

Lab 4 conversion

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Q 0.125₁₀ convert to both NASA and IEEE 754 format

$$0.125_{10} \rightarrow 0.2_{16} \rightarrow 0.0010_2$$

$$0.125 \times 16 = 2 \rightarrow 0.0010 \times 2^0$$

Key Binary NASA float: 0.1 × 2⁻² → 2's complement

$$\begin{array}{r} 00000010 \\ 11111101 \\ \hline 11111110 \end{array}$$

$$\begin{array}{cccccccc} 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ \hline 4 & 0 & & 0 & 0 & & 0 & 0 \end{array} \quad \begin{array}{cccccccc} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \hline & & & & & & & \end{array} \quad \begin{array}{cccccccc} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \hline & & & & & & & \end{array} \quad \begin{array}{cccccccc} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 \\ \hline & & & & & & & \end{array}$$

Exponent
F E

[Now convert to IEEE 754]

$$0.1 \times 2^{-2} = \underline{1.0 \times 2^{-3}} \rightarrow \text{bias by 127}$$

the exponent -3 becomes 127-3 = 124

$$\begin{array}{cccccccc} 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 \\ \hline 3 & E & & 0 & 0 & & 0 & 0 \end{array} \quad \begin{array}{cccccccc} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \hline & & & & & & & \end{array} \quad \begin{array}{cccccccc} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \hline & & & & & & & \end{array} \quad \begin{array}{cccccccc} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \hline & & & & & & & \end{array}$$

sign

Q 0.3₁₀ convert to both NASA and IEEE 754 format

$$0.3_{10} \rightarrow 0.4_{16} \rightarrow 0.4_{16} \rightarrow 0.01001100_2$$

$$0.3 \times 16 = 4.8$$

$$0.8 \times 16 = 12.8$$

$$0.8 \times 16 = 12.8$$

Key binary NASA float: 0.1001100 × 2⁻¹ → 2's complement

$$\begin{array}{r} 00000001 \\ 11111110 \\ \hline 11111111 \end{array}$$

$$\begin{array}{cccccccc} 0 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ \hline 4 & e & & e & & e & & e \end{array} \quad \begin{array}{cccccccc} 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ \hline & & & & & & & \end{array} \quad \begin{array}{cccccccc} 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 \\ \hline & & & & & & & \end{array} \quad \begin{array}{cccccccc} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ \hline & & & & & & & \end{array}$$

EXP
F F

[Now convert to IEEE 754]

$$0.1001100 \times 2^{-1} = \underline{1.001100} \times 2^{-2} \rightarrow \text{bias by 127, exponent becomes } (127-2) = 125$$

$$\begin{array}{cccccccc} 0 & 0 & 1 & 1 & 1 & 1 & 1 & 0 \\ \hline 3 & E & & 9 & 9 & & 9 & 9 \end{array} \quad \begin{array}{cccccccc} 1 & 0 & 0 & 1 & 1 & 0 & 0 & 1 \\ \hline & & & & & & & \end{array} \quad \begin{array}{cccccccc} 1 & 0 & 0 & 1 & 1 & 0 & 0 & 1 \\ \hline & & & & & & & \end{array} \quad \begin{array}{cccccccc} 1 & 0 & 0 & 1 & 1 & 0 & 0 & 1 \\ \hline & & & & & & & \end{array}$$

sign

A (rounding up)

Final result:

Base 10	NASA Hex format	IEEE 754 Hex format
0.125	400000FE	3E000000
0.3	4ccccceff	3E99999A