

# Digital Image Processing

## CS390S

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2018 Spring



METROPOLITAN STATE UNIVERSITY<sup>SM</sup>  
OF DENVER

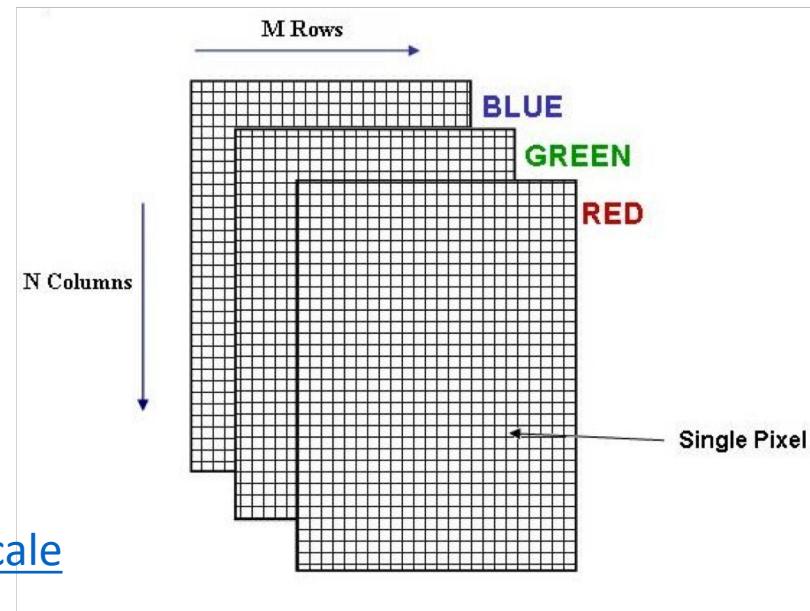
# Review Day 7

- Edge detection
- Filtering in frequency domain

# Day 8 Color Space

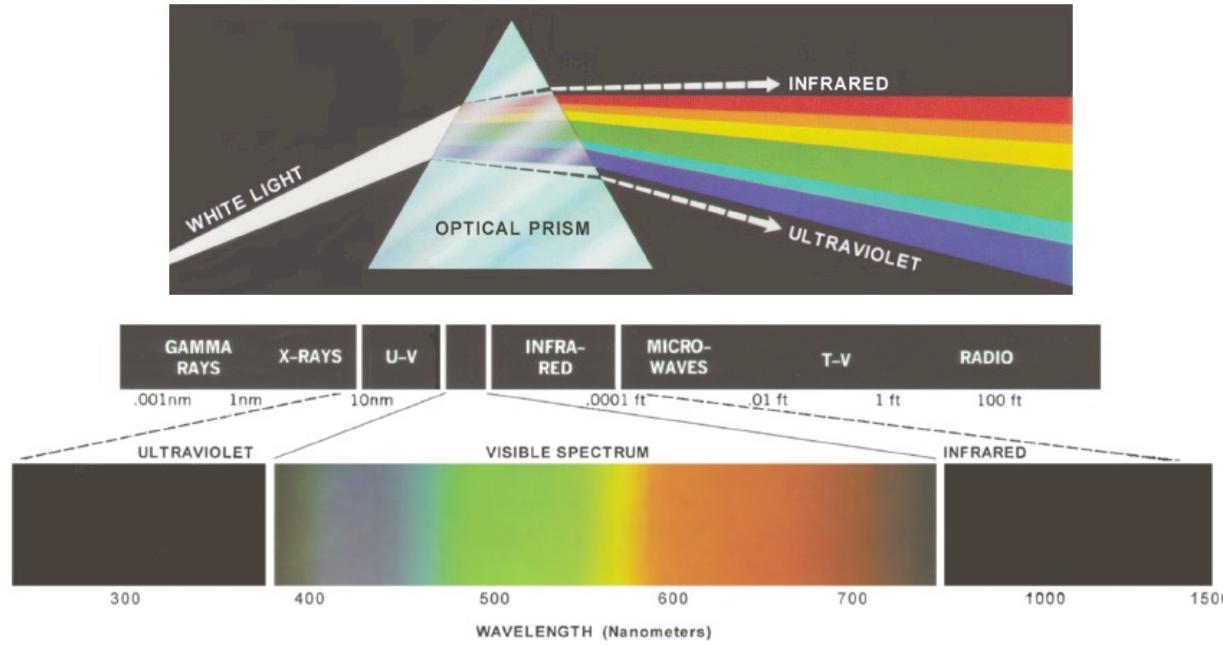
- XYZ CIE standard
- RGB
- HSI (HSV)
- Lab LUV YUV YCrCb

[Color image ->grayscale image](#)  
<https://en.wikipedia.org/wiki/Grayscale>



[Color space: http://dba.med.sc.edu/price/irf/Adobe\\_tg/models/ciexyz.html](http://dba.med.sc.edu/price/irf/Adobe_tg/models/ciexyz.html)

