# Final RL

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```
[1]: from gym import Env
import gym
import pygame
from gym.spaces import Discrete, Box,Dict
import numpy as np
import random
import matplotlib.pyplot as plt
from IPython.display import clear_output
np.set_printoptions(linewidth=500,threshold=np.inf)
```

#### 0.3 ATC Environment

```
[2]: class AirTraffic():
         def __init__(self,planes:int = 2, grid_size:list = [5,5],radius:int =__
      →2, seed = None, destinations: int =None ):
             self.radius = radius
             self.planes = planes
             self.destinations = destinations
             self.GRID_DIM = grid_size
             self.seed = seed
             self._max_dist = np.sqrt(self.GRID_DIM[0]**2 + self.GRID_DIM[1]**2)
             self._action_to_direction = {
                 0: np.array([-1, 0]),
                 1: np.array([-1, 1]),
                 2: np.array([0, 1]),
                 3: np.array([-1 , -1]),
                 4: np.array([0 , -1]),
             }
             self._ACTIONLOOKUP = {
                 0: 'Up',
                 1: 'front right',
                 2: 'right',
```

```
3: 'front left',
           4: 'left'
           }
       self.GRID_DIM = np.array(self.GRID_DIM)
       self.GRID = np.zeros(self.GRID_DIM)
       self.action_space = Discrete(len(self._ACTIONLOOKUP.keys()))
       self.state_space = Discrete(self.GRID_DIM[0]*self.GRID_DIM[1])
       self._ob_space = {}
       for p in range(self.planes):
           self._ob_space[f'plane{p}'] = Box(np.array([0,0]), np.array([self.
\rightarrow GRID_DIM[0]-1,self.GRID_DIM[1] - 1]), shape=(2,), dtype=int)
           self._ob_space[f'dest{p}'] = Box(np.array([0,0]), np.array([self.
→GRID_DIM[0]-1,self.GRID_DIM[1] - 1]), shape=(2,), dtype=int)
       self.observation_space = Dict(self._ob_space)
       self._agent_location = []
       self._target_location = []
       # Randomly initialize the start points of planes and destinations
       if self.seed is not None:
           np.random.seed(seed = seed)
       for p in range(self.planes):
           while (pc:= [np.random.randint(self.GRID_DIM[0]),np.random.
→randint(self.GRID_DIM[1])]) in self._agent_location:
               continue
           self. agent location.append(pc)
           if self.destinations is None:
               while (dc:=[np.random.randint(self.GRID DIM[0]),np.random.
-randint(self.GRID_DIM[1])]) in self._agent_location + self._target_location:
                   continue
               self._target_location.append(dc)
       if self.destinations is not None:
           for d in range(self.destinations):
               while (dc:=[np.random.randint(self.GRID DIM[0]),np.random.
-randint(self.GRID_DIM[1])]) in self._agent_location + self._target_location:
                   continue
               self._target_location.append(dc)
           extra = np.random.choice(range(len(self._target_location)),self.
→planes-self.destinations)
           for d in extra:
               self._target_location.append(self._target_location[d])
       self._agent_location = np.array(self._agent_location)
       self._target_location = np.array(self._target_location)
       self._count = [0]*self.planes # to check if its already landed/reached_
\rightarrow destination
       self._done_prev = [False]*self.planes
```

