Artificial Intelligence(Adversarial Search)

By:

Amna Sajid

Outline

Last Class

- Beyond Classical Search
- Types of Problems
- Optimization problems
- Local Search Algorithms
 - Hill Climbing
 - Hill climbing features
 - Hill climbing Problems
 - Hill Climbing variants

Today

- Adversarial Search
- Formalization of the problem
- Game Tree
- Mini Max Algorithm
- Alpha-beta Pruning

Single Agent environment

- Until now, we have discussed single agent environment
 - only one person or agent searching the solution space to find the goal or the solution.
 - often expressed in the form of a sequence of actions
- There might be some situations where more than one agent/person is searching for the solution in the same search space
 - usually occurs in game playing where two opponents (adversaries) are searching for a goal.
 - Multi-agent environment

Multi-agent environment

- The environment with more than one agent
- Each agent is an opponent of other agent and playing against each other
- Each agent needs to consider the action of other agent and effect of that action on their performance.

Adversarial Search

- Adversarial Search
 - Searches in which two or more players with conflicting goals are trying to explore the same search space for the solution
 - often known as Games
- For example, in a game of tic-tac-toe player one might want that he should complete a line with crosses while at the same time player two wants to complete a line of zeros

Types of Games in Al

	Deterministic	Chance Moves
Perfect information	Chess, Checkers, go, Othello	Backgammon, monopoly
Imperfect information	Battleships, blind, tic-tac-toe	Bridge, poker, scrabble, nuclear war

Perfect information

- A game in which agents can look into the complete board.
- Agents have all the information about the game, and they can see each other moves also.
- Examples are Chess, Checkers, Go, etc.

Imperfect information

- A game in which agents do not have all information about the game and not aware with what's going on,
- Examples are tic-tac-toe, Battleship, blind, Bridge, etc.

Deterministic games

- Those games which follow a strict pattern and set of rules for the games, and there is no randomness associated with them.
- Examples are chess, Checkers, Go, tic-tac-toe, etc.

Non-deterministic games

- Those games which have various unpredictable events and has a factor of chance or luck.
- This factor of chance or luck is introduced by either dice or cards. These are random, and each action response is not fixed.
- Also called as stochastic games.
- Example: Backgammon, Monopoly, Poker, etc.

Zero-Sum Game

- Adversarial search which involves pure competition.
- Each agent's gain or loss of utility is exactly balanced by the losses or gains of utility of another agent.
- One player of the game try to maximize one single value, while other player tries to minimize it.
- Each move by one player in the game is called as **ply**.
- Example:
 - Chess and tic-tac-toe.

Formalization of the problem

• A game can be defined as a type of search in AI which can be formalized of the following elements:

Initial state

• It specifies how the game is set up at the start.

Player(s)

• It specifies which player has moved in the state space.

Action(s)

• It returns the set of legal moves in state space.

Result(s, a)

• It is the transition model, which specifies the result of moves in the state space.

Terminal-Test(s)

- The state where the game ends is called terminal states.
- Terminal test is true if the game is over, else it is false at any case.

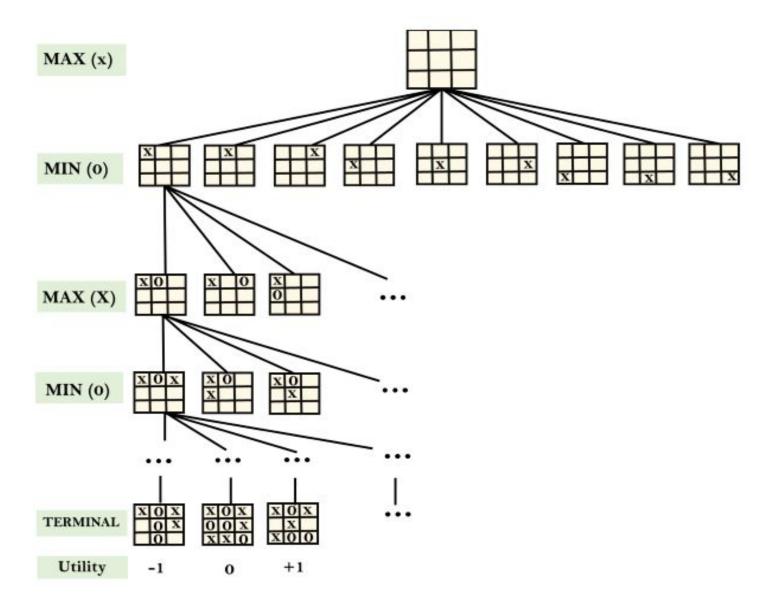
Utility(s, p)

- A utility function gives the final numeric value for a game that ends in terminal states s for player p. It is also called payoff function. (Reward after winning the game)
- For Chess, the outcomes are a win, loss, or draw and its payoff values are +1, 0, $\frac{1}{2}$. And for tic-tac-toe, utility values are +1, -1, and 0

Game tree

• A game tree is a tree where nodes of the tree are the game states and Edges of the tree are the moves by players.

