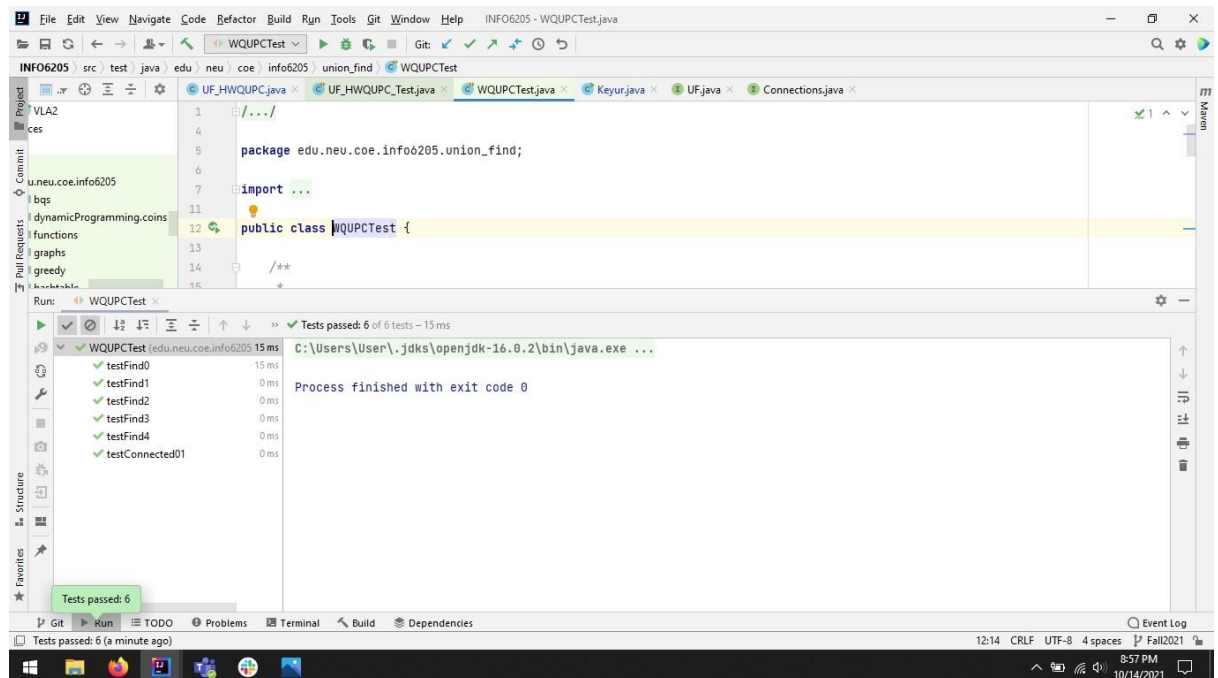
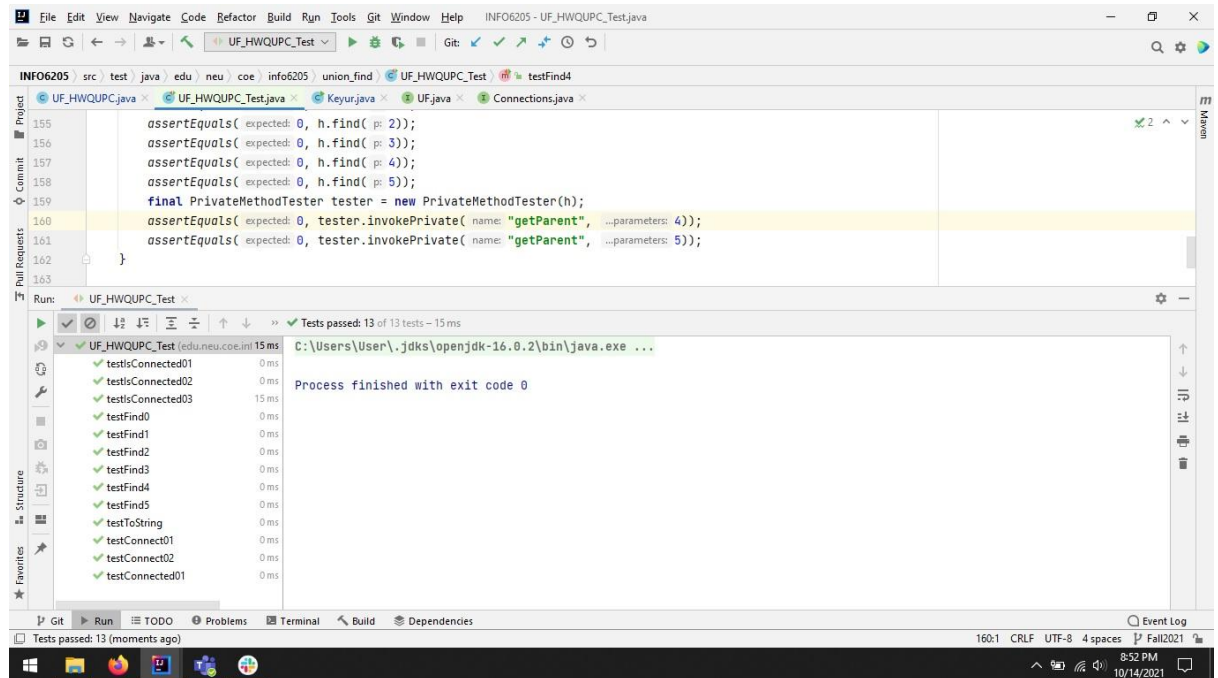
