

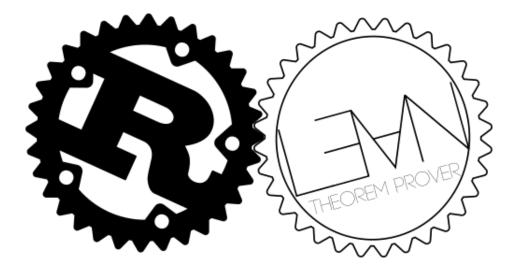
Lehrstuhl Prof. Dr.-Ing. Snelting

Simple Verification of Rust Programs via Functional Purification

Masterarbeit von

Sebastian Ullrich

an der Fakultät für Informatik



Erstgutachter: Prof. Dr.-Ing. Gregor Snelting

Zweitgutachter: ???

Einfache Verifikation von Rust-Programmen

Imperative Programmiersprachen sind in der modernen Softwareentwicklung allgegenwärtig, stellen aber ein Hindernis für formale Softwareverifikation dar durch ihre Verwendung von veränderbaren Variablen und Objekten. Programme in diesen Sprachen können normalerweise nicht direkt auf die unveränderliche Welt von Logik und Mathematik zurückgeführt werden, sondern müssen in eine explizit modellierte Semantik der jeweiligen Sprache eingebettet werden. Diese Indirektion stellt ein Problem für die Benutzung von interaktiven Theorembeweisern dar, da sie die Entwicklung von neuen Werkzeugen, Taktiken und Logiken für diese "innere" Sprache bedingt.

Die vorliegende Arbeit stellt einen Compiler von der imperativen Programmiersprache Rust in die pur funktionale Sprache des Theorembeweisers Lean vor, der nicht nur generell das erste Werkzeug zur Verifikation von Rust-Programmen darstellt, sondern diese insbesondere auch mithilfe der von Lean bereitgestellten Standardwerkzeugen und -logik ermöglicht. Diese Transformation ist nur möglich durch spezielle Eigenschaften von allen validen Rust-Programmen, die die Veränderbarkeit von Werten auf begrenzte Geltungsbereiche einschränken und statisch durch Rusts Typsystem garantiert werden. Die Arbeit demonstriert den Einsatz des Compilers anhand der Verifikation von Realbeispielen und zeigt die Erweiterbarkeit des Projekts über reine Verifikation hinaus am Beispiel von asymptotischer Laufzeitanalyse auf.

Abstract

Imperative programming, and aliasing in particular, represents a major obstacle in formally reasoning about everyday code. By utilizing restrictions the imperative programming language Rust imposes on mutable aliasing, we present a scheme for shallowly embedding a substantial part of the Rust language into the purely functional language of the Lean theorem prover. We use this scheme to verify the correctness of real-world examples of Rust code without the need for special semantics or logics. We furthermore show the extensibility of our transformation by incorporating an analysis of asymptotic runtimes.

Contents

1	\mathbf{Intr}	oduction	on	1				
2	Related Work							
3	Background 5							
	3.1	Rust .		5				
	3.2	Lean .		8				
4	The	Basic	Transformation	13				
	4.1	The M	IR	13				
	4.2		iers					
	4.3		ms and Files					
	4.4	_		15				
		4.4.1	Primitive Types	15				
		4.4.2	Structs and Enums	16				
		4.4.3	References	16				
	4.5	_		16				
	1.0	4.5.1	Default Methods	16				
		4.5.2	Associated Types	18				
		4.5.3	Trait Objects	19				
	4.6	1.0.0	emantics Monad	20				
	4.7		nents and Control Flow	$\frac{20}{21}$				
	4.1	4.7.1						
	10		1					
	4.8	-	ssions					
		4.8.1	Arithmetic Operators					
		4.8.2	Bitwise Operators					
		4.8.3	Index Expressions	27				

	4.8.4 Lambda Expressions	27
5	Case Study: Verification of [T]::binary_search	29
6	Transformation of Mutable References	33
7	Case Study: Verification of fixedbitset	33
8	Conclusion and Future Work	33

1

1 Introduction

Imperative programming languages are ubiquitous in today's software development, making them prime targets for formal reasoning. Unfortunately, their semantics differ from those of mathematics and logic – the languages of formal methods – in some significant details, starting with the very concept of "variables". The problem of mutability is only exacerbated for languages that allow references to *alias*, or point to the same memory location, enabling non-local mutation.

The standard way of verifying programs in such languages with the help of an interactive theorem prover is to explicitly model the semantics of the language in the language of the theorem prover, then translate the program to this representation (a "deep" embedding) and finally prove the correctness of its formalized behavior. This general approach is very flexible and allows for the verification of meta programs such as program transformations. The downside of the approach is that the theorem prover's tools and tactics may not be directly applicable to the embedded language, defeating many amenities of modern theorem provers. Alternatively, programs can be "shallowly" embedded by directly translating them into terms in the theorem prover's language without the use of an explicit inner semantics. This simplifies many semantic details such as the identification and substitution of bound variables, but it is harder to accomplish the more the semantics of the source language differs from the theorem prover's own semantics.

Regardless of the type of embedding, an explicit heap that references can point into must generally be modeled and passed around in order to deal with the aliasing problem. References in this model may be as simple as indices into a uniform heap, but various logics such as separation logic [18] have been developed to work on a more abstract representation and to express aliasing-free sets of references.

Languages with more restricted forms of aliasing exist, however. Rust [14], a new, imperative systems programming language, imposes on mutable references the restriction of never being aliased by any other reference, mutable or immutable. This restriction eliminates the possibility of data races and other common bugs created by the presence of mutable sharing such as iterator invalidation. It furthermore enables more aggressive optimizations.

While the full Rust language also provides raw pointers, which are not bound by the aliasing restriction, and other "unsafe" operations, a memory model for Rust (informal or formal) has yet to be proposed. We therefore focus on the "safe" subset of Rust that has no unsolved semantic details.

We utilize safe Rust's aliasing restriction to design a monadic shallow embedding of a substantial subset of Rust into the purely functional language of the Lean [7] theorem prover, without the need for any heap-like indirection. This allows us to reason about unannotated, real-world Rust code in mostly the same manner one would reason about native Lean definitions. The monadic approach gives us further flexibility in modeling additional effects such as function runtime.

We first discuss the simpler cases of the translation, notably excluding mutable references, in Section 4. We show their application by giving a formal verification of Rust's [T]::binary_search method in Section 5. Section 6 discusses the translation of most usages of mutable references, which is used in Section 7 for a verification of the fixedbitset crate.

2 Related Work

While this thesis presents the first verification tool for Rust programs, tools for many other imperative languages have been developed before.