```
self._prev_agent_location = self._agent_location.copy()
   def step(self,action):
       self._prev_agent_location = self._agent_location.copy()#### Find the
→vector of agent from destination to find ### reward of terminal state for a_
→plane is 0 and that plane cant move now
       moved_plane = [False]*self.planes
       moved_plane = self._move(action)
       done,reward = self._is_over()
       observation = self._get_obs()
       info = self._get_info()
       self._done_prev = done.copy()
       return observation, reward, done, info
   def move(self, action):
        ##### Find the vector of agent from destination to find
       ### reward of terminal state for a plane is \_todestination and that_{\sqcup}
→plane cant move now
       self._prev_agent_location = self._agent_location
       for plane,act in enumerate(action):
           if np.array_equal(self._agent_location[plane],self.
→_target_location[plane]):
               self. count[plane]+=1
               continue
           elif np.sign(self._target_location[plane]-self.
→_prev_agent_location[plane])[0]<=0:</pre>
               self._agent_location[plane] = np.clip(self.
→_agent_location[plane] + self._action_to_direction[act],[0,0],[self.
\rightarrowGRID_DIM[0] - 1, self.GRID_DIM[1] - 1])
           else:
               self._agent_location[plane] = np.clip(self.
→_agent_location[plane] + -1*self._action_to_direction[act],[0,0],[self.
\hookrightarrow GRID DIM[0] - 1, self.GRID DIM[1] - 1])
       return self._prev_agent_location== self._agent_location
   def _is_over(self):
       done = (self._agent_location==self._target_location).all(axis = 1)
       reward = self._get_reward()
       return done, reward
   def _get_reward(self):
       reward = []
       # reward will be intruder + todestination
       distance, closest_dist ,_1,_2= self._get_info()
       for index,plane in enumerate(range(self.planes)):
           if self. count[plane] >0:
               reward.append(100)## terminating state reward
```

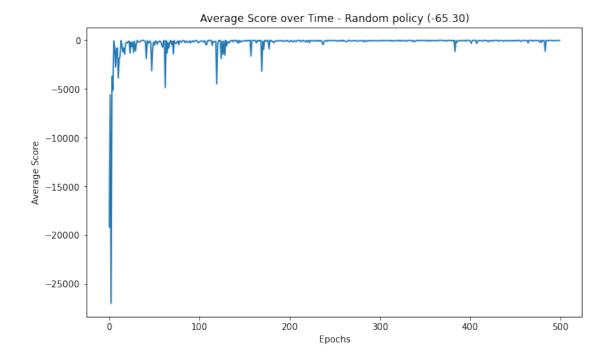
```
else:
               self._intruder = 0
               if closest_dist[plane] <self.radius:</pre>
                   self._intruder = -(self.radius **2 -_
→closest_dist[plane]**2)/(self.radius**2/500)
               self._todestination = 100 - distance[plane]
               reward.append(self. todestination + self. intruder)
       return reward
   def _get_obs(self):
       return {'planes': self._agent_location, 'destinations':self.
→_target_location}
   def _get_info(self):
           closest_dist = []
           distance = []
           plane_theta = []
           plane_rho = []
           dne= self._done_prev
           for index,plane in enumerate(range(self.planes)):
               dist = np.linalg.norm([self._agent_location[plane]]*self.
→planes-self._agent_location,axis = 1)
               dist[plane] = np.inf
               dist[dne] = np.inf
               if dne[plane]:
                   dist += np.inf
                   plane_rho.append(np.inf)
                   plane_theta.append(np.inf)
                   closest_dist .append(np.min(dist))
               else:
                   closest_dist .append(np.min(dist))
                   arg_plane = np.argmin(dist)
                   if (self._prev_agent_location==None).all():
                       self._prev_agent_location = self._agent_location.copy()
                   ownship = self._agent_location[plane]-self.
→_prev_agent_location[plane]
                   intruder = self._agent_location[arg_plane]-self.
→_prev_agent_location[arg_plane]
                   closest_path = self._agent_location[arg_plane]-self.
→_agent_location[plane]
                   y = np.array([intruder[1],ownship[1]])
                   x = np.array([intruder[0],ownship[0]])
                   degree = np.rad2deg(np.arctan2(y,x))
                   deg = degree[1]-degree[0]
```