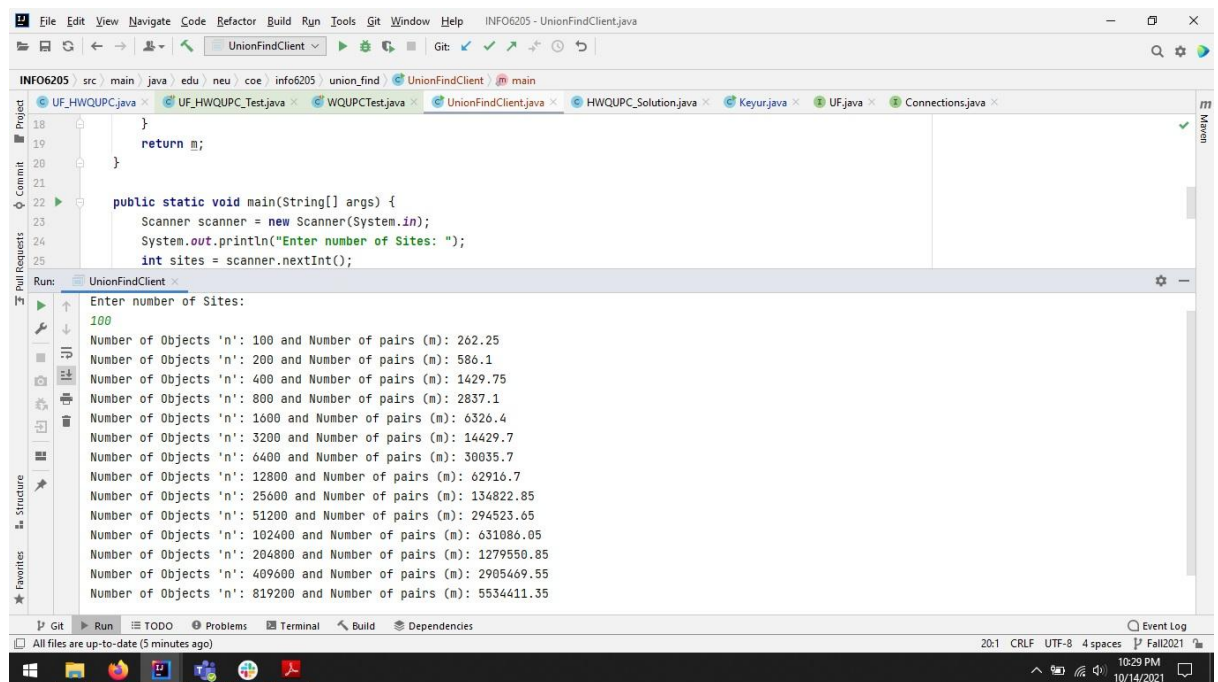