The Why3 project [3] is notable for its generality. It provides an imperative ML-like language WhyML together with a verification condition generator that can interface with a multitude of both automatic and interactive theorem provers. While WhyML supports advanced language features such as type polymorphism and exceptions, it does not support higher-order functions, which are ubiquitous in Rust code. WhyML provides a reference type ref that can point to a fresh cell on the heap and is statically checked not to alias with other ref instances, but cannot point into some existing datum like Rust references can. For example, the first of the following two WhyML functions fails to type check because the array elements are not known to be alias-free, while the second one will return a reference to a copy of a[i].

```
let get_mut (a : array (ref int)) (i : int) : ref int = a[i]
let get_mut (a : array int) (i : int) : ref int = ref a[i]
```

In contrast, Rust can provide a perfectly safe function with this functionality.

```
fn slice::get_mut<T>(slice: &mut [T], index: usize) -> Option<&mut T>
```

WhyML is also being used as an intermediate language for the verification of programs in Ada [11], C [6] and Java [8]. For the latter two languages, aliasing is reintroduced by way of an explicit heap.

The remarkable SeL4 project [13] delivers a full formal verification of an operating system microkernel by way of multiple levels of program verification and refinement steps. The C code that produces the final kernel binary is verified by embedding it into the theorem prover Isabelle/HOL [15], using a deep embedding for statements and a shallow one for expressions. The C memory model used allows type-unsafe operations by use of a byte-size heap, but as with Why3, higher-order functions are not supported. The AutoCorres [9, 10] tool then transforms this representation into a shallow monadic embedding, dealing with the 'uninteresting complexities of C' [10] on the way. The result is an abstracted representation that is quite similar to ours (and in fact inspired it in part, as we shall note below), but doesn't go the last mile of completely eliminating the heap where possible. Thus the user still has to worry and reason about (the absence of) aliasing manually or through a nested logic such as separation logic. Without explicit no-alias annotations, the semantics of C would allow eliminating the heap in far fewer places than those of Rust in any case.

It should be noted that our work, like most verification projects based on either embedding or code extraction, relies on both an unverified compiler and an unverified embedding tool, effectively making both part of the trusted computing base. SeL4 is a notable exception in this, providing (at lower optimization levels) a direct equivalence proof [19] between the produced kernel binary and the verified embedded code, thus completely removing the original C code from the trusted computing base.

While not an imperative language, the purely functional, total Cogent language [16] uses linear types in the style of Wadler [21] for safe manual memory management, much like Rust. The language is designed both to be easily verifiable (by building on AutoCorres) and to compile down to efficient C code. As we shall see in Subsection 3.1, the biggest differences between Wadler-style purely functional linear languages and Rust are the existence of mutable references as well as sophisticated interprocedural reference tracking in the latter. For example, the aforementioned get_mut function can only be expressed as a higher-order function in Cogent, even in the immutable case.

3 Background

We start by giving a basic introduction to our source and target languages, focusing on the parts relevant to our work. We will discuss finer semantic details where needed in Section 4 and Section 6.

3.1 Rust

Rust [14] is a modern, multi-paradigm systems programming language sponsored by Mozilla Research and developed as an open-source community effort. Rust is still a quite young language, with its first stable version having been released on May 15, 2015. The two biggest Rust projects as of this writing are the Servo¹ [1] web browser engine and the Rust compiler rustc² itself.

As a partly functional language, Rust is primarily inspired by ML and shares much of its syntax, as evidenced in Listing 1. However, the syntax also shows influences by C, the dominant systems programming language at present. Finally, Rust also features a *trait* system modeled after Haskell's type classes.

Many features of Rust other than the syntax can be explained by Rust's desire to feature an ML-like abstraction level while still running as efficiently as C, even on resource-constrained systems that may not allow dynamic allocation at all. Most prominently, Rust uses manual memory management just like C and C++, but guarantees memory safety through its *ownership* and *borrowing* systems. Rust also features an *unsafe* language subset that allows everything-goes programming on the level of C, but which is usually

Listing 1: A first example of functional programming in Rust, showing algebraic data types, polymorphic and higher-order functions, pattern matching, type inference and the expression-oriented syntax

reserved for implementing low-level primitives on which the *safe* part of the language can then build. In general, safe Rust is (thought to be) a type-safe language like ML and unlike either C or C++. We focus on safe Rust in the following and in our work in order to peruse these guarantees.

Ownership describes the application of *linear types* to memory management as proposed by Wadler [21]. The owner of a Rust object is the binding that is responsible for freeing the object's resources (by calling a method of the Drop trait), which generally happens at the end of the binding's scope. Because an object managing resources should only ever have one owner, types that implement Drop are linear types: A value may only be used once, at which point it is consumed and ownership is transferred to its new binding.³ In the following example, we extract an element from a Vec (a dynamically-sized array type that has to free heap space in its Drop implementation), after which we are not permitted to use the Vec again.

```
fn get<T>(v: Vec<T>, idx: usize) -> T {
    v[idx]
    // v will be freed here
}
let v: Vec<u32> = vec![1];
let x = get(v, 0);
// get(v, 1); // error[E0382]: use of moved value: `v`
```

One way to retain access to the Vec would be to also return it from the function, regaining ownership. However, since T in general is a linear type too, get would have to remove the indexed element before returning the Vec.

A much better alternative is to use *references*, which provide standard pointer indirection. Because a reference does not take ownership of the pointee, creating it is also called *borrowing*.

```
fn get<T>(v: &Vec<T>, idx: usize) -> &T {
    &v[idx]
}
let v: Vec<u32> = vec![1];
let x = get(&v, 0); // x: &u32
```

Here &T represents an immutable reference to a value of type T. Note that the compiler would stop us if we tried to return v[idx] by value:

```
error[E0507]: cannot move out of indexed content
```

³Technically, because leaking resources (i.e. not consuming the object at all) is a safe operation in Rust, such types are merely *affine*. However, the distinction is not relevant for our purposes.

Still, coming from other languages with manual memory management, this might look like a potentially unsafe thing to do: The function signature does not tell the callee that the returned reference is only valid as long as the Vec. Even Wadler tells us that a temporary reference to a linear value must be checked not to escape from the local scope. Indeed, it seems like the following program should produce a dangling pointer.

```
fn dangling() -> u32 {
    let x = {
        let v: Vec<u32> = vec![1];
        get(&v, 0)
        // v will be freed here
    };
    *x
}
```

However, the Rust compiler will stop us from doing this, printing an elaborate error message:

```
error: `v` does not live long enough

| get(&v, 0)
| ^ does not live long enough
| };
| - borrowed value only lives until here
| *x
| }
| - borrowed value needs to live until here
```

The compiler must have had some information about the relationship of x and v in order to deduce this without resorting to inter-procedural analysis. It turns out that the full signature of the get function is as follows:

```
fn get<'a, T>(v: &'a Vec<T>, idx: usize) -> &'a T
```

'a is called a *formal lifetime parameter*. It specifies that the returned reference is indeed only valid as long as the first argument. By integrating lifetimes into the type system like this, Rust can reason about references even when confronted with complex, inter-procedural, higher-order reference lifetime relations.

