

① Univariate Normal Distribution

$$p(x; \mu, \sigma^2) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{1}{2\sigma^2} (x-\mu)^2\right)$$

$$x \sim \mathcal{N}(\mu, \sigma^2)$$

② Multivariate Normal Distribution

$$\mathbf{X} = [x_1, x_2, x_3, \dots]^T$$

$$p(\mathbf{X}; \mu, \Sigma) = \frac{1}{(\sqrt{2\pi})^n |\Sigma|^{\frac{1}{2}}} \exp\left(-\frac{1}{2} (\mathbf{x}-\mu)^T \Sigma^{-1} (\mathbf{x}-\mu)\right)$$

$$\mathbf{X} \sim \mathcal{N}(\mu, \Sigma)$$

③ Bivariate Normal Distribution

$$f_{x,y}(x,y) = \frac{1}{2\pi\sigma_x\sigma_y\sqrt{1-\rho^2}} \exp\left\{-\frac{1}{2(1-\rho^2)}\left[\left(\frac{x-\mu_x}{\sigma_x}\right)^2 + \left(\frac{y-\mu_y}{\sigma_y}\right)^2 - 2\rho\frac{(x-\mu_x)(y-\mu_y)}{\sigma_x\sigma_y}\right]\right\}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} \sim \mathcal{N}\left[\begin{pmatrix} \mu_x \\ \mu_y \end{pmatrix}, \begin{pmatrix} \sigma_x^2 & \rho\sigma_x\sigma_y \\ \rho\sigma_x\sigma_y & \sigma_y^2 \end{pmatrix}\right]$$