Answer Sketch for Homework 5

$431\ Staff\ and\ Professor\ Love$

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Не	ere's the complete R setup we used.	
op	<pre>itr::opts_chunk\$set(comment=NA) tions(width = 70) brary(magrittr); library(tidyverse)</pre>	

We'll include the bootdif function here, because it might be useful in Question 7 or 8.

```
bootdif` <-
function(y, g, conf.level=0.95, B.reps = 2000) {
    require(Hmisc)
    lowq = (1 - conf.level)/2
    g <- as.factor(g)
    a <- attr(smean.cl.boot(y[g==levels(g)[1]], B=B.reps, reps=TRUE),'reps')
    b <- attr(smean.cl.boot(y[g==levels(g)[2]], B=B.reps, reps=TRUE),'reps')
    meandif <- diff(tapply(y, g, mean, na.rm=TRUE))
    a.b <- quantile(b-a, c(lowq,1-lowq))
    res <- c(meandif, a.b)
    names(res) <- c('Mean Difference',lowq, 1-lowq)
    res
}</pre>
```

We are grading questions 1-6 and 8.

1 Question 1 (5 points)

Specify the URL where we can see the headline and news story describing the findings of the study. You should provide a complete reference, including the names of the author(s) of the news story, and its full title, and source.

We accept any working reference that included the specified information.

2 Question 2 (5 points)

Specify a URL where we can see at least the abstract of the complete study. Again, provide a complete reference to the study, too.

We would accept any working reference that included the specified information.

3 Question 3 (5 points)

Describe your opinion (gut feeling) related to the conclusions of the study as summarized in the headline and news article, first in terms of a probability statement, and then calculate the appropriate odds. Motivate your internal prior probability, describing your relevant personal experiences or other factors that drove your gut feeling.

We want to see an accurate calculation given your probability, and at least a reasonable attempt at motivation for your initial probability.

4 Question 4 (12 points)

Evaluate the study in terms of the six specifications proposed by Leek when evaluating study support.

We want to see a clear, motivated conclusion about each of the six specifications (each being worth 2 points), as well as direct quotes and evidence summaries to address the issues raised and justify conclusions.

The six specifications we are looking for are:

1. Was the study a clinical study in humans?

- 2. Was the outcome of the study something directly related to human health like longer life or less disease? Was the outcome something you care about, such as living longer or feeling better?
- 3. Was the study a randomized, controlled trial (RCT)?
- 4. Was it a large study at least hundreds of patients?
- 5. Did the treatment have a major impact on the outcome?
- 6. Did predictions hold up in at least two separate groups of people?

5 Question 5 (5 points)

Incorporate the study support assessment into a Bayes' Rule calculation to obtain the final odds you should now be willing to give to the headline, and specify this value in terms of a probability statement, as well.

We wanted to see correct calculations of both the odds and probability in light of the prior probability established in Question 3 and the answers to the specifications described in Question 4.

6 Question 6 (8 points)

React to the final conclusion specified by this approach in a sentence or two. How does your subjective posterior probability that the headline is true match up with the formula's conclusions? Do you feel that the formulaic approach has yielded an appropriate conclusion for you in this case? Why or why not?

We wanted to see you specify your subjective feeling about what the probability *should* be, and then match that up with the result of the calculation.

7 Question 7 (not graded)

For 10 diabetic adults treated with a special diet, the fasting blood sugar values (in mg/dl) before and after treatment were as shown below.

```
## Option 1 - create a hw4q7 data set in Excel, and import it into R
## using read.csv and tbl_df to make it into a tibble.
##
## Option 2 - build the tibble directly in R
hw4q7 <- tibble(
    person = LETTERS[1:10],
    before = c(340, 335, 220, 285, 320, 230, 190, 210, 295, 270),
    after = c(290, 315, 250, 280, 311, 213, 200, 208, 279, 258)
)</pre>
hw4q7
```

```
# A tibble: 10 x 3
   person before after
   <chr>>
            <dbl> <dbl>
 1 A
              340
                     290
 2 B
              335
                     315
 3 C
              220
                     250
 4 D
              285
                     280
 5 E
              320
                     311
 6 F
              230
                     213
 7 G
              190
                     200
 8 H
              210
                     208
9 I
              295
                     279
10 J
              270
                     258
```

7.1 Question 7a. Outcome

The outcome is the before - after difference in fasting blood sugar (in mg/dl).

7.2 Question 7b. Exposure/Treatment Groups

The treatment is the special diet. The two groups are the patients before the diet and the same patients after the diet.

7.3 Question 7c. Paired or Independent Samples

These are paired samples. The data are paired by subject. Each subject provides a before and an after result.

7.4 Question 7d. Random Sample? Representative?

This isn't a random sample from the population of interest - which could be defined as adult patients with diabetes. The treatments were not assigned at random. Each patient provides a difference in blood sugar before and after the diet. It should be reasonable to treat this small sample of 10 observations as not clearly

biased towards any particular end of the true population distribution, and so in that sense, we can think of it as representative.

