

# Lowpass / Bandpass filter design

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EECE5356 – Digital Signal Processing

## 1. Butterworth filter

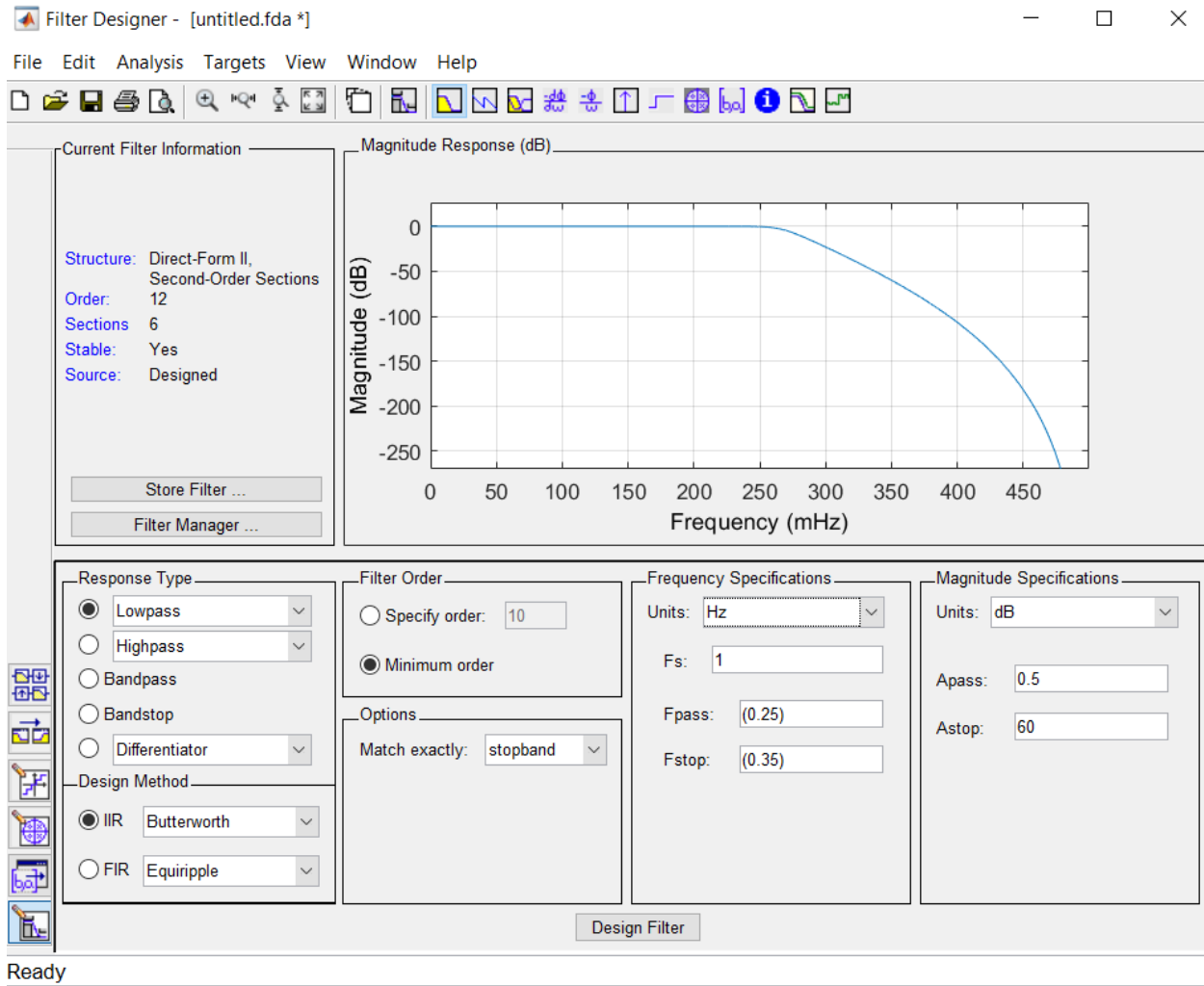


Figure 1. Butterworth filter and specs. Order: **12**. Since there are no ripples, passband must match exactly -0.5dB, and stopband must match exactly -60dB.

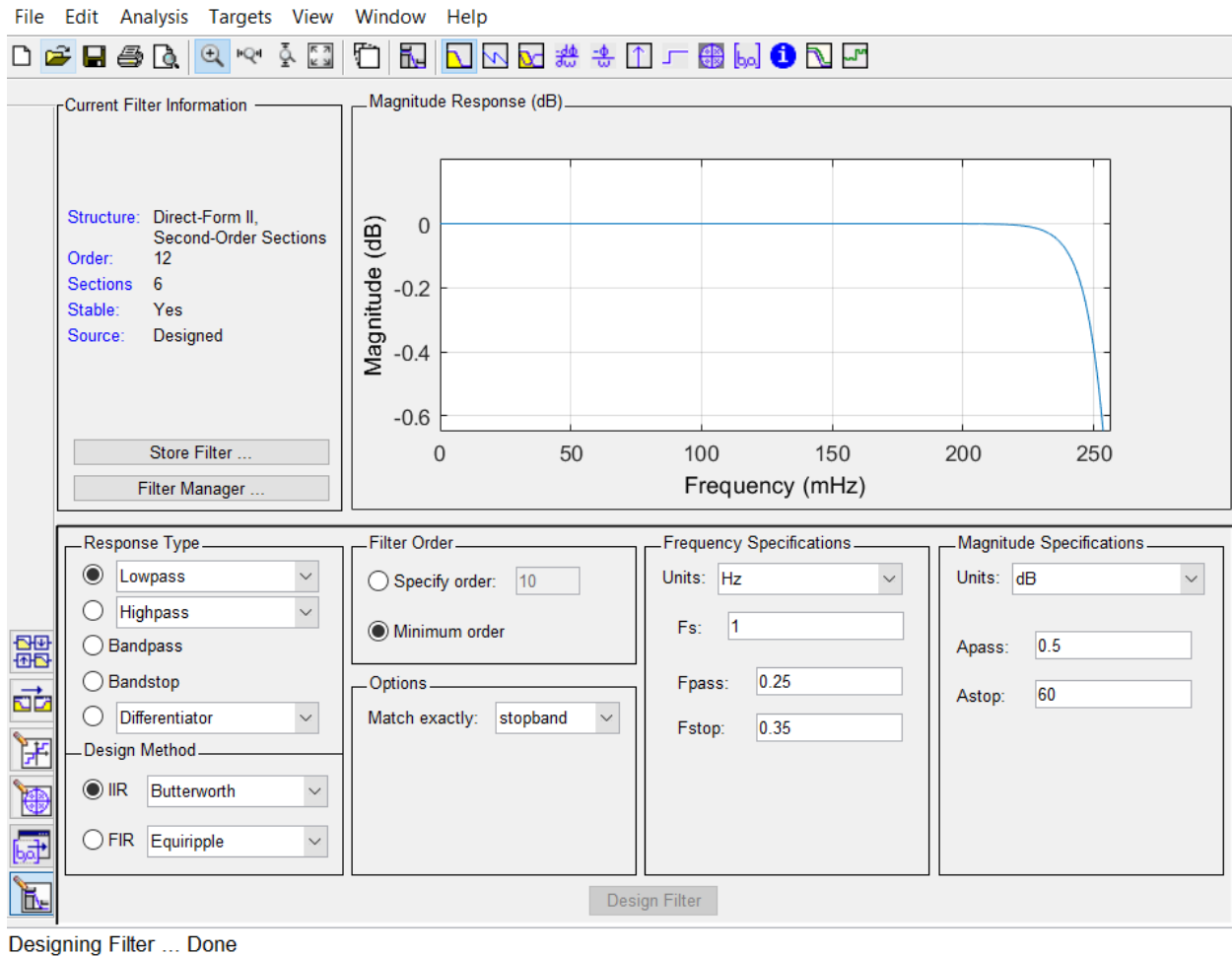


Figure 2. Butterworth filter zoomed-in at passband. Magnitude within  $\pm 0.5$  dB at 0.25Hz