While we have solved the dangling pointer problem for immutable data, mutability as so often aggravates the problem.

```
fn dangling2() -> u32 {
    let mut v: Vec<u32> = vec![1];
    let x = get(&v, 0);
```

```
// remove all elements from v
v.clear(); // shorthand for (&mut v).clear();
*x
    // v will be freed here
}
```

By clearing the vector while we still hold a reference to its content, we should again produce a dangling pointer – even though this time, v indeed outlives x. Fortunately, the Rust compiler will again stop us:

We have finally arrived at the aliasing problem: In a language with manual memory management, we can create type unsafety through the mere existence of two pointers, at least one of them mutable, to the same datum. Thus, Rust detects and forbids any occurrences of mutable aliasing, as shown above.

The beauty of forbidding mutable aliasing is that it solves many sources of bugs in imperative programs even outside of managed memory management. Indeed, as Wadler notes, it makes mutable references safe even in a referentially transparent language: "In order for destructive updating of a value to be safe, it is essential that there be only one reference to the value when the update occurs" [21]. While Rust does introduce APIs, such as for I/O, that break referential transparency, the absence of mutable aliasing still provides safety guarantees that are usually only attributed to purely functional languages, first and foremost among them the elimination of data races. By focusing on a subset of Rust and its APIs that is truly referentially transparent, we obtain a sufficiently narrow gap between Rust and the purely functional language Lean that our transformation between them becomes feasible.

3.2 Lean

The Lean [7] theorem prover is an open source, dependently typed, interactive theorem prover developed jointly at Microsoft Research and Carnegie Mellon

University. The first official release of Lean was announced at CADE-25 in August 2015, making it just a few months younger than Rust. As of this writing, development on Lean is focused on the next, unreleased version that will feature powerful automation written in Lean itself.

Lean supports two different interpretations of Martin-Löf type theory: a purely constructive one based on Homotopy Type Theory, and one based on the Calculus of Inductive Constructions [5, 17] as championed by the Coq [2] theorem prover, which supports both constructive and classical reasoning. We use the latter in our work.

The primitive type in dependent type theory is the dependent function (or product) type $\Pi x : A, B$, where x may occur in B; if it does not, we obtain the standard function type $A \to B$. Function abstraction and application extend naturally to dependent functions, as perhaps best described by their formal typing rules.

$$\frac{\Gamma, x : A \vdash e : B}{\Gamma \vdash (\lambda x : A, e) : \Pi x : A, B} \qquad \frac{\Gamma \vdash f : \Pi x : A, B \qquad \Gamma \vdash e : A}{\Gamma \vdash f e : [e/x]B}$$

The Calculus of Inductive Constructions extends basic dependent type theory with a type scheme for inductive types, which are described by a set of (possibly dependent) functions, their *constructors*. Listing 2 shows basic inductive definitions from the Lean standard library.

As we can see in Listing 2, inductive types themselves are instances of a type, namely **Type**. This turns out to be a slight simplification, however. More specifically, Lean has a whole hierarchy of indexed types or *universes* **Type**. {i}, with **Type**. {i} : **Type**. {i+1}. The universe hierarchy is needed to avoid the type theoretic equivalent of Russell's paradox. When we write just **Type** for the type of an inductive definition like in Listing 2, a correct universe level $i \geq 1$ (possibly dependent on argument universe levels) will automatically be inferred. The reason for skipping **Type**. {0} is that it has a special function that is suggested by its more common name, **Prop**: It is the universe we normally declare types in that are to be interpreted as propositions.

Under the Curry-Howard isomorphism, an objects of a type can be interpreted as a proof of a proposition. The reason Lean uses a separate universe for this interpretation is that **Prop** is given a specific property that would not make sense for the other universes: By *proof irrelevance*, any two objects of a type in **Prop** are definitionally equal. In other words, proofs are irrelevant

⁴The hierarchy is, however, not cumulative: It is not true that Type.{i}: Type.{i+2}.

```
inductive empty : Type
inductive unit : Type :=
star : unit
inductive prod (A B : Type) : Type :=
mk : A \rightarrow B \rightarrow prod A B
inductive sum (A B : Type) : Type :=
\mid inl : A \rightarrow sum A B
\mid inr : B \rightarrow sum A B
-- the dependent sum type
inductive sigma (A : Type) (B : A → Type) : Type :=
mk : \Pi(x : A), B x \rightarrow sigma A B
inductive bool : Type :=
| ff : bool
| tt : bool
inductive option (A : Type) : Type :=
| none : option A
| some : A → option A
inductive nat : Type :=
zero : nat
succ : nat → nat
```

Listing 2: The most basic inductive types as well as some basic types from functional programming in Lean

~ -	e (notation)
in Type	in Prop
empty	false
unit	true
prod (×)	and (Λ)
sum(+)	or (v)
sigma (Σ x : A, B)	Exists $(\exists x : A, B)$
Пх: А, В	∀ x : A, B
$A \rightarrow B$	$A \rightarrow B$

Table 1: The basic Curry-Howard correspondence. The table lists types from Listing 2 and the corresponding types from the standard library with the same constructors, but declared in **Prop**. We also show their notations as well as the special universal quantifier notation for dependent functions into **Prop**. Nondependent functions and implications are not distinguished by notation.

for computation. Finally, **Prop** is also *impredicative*: If B : Prop, then also ($\Pi \times A$, B): **Prop** for any A. This property ensures that predicates and universal quantifications are still propositions. The separation of inductive types and inductive propositions can lead to some duplication, which however turns out to be very useful in ensuring suggestive names and notations for each side (Table 1).

On top of its interpretation of dependent type theory, Lean includes many notational amenities. On the type level, in addition to basic and inductive definitions, it features syntactic **abbreviations** as well as **structures**. The latter are single-constructor inductive types that automatically define projections to each of their constructor parameters (or *fields*) and furthermore support inheriting fields from other structures.

```
structure point2 :=
(x : N)
(y : N)

structure point3 extends point2 :=
(z : N)

example : point2 := {point2, x := 0, y := 1}
check point3.x -- point3.x : point3 > N
```

In addition to the standard parameter syntax (x : A), Lean also supports two more binding modes, $\{x : A\}$ and [x : A]. In the first one, x is an

implicit parameter and will be inferred from other parameters or the expected result type, such as in the constructor of the ubiquitous type **eq** modeling Leibniz equality:

```
inductive eq {A : Type} (a : A) : A → Prop :=
refl : eq a a -- explicit form: @eq A a a
```

The binding mode [x : A] instructs Lean to infer x by type class inference. Type classes are arbitrary definitions annotated with the [class] attribute. Type class inference synthesizes instances of a class by a Prologlike search through definitions of the class type marked with [instance].

```
structure inhabited [class] (A : Type) : Type :=
  (value : A)

definition default (A : Type) [inhabited A] : A :=
  inhabited.value A

definition nat.is_inhabited [instance] : inhabited N :=
  {inhabited, value := 0}

definition prod.is_inhabited [instance] (A B : Type)
  [inhabited A] [inhabited B] : inhabited (A × B) :=
  {inhabited, value := (default A, default B)}

eval default (N × N) -- (0, 0)
```

In order to keep definition signatures short, we will also make use of Lean's **section** mechanism that allows us to fix common parameters for a set of definitions.

```
section
   -- in this section, implicit in signatures and in use sites
   parameter (A: Type)
   -- implicit in signatures but explicit in use sites
   variable (x: A)

   definition f: A:= x
   check f -- f: A → A
end

check f -- f: A: Type, A → A
```

extend ad nauseam when needed

4 The Basic Transformation

In this section, we describe the basic translation from Rust to Lean that includes pure code as well as mutable local variables and loops, but not mutable references (see Section 6). We focus on the parts that are unique to Rust or are nontrivial to translate. We roughly follow the structure of the Rust Reference.⁵ Because our translation output is not optimized for readability, all sample translations in this section have been prettified manually without changing their semantics.