```
alpha = np.rad2deg(np.arctan2(ownship[1],ownship[1]))
                   beta = np.rad2deg(np.
→arctan2(closest_path[1],closest_path[0]))
                   deg rho = (alpha-beta)
                   plane_rho.append(deg_rho)
                   plane theta.append( deg)
               distance .append(np.linalg.norm(self.
→_target_location[plane]-self._agent_location[plane]))
           return distance, closest_dist, plane_theta, plane_rho
   def _did_collide(self):
       distance,closest_dist,plane_theta,plane_rho = self._get_info()
       collide = np.array(closest_dist).all()
       return collide
   def _state_to_index(self):
       _,closest_dist,plane_theta,plane_rho = self._get_info()
       dis_bin = np.arange(self.radius)
       angle_bins = np.arange(-180, 180, 10)
       dist_index = np.digitize(closest_dist,dis_bin) -1
       theta_index = np.digitize(plane_theta,angle_bins) -1
       rho_index = np.digitize(plane_rho,angle_bins) -1
       return dist_index,theta_index,rho_index
   def _state_in_seq(self):
       seq = []
       for plane in self._agent_location:
           m, n = plane
           seq.append(m * self.GRID.shape[1] + n)
       return seq
   def render(self):
       rend = self.GRID.copy().astype(dtype = 'U2')
       for plane in range(self.planes):
           rend[self._agent_location[plane][0],self._agent_location[plane][1]]_
→= f'p{plane}'
           rend[self._target_location[plane][0],self.
→_target_location[plane][1]] = f'd{plane}'
       return print(rend)
   def reset(self):
       self._agent_location = []
       self._target_location = []
       if self.seed is not None:
           np.random.seed(seed = self.seed)
       for p in range(self.planes):
```

## 0.4 Random Policy Agent

```
[3]: def random_policy(env,episodes):
         action_space ={
             0: np.array([-1, 0]),
             1: np.array([-1, 1]),
             2: np.array([0, 1]),
             3: np.array([-1 , -1]),
             4: np.array([0 , -1]),
         }
         timestep reward = []
         cumsum_reward = []
         cumsum ep= []
         for ep in range(episodes):
             env.reset()
             done = [False] *env.planes
             total_reward = [0]*env.planes
             while (not np.array(done).all()) and env._did_collide() and t<1e6:
                 action = []
                 distance,closest_dist,plane_theta,plane_rh = env._get_info()
                 for plane in range(env.planes):
                     if closest_dist[plane] < env.radius:</pre>
                         action.append(np.random.randint(env.action_space.n))
                     else:
                         if np.array_equal(env._target_location[plane],env.
      →_agent_location[plane]):
                             action.append(0)
                         else:
                             x = np.sign(env._target_location[plane] - env.
      →_agent_location[plane])
                             if x[0] in [0,-1]:
                                  for act,a in enumerate(action_space.values()):
                                      _ = np.array_equal(x,a)
```

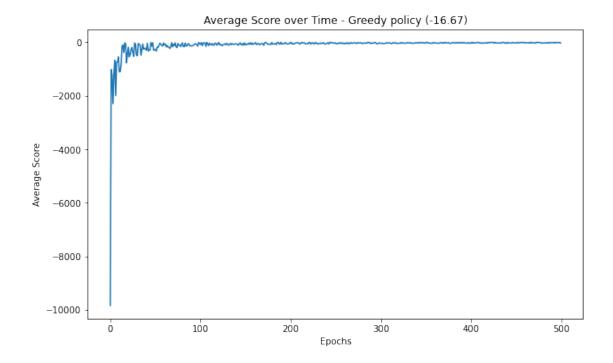
```
if _:
          #
                                            print(_)
                                          action.append(act)
                                          break
                              else:
                                  x = -x
                                  for act,a in enumerate(action_space.values()):
                                      _ = np.array_equal(x,a)
                                      if :
                                          action.append(act)
                                          break
                  t+=1
                  obs,reward,done,info = env.step(action)
                  total_reward= np.add(total_reward,reward)
                  print(t,ep,end=' ')
                  clear_output(wait=True)
              cumsum_reward.append(total_reward/t)
              timestep_reward.append(np.average(total_reward))
              cumsum_ep.append(np.average(total_reward)/(ep+1))
          clear_output()
          return timestep_reward,cumsum_reward,cumsum_ep
 [4]: env = AirTraffic(planes=25,grid_size=[100,100],radius=50,destinations=1)
      episodes = 500
      timestep_reward,cumsum_reward_rand,cumsum_ep_rand = random_policy(env,episodes)
[75]: # cumsum_plane_avg_rand = np.average(cumsum_reward_rand,axis=1)
      plt.figure(figsize = (10,6))
      plt.title(label=f'Average Score over Time - Random policy ({np.
      →average(cumsum_ep_rand[-50:]) :.2f})')
      plt.plot(cumsum ep rand)
      plt.xlabel('Epochs')
      plt.ylabel(f'Average Score')
[75]: Text(0, 0.5, 'Average Score')
```



## 0.5 Greedy Policy Agent