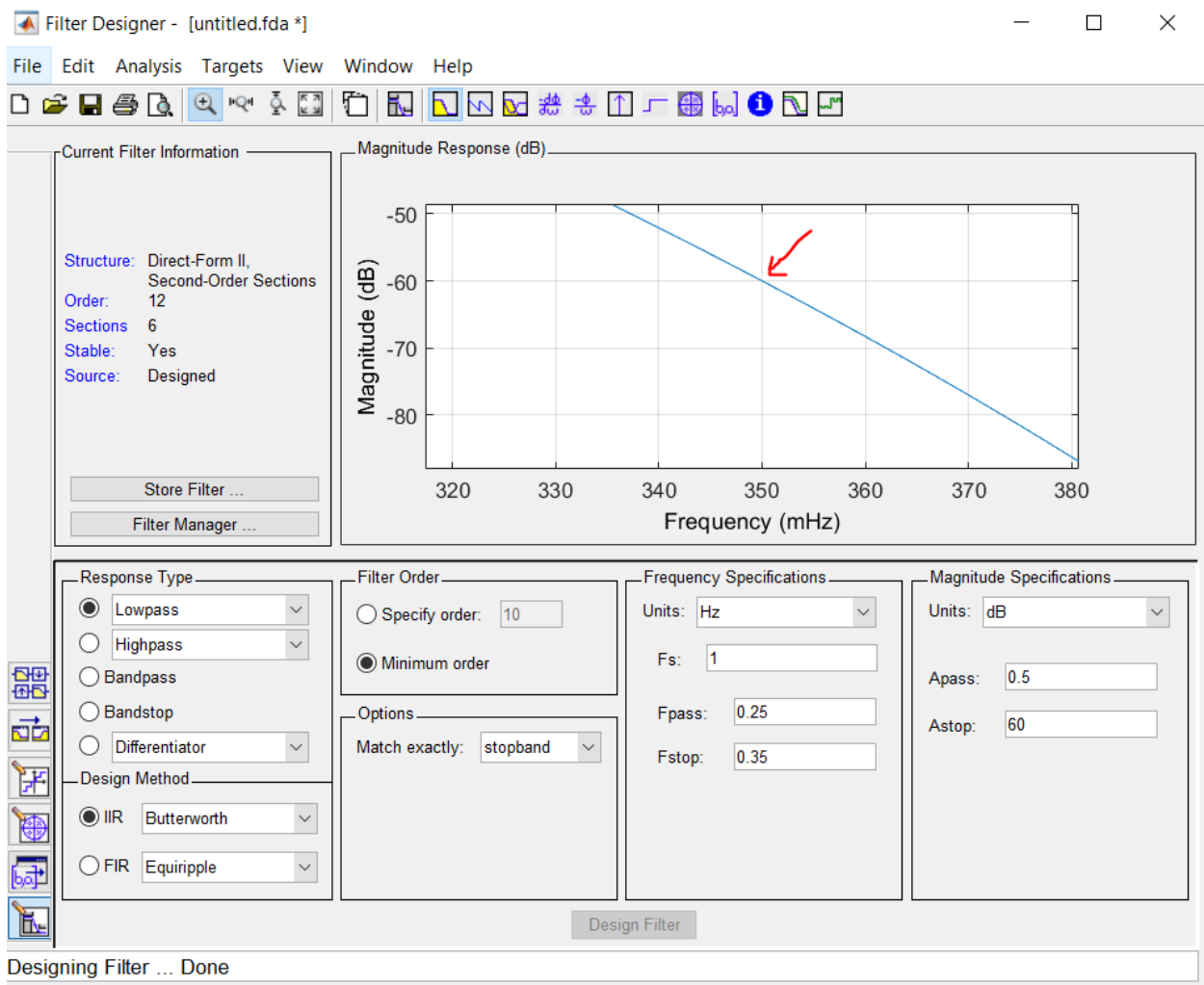


Figure 3. Butterworth filter zoomed-in at stop band. Magnitude 60dB at 0.35Hz.

```
>> bwB
bwB =
    0.0016    0.0193    0.1059    0.3529    0.7941    1.2706    1.4823    1.2706    0.7941    0.3529    0.1059    0.0193    0.0016

>> bwA
bwA =
    1.0000    0.7501    1.8627    1.0152    1.1299    0.4384    0.2728    0.0717    0.0254    0.0041    0.0007    0.0001    0.0000
```

Figure 4. Coefficients bwB for numerator, bwA for denominator.