Tic-Tac-Toe game tree

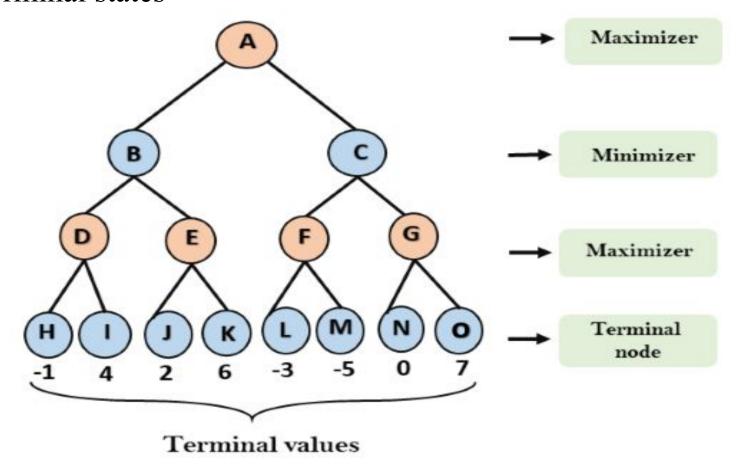


Mini-Max Algorithm

- A recursive or **backtracking** algorithm
 - The algorithm proceeds all the way down to the terminal node of the tree, compare the values and backtrack the tree to root node to decide the move.
- Performs a depth-first search algorithm for the exploration of the complete game tree.
 - Why not BFS??
- Best Move strategy used
 - Both players will adopt best move to not allow the opponent to win
- Computes the minimax decision for the current state
 - Max will try to maximize its utility (Best move)
 - Min will try to minimize the utility (Worst move)

Working of Min-Max Algorithm

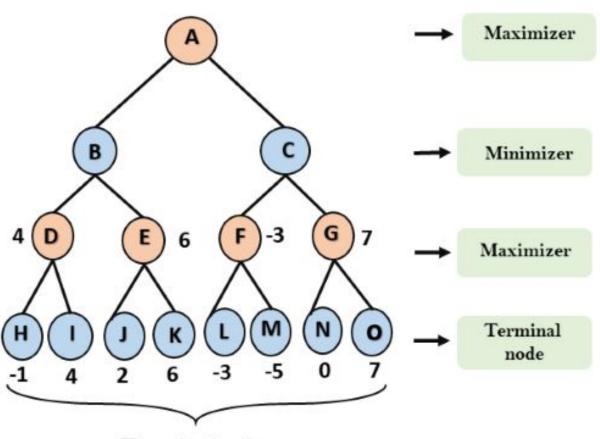
• In the first step, the algorithm generates the entire game-tree and applies the utility function to get the utility values for the terminal states



- Step 1
 - let's take A is the initial state of the tree. Suppose maximizer takes first turn (normally max takes first move)
 - Then min will take second move and then again max, so on
- Step2
 - Start from terminal values, and find utilities for the maximizer by comparing the values of terminal nodes

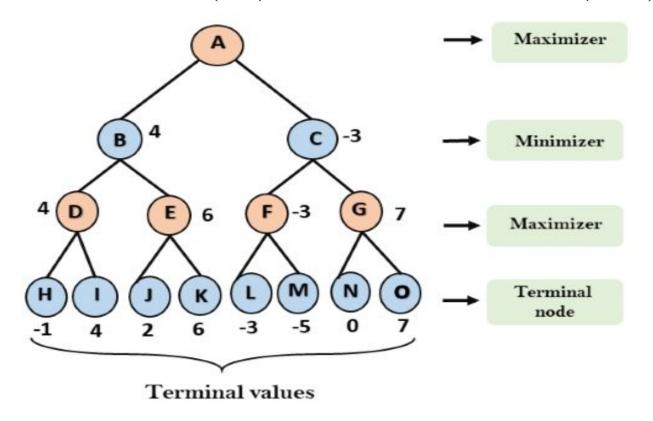
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For node D max(-1,4)=4
For Node E max(2, 6)=6
For Node F max(-3,-5)=-3
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For node G max(0, 7) = 7