```
[6]: def greedy_policy(env,episodes):
         action_space ={
             0: np.array([-1, 0]),
             1: np.array([-1, 1]),
             2: np.array([0, 1]),
             3: np.array([-1 , -1]),
             4: np.array([0 , -1]),
         }
         timestep_reward = []
         cumsum_reward = []
         cumsum_ep= []
         max_step=1e6
         for ep in range(episodes):
             env.reset()
               print(env._get_obs())
             done = [False] *env.planes
             total_reward = [0]*env.planes
             while (not np.array(done).all()) and env._did_collide() and t<max_step:</pre>
                 action = []
                 for plane in range(env.planes):
```

```
x = np.sign(env._target_location[plane] - env.
       →_agent_location[plane])
                      if x[0] in [0,-1]:
                          for act,a in enumerate(action space.values()):
                              _ = np.array_equal(x,a)
                              if :
          #
                                             print( )
                                  action.append(act)
                                  break
                          else:
                              action.append(0)
                      else:
                          x = -x
                          for act,a in enumerate(action_space.values()):
                              _ = np.array_equal(x,a)
                                  action.append(act)
                                  break
                  t.+=1
                  obs,reward,done,info = env.step(action)
                  total reward= np.add(total reward,reward)
                  print(t,ep,end=' ')
                  clear_output(wait=True)
              cumsum_reward.append(total_reward/t)
              timestep_reward.append(np.average(total_reward))
              cumsum_ep.append(np.average(total_reward)/(ep+1))
              clear_output()
          return timestep_reward,cumsum_reward,cumsum_ep
 [7]: env = AirTraffic(planes=25,grid_size=[100,100],radius=50,destinations=1)
      episodes = 500
      timestep_reward,cumsum_reward_greedy,cumsum_ep_greedy =_
       →greedy_policy(env,episodes)
[76]: plt.figure(figsize = (10,6))
      plt.title(label=f'Average Score over Time - Greedy policy ({np.
       →average(cumsum_ep_greedy[-50:]) :.2f})')
      plt.plot(cumsum_ep_greedy)
      plt.xlabel('Epochs')
      plt.ylabel(f'Average Score')
[76]: Text(0, 0.5, 'Average Score')
```



## 0.6 Multi-Agent SARSA

```
[9]: def ep_greedy(env,Q,count_state,epsilon=0.1):
         dist_index,theta_index,rho_index = env._state_to_index()
         action = []
         for plane in range(env.planes):
             if np.random.random()>epsilon:
      \rightarrow x = (count\_state[dist\_index[plane], theta\_index[plane], rho\_index[plane], :]!=0).
      \rightarrow all()
                  if True :
                      action.append(np.
      argmax(Q[dist_index[plane],theta_index[plane],rho_index[plane],:]))
                  else:
                      axn = np.
      →where(Q[dist_index[plane],theta_index[plane],rho_index[plane],:]==0)[0]
                      action.append(axn[0])
             else:
                  action.append(np.random.randint(env.action_space.n))
         return action
     def Sarsa(env,alpha, gamma, epsilon, episodes,temperature=None):
         cumsum_reward = []
```

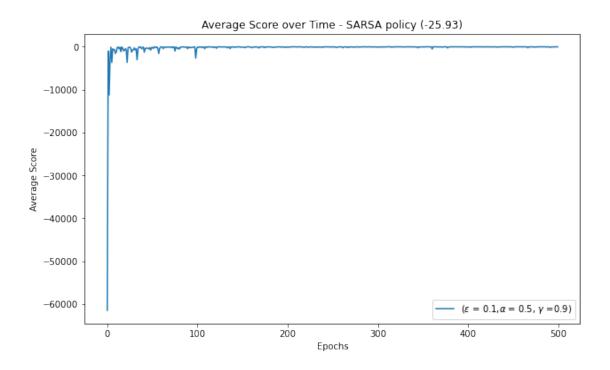
```
count_state = np.zeros_like(Q)
   Q_temp = np.zeros_like(Q)
   for ep in range(episodes):
       env.reset()
       done = [False]*env.planes
       total_reward = [0]*env.planes
       curr_dist_index,curr_theta_index,curr_rho_index = env._state_to_index()
       curr_a = ep_greedy(env,Q,epsilon=epsilon,count_state=count_state)
       while (not np.array(done).all()) and env._did_collide() and t<1.2e4:
           for plane in range(env.planes):
-count_state[curr_dist_index[plane],curr_theta_index[plane],curr_rho_index[plane],curr_a[plane]
           obs, reward, done, info = env.step(curr_a)
           nxt_dist_id,nxt_theta_id,nxt_rho_id = env._state_to_index()
           total_reward= np.add(total_reward,reward)
           next_act = ep_greedy(env,Q,epsilon=epsilon,count_state=count_state)
           t + = 1
           for plane in range(env.planes):
→Q[curr_dist_index[plane],curr_theta_index[plane],curr_rho_index[plane],curr_a[plane]]_
→+= alpha * ( reward[plane] + (gamma *⊔
→Q[nxt_dist_id[plane],nxt_theta_id[plane],nxt_rho_id[plane], next_act[plane]]_
→)
→Q[curr_dist_index[plane],curr_theta_index[plane],curr_rho_index[plane],curr_a[plane]]_
→)
           curr_dist_index,curr_theta_index,curr_rho_index =_
→nxt_dist_id,nxt_theta_id,nxt_rho_id
           curr_a = next_act
           print(t,ep,end=' ')
           clear output(wait=True)
       cumsum_reward.append(total_reward/t)
       timestep reward.append(np.average(total reward))
       cumsum_ep.append(np.average(total_reward)/(ep+1))
       if temperature is not None and ep%temperature==0:
           epsilon = 0.9*epsilon
           print(epsilon)
   clear_output()
   return timestep_reward,cumsum_reward, cumsum_ep
```

## 0.6.1 Constant Temperature SARSA