## 2. Elliptic filter

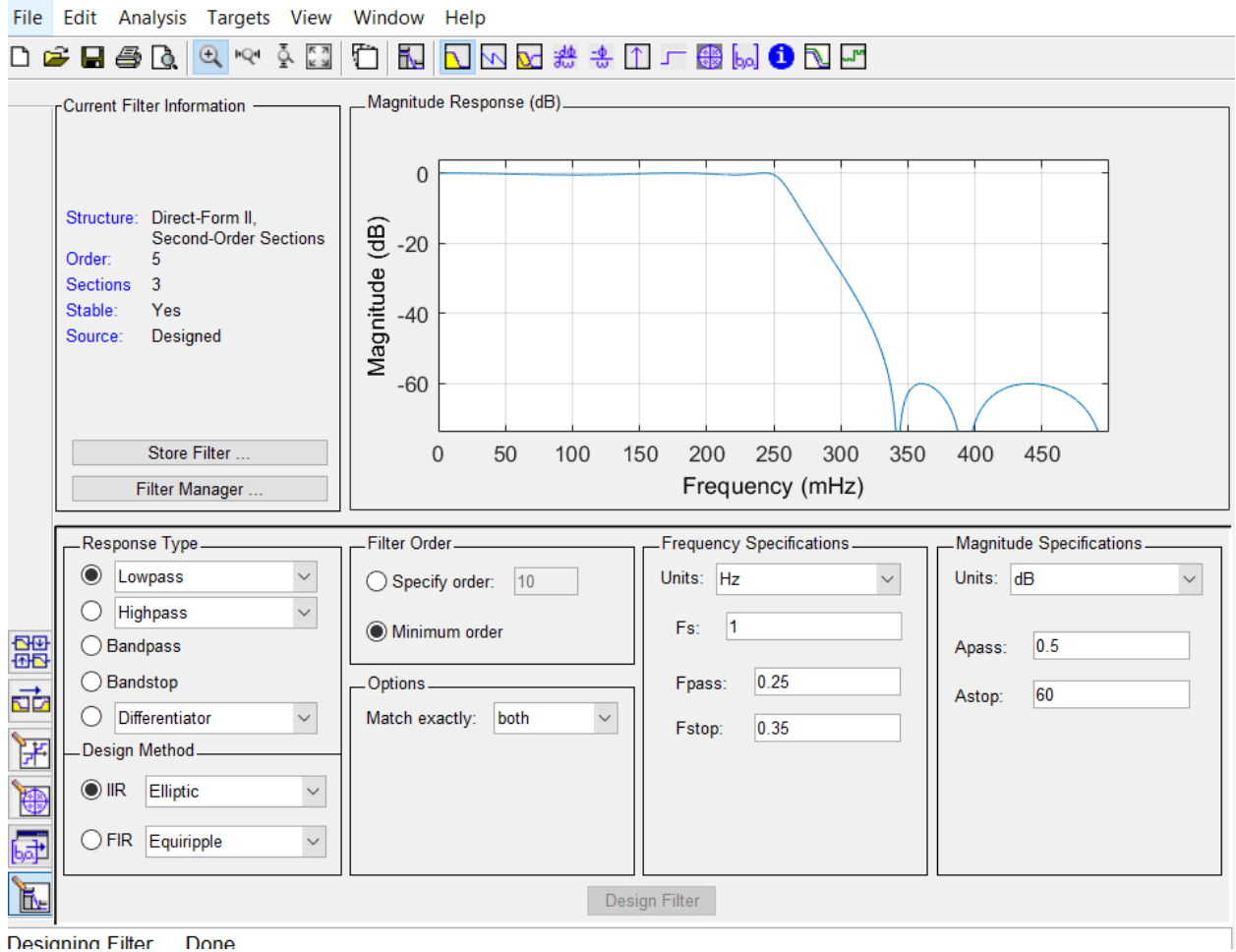


Figure 5. Elliptic filter and specs. Order: 5. Since there are ripples, passband must be within 0 to -0.5dB, and stopband max peaks must be less than -60dB.

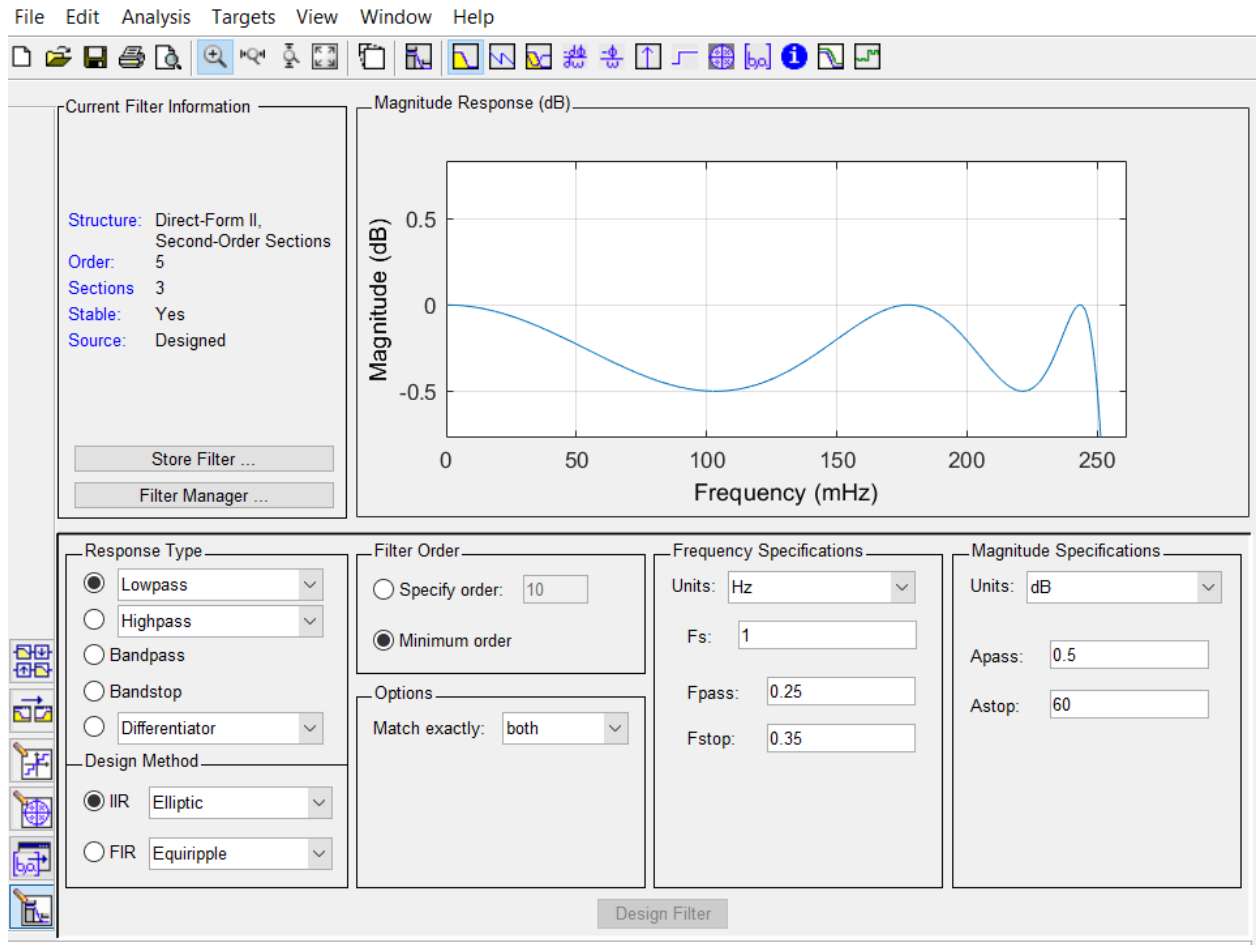


Figure 6. Elliptic filter zoomed-in at passband. Magnitude within  $\pm 0.5$  dB from 0 Hz - 0.25 Hz