4.1 The MIR

Because Rust makes extensive use of inference algorithms for types, lifetimes and typeclasses, correctly parsing Rust code is no small feat. Therefore, we use the Rust Compiler rustc itself as a frontend and work on the completely explicit and much simpler *mid-level intermediate representation* (MIR) (Figure 1). By writing our translation program in Rust, we can import the rustc libraries to gain access to the MIR and many convenient helper functions.

The MIR is a control flow graph (CFG) representation where a basic block consists of a list of statements followed by a terminator that (conditionally or

⁵https://doc.rust-lang.org/reference.html

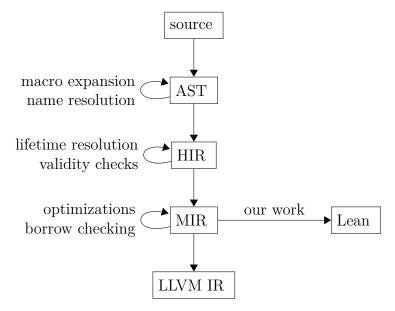


Figure 1: Overview of the Rust compiler pipeline and our work in that context

unconditionally) transfers control to other basic blocks. For readability, this section will mostly argue on the Rust source level, but the graph structure will be important for translating control flow.

4.2 Identifiers

Working on top of the MIR, we do not have to worry about the lexical structure of Rust. We do, however, have to make sure we emit lexically correct Lean code. This is only a problem with identifiers, which we would like to transfer with minimal changes. Both languages are based on segmented identifiers, just with different separators (a::b::c in Rust versus a.b.c in Lean). However, some identifier parts in Rust such as [T] or <F<T> as S> are not valid in Lean. To retain readability, we have therefore extended Lean with a general escaping syntax for identifiers that allows arbitrary symbols by surrounding them with « and »: The identifier «[T]».«a.b» is now a valid Lean identifier consisting of the parts «[T]» and «a.b».

4.3 Programs and Files

Rust's unit of compilation is called a *crate*. A crate consists of one or more .rs files and can be compiled to an executable or library. Files inside a crate may freely reference declarations between them. On the other hand, Lean files may only import other files non-recursively and declarations must be strictly sorted in order of usage for termination checking. We therefore translate a crate into a single Lean file and perform a topological sort on its declarations. While Lean does support explicit declarations of mutually recursive types and functions, we have not yet encountered such declarations in Rust code as part of our formalization work and thus have not implemented support for them so far.

In detail, our tool creates a file called generated.lean in a separate folder for each crate and connects them using Lean's import directive according to the inter-crate dependencies. The user can additionally create a pre.lean file that will automatically be imported and can be used for axiomatizations as well as a config.toml file that can influence the translation (see below for examples). We use a third Lean file thy.lean per crate for the proofs, which will import both the generated code and proof files from other crates.

4.4 Types

4.4.1 Primitive Types

Rust's primitive types are the boolean type, machine-independent and machine-dependent integer types, tuples, arrays, slices, and function types.

Following AutoCorres's design (see ??), we map the primitive integer types to Lean's native arbitrary-sized types and instead handle overflow explicitly during computation (Subsection 4.8.1).

```
abbreviation u8 [parsing_only] := nat
abbreviation u16 [parsing_only] := nat
abbreviation u32 [parsing_only] := nat
abbreviation u64 [parsing_only] := nat
abbreviation usize [parsing_only] := nat
abbreviation i8 [parsing_only] := int
// ...

definition u8.bits [reducible] : N := 8
// ...

definition usize.bits : N := 16
lemma usize.bits_ge_16 : usize.bits ≥ 16 := dec_trivial
attribute usize.bits [irreducible]
```

For the machine-size integer types **usize** and **isize**, we only expose the conservative assumption that their bit sizes are at least 16. We still define **usize.bits** to be exactly 16 so that it is computable, but by then marking the definition as [irreducible], this fact is only accessible in proofs when explicitly unfolding the definition. When a proof does rely on the bounds of a parameter, we can add a separate hypothesis, for which we make use of typeclasses. The bounds of an expression can often be determined just from partial information, such as with unsigned division.

```
definition is_bounded_nat [class] (bits x : N) := x < 2^bits
abbreviation is_usize := is_bounded_nat usize.bits

lemma div_is_bounded_nat [instance] (bits x y : N)
  [is_bounded_nat bits x] : is_bounded_nat bits (x / y) := ...</pre>
```

We use the same approach for arrays ([T; N]) and slices (&[T]), mapping both the to arbitrary-length list type. While Rust arrays have a constant length encoded in the type, slices are dynamic views into contiguous sequences like arrays or Vecs and bounded only by the memory size. More specifically, they (and any Rust type) are assumed to be no larger than isize::MAX bytes so that the pointer difference of any two elements can be represented by an isize value.

```
abbreviation array [parsing_only] (A : Type₁) (n : N) := list A
abbreviation slice [parsing_only] := list

definition is_slice [class] {A : Type₁} (xs : slice A) := length xs < 2^(usize.bits-1)</pre>
```

4.4.2 Structs and Enums

Because Rust does not feature inheritance, struct types and enumerated types are true Algebraic Data Types and can directly be translated to their Lean equivalents (**structure** and **inductive**, respectively).

4.4.3 References

An immutable reference &'a T is checked by the Rust compiler not to alias with any mutable reference and thus can be safely replaced with the translation of T itself. We drop all lifetime specifiers in general because we trust the Rust compiler to already have made all memory safety checks.

We will discuss mutable references in Section 6.

4.5 Traits

Rust's trait system is similar to Haskell's type classes, but borrows some syntax from more object-oriented *interface* systems. In particular, in addition to functions a trait may also contain methods that can be called on any object of a type the trait is implemented *on*. This is implemented via an implicit type parameter Self that is used for the type of the self parameter and is specified at a special syntactic position in trait implementations and trait bounds.

The translation of basic traits into Lean type classes is straightforward (Figure 2). We will discuss the details of the function-level translation and the sem monad below. While **impl** blocks in Rust are anonymous, we need to name all definitions in Lean and do so using a naming scheme similar to rustc's own internal representation.

4.5.1 Default Methods

As shown in Figure 2, we generate separate definitions for functions in trait implementations before assembling them into a type class instance. This way, and by eliminating the type class indirection in calls to a statically known implementation, we can allow trait implementation functions to call each other using our standard topological dependency ordering.

```
struct S { i: i32 }
                          structure S := (i : i32)
trait Trait<T> {
                          structure Trait [class] (Self T : Type1) :=
  fn f(self) -> T;
                          (f : Self → sem T)
impl Trait<i32> for S {
                          definition «S as Trait<i32>».f (self : S) :
  fn f(self) -> i32 {
                          → sem i32 :=
    self.i
                          return (S.i self)
}
                          definition «S as Trait<i32>» [instance] :=
                          {Trait S i32, f := «S as Trait<i32>».f}
fn g<T : Trait<i32>>
  (t: T) -> i32 {
                          definition g {T : Type1} [Trait T i32] (t :
  t.f()
                          → T) : sem i32 :=
                          sem.incr 1 (Trait.f _ t)
fn h() -> i32 {
                          definition h : sem i32 :=
 g(S { i: 0 })
                          sem.incr 1 (g (S.mk 0))
```

Figure 2: A parametric trait in Rust and its translation.

```
structure S := (i : i32)
struct S;
                          structure Trait [class] (Self : Type1) :=
                          (f : Self → sem unit)
trait Trait {
                          (g : Self → sem unit)
  fn f(self);
                          definition «S as Trait».g (self : S) : sem
  fn g(self);
                          → unit :=
                          return unit.star
impl Trait for S {
                          definition «S as Trait».f (self: S): sem
  fn f(self) {
    self.g()

    unit :=

                          sem.incr 1 («S as Trait».g self)
  fn g(self) {}
}
                          definition «S as Trait» [instance] :=
                          {Trait S, f := «S as Trait».f, g := «S as
                          → Trait».g}
```

However, just like Haskell, Rust also allows default implementations of trait methods that may arbitrarily call and be called from other trait methods that will only be defined in some implementation of the trait later on. This makes static ordering of dependencies impossible.

In essence, a default method in a trait takes as input an instance of that trait to call other trait methods with, but at the same time has to be a slot in the very same trait because it may be overridden in an implementation.

We could try to dynamically solve this cyclic dependency in a general way, computing its least fixed point by use of the Knaster-Tarski theorem [20] as usual in denotational semantics. Or we can restrict ourselves to special cases that break the cycle. If we remove the trait instance as an input to the default method, it cannot call other trait methods. If, on the other hand, we do not make default methods part of the trait instance, it cannot be overridden or be called from inside implementations of the trait.

We could implement all three approaches and automatically or manually choose between them on a case-by-case basis. It turns out, however, that in the Rust standard library, default methods are often just convenience wrappers around other trait methods, like in the PartialEq trait.

```
pub trait PartialEq<Rhs> {
    fn eq(&self, other: &Rhs) -> bool;
    fn ne(&self, other: &Rhs) -> bool { !self.eq(other) }
}
```

Therefore, as of now we have only implemented the third approach of declaring default methods outside of their trait, which turned out to be sufficient for our verification work so far.

4.5.2 Associated Types

There is one further advanced trait feature Rust shares with Haskell called associated types: trait members that are not functions, but types.

```
pub trait Add<RHS> {
  type Output;
  fn add(self, rhs: RHS) -> Output;
}
```

Making Output an associated type instead of a type parameter fundamentally changes type class inference: Instead of being an input parameter to the inference like Self and RHS, Output is *determined* by the inferred trait

instance. This means that inference on add can succeed even if the expected return type is unknown.

As a dependently typed language, Lean has no problem with representing such traits as type classes. What it cannot represent, however, is a special class of trait bounds Rust supports: T: Add<RHS, Output=RHS> asserts a definitional equality on the associated type; but definitional equality exists only as a judgment in Lean, not as a proposition we could pass as a parameter. Instead, we follow the original paper [4] on associated types in Haskell that translates type classes with associated types into System F by turning them into type parameters.

```
structure Add [class] (Self RHS Output : Type1) :=
(add : Self → RHS → sem Output)
```

This transformation does weaken type class inference, which means that in the generated Lean code, we have to resort to passing type class arguments explicitly using the @ notation. We might be able to regain inference in a potential future version of Lean that supports functional dependencies [12].

4.5.3 Trait Objects

Lastly, Rust's trait system exhibits a feature that does not directly exist in Haskell. In Haskell, type classes are not types - they cannot explicitly be passed by value, only implicitly through inference. In Rust, traits are dynamically sized types, which means they can be used as values, but only behind some indirection like &Trait. These trait objects are represented as a pointer to a vtable of the trait implementation and another pointer to the Self value.

This "fat pointer" representation would translate quite naturally to an existential type Σ (Self: Type), (Trait Self × Self). What is not apparent in this natural definition, however, is the fact that it necessarily lives in a higher universe than Self. This is the only construct currently in Rust that can give rise to a type not in Type1 (but, in fact, to a type in an arbitrarily high universe through nesting). It is an open problem in the Lean community if and how a monad over types of different universes can cleanly work given Lean's non-cumulative universe hierarchy. Fortunately, trait objects are a rare feature in Rust code that we do not expect to find on the algorithmical level of our current verification work, so we have not investigated this issue any further for now.

4.6 The Semantics Monad

The core part for representing Rust's dynamic semantics is the monadic embedding. While higher-order unification issues in the current Lean version prevent us from outright parameterizing the embedding by an arbitrary monad instance, we still try to keep the interface of our specific monad abstract so that the monad can be extended in the future.

We currently model abnormal termination⁶ and nontermination as well as an abstract step counter for asymptotic run time analysis.

```
definition sem (A : Type₁) := option (A × N)
```

We provide the standard monadic operations on the type, including a do-notation. The model-specific operations are mzero indicating abnormal termination/nontermination, and sem.incr, which increments the step counter (if any). An increment of one is emitted around every Rust function call and before each loop iteration.

The semantics monad follows the usual monad laws, which we will make use of in proofs.

```
lemma return_bind {A B : Type1} {a : A} {f : A → sem B}
    : (return a >>= f) = f a := ...
lemma bind_return {A : Type1} {m : sem A} : (m >>= return) = m := ...
lemma bind.assoc {A B C : Type1} {m : sem A} {f : A → sem B}
    {g : B → sem C} : (m >>= f >>= g) = (m >>= (\(\lambda x\), f x >>= g)) := ...
```

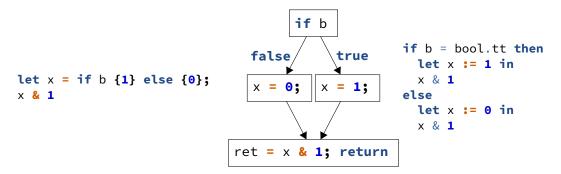
⁶unspecified behavior like integer overflow and *panics* from out-of-bounds array accesses or explicit panic! calls. Rust does not have exceptions.

4.7 Statements and Control Flow

The local state of a Rust function consists of its arguments, variables, and temporaries (variables introduced by the compiler). Without mutable references, these locals can only be manipulated by assignments, the single statement kind available in the MIR. In linear code, keeping track of assignments is as easy as transforming them to redeclarations.

```
p.x += 1; let p = Point { x = p.x + 1, ...p };
```

Nonlinear control flow is introduced by Rust's **if** and **match** constructs as well as its three loop constructs (which have a single common representation in the MIR). We map the first two cases to Lean's corresponding constructs of the same names.



As can be seen, we currently translate each branch of a conditional block terminator independently, which can lead to code duplication if those branches converge again. While this has not manifested any problems in our verification work so far, we may want to mitigate it in the future by factoring out the common translated code into a separate definition.

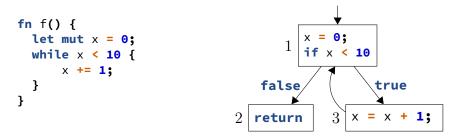


Figure 3: A **while** loop and the corresponding (simplified) MIR graph. Blocks 1 and 3 from a strongly connected component, which is dominated by block 1, the loop header.

We do need to factor out common code in the case of loops. There is no special terminator signifying loops in the MIR; instead, we have to search for (nontrivial) strongly connected components (SCCs) of basic blocks (Figure 3). Because Rust's control flow is reducible (notably, lacking a goto instruction), we may assume that such an SCC can only be entered from a single node (dominating the SCC). With this, we can describe the semantics of the SCC in more traditional terms of iteration: The dominating node is the loop header, while the rest of the SCC is the body. Jumping back to the header signifies a new iteration, while jumping out of the SCC means breaking the loop. By breaking up the SCC at the header, we can thus translate a single iteration to a function of type

```
State → sem (State + Res)
```

that takes a tuple State of loop variables and either returns the new state for the next iteration, or a value of the source function's return type Res when breaking out of the loop. We tie this into a single value of type sem Res by use of a general *loop combinator*.

4.7.1 The Loop Combinator

The loop combinator has the signature

```
noncomputable definition loop {State Res : Type1}
  (body : State → sem (State + Res)) (s : State) : sem Res
```

Its task is to apply body repeatedly (starting with s) until some Res is returned; if the loop does not terminate, it returns mzero (which body may also return by itself). Termination for arbitrary values of body obviously is not a decidable property. Therefore we will have to leave the constructive subset of Lean, as signified by the **noncomputable** specifier. The (simplified) translation of the Rust code in Figure 3 via loop is as follows:

```
definition f.loop_1 (x : i32) : sem (i32 + unit) :=
if x < 10 then
  let x := x + 1 in
  return (sum.inl x)
else
  return (sum.inr unit.star)

definition f : sem unit :=
let x := 0 in
loop f.loop_1 x</pre>
```

As a total, purely functional language, Lean cannot express iteration directly, and the only primitive kind of recursion available in Lean is structural recursion over an inductive datatype. On top of structural recursion, the Lean standard library defines the more general concept of *well-founded* recursion: A relation $R: A \rightarrow A \rightarrow Prop$ on a type A is well-founded if every element of A is *accessible* through the relation, which is defined inductively as all predecessors of the element under the relation being accessible.

```
inductive acc {A : Type} (R : A \rightarrow A \rightarrow Prop) : A \rightarrow Prop := intro : \forall x, (\forall y, R y x \rightarrow acc R y) \rightarrow acc R x

inductive well_founded [class] {A : Type} (R : A \rightarrow A \rightarrow Prop) : Prop

\Rightarrow := intro : (\forall a, acc R a) \rightarrow well_founded R
```

Using structural recursion over the acc predicate, the standard library defines a fixed-point combinator for functionals respecting a well-founded relation, and proves that the combinator satisfies the fixpoint equation.

```
namespace well_founded
section
  variables {A : Type} {C : A → Type} {R : A → A → Prop}

definition fix [well_founded R] (F : Πx, (Πy, R y x → C y) → C x)
  (x : A) : C x := ...

theorem fix_eq [well_founded R] (F : Πx, (Πy, R y x → C y) → C x)
  (x : A) : fix F x = F x (λy h, fix F y) := ...
end
end well_founded
```

We use well-founded recursion to define loop: If repeatedly applying body to s yields a sequence of states, this sequence will terminate iff there exists a well-founded relation on State such that the sequence is a descending chain. This is true because descending chains in well-founded relations are finite, and conversely a finite sequence $s_1 = s, \ldots, s_n$ is a descending chain in the trivial well-founded relation $R = \{(s_{i+1}, s_i) | 1 \le i < n\}$.

In the formalization, given a well-founded relation R on State, we first have to take care of lifting it to a well-founded relation R' on State + Res.

```
section
  parameters {State Res : Type1}
  parameter (body : State → sem (State + Res))
  parameter (R : State → State → Prop)

definition State' := State + Res
```

We can then wrap body in a functional respecting R' that we can pass to well_founded.fix.

```
definition F (x : State') (f : \Pi (x' : State'), R' x' x \rightarrow sem
→ State') : sem State' :=
 match x with
 | inr _ := mzero -- unreachable
 | inl s :=
   do x' ← sem.incr 1 (body s);
   match x' with
   | inr r := return (inr r)
          := if H : R' x' x then f x' H else mzero
   end
 end
 definition loop.fix [well_founded R] (s : State) : sem Res :=
 do x ← well_founded.fix F (inl s);
 match x with
 | inr r := return r
 | inl _ := mzero -- unreachable
 end
```

Finally, we implement loop by choosing any well-founded relation R that makes the loop terminate, if any, or else return mzero.

```
definition terminating (s : State) :=
∃ Hwf : well_founded R, loop.fix s ≠ mzero

noncomputable definition loop (s : State) : sem Res :=
if Hex : ∃ R, terminating R s then
  @loop.fix (classical.some Hex) _ (classical.some
→ (classical.some_spec Hex)) s
else mzero
```

Here we make use of the *dependent if-then-else* notation that allows us to test for a property and then bind a name to a proof of it in case it holds. We then destructure that proof object to obtain the relation and its well-foundedness proof so that we can pass them to loop.fix. The classical.some and classical.some_spec definitions are based on Hilbert's epsilon operator.

```
noncomputable definition classical.some {A : Type} {P : A \rightarrow Prop} (H \hookrightarrow : \exists x, P x) : A := ... theorem classical.some_spec {A : Type} {P : A \rightarrow Prop} (H : \exists x, P x) : \hookrightarrow P (some H) := ...
```

The use of classical.some as well as the undecidable conditional \exists R, terminating R s make loop non-computable.

When verifying loops, we will first verify the corresponding application of loop.fix using a specific well-founded relation, for which we can prove a convenient fixpoint equation.

```
theorem loop.fix_eq
{R : State → State → Prop} [well_founded R] {s : State} :
loop.fix R s =
    do x' ← sem.incr 1 (body s);
    match x' with
    | inl s' := if R s' s then loop.fix R s' else mzero
    | inr r := return r
    end := ...
```

If the application of loop.fix terminates, we can show that the original application loop will do so too with the same return value, via a helper lemma that says that all terminating loop.fix applications are equal.

```
lemma loop.fix_eq_fix
  {R1 R2 : State → State → Prop} [well_founded R1] [well_founded R2]
  {s : State}
  (Hterm1 : loop.fix R1 s ≠ mzero)
    (Hterm2 : loop.fix R2 s ≠ mzero) :
    loop.fix R1 s = loop.fix R2 s := ...

theorem loop.fix_eq_loop
  {R : State → State → Prop} [well_founded R]
  {s : State}
  (Hterm : loop.fix R s ≠ mzero) :
    loop.fix R s = loop s := ...
```

4.8 Expressions

4.8.1 Arithmetic Operators

Rust's arithmetic semantics is based on the premise that in most circumstances, arithmetic overflow is unintended by the programmer,⁷ and constitutes a bug in the program. Therefore, in debug builds, the built-in arithmetic operators will panic on any overflow. In release builds, overflows for both signed and unsigned types will wrap for performance reasons.

⁷When overflowing is indeed intended, the programmer may use special methods such as u8::wrapping_add

We thus regard arithmetic overflow in those operators as *unspecified* and return the bottom value in such cases, using the predicate <code>is_bounded_nat</code> from Subsection 4.4.1.

We can avoid the check in operations that cannot overflow, such as unsigned division. We still have to check for division by zero, of course.

```
definition checked.div (bits : \mathbb{N}) (x y : nat) : sem nat := sem.guard (y \neq 0) (return (div x y))
```

The signed implementations are equivalent, except that we do have to check for overflow during signed division.

4.8.2 Bitwise Operators

We implement all bitwise operations on integral types by converting them to and from the bitvec type, which we adapted from the Lean standard library and expanded significantly.

```
abbreviation binary_bitwise_op (bits: N) (op: bitvec bits → bitvec

    bits → bitvec bits)
    (a b: nat): nat :=
bitvec.to N (op (bitvec.of bits a) (bitvec.of bits b))

definition bitor bits:= binary_bitwise_op bits bitvec.or
```

Some care must be taken when implementing bitwise shift: Shifting by the bitsize of a type or more bits will panic in Rust.

4.8.3 Index Expressions

While indexing is desugared to a call to the Index trait for most types, it is a primitive operation on arrays. Out-of-bounds accesses will panic in Rust. By identifying arrays with Lean lists, we can use the existing list.nth function and *lifting* its result into the semantics monad.

4.8.4 Lambda Expressions

Each lambda expression in Rust has a unique type that represents its *closure*, the set of variables captured from the outer scope. As necessitated by its ownership and mutability tracking, Rust files each closure type into one of three traits that together form a hierarchy:

```
pub trait FnOnce<Args> {
   type Output;
   fn call_once(self, args: Args) -> Output;
}

pub trait FnMut<Args> : FnOnce<Args> {
   fn call_mut(&mut self, args: Args) -> Output;
}

pub trait Fn<Args> : FnMut<Args> {
   fn call(&self, args: Args) -> Output;
}
```

Rust will automatically infer the most general trait based on the lambda expression's requirements: If it has to move ownership of a captured variable, it can only implement FnOnce; if it needs a mutable reference to a variable, it can only implement FnMut; otherwise, it will implement Fn.

Because we lose the restrictions of linear typing during our translation, we can simplify the hierarchy: FnOnce can be implemented using FnMut, if implemented, which in turn can be implemented using Fn (because the closure must be immutable in that case).

```
structure FnOnce [class] (Self Args Output : Type1) :=
(call_once : Self → Args → sem Output)

structure FnMut [class] (Self Args Output : Type1) :=
(call_mut : Self → Args → sem (Output × Self))

definition FnMut_to_FnOnce [instance] (Self Args Output : Type1)
```

```
[FnMut Self Args Output] : FnOnce Self Args Output :=
{FnOnce, call_once := λ self args, do x ← FnMut.call_mut _ self args;
  return x.1}

structure Fn [class] (Self : Type1) (Args : Type1) (Output : Type1) :=
(call : Self → Args → sem Output)

definition Fn_to_FnMut [instance] (Self Args Output : Type1) [Fn Self → Args Output]
  : FnMut Self Args Output :=
{FnMut, call_mut := λ self args, do x ← Fn.call _ self args;
  return (x, self)}
```

Translating a lambda expression means declaring a closure type according to the captured environment and creating a trait implementation according to the closure kind as reported by the compiler. Calling a lambda expression, on the other hand, is no different from other trait method calls and does not need any special casing.

5 Case Study: Verification of [T]::binary_search

As a first test of the translation tool, we set out to verify the correctness the binary search implementation in the Rust standard library, an algorithm of medium complexity.

Before we can even the algorithmic complexity, we have to cope with the design complexity of a real-world library. The public implementation of the method on any slice type can be found in the collections crate.

As can be seen from the method's documentation and signature, it is very general: The method works on all slices whose element type implements the Ord trait, and it returns information in both the success and the failure case. The implementation, however, turns out to be merely a redirection to a trait method in the base crate core. The trait is only implemented on the slice type.

```
pub trait SliceExt {
   type Item;

fn binary_search(&self, x: &Self::Item) -> Result<usize, usize>
    where Self::Item: Ord;
   fn len(&self) -> usize;
   fn is_empty(&self) -> bool { self.len() == 0 }
   ...
}

impl<T> SliceExt for [T] {
   type Item = T;
```

```
fn binary_search_by<'a, F>(&'a self, mut f: F) -> Result<usize,</pre>

    usize>

    where F: FnMut(&'a T) -> Ordering
{
    let mut base = Ousize:
    let mut s = self;
    loop {
        let (head, tail) = s.split_at(s.len() >> 1);
        if tail.is_empty() {
            return Err(base)
        }
        match f(&tail[0]) {
            Less => {
                 base += head.len() + 1;
                 s = &tail[1..];
            }
            Greater => s = head,
            Equal => return Ok(base + head.len()),
        }
    }
}
```

Listing 3: Implementation of the binary_search_by method. A subslice s of self is iteratively bisected until it is empty or the element has been found. The tail[1..] slicing syntax is syntax sugar for tail.index(RangeFrom{start: 1}).

This indirection seems pointless at first, but follows from a technical restriction: There may be at most one <code>impl</code> block for a primitive type like <code>[T]</code>. Because the <code>core</code> crate does not depend on the existence of a heap allocator, but some methods on <code>[T]</code> like its merge sort implementation do need dynamic allocation, the <code>impl</code> block is only declared in the later <code>collections</code> crate. Since <code>binary_search</code> does not need an allocator, it should still reside in <code>core</code>, and instead is associated to the slice type via the helper trait.

This final version of binary_search, which we represent as core::<[T] as SliceExt>::binary_search, is implemented by way of a more general method binary_search_by that takes a comparison function instead of be-

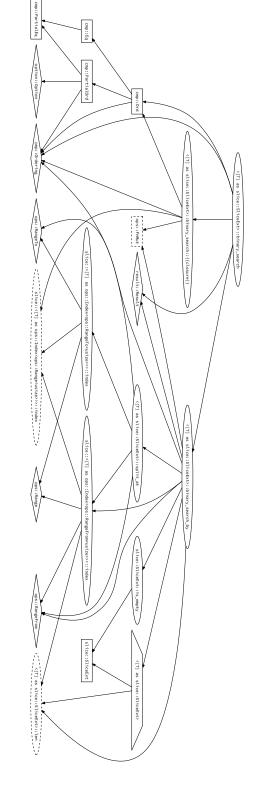
ing constrained to Ord (Listing 3). This method, finally, turns out to be more abstract than one might expect: instead of the standard implementation that iteratively reduces the search range via two indices, the range is represented as a subslice and manipulated via high-level slice methods such as split_at. The reasoning behind this is a great show case for Rust's zero-cost (or even negative-cost, in this case) abstractions philosophy – the abstract implementation actually surpasses the direct implementation in terms of efficiency because it helps the compiler to eliminate all bounds checks in it. It also elegantly avoids the common pitfall⁸ of a potential integer overflow in less abstract code like mid = (low + high) / 2.

For our purposes, the abstract implementation primarily means a fair number of additional dependencies we have to support and inspect (Figure 4). All in all, binary_search turned out to be an ideal first test not only because of its algorithmic complexity, but also because of its use of numerous Rust language features including enums, structs, traits with associated types and default methods, higher-order functions, and loops.

When trying to translate the binary_search method including its dependencies, we will not get back a working definition at first. Our tool refuses to translate some dependencies because they use unsafe code, as marked in Figure 4. We will have to translate these functions manually, basically adding the correctness of their translation as axioms to the project.

Apart from our custom translation of FnMut we discussed in Subsection 4.8.4, both axiomatized functions operate on slices and are straightforward to implement using our identification of slices with Lean lists.

⁸https://research.googleblog.com/2006/06/extra-extra-read-all-about-it-nearly.html



the full Index implementation for [T], and even the trait itself. possible, such as to the index method of Index<RangeFrom<usize>> for [T], we can avoid some dependencies like code in the original implementation are marked by dashed borders. Because we eagerly resolve trait method calls where between Figure 4: A complete graph of the translation dependencies of binary_search in the core crate, distinguishing functions types , traits >, and trait implementations . Axiomatized items that use unsafe

- 6 Transformation of Mutable References
- 7 Case Study: Verification of fixedbitset
- 8 Conclusion and Future Work

34 REFERENCES

References

[1] B. Anderson, L. Bergstrom, M. Goregaokar, J. Matthews, K. McAllister, J. Moffitt, and S. Sapin. Engineering the Servo web browser engine using Rust. In *Proceedings of the 38th International Conference on Software Engineering Companion*, pages 81–89. ACM, 2016.

- [2] B. Barras, S. Boutin, C. Cornes, J. Courant, J.-C. Filliatre, E. Gimenez, H. Herbelin, G. Huet, C. Munoz, C. Murthy, et al. *The Coq proof assistant reference manual: Version 6.1.* PhD thesis, Inria, 1997.
- [3] F. Bobot, J.-C. Filliâtre, C. Marché, and A. Paskevich. Why3: Shepherd your herd of provers. In *Boogie 2011: First International Workshop on Intermediate Verification Languages*, pages 53–64, 2011.
- [4] M. M. Chakravarty, G. Keller, S. P. Jones, and S. Marlow. Associated types with class. In ACM SIGPLAN Notices, volume 40, pages 1–13. ACM, 2005.
- [5] T. Coquand and G. Huet. The calculus of constructions. *Information and computation*, 76(2-3):95–120, 1988.
- [6] P. Cuoq, F. Kirchner, N. Kosmatov, V. Prevosto, J. Signoles, and B. Yakobowski. Frama-C. In *International Conference on Software Engineering and Formal Methods*, pages 233–247. Springer, 2012.
- [7] L. de Moura, S. Kong, J. Avigad, F. Van Doorn, and J. von Raumer. The Lean theorem prover (system description). In *International Conference on Automated Deduction*, pages 378–388. Springer, 2015.
- [8] J.-C. Filliâtre and C. Marché. The Why/Krakatoa/Caduceus platform for deductive program verification. In *International Conference on Computer Aided Verification*, pages 173–177. Springer, 2007.
- [9] D. Greenaway, J. Andronick, and G. Klein. Bridging the gap: Automatic verified abstraction of C. In *International Conference on Interactive Theorem Proving*, pages 99–115. Springer, 2012.
- [10] D. Greenaway, J. Lim, J. Andronick, and G. Klein. Don't sweat the small stuff: formal verification of C code without the pain. ACM SIGPLAN Notices, 49(6):429–439, 2014.
- [11] J. Guitton, J. Kanig, and Y. Moy. Why Hi-Lite Ada. 2011.

REFERENCES 35

[12] M. P. Jones. Type classes with functional dependencies. In *European Symposium on Programming*, pages 230–244. Springer, 2000.

- [13] G. Klein, K. Elphinstone, G. Heiser, J. Andronick, D. Cock, P. Derrin, D. Elkaduwe, K. Engelhardt, R. Kolanski, M. Norrish, et al. sel4: Formal verification of an OS kernel. In *Proceedings of the ACM SIGOPS 22nd* symposium on Operating systems principles, pages 207–220. ACM, 2009.
- [14] N. D. Matsakis and F. S. Klock II. The Rust language. In *ACM SIGAda Ada Letters*, volume 34, pages 103–104. ACM, 2014.
- [15] T. Nipkow, L. C. Paulson, and M. Wenzel. Isabelle/HOL: a proof assistant for higher-order logic, volume 2283. Springer Science & Business Media, 2002.
- [16] L. O'Connor, Z. Chen, C. Rizkallah, S. Amani, J. Lim, T. Murray, Y. Nagashima, T. Sewell, and G. Klein. Refinement through restraint: bringing down the cost of verification. In *Proceedings of the 21st ACM SIGPLAN International Conference on Functional Programming*, pages 89–102. ACM, 2016.
- [17] F. Pfenning and C. Paulin-Mohring. Inductively defined types in the calculus of constructions. In *International Conference on Mathematical Foundations of Programming Semantics*, pages 209–228. Springer, 1989.
- [18] J. C. Reynolds. Separation logic: A logic for shared mutable data structures. In *Logic in Computer Science*, 2002. Proceedings. 17th Annual IEEE Symposium on, pages 55–74. IEEE, 2002.
- [19] T. A. L. Sewell, M. O. Myreen, and G. Klein. Translation validation for a verified OS kernel. In *Proceedings of the 34th ACM SIGPLAN Con*ference on *Programming Language Design and Implementation*, PLDI '13, pages 471–482, New York, NY, USA, 2013. ACM.
- [20] A. Tarski et al. A lattice-theoretical fixpoint theorem and its applications. *Pacific journal of Mathematics*, 5(2):285–309, 1955.
- [21] P. Wadler. Linear types can change the world. In *IFIP TC*, volume 2, pages 347–359. Citeseer, 1990.

36 REFERENCES

Erklärung

Ort, Datum

Hiermit erkläre ich, Sebastian Andreas Ullrich, dass ich die vorliegende Masterarbeit selbstständig verfasst habe und keine anderen als die angegebenen Quellen und Hilfsmittel benutzt habe, die wörtlich oder inhaltlich übernommenen Stellen als solche kenntlich gemacht und die Satzung des KIT zur Sicherung guter wissenschaftlicher Praxis beachtet habe.

Unterschrift