

Two Pointers Technique

- Pointer = index
 - No relationship to C++ pointers `int **x;`
- It is not a specific algorithm. Just easy idea that might be effective for specific problems
- You probably coded it before, but don't know a name for it
- In 2010, with a Codeforces tag, the name become more popular
- I will utilize this [tutorial](#)

Two Pointers Technique

- Technique that uses 2 **constrained** indices (move of one **can** be limited by the another)
 - Typically each pointer iterates on $O(N)$ array positions.
 - Hence overall **increment/decrement** is $O(N)$
- Applications
 - In sorted arrays, where we want to find some positions
 - Or cumulative array of positive numbers array (sorted)
 - Variable size sliding window, where we search for a window (range) of specific property (max sum)
 - Ad Hoc cases

Sum of 2 numbers problem

- It is one of the best problems to clarify the 2-pointers technique
- Given a **sorted** array A, having N integers. You need to find any **pair(i,j)** having sum as given number **X**.
 - $O(N^2)$: 2 nested loops and compare the sum
 - $O(N \log n)$: For each array value V, binary search for $X - V$
 - $O(N)$ using 2-pointers!

Sum of 2 numbers problem

- 2-pointers based on the sortedness of array
 - Let pointer(index) p1 on the first element of array
 - Let p2 on the last element of the array
 - Let Y = the sum of these 2 numbers
 - If $Y > X \Rightarrow$ shift p2 to the left \Rightarrow decrease Y
 - If $Y < X \Rightarrow$ shift p1 to the right \Rightarrow increase Y
 - Keep doing so until $Y == X$ or no way
 - Then each pointer moves $O(N)$, total $O(N)$

Sum of 2 numbers problem

- Let $A = \{2, 4, 5, 7, 8, 20\}$, $X = 11$
 - $P1 = 0, P2 = 5, Y = 2 + 20 = 22 > 11$
 - The only thing we can do is to move **p2 left**
 - $P1 = 0, P2 = 4, Y = 2 + 8 = 10 < 11$
 - Now we need bigger sum \Rightarrow move **p1 right**
 - $P1 = 1, P2 = 4, Y = 4 + 8 = 12 > 11$
 - Again, move **p2 left** to decrease sum
 - $P1 = 1, P2 = 3, Y = 4 + 7 = 11 == 11$ (Found)

Sum of 2 numbers problem

```
#define lli long long

bool f(lli sum) {
    int l = 0, r = n - 1; //two pointers
    while ( l < r ) {
        if ( A[l] + A[r] == sum ) return 1;
        else if ( A[l] + A[r] > sum ) r--;
        else l++;
    }
    return 0;
}
```

Sliding Windows

- A window is a range with start/end indices
 - So by definition, we have a point for its start & end
 - **Fixed size window of length K**
 - In this windows, we have specific range and searching for a range with specific property. Easy to handle
 - **Variable size window**
 - In this windows, the window can be of any size. More tricky