Hen 
$$\sqrt{1} = \begin{bmatrix} 1 & 0 & 0 & -0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 2r \\ 0 & 0 & 1 & 2r \end{bmatrix}$$

$$\frac{1}{2} R_{2} 2r$$
Rotation annual the  $X - \alpha xis$ :
$$d = 2\pi x \cdot \theta \quad \text{same } d, Y_{b} = 2r\alpha \Rightarrow \theta_{b} = \frac{1}{3}\theta_{a}$$

$$T_{1} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$alb = \begin{bmatrix} 0 & 0 & 0 \\ 0 & cus\theta & -sn\theta & Lcos2\theta \\ 0 & sin\theta & cus\theta & Lsin2\theta \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

aTc = bTc 
$$\times$$
 aTb =

 $\begin{bmatrix}
0 & \cos\theta & -\sin\theta & \cos\theta & -\cos\theta \\
0 & \sin\theta & \cos\theta & \cos\theta & + 4\sin\theta \\
0 & 0 & 0
\end{bmatrix}$ 

From  $\sin 2 + \cos 2 + \cos 2 = \cos 2$ 

For 
$$so 2$$
:

$$G = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} \quad \vec{\beta} = \theta \cdot \vec{G} = \begin{bmatrix} 0 & 0 \\ -1 & 0 \end{bmatrix} \in so2.$$

$$\exp(\vec{\beta}) = \begin{bmatrix} 1 + \begin{bmatrix} 0 & -0 \\ 0 & 0 \end{bmatrix} + \frac{1}{2!} \begin{bmatrix} -6^2 & 0 \\ 0 & -6^2 \end{bmatrix} + \frac{1}{3!} \begin{bmatrix} -6^3 & 0 \end{bmatrix} + \cdots$$

$$= \begin{bmatrix} 1 - \frac{6^2}{2!} + \frac{6^4}{4!} - \cdots - 0 + \frac{6^3}{2!} - \frac{6^3}{2!} + \cdots \\ 0 - \frac{6^3}{3!} + \frac{6^3}{5!} - \cdots - 1 - \frac{6^2}{2!} + \frac{6^4}{4!} - \cdots \end{bmatrix}$$

$$= \begin{bmatrix} cos \theta & -sn\theta \\ sn\theta & ces \theta \end{bmatrix} \in SO2.$$

From 
$$SO_2$$
 to  $SO_2$ .

 $R = \begin{bmatrix} R_{ij} & R_{ik} \\ R_{ik} \end{bmatrix} \in SO_2$ .

 $\theta = log(R)^v = anton(\frac{R_{ij}}{R_{ii}})$  or  $\frac{l(\theta)l}{2sin|\theta|l}(R-R^i)$ 

From  $SO_2$  to  $SO_2$ .

 $SO_2 = log(R)^v = anton(\frac{R_{ij}}{R_{ii}})$  or  $\frac{l(\theta)l}{2sin|\theta|l}(R-R^i)$ 
 $T = exp(\delta) = \begin{bmatrix} exp(\delta) \\ 0^7 \end{bmatrix} \int_{L(\theta)P} = \sum_{n=0}^{\infty} \frac{1}{(n+1)!}(\delta)^n$ 
 $= 7 + \delta + \frac{1}{2!} \delta^2 + \frac{1}{3!} \delta^3 \delta^4 \cdots$ 

$$= \begin{bmatrix} 1+\hat{6} + \frac{1}{2!}\hat{6}^2 + \cdots & P(I+\hat{6}^2+\hat{6}^2+\cdots) \\ 0 & 1 \end{bmatrix}$$

Let's home 
$$V = I + \hat{b}^2 + \hat{b}^3 + \cdots$$
  
then we have:  

$$\begin{bmatrix} \exp(\hat{b}) & PV \\ 0 & 1 \end{bmatrix} \text{ or } \begin{bmatrix} \exp(\hat{b} & \int_{\Sigma} (\hat{b})P \\ 0 & 1 \end{bmatrix}$$

SE 2 to se2
$$S = \begin{bmatrix} 6 \end{bmatrix} = \log (7)^{v} = \log \begin{bmatrix} R & P \\ 0 & 1 \end{bmatrix}$$
 6 Se2.

$$S_{tel} = \begin{bmatrix} \chi_{tel} \\ y_{tel} \\ \theta_{tel} \end{bmatrix} = \begin{bmatrix} \chi_{t} \\ y_{t} \\ \theta_{t} \end{bmatrix} + \zeta \begin{bmatrix} \cos \theta_{t} & 0 \\ \sin \theta_{t} & 0 \\ 0 & l \end{bmatrix} \begin{pmatrix} [u_{t}] \\ w_{t} \end{bmatrix} + w_{t}$$

$$Zt = \begin{bmatrix} vt \\ bt \end{bmatrix} = \begin{bmatrix} \sqrt{xt+yt^2} \\ atom 2(-yt-xt)-0t \end{bmatrix} + \eta_t.$$

$$\hat{G} \text{ not } x.$$

## a. Redution

$$F = \frac{df}{dx} \left( \mu_{t|t}, \mu_{t}, 0 \right) = \begin{bmatrix} 1 & 0 & -\sin \theta_{t} \cdot \nabla \psi_{t} \\ 0 & 1 & \cos \theta_{t} \cdot \nabla \psi_{t} \end{bmatrix}$$

$$Q = \frac{df}{dw} [\mu Ht, ut, 0] = \begin{bmatrix} \tau us \theta_t & 0 \\ \tau s n \theta_t & 0 \\ 0 & \tau \end{bmatrix}$$

$$\mu t u | t = \begin{bmatrix} \chi t + \tau v t \cos \theta_t \\ \theta t + \tau v t \sin \theta_t \\ \theta t + \tau w t \end{bmatrix}.$$

$$\sum t u | t = F \sum t t t F_t + Q_t W Q_t \left( \text{lecture } 14:7 \right)$$

C. Stilt : Etit,
predict Strilt & update strilter.

Prediction:

 $M_{t+1} = F_{t+1} \sum_{t+1} \sum_{t+1} F_{t}^{-17}$   $C_{k+1} = (M_{t+1} + Q_{t+1})^{T}$   $L_{t+1} = I - C_{k+1} \qquad (et \ Y_{t+1} = \Sigma^{T} \mu)$   $Y = L_{t+1} (F_{t+1})^{T} Y_{t+1}$   $S_{t+1} = L_{t+1} M_{t+1} L_{t+1} + C_{t+1} Q_{t+1} C_{t+1}$ 

Upolate:

Styllty = Styllt It where It= Ht Rt Ht

Vtyllty = Vtylt + it where it = 14t Rt 24