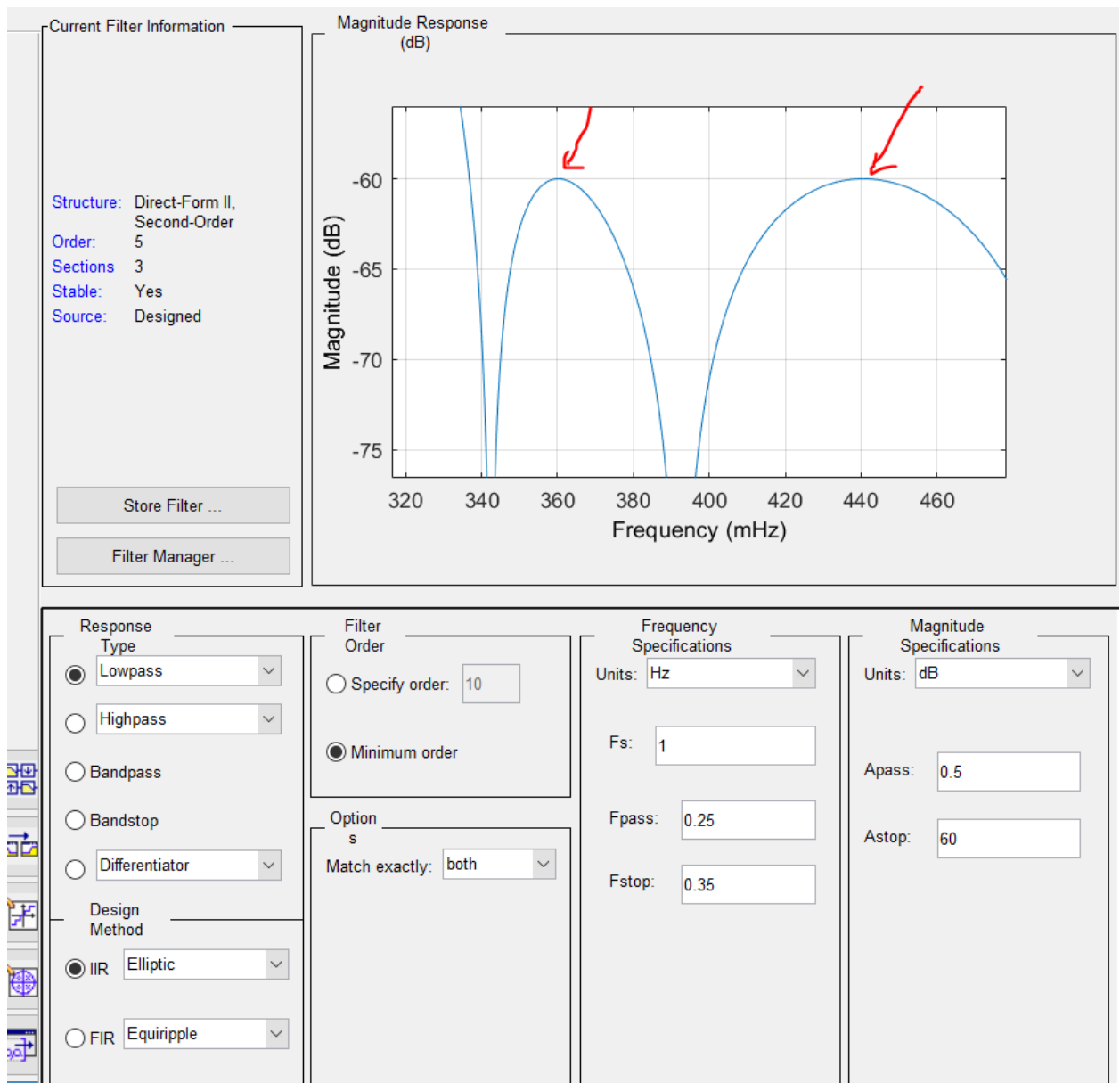


Figure 7. Elliptic filter zoomed-in at stop band. Ripple peaks hit -60dB.

```
>> elipB

elipB =

    0.0496    0.1814    0.3158    0.3158    0.1814    0.0496

>> elipA

elipA =

    1.0000   -0.8291    1.4480   -0.8915    0.5277   -0.1615

>> |
```

Figure 8. Coefficients elipB for numerator, elipA for denominator. Order of **5**.

### 3. Lowpass FIR



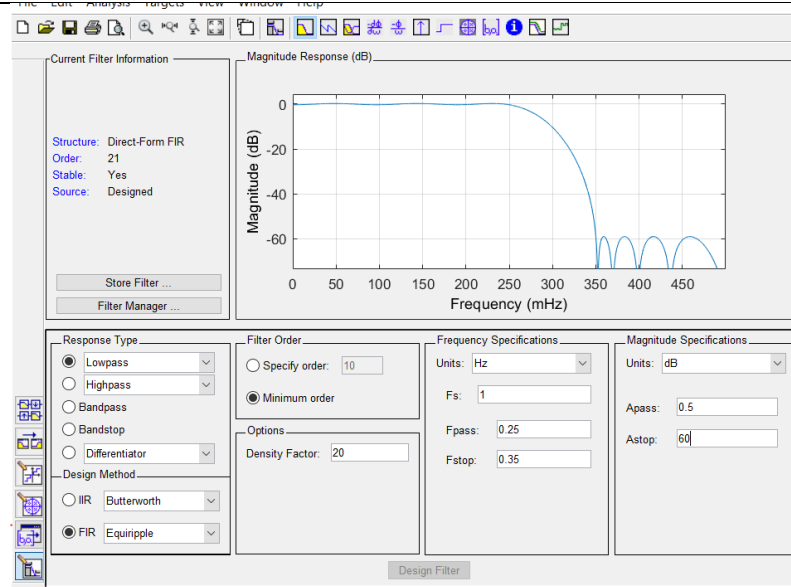


Figure 9. Lowpass FIR filter. Order **21**. We can see stopband exceeds -60dB.

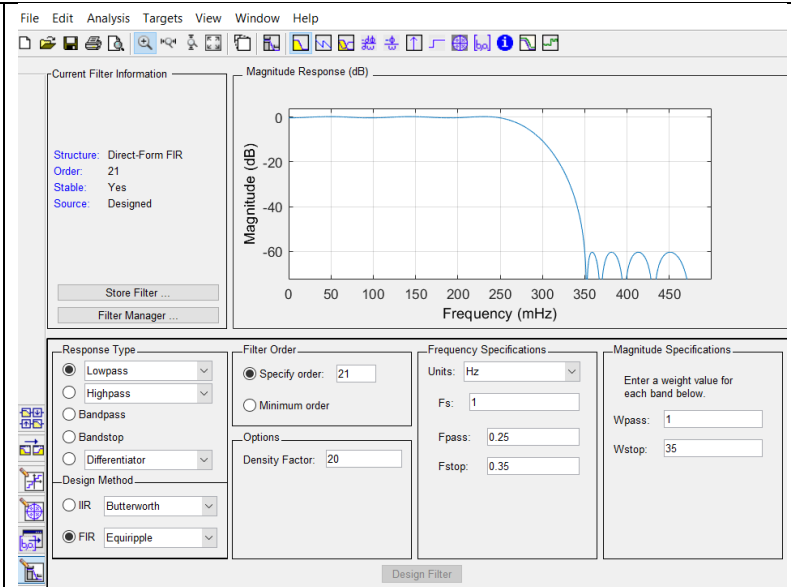


Figure 10. We keep the minimum order of **21**. Adjust the stopband weights for stopband to be smaller than -60dB. Passband weight = 1.

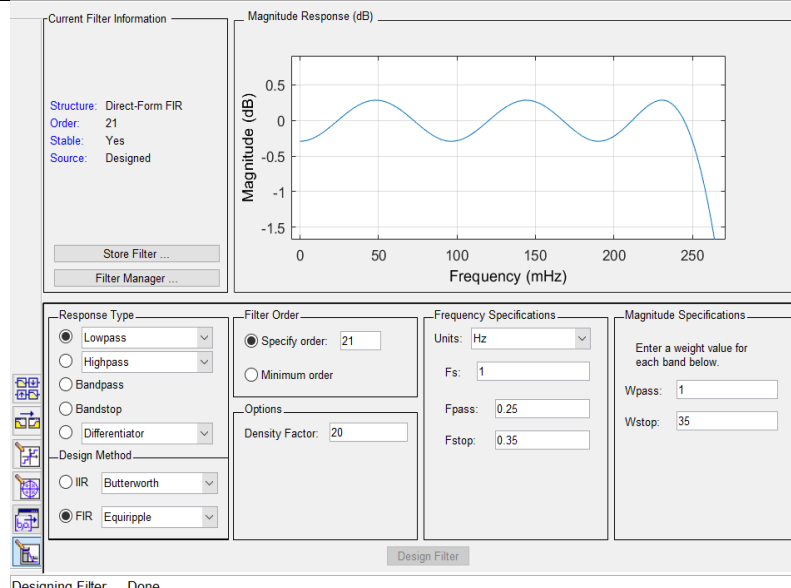


Figure 11. Lowpass FIR filter passband zoomed-in. Ripples are within 0 to -0.5dB.