7.5 Question 7e. Significance Level?

We are using a 5% significance level, or, equivalently, a 95% confidence level.

7.6 Question 7f. One-sided or Two-Sided Inference?

We are looking for a significant change in either a positive or negative direction, so that's a two-sided approach.

7.7 Question 7g. Did pairing help (to reduce nuisance variation)?

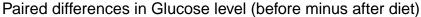
The correlation of the **before** and **after** glucose levels is 0.94, which is positive and strong, suggesting that there is a strong connection between the before and after scores of the subjects. Pairing definitely helped.

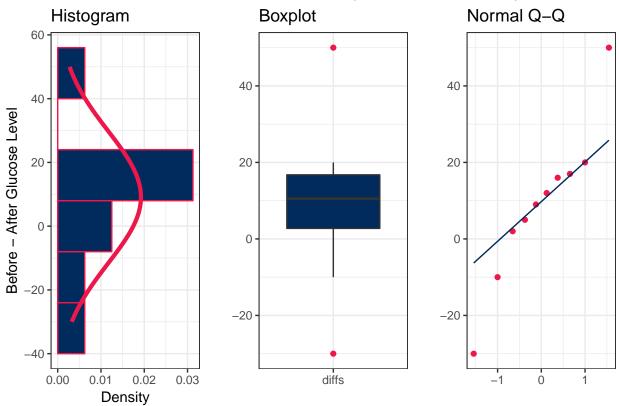
7.8 Question 7h. What does the distribution of sample paired differences tell us about which inferential procedure to use?

Here is our usual set of three plots describing the 10 paired (before - after) differences in glucose level, shown in the colors of the Cleveland Indians (http://teamcolorcodes.com/ is my source for team colors).

```
hw4q7 <- hw4q7 %>%
  mutate(diffs = before - after)
p1 \leftarrow ggplot(hw4q7, aes(x = diffs)) +
  geom histogram(aes(y = ..density..), bins = 6,
                 fill = "#002B5C", col = "#ED174C") +
  stat function(fun = dnorm,
                args = list(mean = mean(hw4q7$diffs),
                             sd = sd(hw4q7\$diffs)),
                lwd = 1.5, col = "#ED174C") +
  coord_flip() +
  theme_bw() +
  labs(title = "Histogram",
       x = "Before - After Glucose Level", y = "Density")
p2 \leftarrow ggplot(hw4q7, aes(x = "diffs", y = diffs)) +
  geom_boxplot(fill = "#002B5C", outlier.color = "#ED174C") +
  theme bw() +
  labs(title = "Boxplot",
       y = "", x = "")
p3 <- ggplot(hw4q7, aes(sample = diffs)) +
  geom qq(col = "#ED174C") +
  geom_qq_line(col = "#002B5C") +
  theme bw() +
  labs(title = "Normal Q-Q",
       y = "", x = "")
```







We have two candidate outliers - one at -30 and one at 50. Based on a sample of 10 observations, it'd be hard to assume that these data were approximately Normally distributed. This suggests the use of a bootstrap confidence interval or a Wilcoxon signed rank test to make inferences about the population mean (or median) difference in glucose level.

7.9 Question 7i does not apply. These are paired samples.

7.10 Question 7j. Did a statistically significant ($\alpha = .05$) change occur after treatment? Include in your response evidence supporting any assumptions you make.

Based on a 95% bootstrap confidence interval, or a Wilcoxon signed rank test, we observe **no** statistically significant (at the 5% significance level) difference in population glucose levels before treatment as compared to after treatment.

Using the seed 43132, I get the following 95% bootstrap confidence interval for the population mean of the paired before - after differences in glucose level.

```
set.seed(43132); Hmisc::smean.cl.boot(hw4q7$diffs)
```

Mean Lower Upper 9.1000 -3.2025 21.2025

From the Wilcoxon signed rank test, we have a p value that is substantially larger than the $\alpha=0.05$ significance level we have established.

Wilcoxon signed rank test with continuity correction

The assumptions with the bootstrap are that we have a random (or at least representative) sample from the population of glucose differences, with those values drawn independently from an identical distribution. We don't require Normality of the distribution of that population.

8 Question 8 (60 points)

In the experiment studied in this question, 40 animals (20 male, 20 female) were randomly assigned either to "control" or to "histamine shock." The tabulated variable is medullary blood vessel surface (in mm^2/mm^3). Ignore the sex information.

```
# A tibble: 40 \times 4
   animal sex
                 trt
                           surface
    <int> <chr> <chr>
                             <dbl>
1
        1 F
                 Control
                               6.4
 2
        2 F
                  Control
                               6.2
 3
        3 F
                  Control
                               6.9
 4
         4 F
                 Control
                               6.9
 5
        5 F
                  Control
                               5.4
 6
        6 F
                               7.5
                  Control
 7
        7 F
                  Control
                               6.1
 8
         8 F
                  Control
                               7.3
9
        9 F
                  Control
                               5.9
10
       10 F
                  Control
                               6.8
# ... with 30 more rows
```

8.1 Question 8a. Outcome (5 points)

The outcome under study is the medullary blood vessel surface measured in square mm per cubic mm.

