

FIR System Identification

You need to model an unknown FIR system. You have placed a random noise signal, \mathbf{x} , at the input of the system and observed the resulting signal, \mathbf{y} . All that is known about the FIR system is that it is **9 points long**. This means the **order Q is 8**.

Since it is an FIR system, $A(z) = 1$ and the order of $\mathbf{A}(z)$ is $\mathbf{P} = 0$. This also means you will need to modify the **system identification code** so that \mathbf{D} is now $\mathbf{D} = \mathbf{X}$ and the estimate of the **B coefficients** is the **theta** result.

Estimate the **impulse response, h**, of this system.

The signals, \mathbf{x} and \mathbf{y} , are in the file FIRSystemIDHwk.

Turn in your Matlab code and your estimated \mathbf{h} values (numbers, not a plot).

Solution:

Since $H(z) = \frac{B(z)}{A(z)}$ and $A(z) = 1$, $H(z) = B(z)$.

We also have

$$\sum_{n=-\infty}^{\infty} h[n]z^{-n} = h[0] + h[1]z^{-1} + \dots + h[n]z^{-n} = B(z) = b_0 + b_1z^{-1} + \dots + b_nz^{-n}$$

Then impulse response $h[n]$ coefficients are simply coefficients of $B(z)$, we don't have to do the Inverse Z-transform of the system's frequency response $H(z)$.

Matlab Code:

```
% This is similar to AR signal but we observe both the input x (Q-order) and
% output y (P-order)
load('FIRSystemIDHwkData.mat')
N=length(x);
P = 0; % A has 0 order
Q = 8;
L = max(P,Q);
yvec= y((L+1):N);
xFirstCol = x((L+1):N);
xFirstRow = x((L+1):(-1):(L-Q+1));
X=toeplitz(xFirstCol,xFirstRow);
% since we are doing FIR system ID, we ignore
Y=toeplitz(yFirstCol,yFirstRow);
D=X;
theta = pinv(D)*yvec;
A=1;
B=theta
```

```
>> FIRSystemID
```

```
B =
```

```
    1.0000  
   -2.0000  
    3.0000  
   -4.0000  
    5.0000  
    4.0000  
    3.0000  
    2.0000  
    1.0000
```

```
fx >>
```