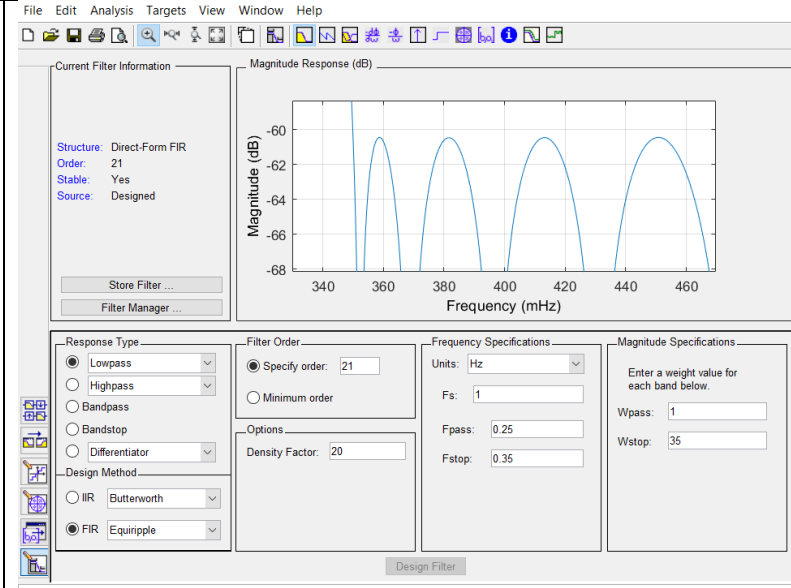


Figure 12. Lowpass FIR filter stopband zoomed-in. Peaks are less than -60dB.

```
>> lowpassFIR_B
lowpassFIR_B =
Columns 1 through 16
-0.0094 -0.0163 0.0074 0.0189 -0.0240 -0.0199 0.0555 0.0028 -0.1172 0.0867 0.4989 0.4989 0.0867 -0.1172 0.0028 0.0555
Columns 17 through 22
-0.0199 -0.0240 0.0189 0.0074 -0.0163 -0.0094
```

Figure 13. Lowpass FIR coefficient for order of **21**.

#### 4. Chebyshev Type 1 (IIR)

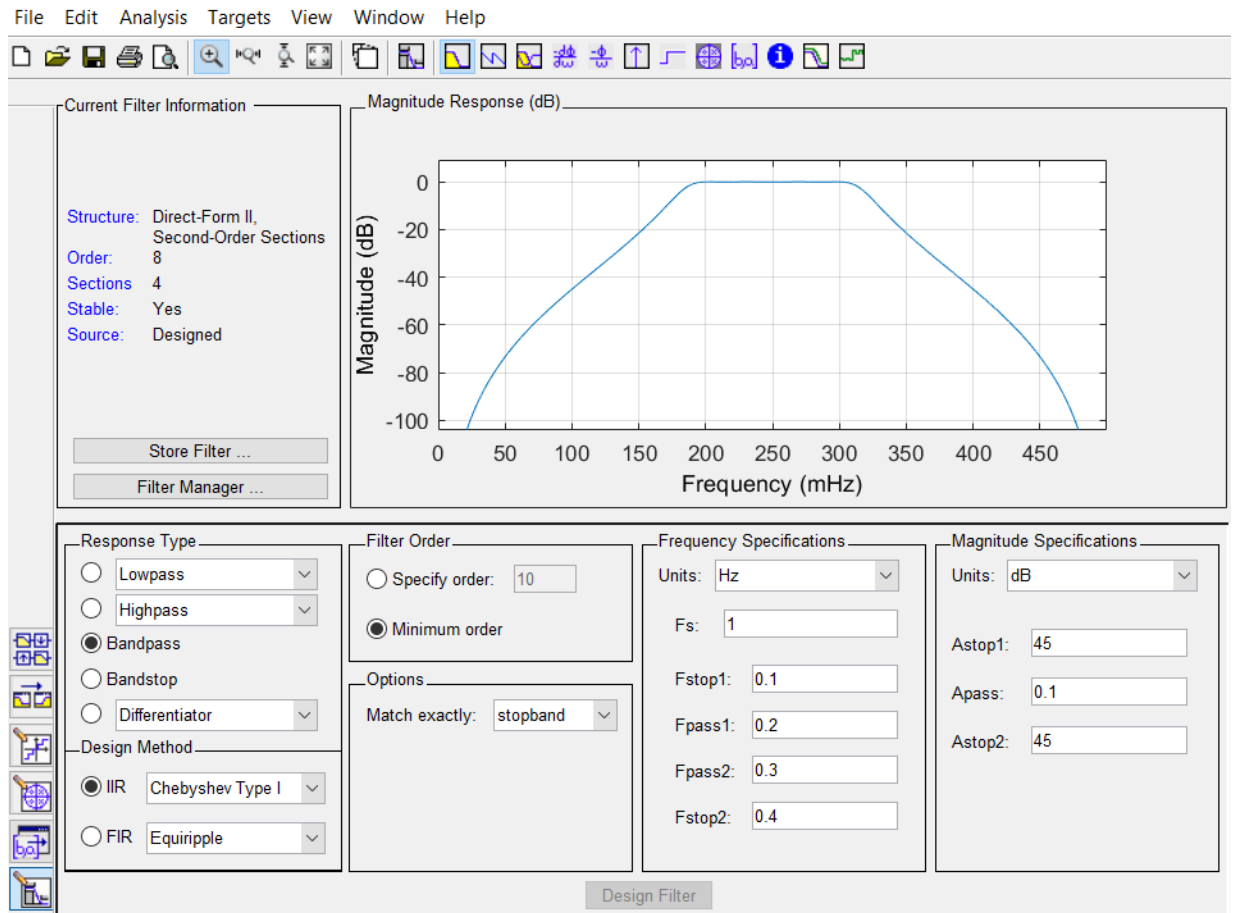


Figure 14. Chebyshev Type1 filter and specs. Order: **8**. We choose the option of matching exactly ‘stopband’