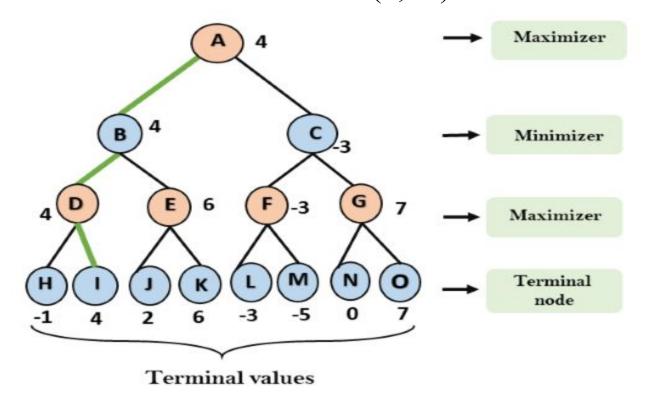


Terminal values

- Step 3
 - In the next step, it's a turn for minimizer
 - it will compare all nodes value, and will find the min values. For node B= min(4,6) = 4 For node C= min(-3, 7) = -3

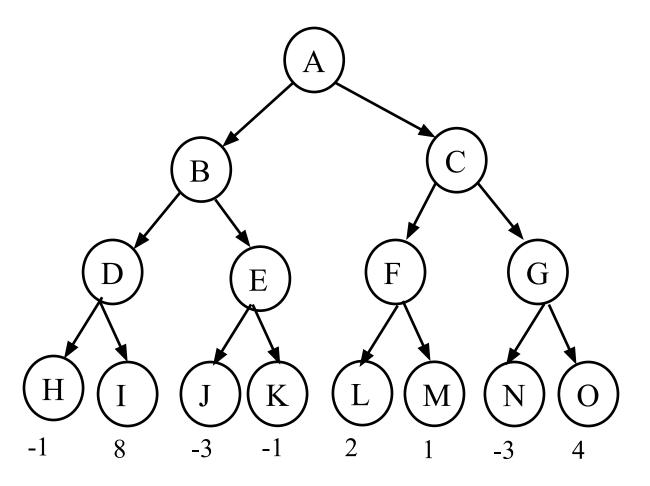


- Step 4
- Now it's a turn for Maximizer, and it will again choose the maximum of all nodes value and find the maximum value for the root node. i.e. For node A max(4, -3)= 4



• So, if max follows A->B->D->I, it will definitely win with the utility of 4.

Task



Performance Measurement

Complete ?

• YES, It will definitely find a solution (if exist), in the finite search tree.

Optimal ?

• YES, if both opponents are playing optimally

Time ?

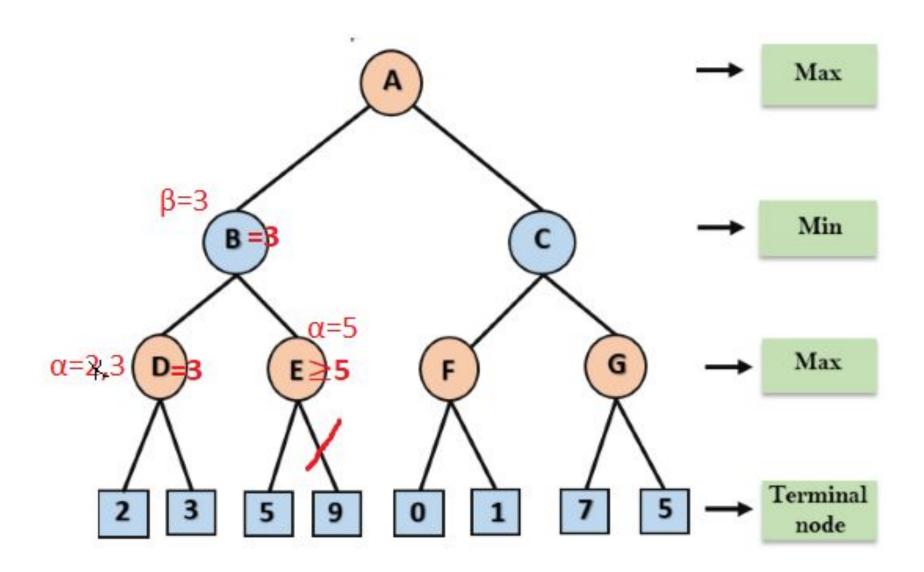
• The worst case time complexity is $O(b^d)$. Simply O(n)

• Space?

