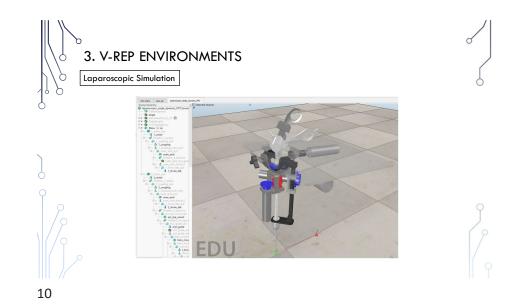
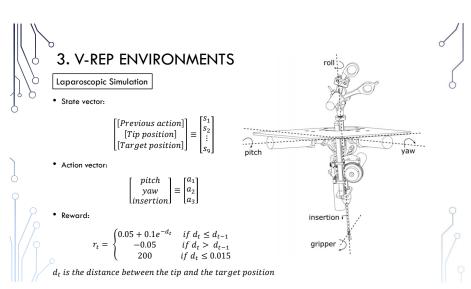
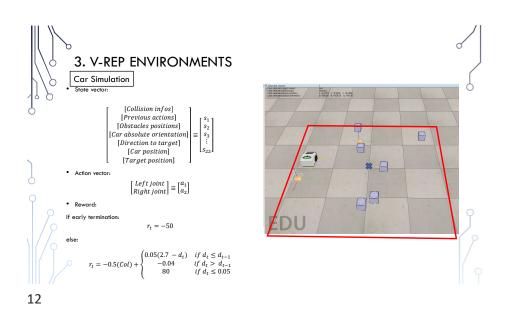


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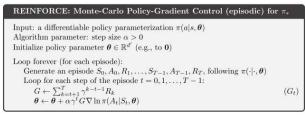


### 4. LEARNING ALGORITHM

**Policy Gradient** 

Returns: 
$$G = E_{s_{t+1} \sim P_{a(s_t, s_{t+1})}} \left[ \sum_{t=0}^{\infty} \gamma^t R_{a_t}(s_t, s_{t+1}) \right] = E_{\tau}[R(\tau)]$$

- Directly evaluating G as an objective function
- Represent policy as a function approximator (e.g. neural network):  $\pi(a|s)$
- Use gradient ascent and backpropagation to improve  $\pi(a|s)$





#### 4. LEARNING ALGORITHM

Proximal Policy Optimization (PPO)

- · Limit the deviation of new policy Avoid destructive updates
- Use Advantage instead of Monte-Carlo return
  - ➤ Reduce gradient variance
- · Can monotonically improve policy



Algorithm 5 PPO with Clipped Objective

Input: initial policy parameters  $\theta_0$ , clipping threshold  $\epsilon$ 

Collect set of partial trajectories  $\mathcal{D}_k$  on policy  $\pi_k=\pi(\theta_k)$  Estimate advantages  $\hat{A}_t^{\pi_k}$  using any advantage estimation algorithm Compute policy update

 $\theta_{k+1} = \arg \max_{a} \mathcal{L}_{\theta_k}^{\mathit{CLIP}}(\theta)$ 

by taking K steps of minibatch SGD (via Adam), where

$$\mathcal{L}_{\theta_k}^{\textit{CLIP}}(\theta) = \underset{\tau \sim \pi_k}{\text{E}} \left[ \sum_{t=0}^{T} \left[ \min(r_t(\theta) \hat{A}_t^{\pi_k}, \text{clip}\left(r_t(\theta), 1 - \epsilon, 1 + \epsilon\right) \hat{A}_t^{\pi_k}) \right] \right. \\ \left. \left. \left[ r_t(\theta) = \frac{\pi_{\theta(\text{cl}\ \mid s_t)}}{\pi_{\theta_{\text{old}}}(a_t \mid s_t)} \right] \right. \right.$$

end for



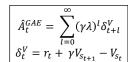
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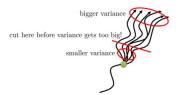




Generalized Advantage Estimates (GAE)

- Similar approach with TD(λ)
- Bias-Variance trade-off
  - λ = 0: 1-step return
  - λ = 1: Monte-Carlo return with baseline
- Only estimate value function (V)











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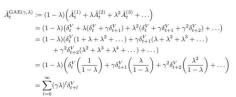
## 4. LEARNING ALGORITHM

Proposed Modifications



• Use advantage definition

$$\delta_t^A = Q_{s_t} - V_{s_t}$$



Use Q-function to estimate action values



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## 4. LEARNING ALGORITHM

Q-function Approximation (Theory)

