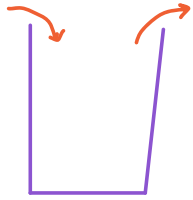
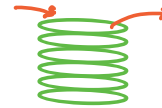


Stacks

LIFO
last in
first out.



1) Stack of plates



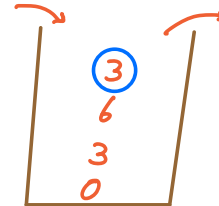
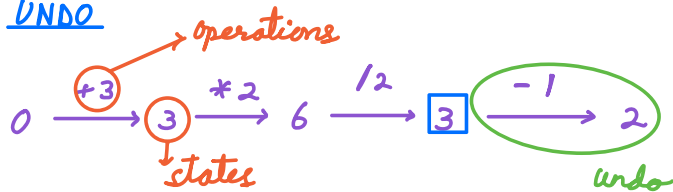
2) Glass of water/milk

3) Stack of books

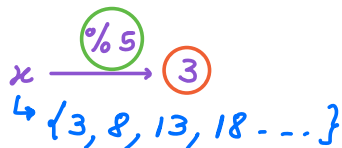
4) Stack of chairs

5) Stack of CD's

6) UNDO

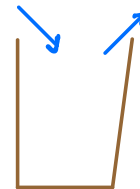


store state in stack



Operations

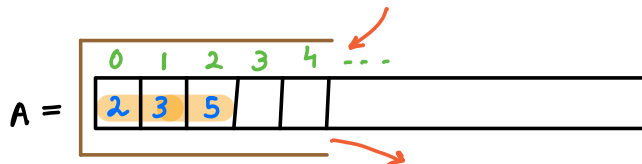
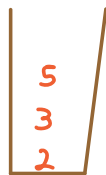
- 1) $\text{push}(x) \rightarrow$ insert x at top of stack.
- 2) $\text{pop}() \rightarrow$ remove top element from stack.
- 3) $\text{top}()/\text{peek}() \rightarrow$ get top element from stack.
- 4) $\text{isEmpty}() \rightarrow$ check if stack is empty.



TC = O(1) \forall operations

Q \rightarrow Implement stack using array.

- ✓ $\text{push}(2)$
- ✓ $\text{push}(3)$
- ✓ $\text{push}(8)$
- ✓ $\text{pop}()$
- ✓ $\text{peek}() \rightarrow 3$ ✓
- ✓ $\text{push}(5)$
- ✓ $\text{isEmpty}() \rightarrow \text{false}$ ✓

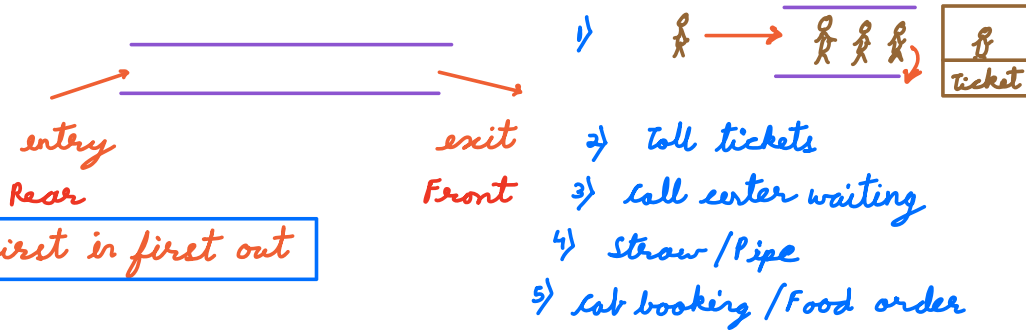


stack is from index 0 to top.

initially $\text{top} = \underline{-1}$ or $\underline{2}$

<pre>void push(int x) { top += 1; A[top] = x; }</pre> <p><u>overflow</u> → <u>dynamic array</u></p>	<pre>void pop() { if(!isEmpty()) top -= 1; }</pre> <p><u>underflow</u></p>	<pre>int peek() { if(!isEmpty()) return A[top]; else return -1; }</pre> <p><u>Index out of bounds</u></p>	<pre>boolean isEmpty() { return (top == -1); }</pre> <p>TC = O(1) <u>Operations</u></p>
---	--	---	---

Queues

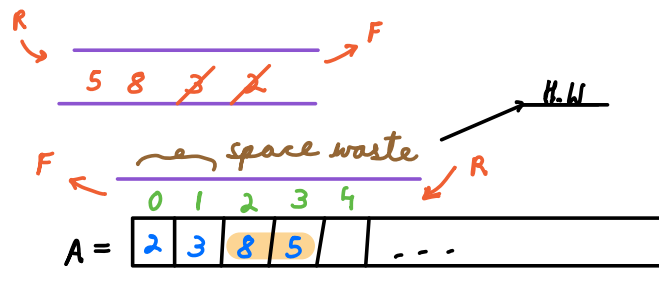


Operations

- 1) enqueue(x) → insert x from rear end.
 - 2) dequeue() → remove front element from queue.
 - 3) isEmpty() → checks if queue is empty.
 - 4) front() → get front element.
 - 5) rear() → get rear element.
- TC = O(1) Operations

Q → Implement queue using array.

- ✓ enqueue(2)
- ✓ enqueue(3)
- ✓ enqueue(8)
- ✓ dequeue()
- ✓ front() → 3 ✓
- ✓ rear() → 8 ✓
- ✓ dequeue()



Queue is from index f to r

✓ isEmpty() → false ✓
 ✓ enqueue(5)

f = 0 + 2 r = -1 + 2 = 3

<pre>void enqueue(int x){ r += 1; A[r] = x; }</pre>	<pre>void dequeue(){ if(!isEmpty()) f += 1; }</pre>	<pre>boolean isEmpty(){ return f > r; }</pre>
---	---	--

overflow → dynamic array

underflow

TC = O(1) ∀ operations

<pre>int front(){ if(!isEmpty()) return A[f]; else return -1; }</pre>	<pre>int rear(){ if(!isEmpty()) return A[r]; else return -1; }</pre>
---	--

Q → Check whether the given sequence of parenthesis is valid.

ANS
 sutherland
 Walmart

{, }, (,), [,]

s = "() [{ } () " → valid
 s = "() [{ } } (" → invalid

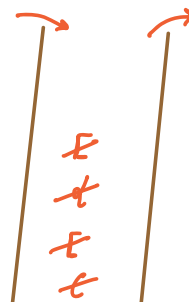
s = "() [{ }] [] " → Ans = true
 s = "({) } " → Ans = false

s = "({ })) (" → Ans = false

s = "({ } [" → Ans = false

s = "() [{ }] [] "

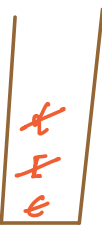
() ✓ [] ✓
 { } ✓ [] ✓



stack
 Closing brackets
 check if the last
opening bracket matches.

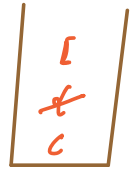
Ans = true

$s = "() / ({ }) [] "$
 $\uparrow \uparrow \uparrow$
 $() \checkmark$
 $\{ \} \checkmark$
 $[] \times$ Ans = false



$TC = O(N)$
 $SC = \underline{O(N)}$

$s = "({ } ["$
 $\uparrow \uparrow \uparrow$
 $\{ \} \checkmark$
 Ans = false
 stack should be
 empty in the end.



$s = "d ({ } "$
 $\uparrow \uparrow$
 ${ \} \times$
 Ans = false