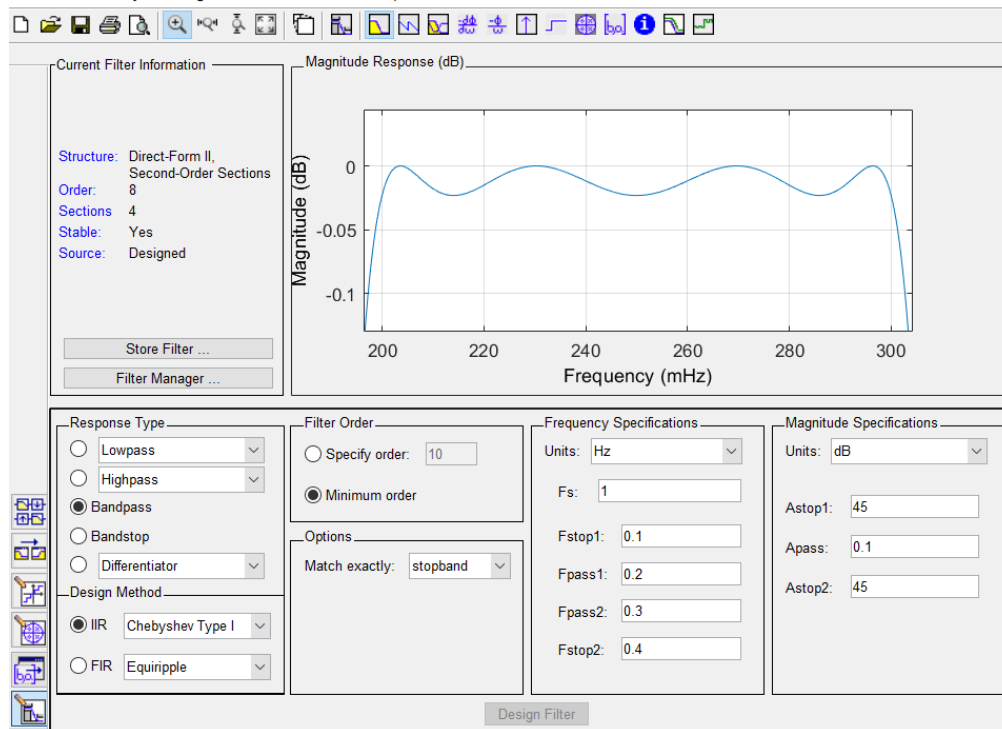
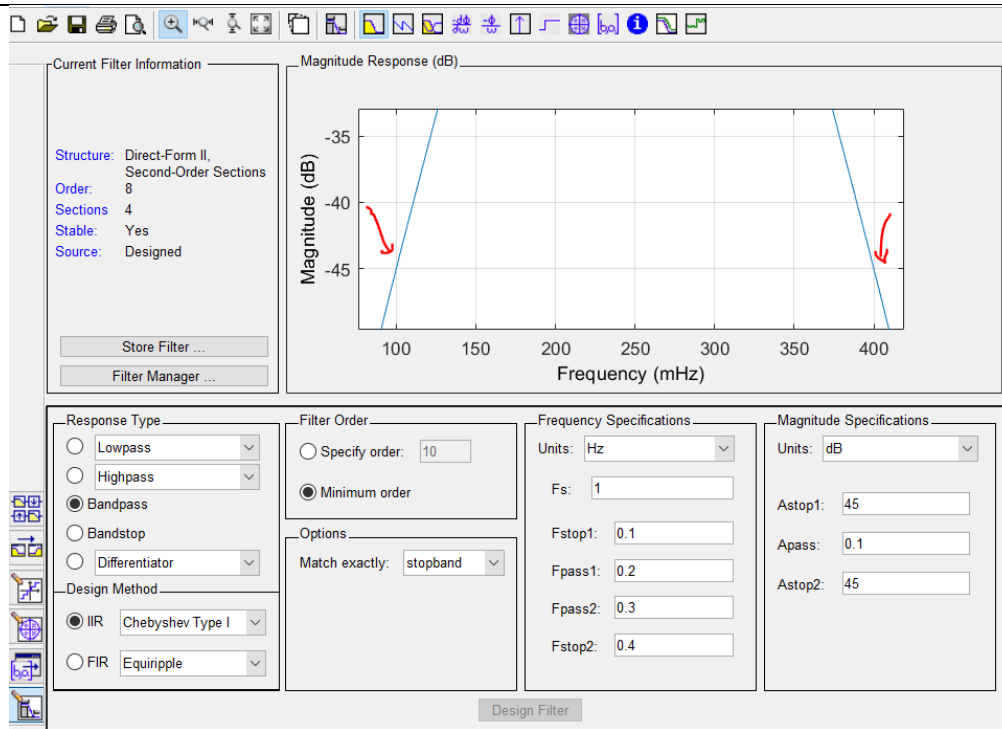


Figure 15. Chebyshev Type I passband @0.2Hz and 0.3Hz



Designing Filter ... Done

Figure 16. Chebyshev Type I stopband @0.1Hz and 0.4Hz

```
>> chev1B

chev1B =

    0.0081    0   -0.0325    0    0.0488    0   -0.0325    0    0.0081

>> chev1A

chev1A =

    1.0000   -0.0000    2.2381   -0.0000    2.2553    0.0000    1.1098    0.0000    0.2231
```

Figure 17. Chebyshev Type 1 coefficients. Order of 8.

## 5. Chebyshev Type 2 (IIR)

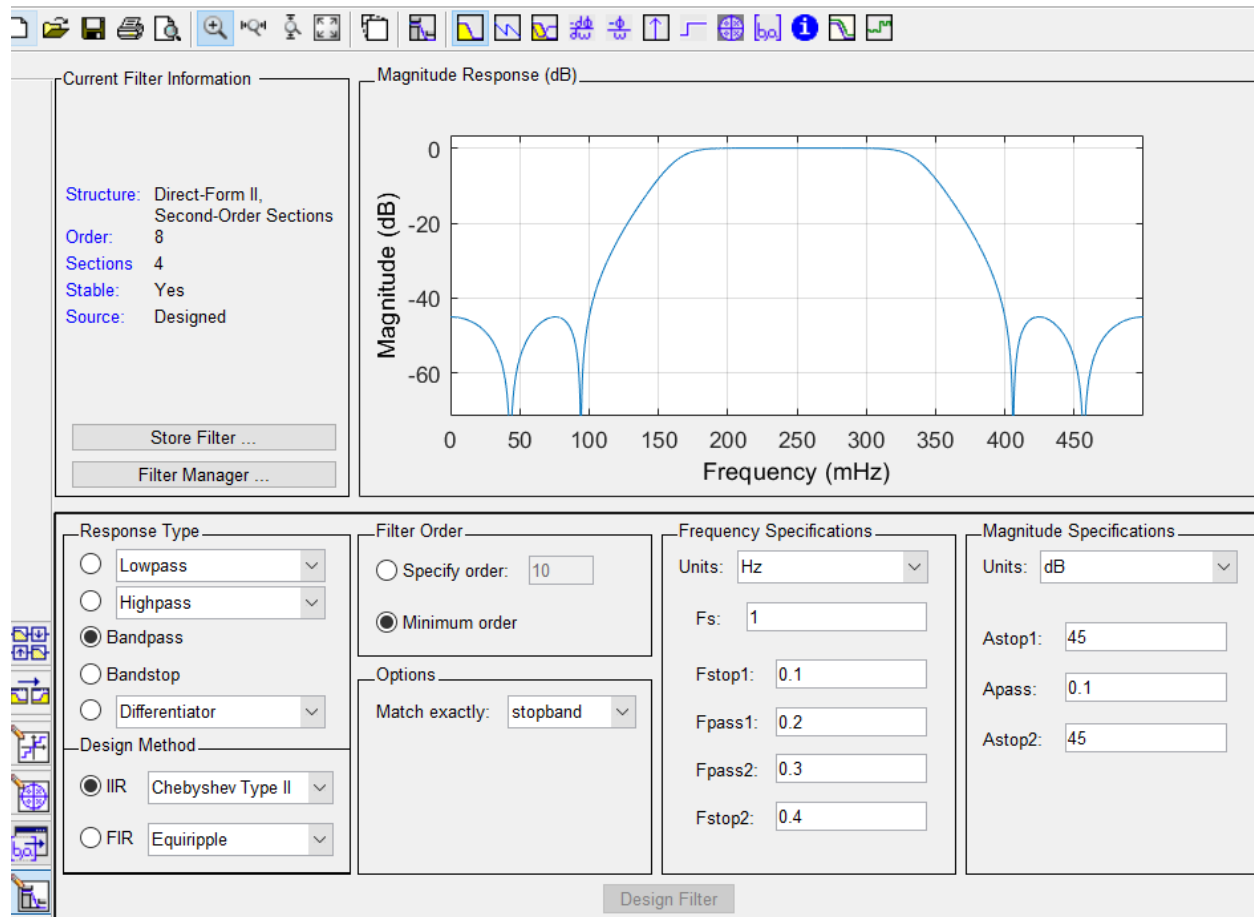


Figure 18. Chebyshev Type 2 filter and specs. Order: 8. We choose the option of matching exactly 'stopband'