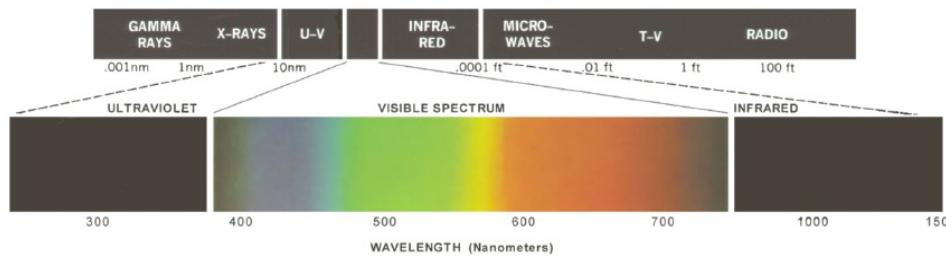
# Color Space



- E.g. Green object reflect the light with 500 nm wavelength

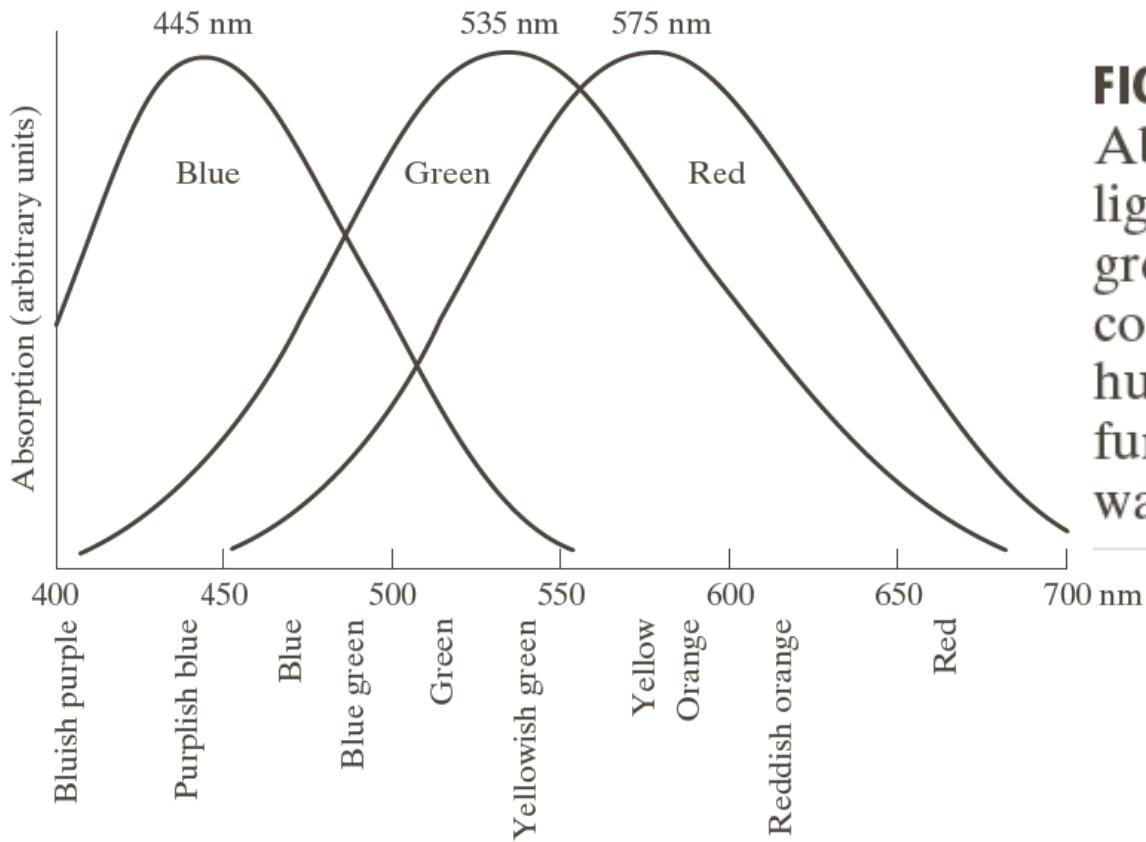
# Color Space

- Achromatic light (gray level, intensity)
- Chromatic light (400-700 nm)
- luminance, radiance and brightness (subjective, achromatic intensity)



- Human eyes: 6-7 million cones (65% R 33% G 2% B)
- Primary colors (R G B)

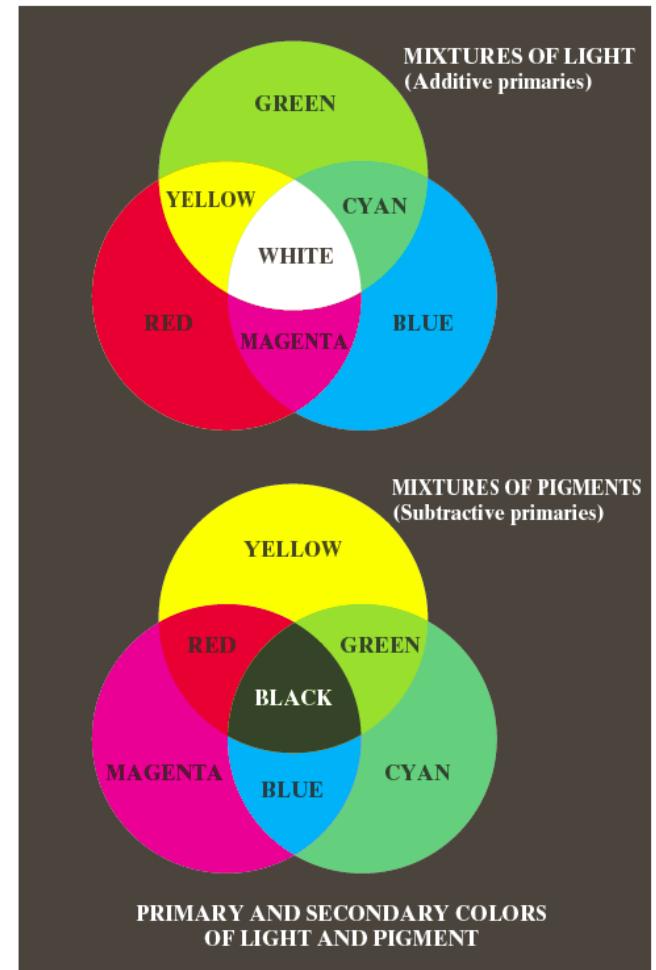
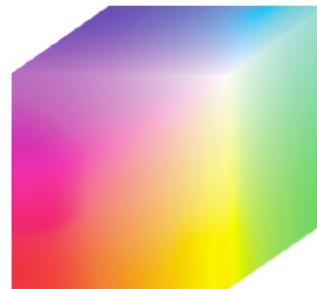
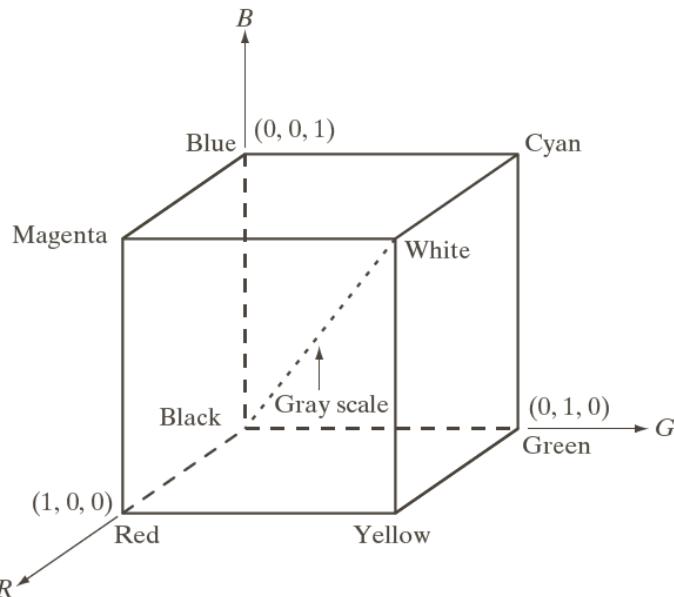
# Color Space



**FIGURE 6.3**  
Absorption of light by the red, green, and blue cones in the human eye as a function of wavelength.

# Color Space

- Primary color
- Secondary color



# Color Space

- To distinguish colors :
  - Chromaticity: Hue and Saturation
    - Hue: measures dominant wavelength of light waves
    - Saturation: amount of white light mixed with a hue
    - E.g. pink = red +white
  - Brightness (subjective, impossible to measure, achromatic notion of intensity)

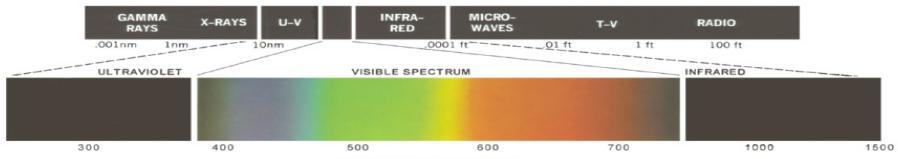
# Color Space

- Tristimulus

- The amount of Red, Green and Blue needed to form a particular color (denoted by X, Y and Z)
- A color is then specified by its "Tri-chromatic Coefficients"

