

Lab 2 Conversions Base 2, 8, 10, 16

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* 0.25 Base 10 to Base 2, 8, 16

$$\begin{aligned} 0.25_{10} &\rightarrow 0.25 \times 2 = 0.5 \mid 0 \\ &\quad 0.5 \times 2 = 1.0 \mid 1 \downarrow \\ &\rightarrow \boxed{0.01_2} \end{aligned}$$

$$\begin{aligned} 0.25_{10} &\rightarrow 0.25 \times 8 = 2.0 \\ &\rightarrow \boxed{0.2_8} \end{aligned}$$

$$\begin{aligned} 0.25_{10} &\rightarrow 0.25 \times 16 = 4.0 \\ &\rightarrow \boxed{0.4_{16}} \quad [\text{Let check: } 4 \times 16^{-1} = \frac{4}{16} = \frac{1}{4} = \underline{0.25_{10}}] \end{aligned}$$

* 0.25 Base 8 to Base 2, 10, 16

$$\begin{aligned} 0.25_8 &\rightarrow 0.2 \ 5 \text{ (convert each octal digit to 3 binary digit)} \\ &\quad 00.010 \ 101 \\ &\rightarrow \boxed{00.010101_2} \end{aligned}$$

$$0.25_8 \rightarrow 2 \times 8^{-1} + 5 \times 8^{-2} = \frac{2}{8} + \frac{5}{64} = \frac{21}{64} = \boxed{0.328125_{10}}$$

$$\begin{aligned} 0.25_8 &\rightarrow 0.2 \ 5 \\ &\rightarrow 0.010 \ 101 \text{ (first convert 3 binary digit)} \\ &\rightarrow 0.01010100 \\ &\rightarrow \boxed{0.54_{16}} \end{aligned}$$

$$\begin{aligned} \text{Let check: } &5 \times 16^{-1} + 4 \times 16^{-2} \\ &= \frac{5}{16} + \frac{4}{256} \\ &= \frac{84}{256} = 0.328125_{10} \end{aligned}$$

* 0.25 Base 16 to Base 2, 8, 16

$$\begin{aligned} 0.25_{16} &\longrightarrow 0.2 \ 5 \text{ (convert each hex digit to 4} \\ &\longrightarrow 000.0010 \ 0101 \text{ binary digit)} \\ &\longrightarrow \boxed{000.00100101_2} \end{aligned}$$

$$\begin{aligned} 0.25_{16} &\longrightarrow 0.2 \ 5 \\ &\longrightarrow 0.0010 \ 0101 \text{ (first convert to 4 Binary digit)} \\ &\longrightarrow 0.001 \ 001 \ 010 \text{ (then convert 3 binary digit to} \\ &\longrightarrow \boxed{0.112_8} \text{ octal)} \end{aligned}$$

$$\begin{aligned} 0.25_{16} &\longrightarrow 2 \times 16^{-1} + 5 \times 16^{-2} = \frac{2}{16} + \frac{5}{256} = \frac{37}{256} \\ &= 0.14453125_{10} \\ 0.14453125 \times 16 &= 2.3125 \quad \begin{array}{c|c} 2 & \downarrow \\ \hline & 5 \end{array} \\ 0.3125 \times 16 &= 5.0 \\ 0.14453125_{10} &\longrightarrow \boxed{0.25_{16}} \end{aligned}$$

* 0.1101 Base 2 to Base 2, 10, 16

$$\begin{aligned} 0.1101_2 &\longrightarrow 1 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3} + 1 \times 2^{-4} = \frac{1}{2} + \frac{1}{4} + \frac{1}{16} \\ &= \frac{13}{16} = \boxed{0.8125_{10}} \end{aligned}$$

$$\begin{aligned} 0.8125 \times 2 &= 1.625 \quad \begin{array}{c|c} 1 & \downarrow \\ \hline & 1 \end{array} \\ 0.625 \times 2 &= 1.25 \quad \begin{array}{c|c} 1 & \downarrow \\ \hline & 0 \end{array} \\ 0.25 \times 2 &= 0.5 \quad \begin{array}{c|c} 0 & \downarrow \\ \hline & 1 \end{array} \\ 0.5 \times 2 &= 1.0 \quad \begin{array}{c|c} 1 & \downarrow \\ \hline & \end{array} \\ 0.8125_{10} &\longrightarrow \boxed{0.1101_2} \end{aligned}$$

$$\begin{aligned} 0.1101_2 &\longrightarrow 0.1101 \text{ (convert every 4 Binary digit} \\ &\longrightarrow 0.1101 \text{ to hex digit)} \\ &\longrightarrow 0.13 \\ &\longrightarrow \boxed{0.D_{16}} \end{aligned}$$