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Program Structures and Algorithms
Fall 2021
Assignment No.3 (WQUPC)

1. Implemented height-weighted Quick Union with Path Compression showing “green” test results.



- Using the implementation of UF_HWQUPC, developed a UnionFindClient function client that takes an integer value n from the command line to determine the number of "sites." Then generates random pairs of integers between 0 and $n-1$, calling connected() to determine if they are connected and union() if not. Loop until all sites are connected then print the number of connections generated. Package your program as a static method count() that takes n as the argument and returns the number of connections; and a main() that takes n from the command line, calls count(), and prints the returned value. If you prefer, you can create a main program that doesn't require any input and runs the experiment for a fixed set of n values.



The screenshot shows an IDE window titled "INFO6205 - UnionFindClient.java". The code in the editor is as follows:

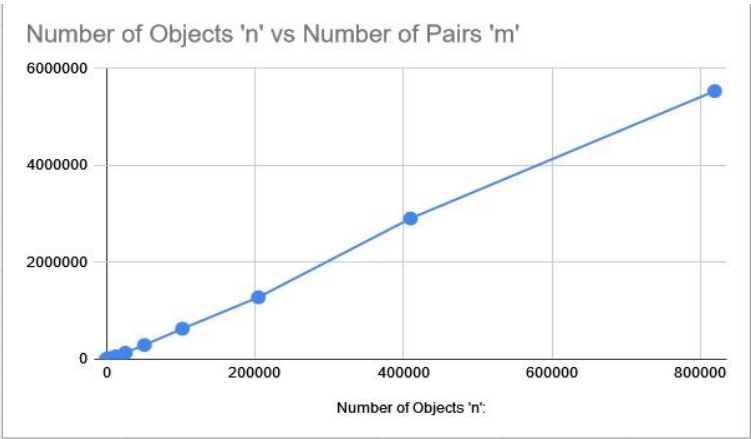
```
18     }
19     return m;
20 }
21
22 public static void main(String[] args) {
23     Scanner scanner = new Scanner(System.in);
24     System.out.println("Enter number of Sites: ");
25     int sites = scanner.nextInt();
```

The Run console shows the following output:

```
Enter number of Sites:
100
Number of Objects 'n': 100 and Number of pairs (m): 262.25
Number of Objects 'n': 200 and Number of pairs (m): 586.1
Number of Objects 'n': 400 and Number of pairs (m): 1429.75
Number of Objects 'n': 800 and Number of pairs (m): 2837.1
Number of Objects 'n': 1600 and Number of pairs (m): 6326.4
Number of Objects 'n': 3200 and Number of pairs (m): 14429.7
Number of Objects 'n': 6400 and Number of pairs (m): 30835.7
Number of Objects 'n': 12800 and Number of pairs (m): 62916.7
Number of Objects 'n': 25600 and Number of pairs (m): 134822.85
Number of Objects 'n': 51200 and Number of pairs (m): 294523.65
Number of Objects 'n': 102400 and Number of pairs (m): 631086.05
Number of Objects 'n': 204800 and Number of pairs (m): 1279550.85
Number of Objects 'n': 409600 and Number of pairs (m): 2905469.55
Number of Objects 'n': 819200 and Number of pairs (m): 5534411.35
```

- The relationship between the number of objects (n) and the number of pairs (m) generated to accomplish this (i.e. to reduce the number of components from n to 1) is
$$\Rightarrow m = f(n) = 0.5 \cdot n \cdot \ln(n)$$

Number of Objects 'n':	Number of Pairs 'm':
100	262.25
200	586.1
400	1429.75
800	2837.1
1600	6326.4
3200	14429.7
6400	30035.7
12800	62916.7
25600	134822.85
51200	294523.65
102400	631086.05
204800	1279550.85
409600	2905469.55
819200	5534411.35



Number of Objects 'n':	Number of Pairs 'm':	$0.5 \cdot n \cdot \ln(n)$
100	262.25	230.25
200	586.1	529.83
400	1429.75	1198.29
800	2837.1	2673.84
1600	6326.4	5902.2
3200	14429.7	12913.44
6400	30035.7	28044.97
12800	62916.7	60526.08
25600	134822.85	129924.44
51200	294523.65	277593.46
102400	631086.05	590676.07
204800	1279550.85	1252330.41
409600	2905469.55	2646617.36
819200	5534411.35	5577147.81