- Represent Q-function as a neural network  $Q_{\phi}$
- Action values recursive relation
  - SARSA(0)

$$Q^{\pi}(s,a) = r + \gamma Q^{\pi}(s',a')$$

• Minimizes Time-Difference Error

$$\phi^* = \underset{\phi}{\operatorname{argmin}} \left( Q_{\phi}(s, a) - \left( r + \gamma Q_{\phi}(s', a') \right) \right)$$



## 4. LEARNING ALGORITHM

Q-function Approximation (Practice)

- Represent 2 Q-functions as neural networks:
  - Learning function  $Q_\phi$
  - ullet Target function  $Q_{\phi_{targ}}$
- Uses replay buffer to store and sample training data
  - (s, a, r, s') tuples
- Minimizes Mean Squared Bellman Error (MSBE):

$$\frac{1}{N} \sum_{i=0}^{N} \left( Q_{\phi}(s_i, a_i) - y(r_i, s_i', d_i) \right)^2$$

where y(.) is the regession target



Deep Q-Network

Deep Deterministic Policy Gradient

Soft Actor-Critic



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Target Q-Values

$$y(r_i, s_i', d_i) = r_i + \gamma (1 - d_i) Q_{\phi_{targ}}(s_i', \tilde{\alpha}')$$

where:

 $d_i$  indicates whether or not the state is terminal,

 $\tilde{a}'$  is the action sampled from the lastest policy for state  $s'_i$ .

- Uses target Q-function,  $Q_{\phi_{targ}}$  to calculate regression targets
- Samples training data from replay buffer
- $ilde{a}'$  ensures that  $Q_{m{\phi}}$  is on-policy
- Update  $Q_{\phi_{targ}}$  by polyak averaging  $\phi'_{targ} = (1-\rho)\phi + \, \rho\phi_{targ}$

$$\phi'_{targ} = (1 - \rho)\phi + \rho\phi_{targ}$$



# 4. LEARNING ALGORITHM

Model-based Reinforcement Learning



- Suppose there exists a function  $\mathcal{T}$  such that:  $\mathcal{T}(s,a)=(s')$
- Approximate  ${\mathcal T}$
- Motivations:
  - Physical interactions are expensive
  - · Hard or unable to simulate environment
- Advantages:
  - · Sample-efficient
  - · Accelerate learning if model is accurate









## 4. LEARNING ALGORITHM

Learning Transition Dynamics

- Model  ${\mathcal T}$  with a function approximator
- Collect state transitions (s, a, s') or sample from replay buffer
- Solve regression problem



 $\mathcal{L}_{dyn} = \frac{1}{N} \sum_{i=1}^{N} (T_{\omega}(s_i, a_i) - s_i')^2$ 

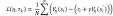
 $\mathcal{T}_{\omega}(.)$  is the dynamic model to be trained with parameters  $\omega,$  N is the number of sampled data from D.



Algorithm 1: Q-PPO
1: Input: - Initial policy parameters  $\theta_0$ 

- Initial value function parameters  $\eta_0$  Initial Q-function parameters  $\phi_0$
- Initial dynamic model parameters  $\omega_0$
- Set target Q-function parameters  $\phi_{targ} \leftarrow \phi_0$

- Greate empty repay buffer  $\mathcal{D}$ . for k=1,2,3,...do Collect set of trajectories  $\{r_k\}$  by running policy  $\pi_{\theta_k}$  in environment. Generate imaginary rollouts using dynamic model  $\mathcal{D}_{\omega_k}$  and add them to  $\{r_k\}$ .
- Add all tuples (s, a, r, s') from  $\{\tau_k\}$  to  $\mathcal{D}$ .
- Compute  $\hat{A}'$  for all collected states s with  $Q_{\phi_k}$  and  $V_{\eta_k}$ .
- Update policy parameter  $\theta_k$  via stochastic gradient ascent. Update value function parameters  $\eta_k$  by minimizing the loss:



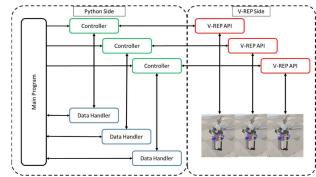
- Sample training set  $\{\mathcal{R}_k\}$  from  $\mathcal{D}$ .
- Update Q-function parameters  $\phi_k$  using samples from  $\{\mathcal{R}_k\}$ 12: 13: Update  $\phi_{targ}$  .
- 14: Upda 15: end for Update dynamic model parameters  $\omega_k$  using samples from  $\{\mathcal{R}_k\}$ .

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4. LEARNING ALGORITHM

Implementation



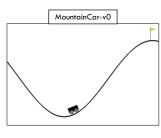


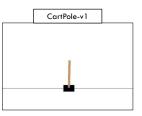


## 5. EXPERIMENTS AND RESULTS

Test Environments (OpenAl Gym)









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