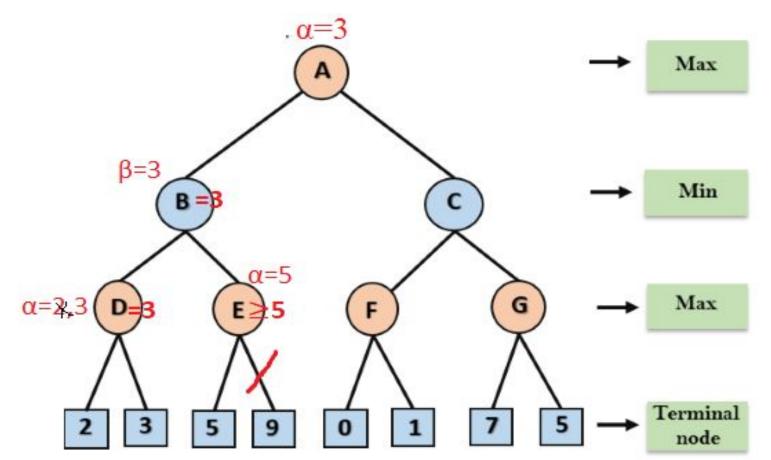
• The worst case space complexity is $O(b^d)$.

Limitation of the minimax Algorithm

- The main drawback of the minimax algorithm is that it gets really slow for complex games such as Chess, go, etc.
- This type of games has a huge branching factor, and the player has lots of choices to decide
 - Traversing becomes complex
- Solution
 - alpha-beta pruning to reduce the tree and increase efficiency

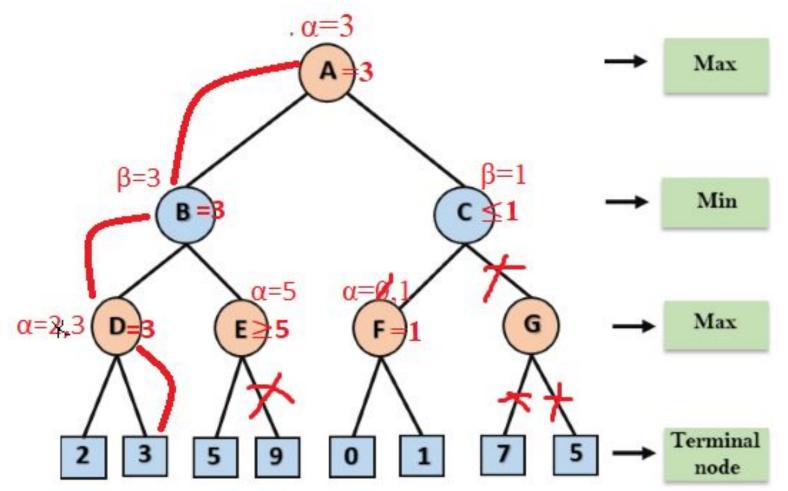


- Step 4: now at node A, α will get value of 3. as its turn of max, so value of A will be ≥ 3 .
- Here any other path that will give value less than 3 will be pruned.



- Step 5:Now, node C from right side will be traversed, which will go downward to F and F will get value of 0 for α . As it s turn of Max so value for F will be ≥ 0 . right successor of F has value 1, so α value be updated with 1 and F will get max value of 1.
- Step 6: F will return value of 1 to β at node C. as its turn of Min and value of C will be ≤ 1 , whereas node A already has max value of 3, so another value generated after traversing nodes further will return value ≤ 1 . Therefore, no need to explore further and right complete branch of C will be pruned.
- A will retain utility value of 3 i.e. optimal value for maximizer.

• So, So, if max follows A->B->D->I, it will definitely win with the utility of 3.



Complexity

• Complexity is dependent on traversal ordering of nodes. It can be of two types:

Worst ordering

- In some cases, alpha-beta pruning algorithm does not prune any of the leaves of the tree, and works exactly as minimax algorithm.
- In this case, the best move occurs on the right side of the tree and it also consumes more time because of alpha-beta factors.
- The time complexity for such an order is $O(b^d)$.

Ideal ordering:

- The ideal ordering for alpha-beta pruning occurs when lots of pruning happens in the tree, and best moves occur at the left side of the tree.
- We apply DFS hence, it first search left of the tree and go deep twice as minimax algorithm in the same amount of time.
- Complexity in ideal ordering is $O(b^{d/2})$.

Task

Find the best path and optimal value for Max using alpha-beta pruning.