8.2 Question 8b. Exposure/Treatment Groups (5 points)

The treatment was assigned as either "control" or "histamine shock."

8.3 Question 8c. Paired or Independent Samples (5 points)

These are independent samples. Each guinea pig was assigned to exactly one of the two treatments.

8.4 Question 8d. Random Sample? Representative? (5 points)

This isn't a random sample from the population of interest - which could be defined as all guinea pigs. The treatments were, however, assigned at random. Each animal was randomly assigned to their treatment, or, more likely, the assignment was done in such a way that all possible assignments of 20 animals to control and 20 to histamine shock were equally likely.

8.5 Question 8e. Significance Level? (5 points)

We are using a 95% confidence interval, so a 5% significance level.

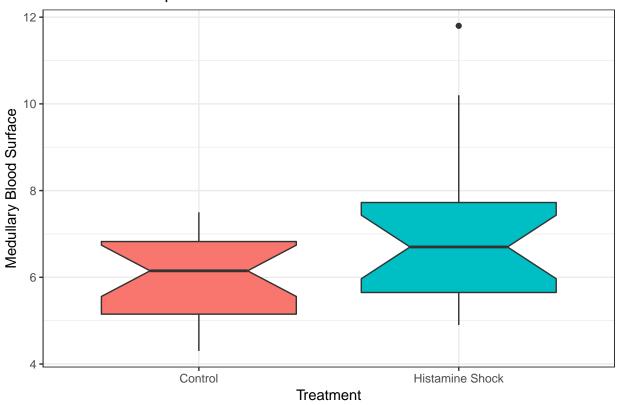
8.6 Question 8f. One-sided or Two-Sided Inference? (5 points)

We are looking for a significant difference between the two treatments, in either direction, so that's a two-sided approach.

8.7 Question 8i. What does the distribution of each individual sample tell us about which inferential procedure to use? (15 points)

Here is a comparison boxplot and a pair of normal Q-Q plots to compare the "control" and "histamine shock" surface results.

Question 8i Boxplot



We have a single outlier in the histamine shock group, at 11.8. Based on a sample of 20 observations, seeing a single outlier isn't a big surprise, certainly, so that by itself isn't enough to push me away from assuming a Normal distribution for each of the two populations (control and histamine shock) here. I'd be inclined to use a confidence interval based on a t test. Given the balanced design with 20 animals in each group, whether or not we assume equal population variance shouldn't matter much.

8.8 Question 8j. On the basis of the most appropriate 95% CI, can you conclude that the outcome differs significantly between "control" and "histamine shock?" Justify your assumptions. (15 points)

Based on a 95% confidence interval using the pooled t procedure, we see a statistically significant (at the 5% significance level) difference between the control results and the results after histamine shock.

```
Two Sample t-test

data: hw4q8$surface by hw4q8$trt

t = -2.2499, df = 38, p-value = 0.03033

alternative hypothesis: true difference in means is not equal to 0

95 percent confidence interval:

-2.0422568 -0.1077432

sample estimates:

mean in group Control mean in group Histamine Shock

5.995

7.070
```

t.test(hw4q8\$surface ~ hw4q8\$trt, var.equal = TRUE)

The confidence interval (-2.04, -0.11) describes the control - histamine shock difference in surface, and does not include zero, although it almost does. The Welch t test gives a very similar confidence interval without requiring the assumption of equal variances, at (-2.05, -0.1). It turns out that the assumption of equal population variances is not very important here, in part because of the balanced design. That's the best answer here, in my view.

8.8.1 A slightly less good answer - the bootstrap

If, on the other hand, we had been unwilling to assume Normality in the two populations here, we would have to consider a bootstrap 95% confidence interval for the histamine shock - control differences. If we use a seed of 43163, we get the following:

Since this confidence interval does not contain zero, it also suggests that there is a statistically significant difference in mean medullary blood vessel surface between the two treatments.

8.8.2 A substantially less good answer - Wilcoxon-Mann-Whitney-based CI

Since we want to use a confidence interval here, I'd be inclined to stay away from the Wilcoxon-Mann-Whitney rank sum test, because it doesn't make a confidence interval about a difference in means, but rather a rather nebulous location variable. I use Wilcoxon-Mann-Whitney tests for p values, occasionally, but rarely do so when I want a confidence interval. If we decide to do it, we should probably turn off the exact part of the test, since we have some ties here.

Wilcoxon rank sum test with continuity correction

In this case, it matters if you do this test, because the confidence interval for the location parameter using that method, which is (-1.7, 0.1), does (barely) include 0. So, if we had used the Wilcoxon-Mann-Whitney procedure, we would have to conclude, barely, that the medullary blood vessel surface does not differ significantly between "control" and "histamine shock".