```
[10]: env = AirTraffic(planes=25,grid size=[100,100],radius=50,destinations=1)
     n_radius,n_theta, n_rho,n_actions = env.radius, 36,36, env.action_space.n
     Q = np.zeros((n_radius,n_theta, n_rho,n_actions))
     alpha = 0.5
     gamma = 0.9
     epsilon = 0.1
     episodes = 500
     cumsum_ep= []
     timestep_reward = []
     timestep_reward,cumsum_reward,cumsum_ep_sarsa = Sarsa(env,alpha, gamma,u
      →epsilon, episodes)
[77]: # cumsum_plane_avg_rand = np.average(cumsum_reward_rand,axis=1)
     plt.figure(figsize = (10,6))
     plt.title(label=f'Average Score over Time - SARSA policy ({np.
      →average(cumsum_ep_sarsa[-50:]) :.2f})')
     plt.plot(cumsum_ep_sarsa, label = r'($epsilon) = '+ f'(epsilon), '+r'(alpha) = __
      plt.xlabel('Epochs')
     plt.ylabel(f'Average Score')
```

## [77]: <matplotlib.legend.Legend at 0x1c7da9c42e0>

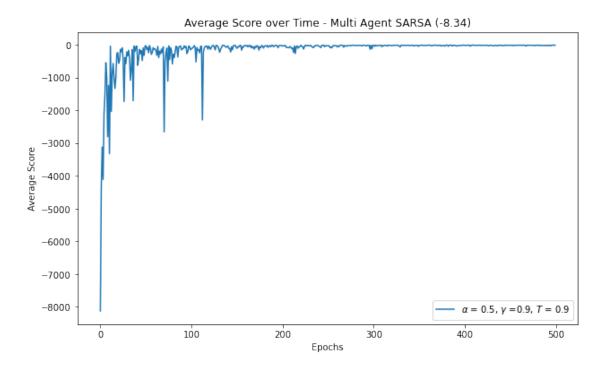
plt.legend()



## 0.6.2 Temperature Controlled Exploration