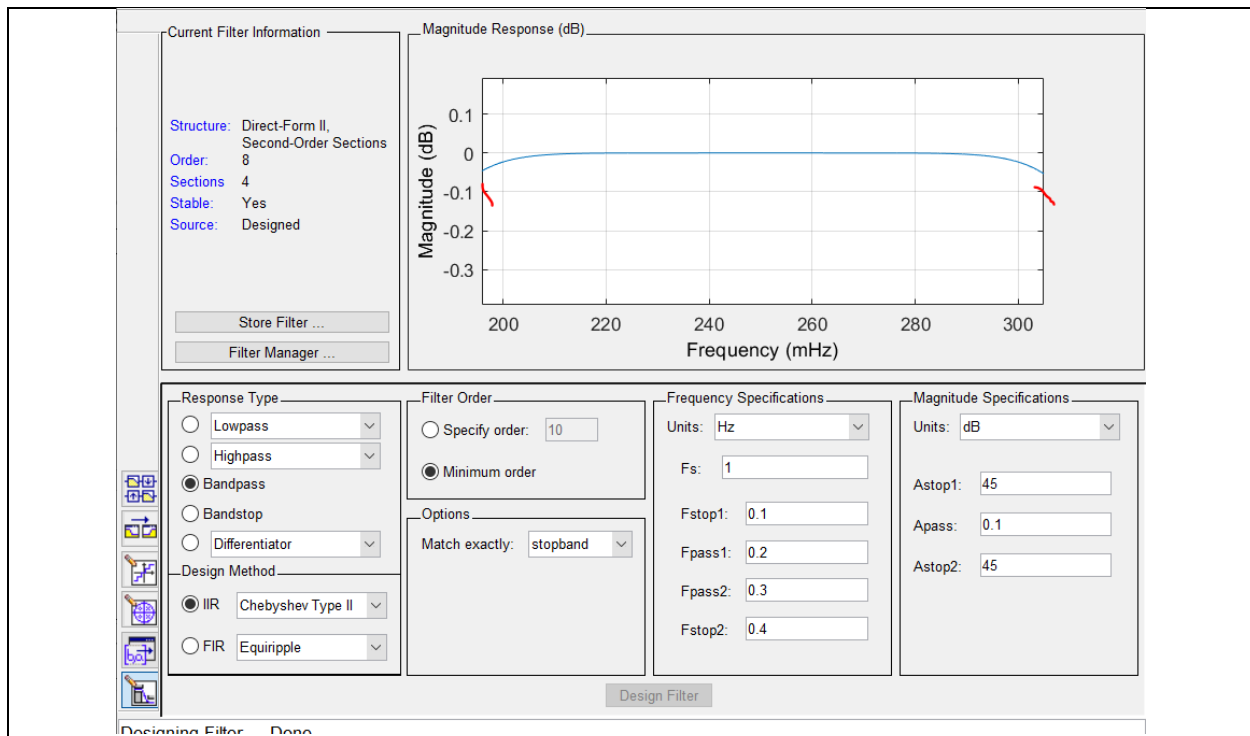


Figure 19. Chebyshev Type 2 passband @0.2Hz and 0.3Hz

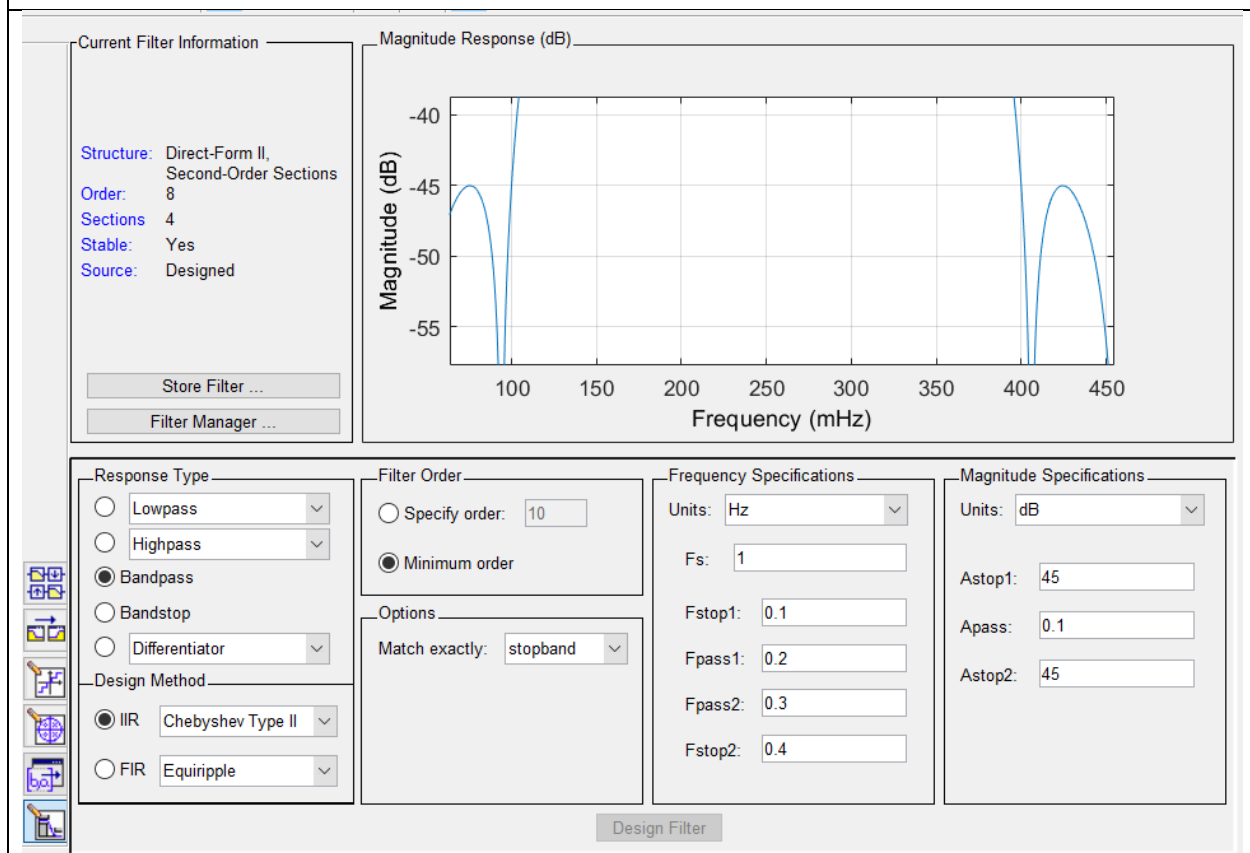


Figure 20. Chebyshev Type 2 lobes beyond 0.1Hz and 0.4Hz peak at -45dB.

```
>> chev2B

chev2B =

    0.0534    0   -0.1318    0    0.1759    0.0000   -0.1318    0    0.0534

>> chev2A

chev2A =

    1.0000    0.0000    1.1286    0.0000    0.9173    0.0000    0.2900    0.0000    0.0476
```

Figure 21. Chebyshev Type 2 coefficients. Order of **8**.