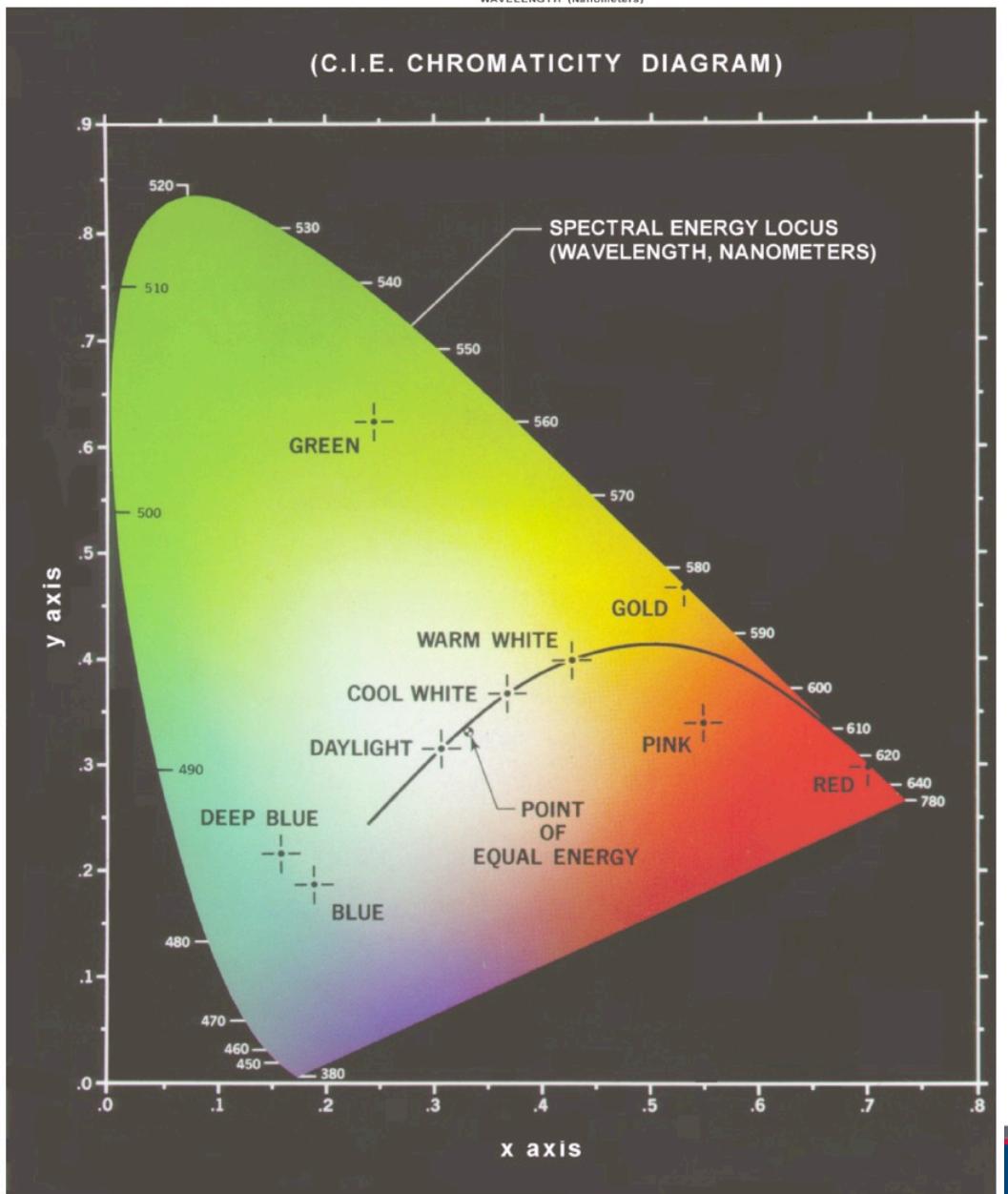
$$x = \frac{X}{X+Y+Z} \quad y = \frac{Y}{X+Y+Z} \quad z = \frac{Z}{X+Y+Z}$$

- Thus  $x+y+z=1$



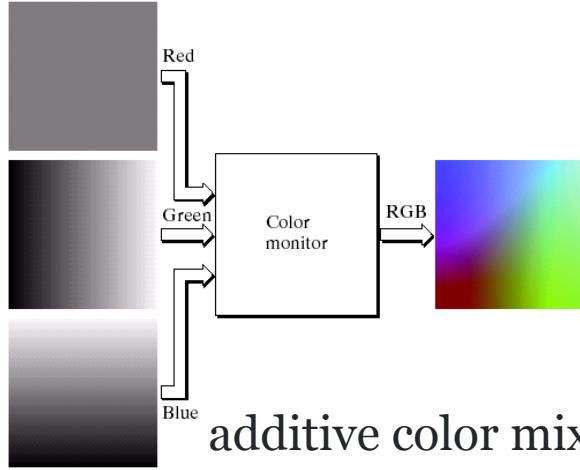
# Color Space

- Color gamut
- Boundary saturated
- White point zero saturation
- Not all visible color by RGB
- Just most efficient

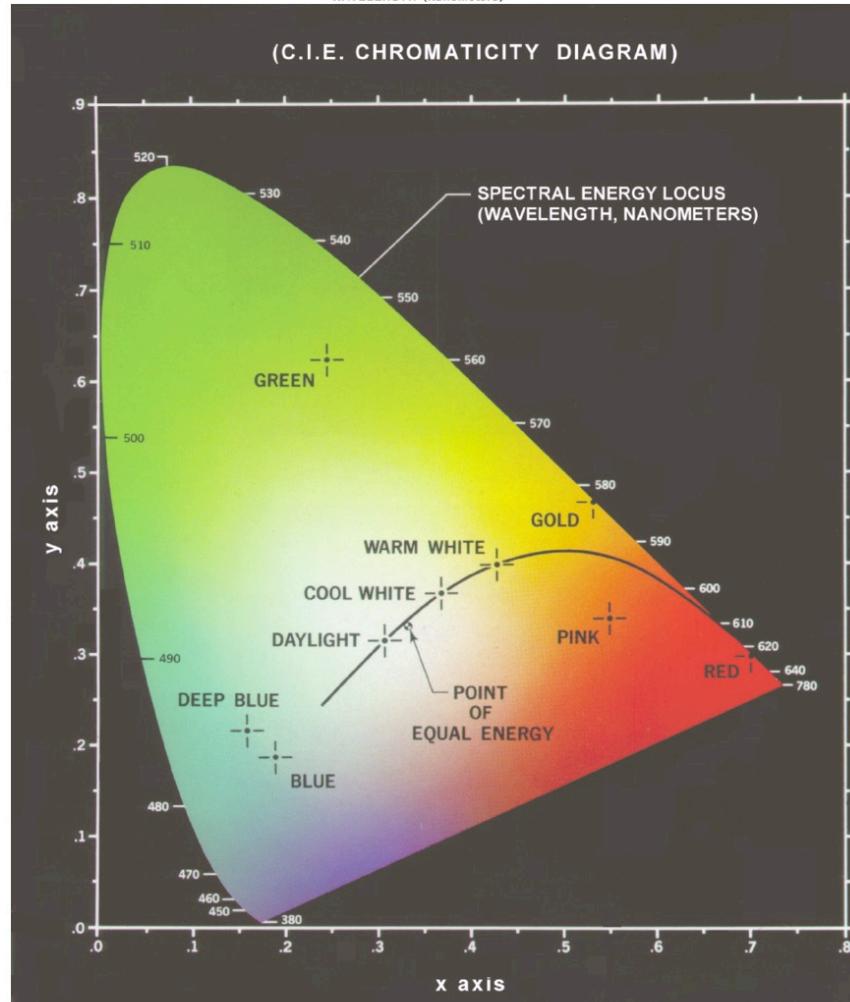
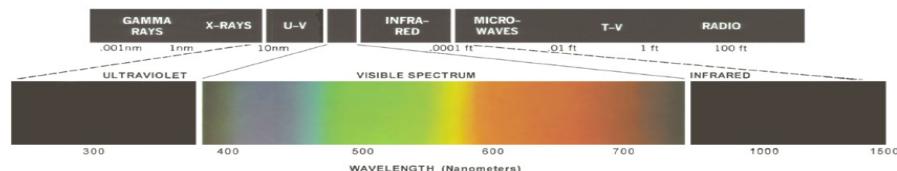
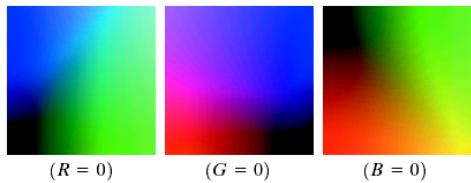