```
env = AirTraffic(planes=25,grid_size=[100,100],radius=50,destinations=1)
n_radius,n_theta, n_rho,n_actions = env.radius, 36,36, env.action_space.n
Q = np.zeros((n_radius,n_theta, n_rho,n_actions))
alpha = 0.5
gamma = 0.9
epsilon = 0.5
episodes = 500
cumsum_ep= []
timestep_reward = []
temperature = 10
timestep_reward,cumsum_reward,cumsum_sarsa_temp = Sarsa(env,alpha, gamma,u_epsilon, episodes,temperature)
```

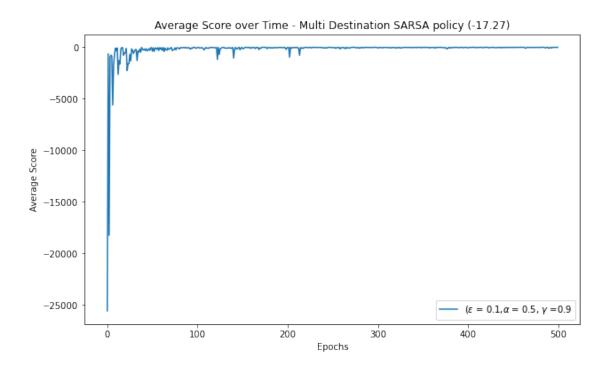
[78]: <matplotlib.legend.Legend at 0x1c7dab0e310>



# 0.7 Multi Agent - Multi Destination SARSA

```
[14]: env = AirTraffic(planes=25,grid_size=[100,100],radius=50)
      n radius, n theta, n rho, n actions = env.radius, 36,36, env.action_space.n
      Q = np.zeros((n_radius,n_theta, n_rho,n_actions))
      alpha = 0.5
      gamma = 0.9
      epsilon = 0.1
      episodes = 500
      cumsum_ep= []
      timestep reward = []
      timestep_reward,cumsum_reward_multi,cumsum_sarsa_multi = Sarsa(env,alpha,_
       →gamma, epsilon, episodes)
[79]: # cumsum_plane_avg_rand = np.average(cumsum_reward_rand,axis=1)
      plt.figure(figsize = (10,6))
      plt.title(label=f'Average Score over Time - Multi Destination SARSA policy ({np.
       →average(cumsum_sarsa_multi[-50:]) :.2f})')
      plt.plot(cumsum_sarsa_multi,label = r'($\epsilon$ = '+ f'{epsilon},'+r'$\alpha$\_
      \rightarrow= ' +f'{alpha}, '+ r'$\gamma$ =' +f'{gamma}')
      plt.xlabel('Epochs')
      plt.ylabel(f'Average Score')
      plt.legend()
```

#### [79]: <matplotlib.legend.Legend at 0x1c7dbca3df0>



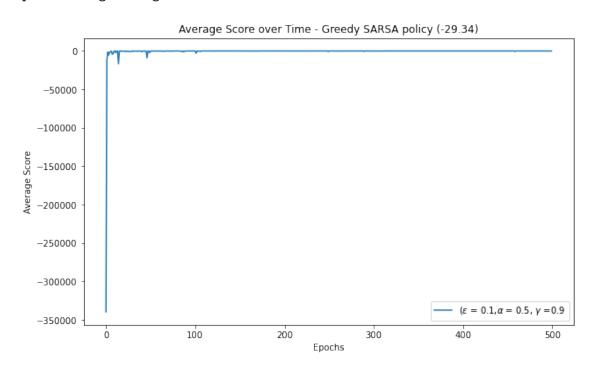
# $0.8 \quad \text{Greedy} + \text{SARSA}$