## 6. Bandpass FIR filter

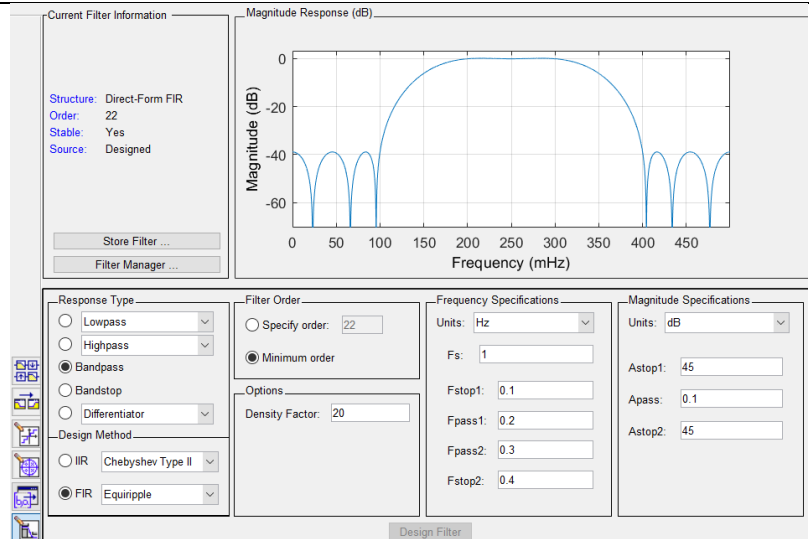


Figure 22. Bandpass FIR filter. Order 22. We can see stopband exceeds -45dB.

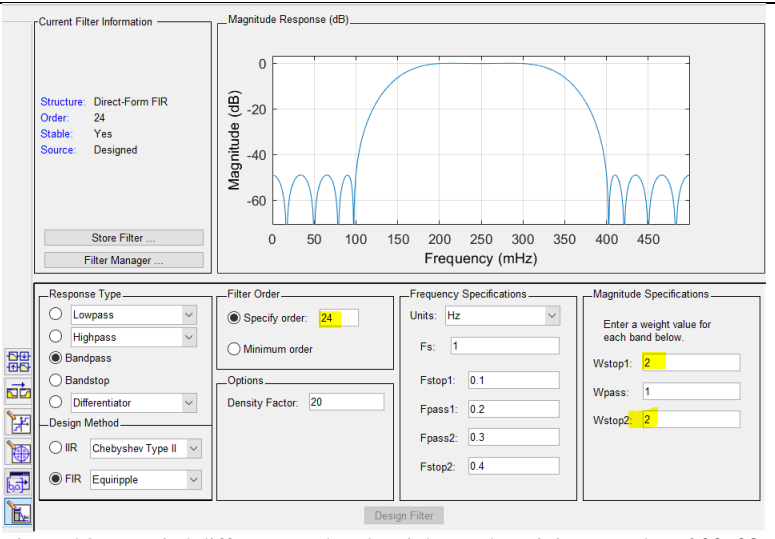


Figure 23. We tried different stopband weights at the minimum order of 22, 23, 24 and got the pass/stop weights as above for passband ripples to be within  $\pm 0.1$  dB, stopband to be smaller than -45dB.

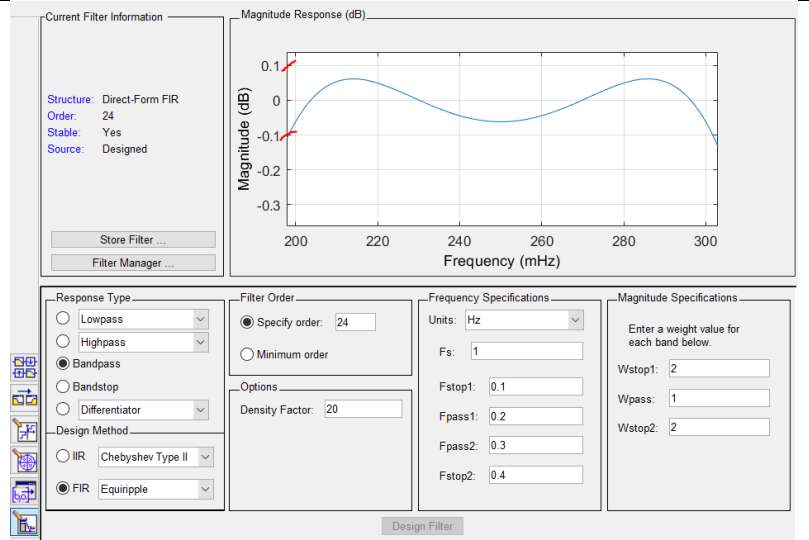


Figure 24. Bandpass FIR filter passband zoomed-in. Ripples are within 0.1 to -0.1dB.

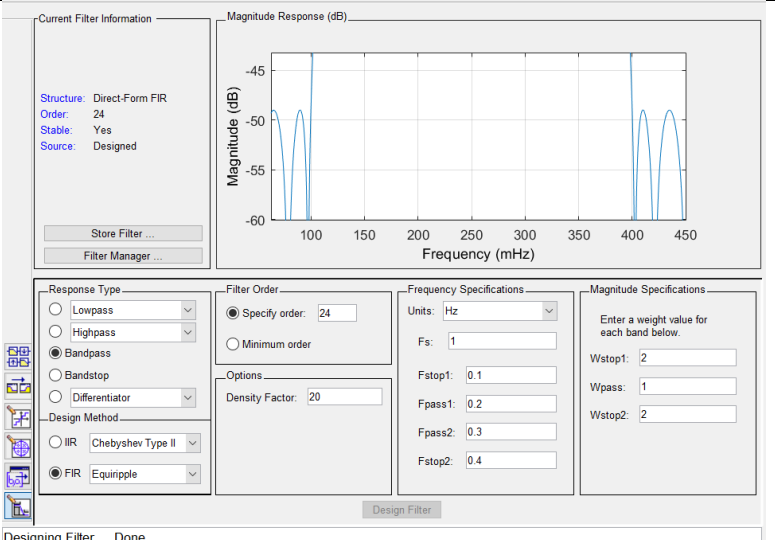


Figure 25. Bandpass FIR filter stopband zoomed-in. Peaks are less than -45dB.

```
>> equippassbandB

equippassbandB =

Columns 1 through 15

    0.0073    -0.0000    0.0014    -0.0000    -0.0380    -0.0000    0.0408    -0.0000    0.0815    0.0000   -0.2895   -0.0000    0.3965   -0.0000   -0.2895

Columns 16 through 25

    0.0000    0.0815   -0.0000    0.0408   -0.0000   -0.0380   -0.0000    0.0014   -0.0000    0.0073
```

Figure 26. Bandpass FIR coefficient for order of 24.