# Color Space

- Color gamut



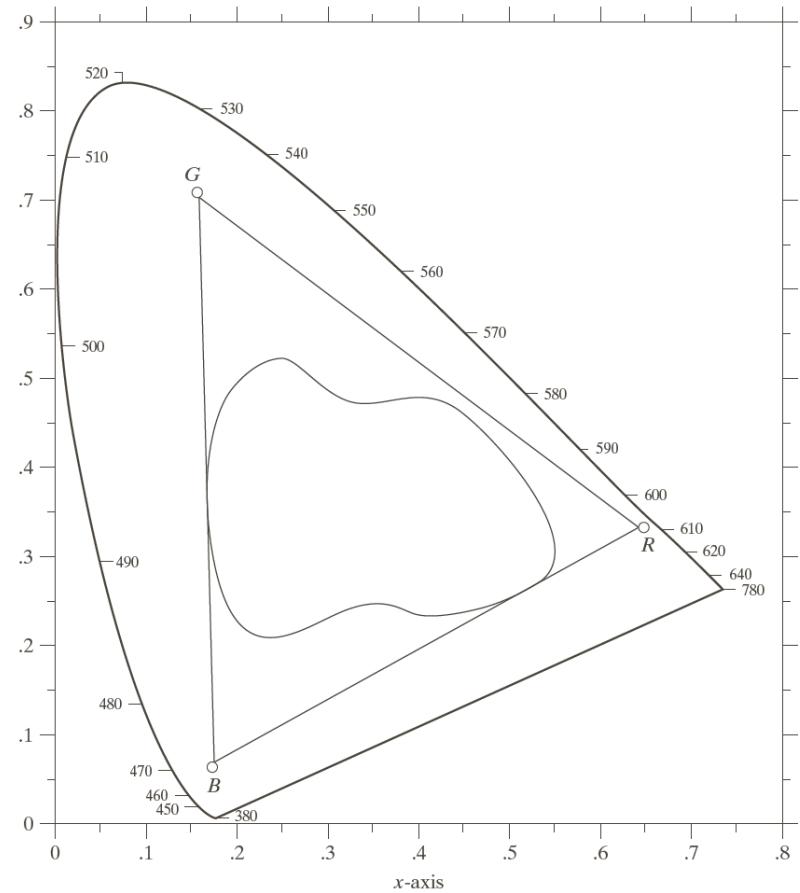
additive color mixture



# Color Space

- RGB – monitor, camera
- CMY, CMYK – printing
- HSI
  - (hue saturation intensity)

**FIGURE 6.6**  
Typical color  
gamut of color  
monitors  
(triangle) and  
color printing  
devices (irregular  
region).



# Color Space

- Tristimulus

- The amount of Red, Green and Blue needed to form a particular color (denoted by X, Y and Z)
- A color is then specified by its "Tri-chromatic Coefficients"

$$x = \frac{X}{X+Y+Z} \quad y = \frac{Y}{X+Y+Z} \quad z = \frac{Z}{X+Y+Z}$$

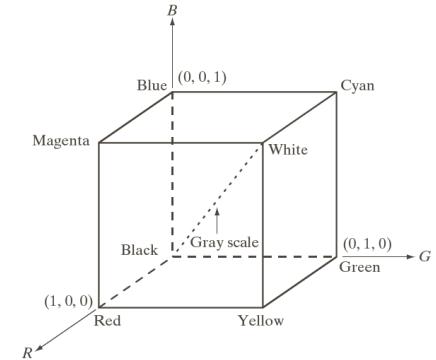
- Thus  $x+y+z=1$

# Color Space

- RGB <-> CMY color space conversion

Convert White from (1, 1, 1) in RGB to (0, 0, 0) in CMY:

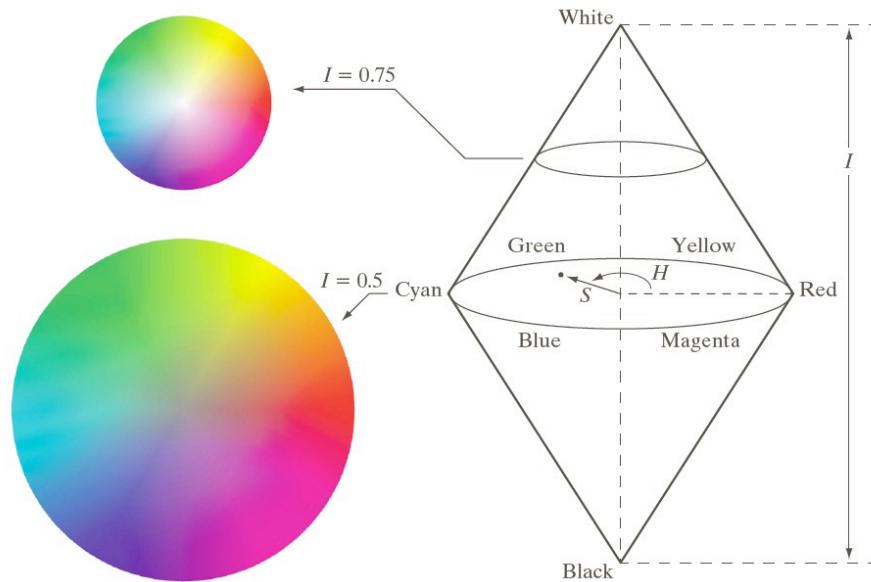
$$\begin{bmatrix} C \\ M \\ Y \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} R \\ G \\ B \end{bmatrix} \quad \begin{bmatrix} R \\ G \\ B \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} C \\ M \\ Y \end{bmatrix}$$



- Sometimes, an alternative CMYK model (K stands for *Black*) is used in color printing (e.g., to produce darker black than simply mixing CMY).

# Color Space

- HSI (Hue, Saturation, Intensity)
  - RGB ideal for color generation
  - HSI natural and intuitive to humans



# Color Space

- HSI (Hue Saturation Intensity)

## ■ RGB → HSI

$$\theta = \cos^{-1} \left\{ \frac{[(R - G) + (R - B)] / 2}{\sqrt{(R - G)^2 + (R - B)(G - B)}} \right\}$$

$$H = \begin{cases} \theta & B \leq G \\ 360 - \theta & B > G \end{cases}$$

$$S = 1 - \frac{3 \cdot \min(R, G, B)}{R + G + B}$$

$$I = (R + G + B) / 3$$

# Color Space

- HSI (Hue Saturation Intensity)

$$H_n = \begin{cases} 0, & \text{if } 0^\circ \leq H \leq 120^\circ; \\ H - 120^\circ, & \text{if } 120^\circ < H \leq 240^\circ; \\ H - 240^\circ, & \text{if } 240^\circ < H < 360^\circ \end{cases}$$

$$R = \begin{cases} I \cdot \left(1 + \frac{S \cdot \cos(H_n)}{\cos(60^\circ - H_n)}\right), & \text{if } 0^\circ \leq H \leq 120^\circ; \\ I - I \cdot S, & \text{if } 120^\circ < H \leq 240^\circ; \\ 3I - G - B, & \text{if } 240^\circ < H < 360^\circ \end{cases}$$

$$G = \begin{cases} 3I - R - B, & \text{if } 0^\circ \leq H \leq 120^\circ; \\ I \cdot \left(1 + \frac{S \cdot \cos(H_n)}{\cos(60^\circ - H_n)}\right), & \text{if } 120^\circ < H \leq 240^\circ; \\ I - I \cdot S, & \text{if } 240^\circ < H < 360^\circ \end{cases}$$

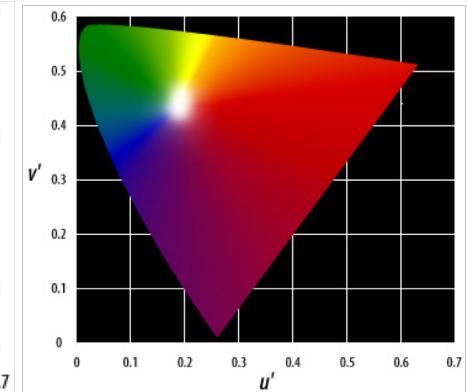
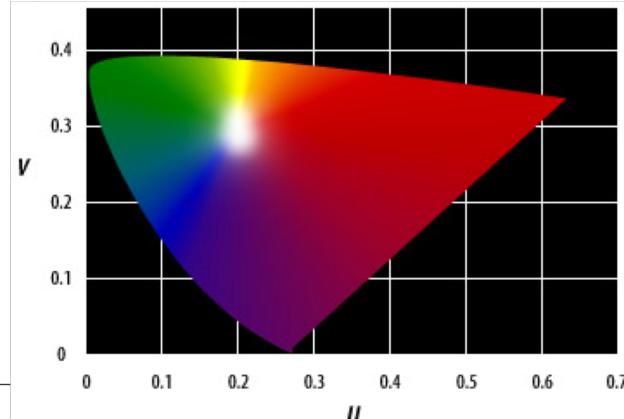
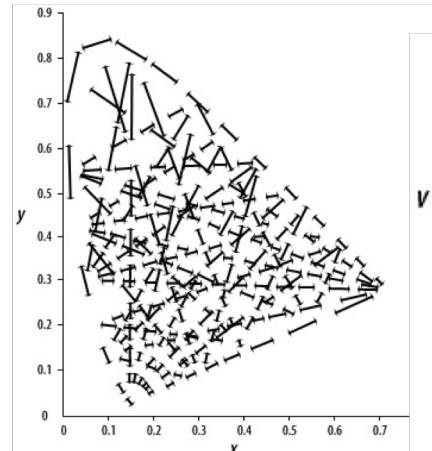
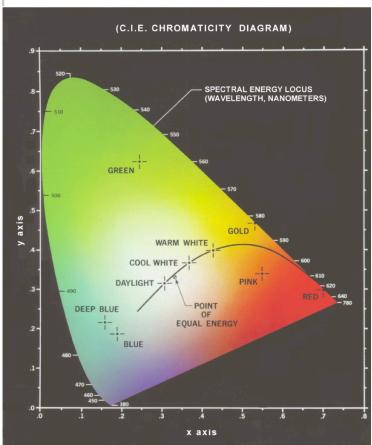
$$B = \begin{cases} I - I \cdot S, & \text{if } 0^\circ \leq H \leq 120^\circ; \\ 3I - R - G, & \text{if } 120^\circ < H \leq 240^\circ; \\ I \cdot \left(1 + \frac{S \cdot \cos(H_n)}{\cos(60^\circ - H_n)}\right), & \text{if } 240^\circ < H < 360^\circ \end{cases}$$

# Color Space

- LUV (CIELUV)

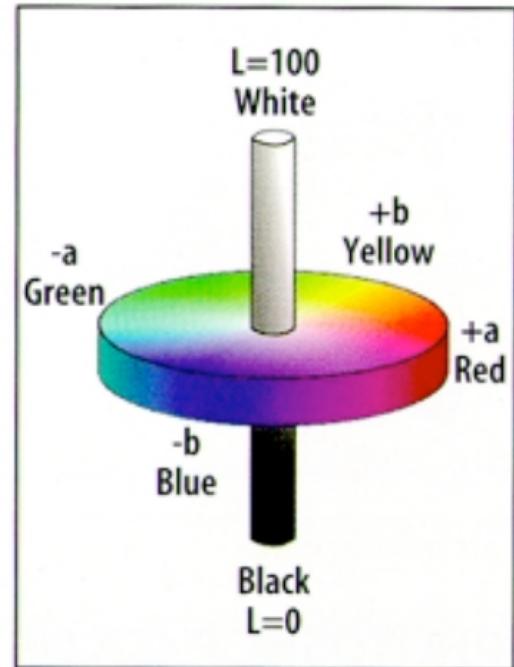
Not uniform  $\rightarrow$  1960, CIE  $u,v$  Chrom Diagram.

$\rightarrow$  still not satisfied  $\rightarrow$  1976 new  $(u',v')$  values  $L$  lightness (0-100)



# Lab: photoshop

- Photoshop uses this model to get more control over color
- It's named CIE Lab model (refined from the original CIE model)
- Liminance: L
- Chrominance: a – ranges from green to red and b ranges from blue to yellow



*Lab model*

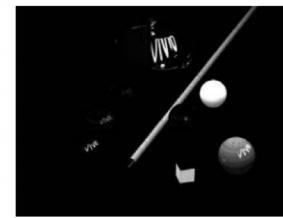
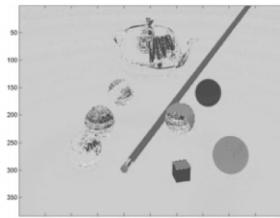
# Color Space

## Yuv and YCrCb: digital video

- Initially, for PAL analog video, it is now also used in CCIR 601 standard for digital video
- Y (luminance) is the CIE Y primary.  
$$Y = 0.299R + 0.587G + 0.114B$$
- *Chrominance* is defined as the difference between a color and a reference white at the same luminance. It can be represented by U and V -- the *color differences*.  
$$U = B - Y; V = R - Y$$
- YCrCb is a scaled and shifted version of YUV and used in JPEG and MPEG (all components are positive)  
$$Cb = (B - Y) / 1.772 + 0.5; Cr = (R - Y) / 1.402 + 0.5$$

# Color Space

## Examples (RGB, HSV, Luv)



# Color Space

- Example
- Applications



Full color



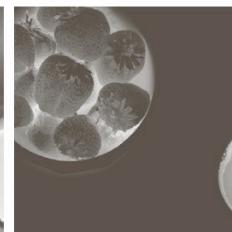
Cyan



Magenta



Yellow



Black



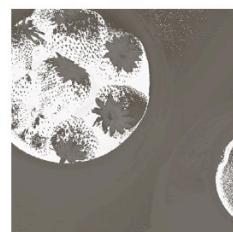
Red



Green



Blue



Hue



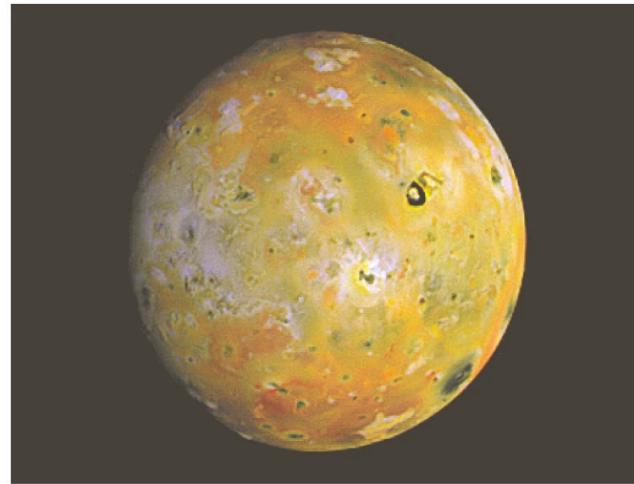
Saturation



Intensity

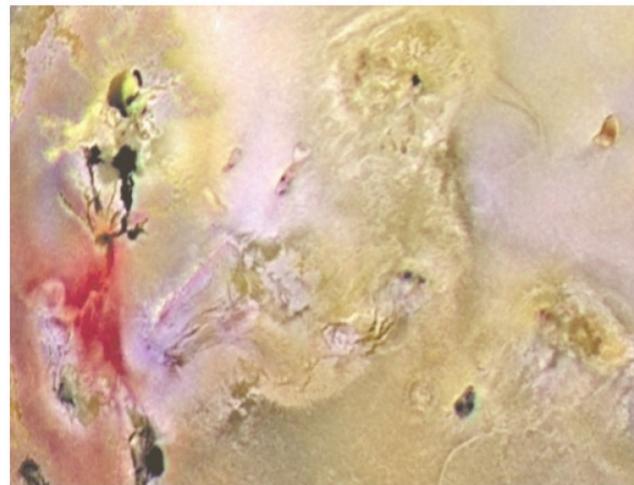
# Color Space

- Example
- Applications



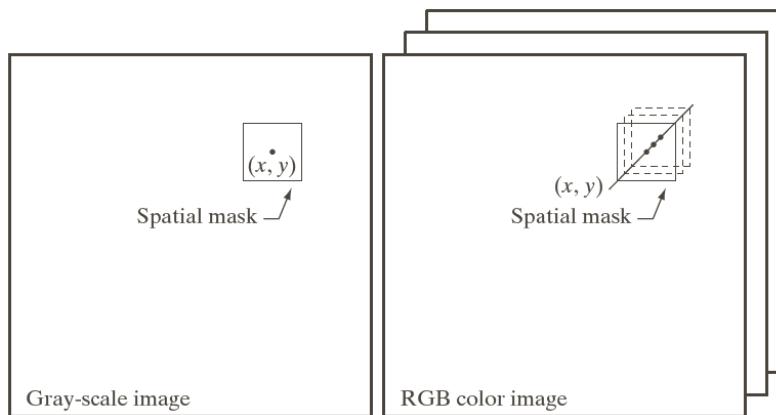
a  
b

**FIGURE 6.28**  
(a) Pseudocolor  
rendition of  
Jupiter Moon Io.  
(b) A close-up.  
(Courtesy of  
NASA.)



# Color Space

- Example
- Applications

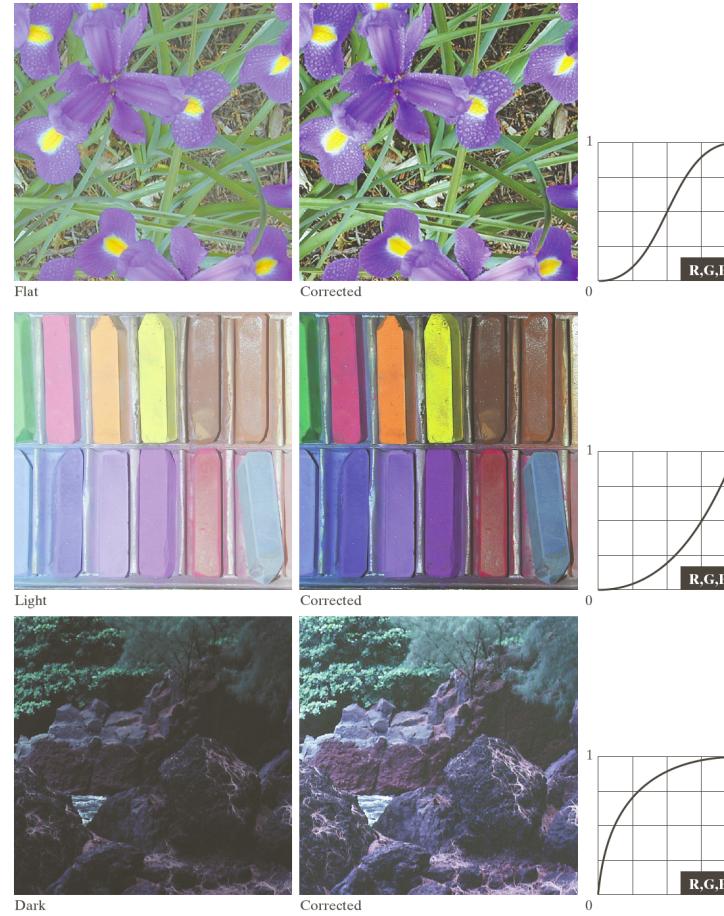


a | b

**FIGURE 6.29**  
Spatial masks for  
gray-scale and  
RGB color  
images.

# Color Space

- Example
- Applications



**FIGURE 6.35** Tonal corrections for flat, light (high key), and dark (low key) color images. Adjusting the red, green, and blue components equally does not always alter the image hues significantly.

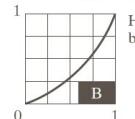
# Color Space

- Example
- Applications

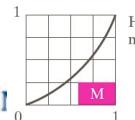


Original/Corrected

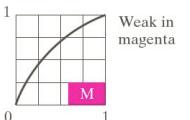
**FIGURE 6.36** Color balancing corrections for CMYK color images.



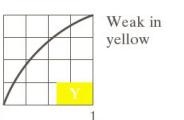
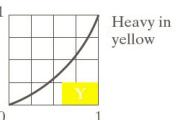
Heavy in black



Heavy in magenta



Weak in magenta

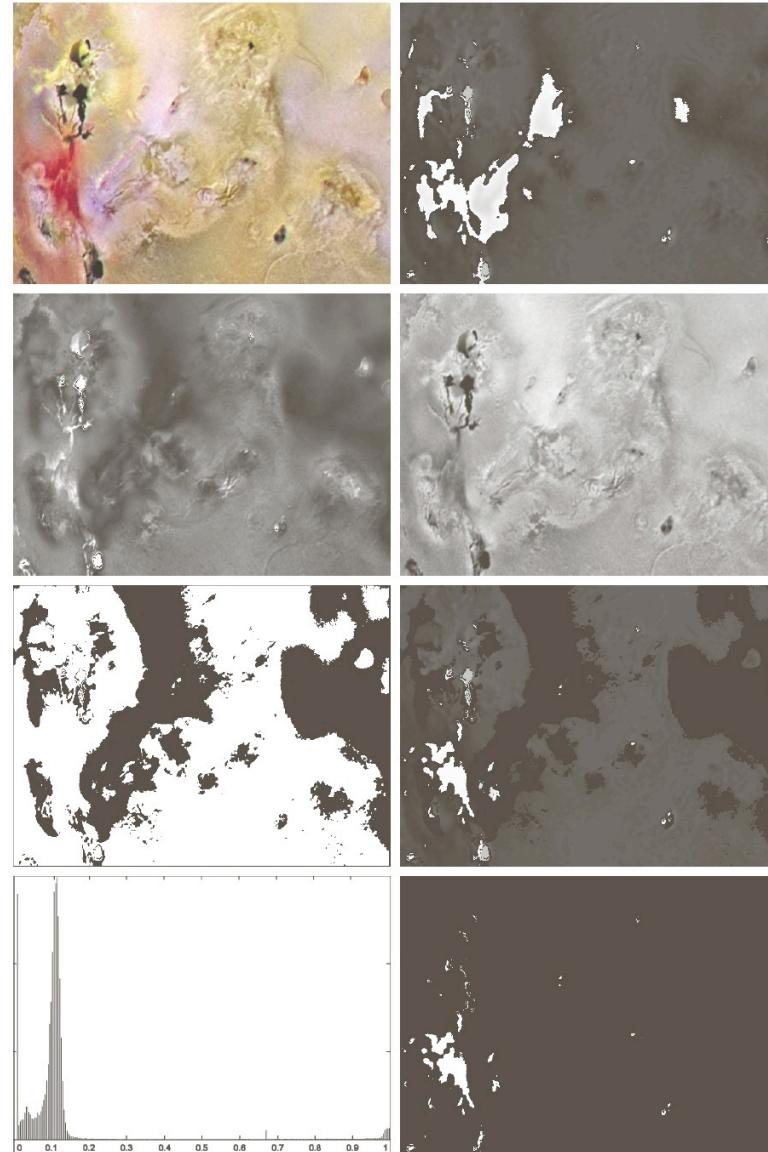


Heavy in yellow

Weak in yellow

# Color Space

- Segmentation in HSI color space (textbook 6.7.1)



a  
b  
c  
d  
e  
f  
g  
h

**FIGURE 6.42** Image segmentation in HSI space. (a) Original. (b) Hue. (c) Saturation. (d) Intensity. (e) Binary saturation mask (black = 0). (f) Product of (b) and (e). (g) Histogram of (f). (h) Segmentation of red components in (a).