```
[16]: def Sarsa_policy(env,Q,epsilon,count_state=None):
          action_space ={
              0: np.array([-1, 0]),
              1: np.array([-1, 1]),
              2: np.array([0, 1]),
              3: np.array([-1 , -1]),
              4: np.array([0 , -1]),
          }
          action = []
          Plane = []
          distance,closest_dist,plane_theta,plane_rh = env._get_info()
          dist_index,theta_index,rho_index = env._state_to_index()
            print(closest_dist)
          for plane in range(env.planes):
              if closest_dist[plane] < env.radius:</pre>
                  if np.random.random()>epsilon:
                      action.append(np.
       argmax(Q[dist_index[plane],theta_index[plane],rho_index[plane],:]))
                  else:
                      action.append(np.random.randint(env.action_space.n))
                  Plane.append(plane)
              else:
                  if np.array_equal(env._target_location[plane],env.
       →_agent_location[plane]):
                      action.append(0)
                  else:
                      x = np.sign(env._target_location[plane] - env.
       →_agent_location[plane])
                      if x[0] in [0,-1]:
                          for act,a in enumerate(action_space.values()):
                               _ = np.array_equal(x,a)
                               if _:
                                             print( )
          #
                                   action.append(act)
                                  break
                      else:
                          x = -x
                          for act,a in enumerate(action_space.values()):
                              = np.array_equal(x,a)
                              if _:
                                   action.append(act)
                                  break
            print(Plane)
          return action, Plane
```

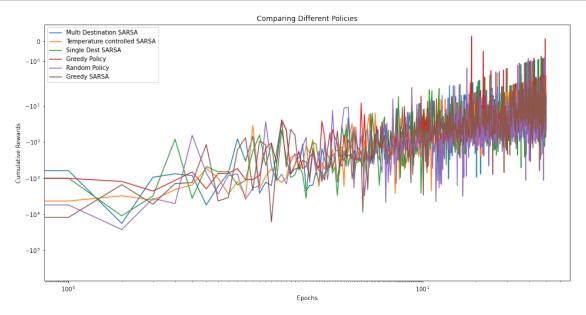
```
def greedy_Sarsa(env,alpha, gamma, epsilon, episodes,temperature=None):
    cumsum_reward = []
    count_state = np.zeros_like(Q)
    Q_temp = np.zeros_like(Q)
    for ep in range(episodes):
        env.reset()
        done = [False] *env.planes
        total reward = [0]*env.planes
        curr_dist_index,curr_theta_index,curr_rho_index = env._state_to_index()
        curr a, curr Planes =
 →Sarsa_policy(env,Q,epsilon=epsilon,count_state=count_state)
        while (not np.array(done).all()) and env._did_collide() and t<1.2e4:</pre>
            obs, reward, done, info = env.step(curr a)
            nxt_dist_id,nxt_theta_id,nxt_rho_id = env._state_to_index()
            total reward= np.add(total reward,reward)
            next_act,nxt_Planes = Sarsa_policy(env,Q,epsilon,count_state=None)
            t+=1
            if len(curr Planes) != 0:
                for plane in curr_Planes:
→Q[curr_dist_index[plane],curr_theta_index[plane],curr_rho_index[plane],curr_a[plane]]_
→+= alpha * ( reward[plane] + (gamma *_
→Q[nxt_dist_id[plane],nxt_theta_id[plane],nxt_rho_id[plane], next_act[plane]])
→Q[curr_dist_index[plane],curr_theta_index[plane],curr_rho_index[plane],curr_a[plane]])
            curr_dist_index,curr_theta_index,curr_rho_index =__
→nxt_dist_id,nxt_theta_id,nxt_rho_id
            curr a = next act
            curr_Planes = nxt_Planes
            print(t,ep,end=' ')
            clear_output(wait=True)
          env.render()
        cumsum_reward.append(total_reward/t)
        timestep_reward.append(np.average(total_reward))
        cumsum_ep.append(np.average(total_reward)/(ep+1))
        if ep\%25 ==0:
            Q_{temp} = Q.copy()
        if temperature is not None and ep%temperature==0:
            epsilon = 0.9*epsilon
            print(epsilon)
    clear_output()
```

#### return timestep\_reward,cumsum\_reward,cumsum\_ep

#### [80]: <matplotlib.legend.Legend at 0x1c7dbd7b910>



```
[71]: plt.figure(figsize = (16,8))
   plt.plot(cumsum_sarsa_multi,label = 'Multi Destination SARSA')
   plt.plot(cumsum_sarsa_temp,label = 'Temperature controlled SARSA')
   plt.plot(cumsum_ep_sarsa, label = 'Single Dest SARSA')
   plt.plot(cumsum_ep_greedy,label = 'Greedy Policy')
   plt.plot(cumsum_ep_rand, label = 'Random Policy')
   plt.plot(cumsum_greedy_sarsa,label = 'Greedy SARSA')
   plt.legend()
   plt.xlabel('Epochs')
   plt.ylabel('Cumulative Rewards')
   plt.title('Comparing Different Policies')
   plt.yscale('symlog')
   plt.semilogx(base = 100)
   plt.show()
```



[]: