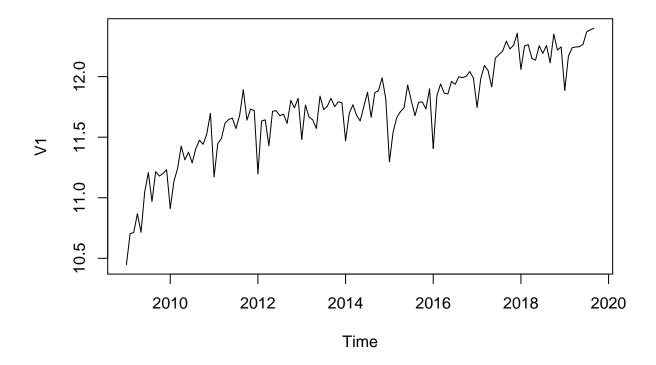
Kevork Sulahian October 28, 2019

```
library(readxl)
library(forecast)
# library(readxl)
df <- read_xlsx("Export_for_TS.xlsx")</pre>
## New names:
## * `` -> ...2
df = df[1,]
df = df[-c(1,2)]
df2 = read_xlsx('export_19xlsx.xlsx')
## New names:
## * `` -> ...1
df = t(df)
df2$...1 = c(paste0(2019,"-",1:9))
rownames(df2) =df2$...1
## Warning: Setting row names on a tibble is deprecated.
df2$...1 = NULL
colnames(df2) = "V1"
df = as.data.frame(df)
df3 = rbind(df, df2)
ts = ts(df3, start=c(2009, 1), frequency = c(12))
```



In this case, it appears that an additive model is not appropriate for describing this time series, since the size of the seasonal fluctuations and random fluctuations seem to increase with the level of the time series. Thus, we may need to transform the time series in order to get a transformed time series that can be described using an additive model. For example, we can transform the time series by calculating the natural log of the original data:

```
log_ts <- log(ts)
plot.ts(log_ts)</pre>
```



### **Decomposing Time Series**

Decomposing a time series means separating it into its constituent components, which are usually a trend component and an irregular component, and if it is a seasonal time series, a seasonal component.

### Decomposing Seasonal Data

A seasonal time series consists of a trend component, a seasonal component and an irregular component. Decomposing the time series means separating the time series into these three components: that is, estimating these three components.

```
ts_components <- decompose(ts)
```

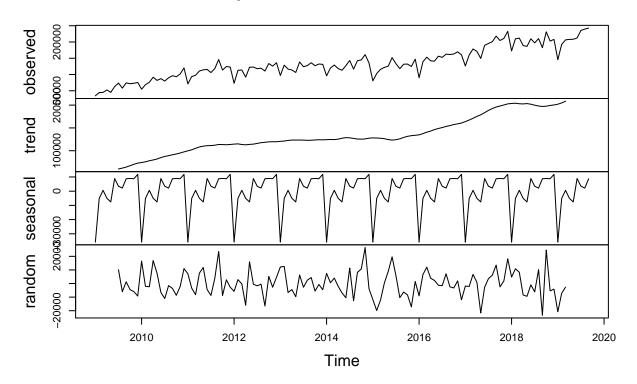
we can print out the estimated values of the seasonal component

#### ts\_components\$seasonal

```
##
                            Feb
                Jan
                                         Mar
                                                     Apr
                                                                  May
## 2009 -35837.3733
                     -5078.4271
                                    614.7571
                                              -5025.8461
                                                          -7561.9849
                     -5078.4271
## 2010 -35837.3733
                                    614.7571
                                              -5025.8461
                                                          -7561.9849
## 2011 -35837.3733
                     -5078.4271
                                    614.7571
                                              -5025.8461
                                                          -7561.9849
## 2012 -35837.3733
                     -5078.4271
                                    614.7571
                                              -5025.8461
                                                          -7561.9849
## 2013 -35837.3733
                     -5078.4271
                                    614.7571 -5025.8461
                                                          -7561.9849
```

```
## 2014 -35837.3733
                     -5078.4271
                                    614.7571 -5025.8461
                                                           -7561.9849
                                    614.7571 -5025.8461
## 2015 -35837.3733
                     -5078.4271
                                                           -7561.9849
## 2016 -35837.3733
                     -5078.4271
                                    614.7571
                                              -5025.8461
                                                           -7561.9849
                                                           -7561.9849
## 2017 -35837.3733
                     -5078.4271
                                    614.7571
                                              -5025.8461
## 2018 -35837.3733
                     -5078.4271
                                    614.7571
                                              -5025.8461
                                                           -7561.9849
                                                           -7561.9849
## 2019 -35837.3733
                     -5078.4271
                                    614.7571
                                              -5025.8461
                Jun
                             Jul
                                         Aug
                                                      Sep
                                                                  Oct
                      3476.2085
                                                            8951.2410
## 2009
          8910.0983
                                   2185.4111
                                               8757.6873
          8910.0983
## 2010
                      3476.2085
                                   2185.4111
                                               8757.6873
                                                            8951.2410
                                   2185.4111
## 2011
          8910.0983
                      3476.2085
                                               8757.6873
                                                            8951.2410
## 2012
          8910.0983
                      3476.2085
                                   2185.4111
                                               8757.6873
                                                            8951.2410
## 2013
          8910.0983
                      3476.2085
                                   2185.4111
                                               8757.6873
                                                            8951.2410
## 2014
          8910.0983
                      3476.2085
                                   2185.4111
                                               8757.6873
                                                            8951.2410
## 2015
          8910.0983
                                   2185.4111
                                                            8951.2410
                      3476.2085
                                               8757.6873
## 2016
          8910.0983
                      3476.2085
                                   2185.4111
                                               8757.6873
                                                            8951.2410
## 2017
          8910.0983
                      3476.2085
                                   2185.4111
                                               8757.6873
                                                            8951.2410
## 2018
          8910.0983
                      3476.2085
                                   2185.4111
                                               8757.6873
                                                            8951.2410
## 2019
          8910.0983
                      3476.2085
                                   2185.4111
                                               8757.6873
##
                            Dec
                Nov
## 2009
          8780.2368
                     11827.9913
## 2010
          8780.2368
                     11827.9913
## 2011
          8780.2368
                     11827.9913
## 2012
          8780.2368
                     11827.9913
## 2013
          8780.2368
                     11827.9913
## 2014
          8780.2368
                     11827.9913
## 2015
          8780.2368
                     11827.9913
## 2016
          8780.2368
                     11827.9913
## 2017
          8780.2368
                     11827.9913
          8780.2368 11827.9913
## 2018
## 2019
```

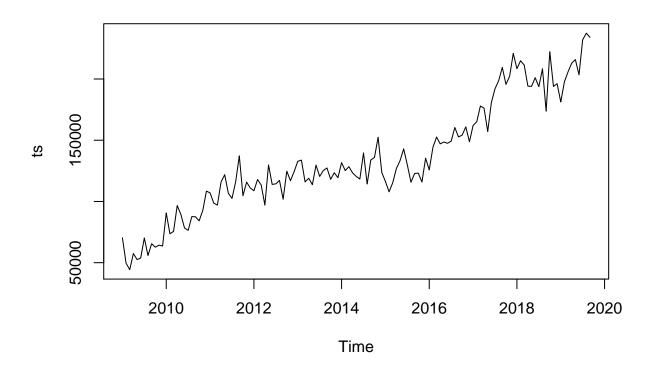
# **Decomposition of additive time series**



The plot above shows the original time series (top), the estimated trend component (second from top), the estimated seasonal component (third from top), and the estimated irregular component (bottom)

### Seasonally Adjusting

ts\_seasonall <- ts - ts\_components\$seasonal</pre>



### **Holt-Winters Exponential Smoothing**

```
ts_forcaste <- HoltWinters(ts)</pre>
ts_forcaste
## Holt-Winters exponential smoothing with trend and additive seasonal component.
##
## Call:
## HoltWinters(x = ts)
##
## Smoothing parameters:
   alpha: 0.3721975
    beta: 0.008388046
##
    gamma: 0.3879005
##
## Coefficients:
##
               [,1]
       234236.22519
## a
## b
         1800.90011
## s1
        10884.32142
## s2
         2422.24425
         6639.03969
## s3
## s4 -45793.46458
```

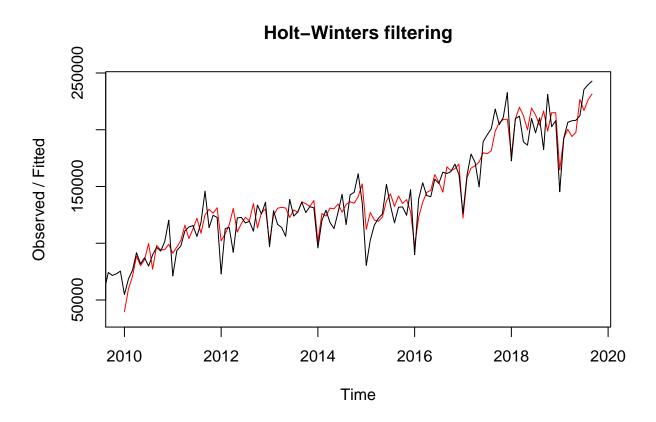
```
## s5
        -7778.48158
## s6
          -48.50151
##
  s7
        -8403.94186
       -12451.28939
##
   s8
##
   s9
         4905.92488
         6841.04904
##
  s10
## s11
         6190.87742
         4206.41639
## s12
```

#

The value of alpha (0.35) is relatively low, indicating that the estimate of the level at the current time point is based upon both recent observations and some observations in the more distant past. The value of beta is 0.01, indicating that the estimate of the slope b of the trend component is updated but doesn't have much effect over the time series, and instead is set equal to its initial value. This makes good intuitive sense, as the level changes quite a bit over the time series, but the slope b of the trend component remains roughly the same. In contrast, the value of gamma (0.38) is high, indicating that the estimate of the seasonal component at the current time point is not just based upon very recent observations

#### ts\_forcaste\$SSE

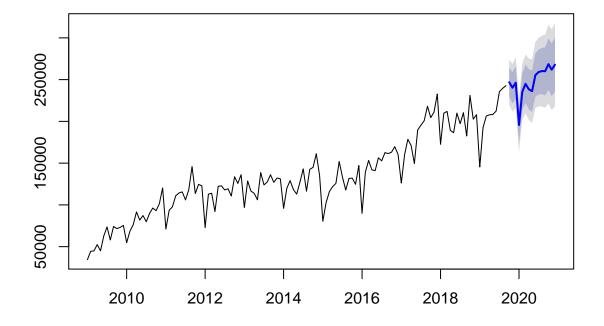
#### ## [1] 21744166076



```
ts_forcaste2 = forecast:::forecast.HoltWinters(ts_forcaste, h= 15)
(as.data.frame(ts_forcaste2))[1]
```

```
Point Forecast
## Oct 2019
                   246921.4
## Nov 2019
                   240260.3
## Dec 2019
                   246278.0
## Jan 2020
                   195646.4
## Feb 2020
                   235462.2
## Mar 2020
                   244993.1
## Apr 2020
                   238438.6
## May 2020
                   236192.1
## Jun 2020
                   255350.3
## Jul 2020
                   259086.3
## Aug 2020
                   260237.0
## Sep 2020
                   260053.4
## Oct 2020
                   268532.2
## Nov 2020
                   261871.1
## Dec 2020
                   267888.8
```

### **Forecasts from HoltWinters**



## Growth

```
year_2019 <- window(ts, 2019)
year_2019_predict_HW <- (as.data.frame(ts_forcaste2))[1][c(1:3),]
sum_year_2019 = sum(c(year_2019,year_2019_predict_HW))
year_2020 = (as.data.frame(ts_forcaste2))[1][c(4:15),]</pre>
```

```
growth_HW <- growth(sum(year_2020),sum_year_2019)
growth_HW</pre>
```

### ## [1] 0.1369446

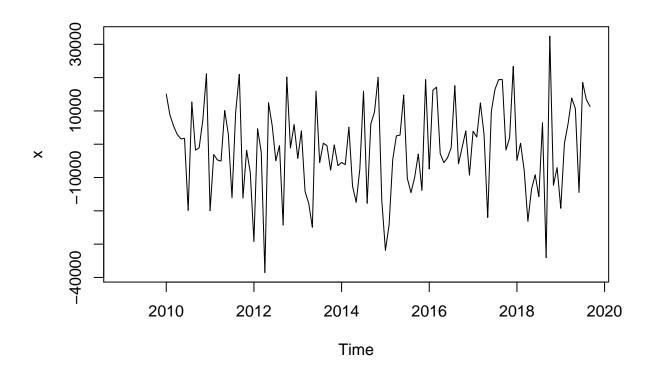
We can investigate whether the predictive model can be improved upon by checking whether the in-sample forecast errors show non-zero autocorrelations at lags 1-20, by making a correlogram and carrying out the Ljung-Box test:

```
##
## Box-Ljung test
##
## data: ts_forcaste2$residuals
## X-squared = 10.37, df = 20, p-value = 0.961
```

The correlogram shows that the autocorrelations for the in-sample forecast errors do not exceed the significance bounds for lags 1-20. Furthermore, the p-value for Ljung-Box test is 0.9, indicating that there is no evidence of non-zero autocorrelations at lags 1-20.

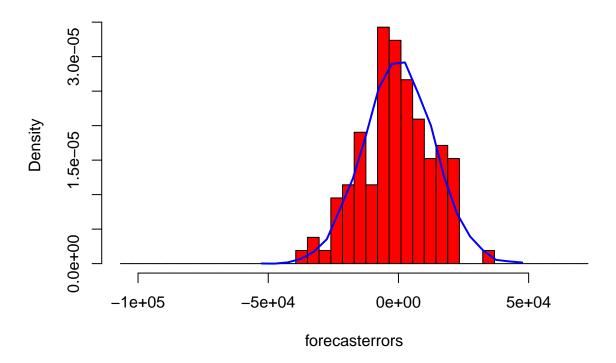
We can check whether the forecast errors have constant variance over time, and are normally distributed with mean zero, by making a time plot of the forecast errors and a histogram (with overlaid normal curve):

```
plot.ts(ts_forcaste2$residuals)
```



plotForecastErrors(ts\_forcaste2\$residuals)

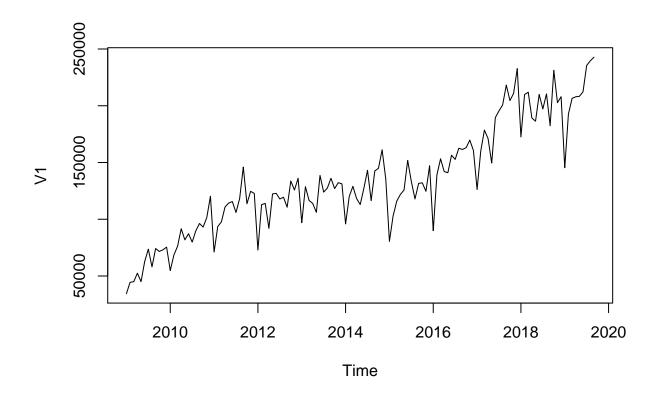
# **Histogram of forecasterrors**



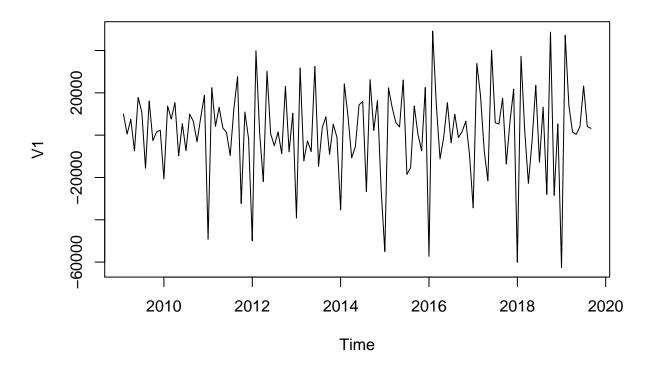
From the time plot, it appears plausible that the forecast errors have constant variance over time. From the histogram of forecast errors, it seems plausible that the forecast errors are normally distributed with mean zero.

Thus, there is little evidence of autocorrelation at lags 1-20 for the forecast errors, and the forecast errors appear to be normally distributed with mean zero and constant variance over time. This suggests that Holt-Winters exponential smoothing provides an adequate predictive model of the log of total productivity, which probably cannot be improved upon. Furthermore, the assumptions upon which the prediction intervals were based are probably valid.

plot.ts(ts)

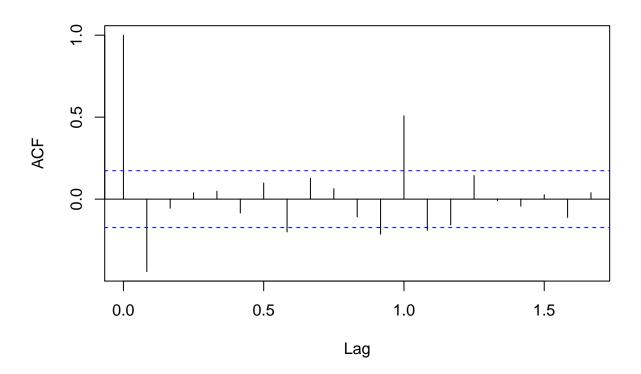


```
ts_diff1 <- diff(ts, differences = 1)
plot.ts(ts_diff1)</pre>
```



The time series of differences (above) does appear to be stationary in mean and variance, as the level of the series stays roughly constant over time, and the variance of the series appears roughly constant over time

acf(ts\_diff1, lag.max=20) # plot a correlogram



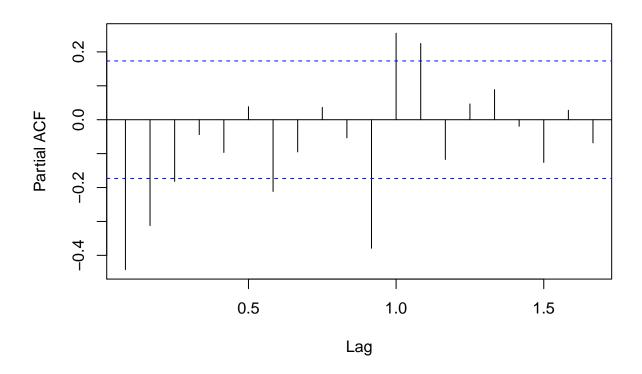
We see from the correlogram that the autocorrelation exceeds the significance bound 3 times but all the others do not exceed

```
acf(ts_diff1, lag.max=20, plot=FALSE) # get the autocorrelation values
```

```
##
## Autocorrelations of series 'ts_diff1', by lag
##
## 0.0000 0.0833 0.1667 0.2500 0.3333 0.4167 0.5000 0.5833 0.6667 0.7500
## 1.000 -0.442 -0.056 0.038 0.049 -0.085 0.098 -0.200 0.126 0.064
## 0.8333 0.9167 1.0000 1.0833 1.1667 1.2500 1.3333 1.4167 1.5000 1.5833
## 1.6667
## 0.039
pacf(ts_diff1, lag.max=20)
```

# plot a partial correlogram

### Series ts\_diff1



```
pacf(ts_diff1, lag.max=20, plot=FALSE) # get the partial autocorrelation values
```

```
## ## Partial autocorrelations of series 'ts_diff1', by lag
##
## 0.0833 0.1667 0.2500 0.3333 0.4167 0.5000 0.5833 0.6667 0.7500 0.8333
## -0.442 -0.312 -0.182 -0.044 -0.097 0.038 -0.211 -0.095 0.036 -0.053
## 0.9167 1.0000 1.0833 1.1667 1.2500 1.3333 1.4167 1.5000 1.5833 1.6667
## -0.379 0.255 0.225 -0.117 0.047 0.089 -0.019 -0.126 0.028 -0.068
```

### Arima, 0,1,0

```
ts_arima = Arima(ts, order=c(0,1,0),seasonal = list(order = c(0,1,0)))
ts_arima

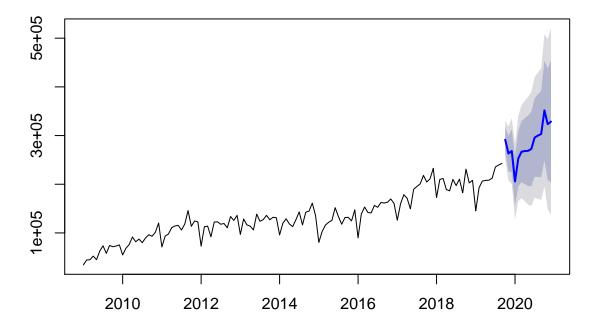
## Series: ts
## ARIMA(0,1,0)(0,1,0)[12]
##
## sigma^2 estimated as 397639845: log likelihood=-1313.06
## AIC=2628.12 AICc=2628.15 BIC=2630.87
```

```
ts_arima_forecast = forecast(ts_arima,h = 15)
ts_arima_forecast
```

```
##
            Point Forecast
                              Lo 80
                                       Hi 80
                                                Lo 95
                                                          Hi 95
                  291503.5 265948.2 317058.8 252420.1 330587.0
## Oct 2019
## Nov 2019
                  263011.9 226871.2 299152.5 207739.5 318284.2
## Dec 2019
                  268333.3 224070.2 312596.4 200638.8 336027.9
## Jan 2020
                  205722.4 154611.8 256833.0 127555.5 283889.3
## Feb 2020
                  252922.4 195779.0 310065.8 165529.1 340315.7
## Mar 2020
                  266822.4 204225.0 329419.9 171087.9 362556.9
## Apr 2020
                  268222.4 200609.4 335835.4 164817.3 371627.5
                  268622.4 196341.1 340903.7 158077.7 379167.1
## May 2020
## Jun 2020
                  272622.4 195956.5 349288.3 155372.0 389872.8
## Jul 2020
                  295822.4 215009.4 376635.4 172229.6 419415.2
## Aug 2020
                  299922.4 215165.1 384679.8 170297.2 429547.6
## Sep 2020
                  303122.4 214596.2 391648.6 167733.3 438511.5
## Oct 2020
                  351825.9 249604.7 454047.1 195492.1 508159.8
## Nov 2020
                  323334.3 209047.5 437621.1 148547.7 498120.8
## Dec 2020
                  328655.7 203460.8 453850.6 137186.6 520124.8
```

forecast:::plot.forecast(ts\_arima\_forecast)

## Forecasts from ARIMA(0,1,0)(0,1,0)[12]



### Growth

```
this_year_predict_ARIMA <- (as.data.frame(ts_arima_forecast))[1]

# growth_ARIMA <- growth(sum(c(this_year,as.numeric(this_year_predict_ARIMA$`Point Forecast`))), sum(la # growth_ARIMA

year_2019_predict_ARIMA <- (as.data.frame(ts_arima_forecast))[1][c(1:3),]
sum_year_2019 = sum(c(year_2019,year_2019_predict_ARIMA))
year_2020 = (as.data.frame(ts_arima_forecast))[1][c(4:15),]
growth_ARIMA <- growth(sum_year_2019, sum(year_2020))
-growth_ARIMA</pre>
```

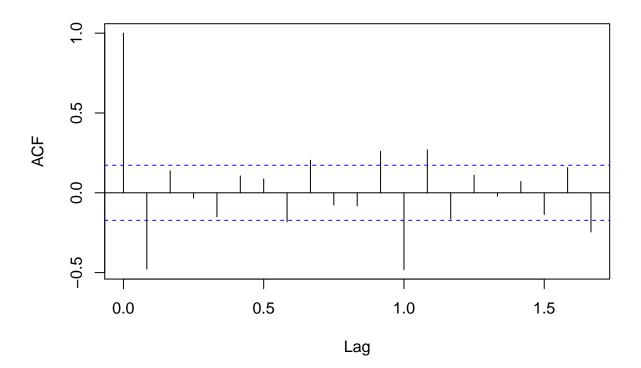
### ## [1] 0.2105728

As in the case of exponential smoothing models, it is a good idea to investigate whether the forecast errors of an ARIMA model are normally distributed with mean zero and constant variance, and whether the are correlations between successive forecast errors.

For example, we can make a correlogram of the forecast errors for our ARIMA(0,1,1) model, and perform the Ljung-Box test for lags 1-20, by typing:

```
acf(ts_arima_forecast$residuals, lag.max=20)
```

### Series ts\_arima\_forecast\$residuals



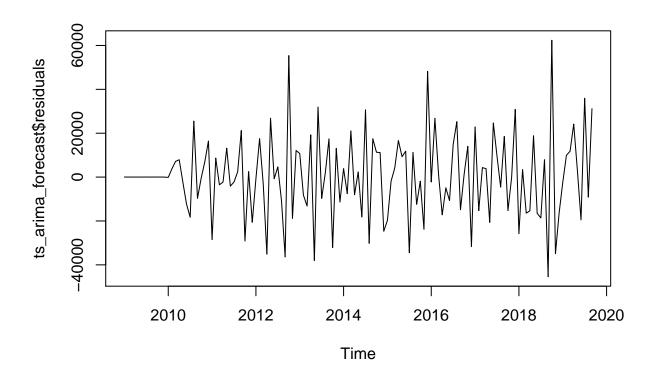
### Box.test(ts\_arima\_forecast\$residuals, lag=20, type="Ljung-Box")

```
##
## Box-Ljung test
##
## data: ts_arima_forecast$residuals
## X-squared = 126.86, df = 20, p-value < 2.2e-16</pre>
```

# p value too high to reject

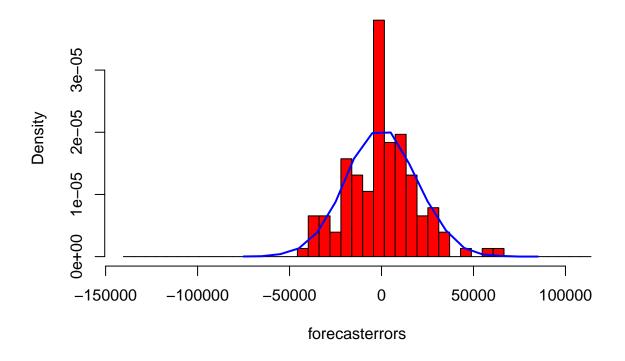
```
plot.ts(ts_arima_forecast$residuals)
```

# make time plot of forecast errors



plotForecastErrors(ts\_arima\_forecast\$residuals)

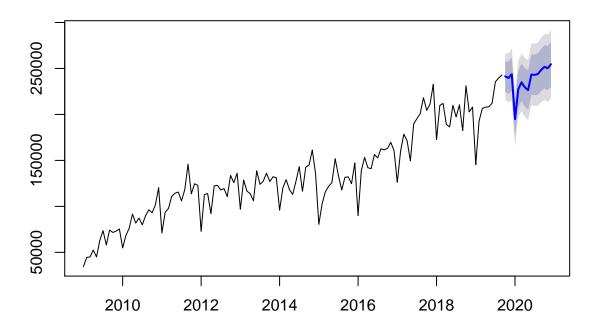
# **Histogram of forecasterrors**



# A model chosen automatically

```
fit3 <- auto.arima(ts)</pre>
fit3
## Series: ts
## ARIMA(1,0,1)(0,1,1)[12] with drift
## Coefficients:
##
            ar1
                     ma1
                             sma1
                                      drift
##
         0.9482 -0.5785 -0.8459 1269.853
## s.e. 0.0409
                  0.0914
                                    203.636
                           0.1186
## sigma^2 estimated as 162448032: log likelihood=-1277.32
## AIC=2564.64 AICc=2565.18
                               BIC=2578.45
fit_forecast = forecast(fit3,h=15)
plot(fit_forecast)
```

### Forecasts from ARIMA(1,0,1)(0,1,1)[12] with drift



```
# str(fit)
```

### Growth

```
year_2019 <- window(ts, 2019)
year_2019_predict_HW <- (as.data.frame(ts_forcaste2))[1][c(1:3),]
sum_year_2019 = sum(c(year_2019,year_2019_predict_HW))
year_2020 = (as.data.frame(ts_forcaste2))[1][c(4:15),]
growth_HW <- growth(sum(year_2020),sum_year_2019)
growth_HW</pre>
```

#### ## [1] 0.1369446

```
year_2019_predict_auto.arima <- (as.data.frame(fit_forecast))[1][c(1:3),]
year_2019_predict_auto.arima_95_low <- (as.data.frame(fit_forecast))[4][c(1:3),]
year_2019_predict_auto.arima_95_high <- (as.data.frame(fit_forecast))[5][c(1:3),]
sum_year_2019 = sum(c(year_2019,year_2019_predict_auto.arima))
sum_year_2019_low = sum(c(year_2019,year_2019_predict_auto.arima_95_low))
sum_year_2019_high = sum(c(year_2019,year_2019_predict_auto.arima_95_high))

year_2020_predict_auto.arima <- (as.data.frame(fit_forecast))[1][c(4:15),]</pre>
```

```
year_2020_predict_auto.arima_95_low <- (as.data.frame(fit_forecast))[4][c(4:15),]
year_2020_predict_auto.arima_95_high <- (as.data.frame(fit_forecast))[5][c(4:15),]

growth_auto.arima <- growth(sum(year_2020_predict_auto.arima),sum_year_2019)
growth_auto.arima_95_low <- growth(sum(year_2020_predict_auto.arima_95_low),sum_year_2019_low)
growth_auto.arima_95_high <- growth(sum(year_2020_predict_auto.arima_95_high),sum_year_2019_high)
growth_auto.arima

## [1] 0.08897661

growth_auto.arima_95_low

## [1] -0.03516189

growth_auto.arima_95_high</pre>
```

## [1] 0.2057449