# Color Space

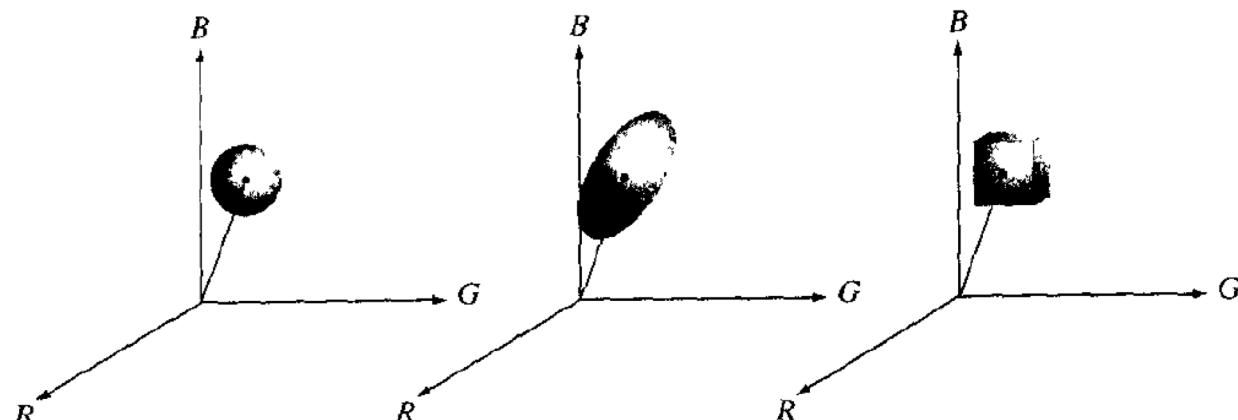
- Segmentation in RGB vector space ( textbook 6.7.2)

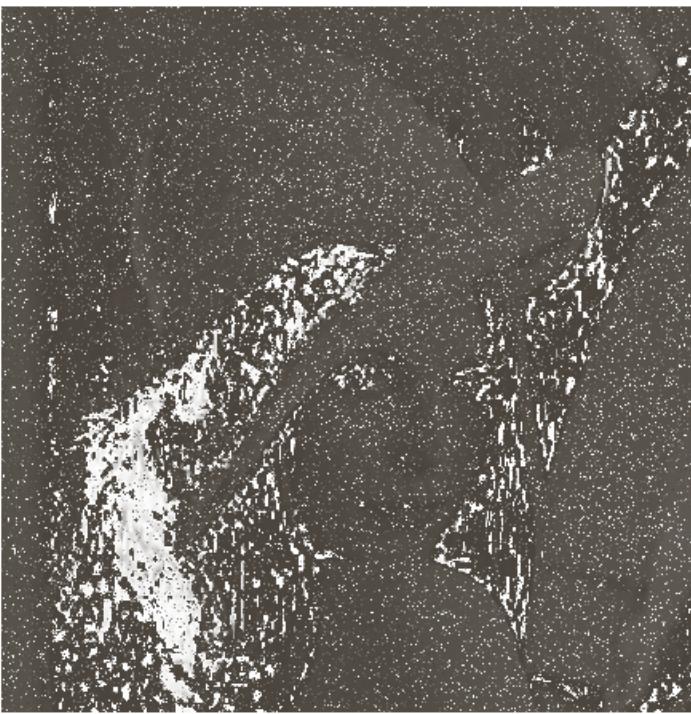
$$\begin{aligned} D(\mathbf{z}, \mathbf{a}) &= \|\mathbf{z} - \mathbf{a}\| \\ &= [(\mathbf{z} - \mathbf{a})^T(\mathbf{z} - \mathbf{a})]^{1/2} \\ &= [(z_R - a_R)^2 + (z_G - a_G)^2 + (z_B - a_B)^2]^{1/2} \end{aligned}$$

$$D(\mathbf{z}, \mathbf{a}) = [(\mathbf{z} - \mathbf{a})^T \mathbf{C}^{-1} (\mathbf{z} - \mathbf{a})]^{1/2}$$

C is the covariance matrix of the samples representative of the color we wish to segment

$$D(\mathbf{z}, \mathbf{a}) \leq D_0$$



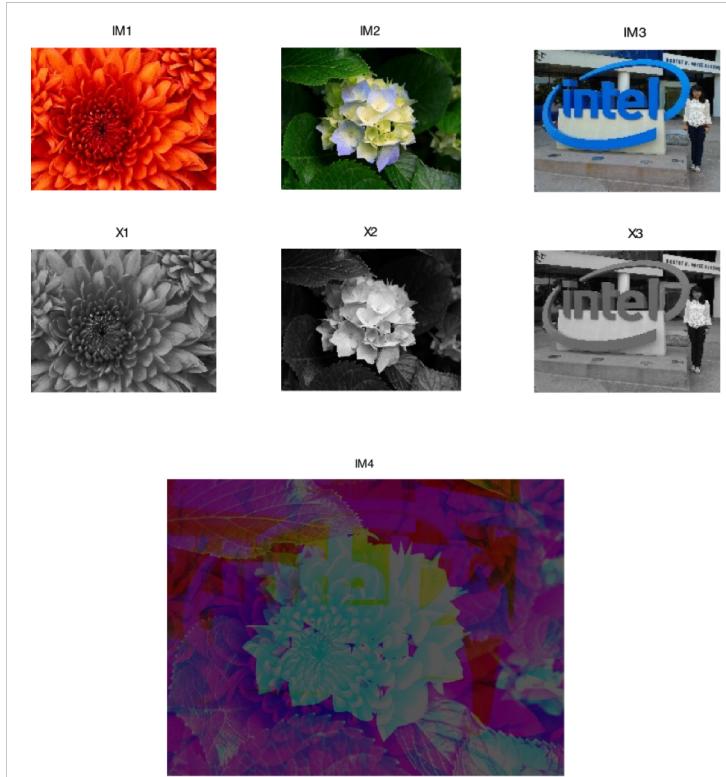


a b  
c d

**FIGURE 6.50** (a) RGB image with green plane corrupted by salt-and-pepper noise.  
(b) Hue component of HSI image.  
(c) Saturation component.  
(d) Intensity component.

# Exercise

- Exercise\_ColorSpace.m
- Creating color image by three different images as R G B components



```
im4 (:,:,1)=X1;  
im4 (:,:,2)=X2;  
im4 (:,:,3)=X3;
```

# Exercise

- Exercise\_ColorSpace.m
- Perform histogram equalization in R G B component of the image

IM4



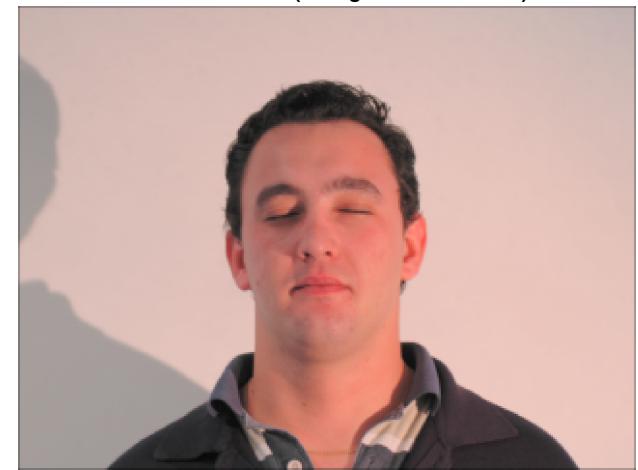
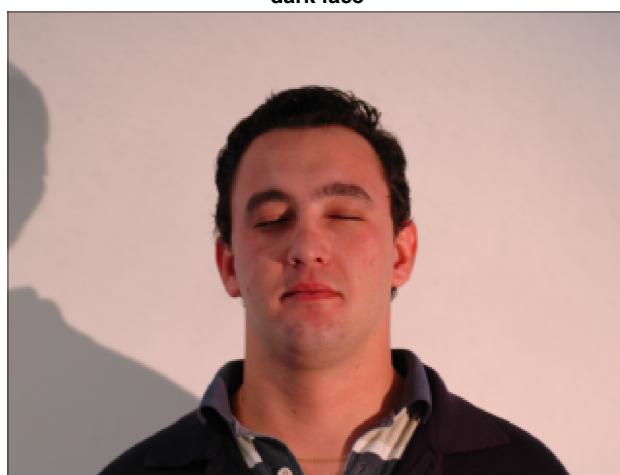
im5



```
Y1=histeq(X1);  
Y2=histeq(X2);  
Y3=histeq(X3);  
  
im5(:,:,:,1)=Y1;  
im5(:,:,:,2)=Y2;  
im5(:,:,:,3)=Y3;
```

# Exercise – image with bad light condition

- Exercise\_ColorSpace\_BackgroundLight.m
- Colorspace.m (function you will need)



# Exercise- skin detection

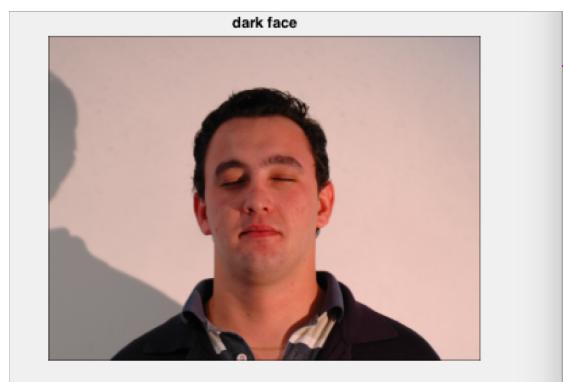
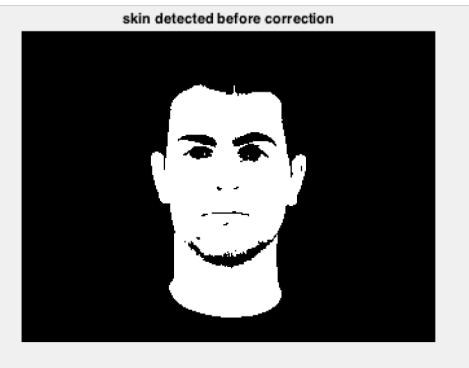
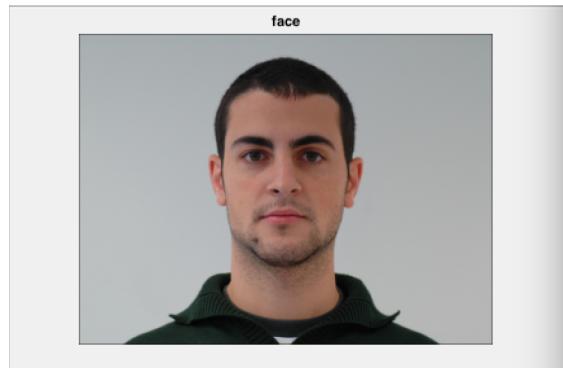
- Paper : Kakumanu, Praveen, Sokratis Makrogiannis, and Nikolaos Bourbakis. "A survey of skin-color modeling and detection methods." *Pattern recognition* 40.3 (2007): 1106-1122.



```
ims1 = (im(:,:,1)>95) & (im(:,:,2)>40) &  
(im(:,:,3)>20);  
ims2 = (im(:,:,1)-im(:,:,2)>15) |  
(im(:,:,1)-im(:,:,3)>15);  
ims3 = (im(:,:,1)-im(:,:,2)>15) &  
(im(:,:,1)>im(:,:,3));  
ims = ims1 & ims2 & ims3;
```

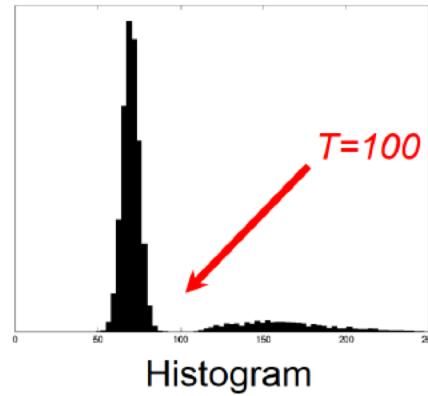
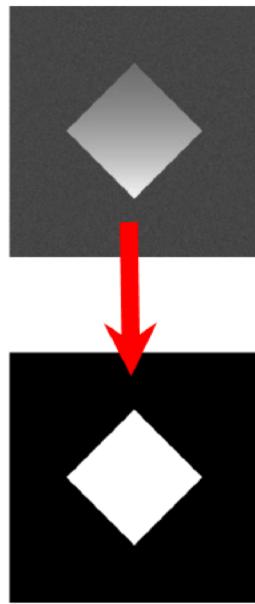
# Assignment 3- skin detection

- A good image and a problematic image



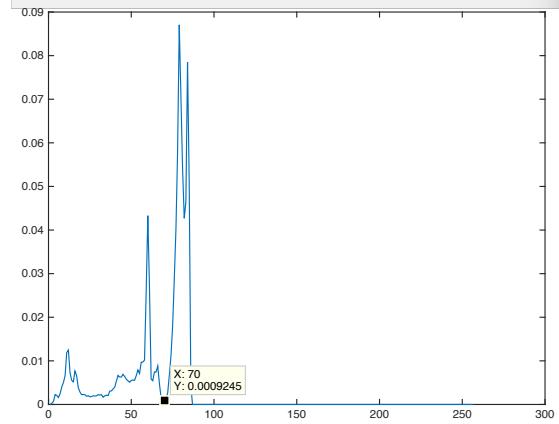
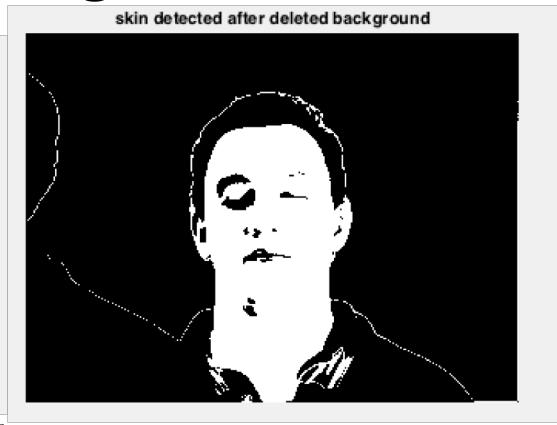
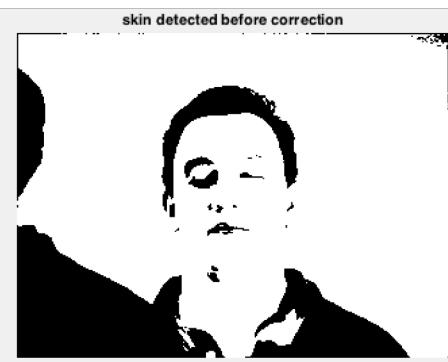
# Assignment 3 -review

## Histogram Applications Choosing a threshold

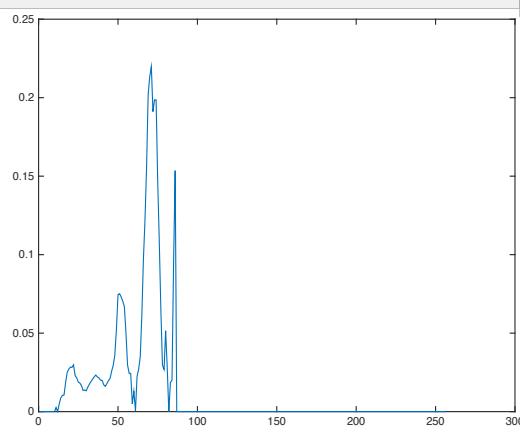


# Assignment 3- skin detection

- A good image and a problematic image



Histogram of the luminance component



Variance of the histogram of the luminance component