



Programming and Data Structures

The exam consists of six Questions in Three Pages.

Total Marks: 110 Marks

1/3

Question 1 [14 Marks]

State True or False and justify your answer:

- The maximum number of nodes in a tree (where each node has maximum B children) that has L levels is B^L (B to the power L)
- A queue should be used when implementing Breadth First Search (BFS).
- In a binary tree, every node has exactly two children.
- Binary Search Tree (BST) operation like insert typically run in $O(d)$ time where d is the number of nodes in the tree.
- In a heap, the left child of a node is always less than the right child of a node.
- The linked-list implementation of a graph is more efficient than matrix representation in finding whether two vertices are directly connected or not.
- The order in which elements are inserted in a binary search tree is unimportant.
- An inorder traversal always processes the elements of a tree in the same order, regardless of the order in which the elements were inserted.
- The running time of finding the maximum element in a heap is $O(\log N)$ where N is the number of elements in the heap.
- The largest value in a binary search tree (BST) is always stored at the root of the tree.
- An $O(\log N)$ algorithm is slower than an $O(N)$ algorithm.
- Adding an element to existing heap -and reheaping- takes $O(N)$ time.
- To delete a dynamically allocated tree, the best traversal method is postorder
- Implementing a priority queue using a heap is more efficient than using a linked-list.

Question 2 [18 Marks]

Given the following infix expression $((x-4)*y+3)/2$

- Represent the expression using binary tree that contains either operand like x, 4, 3 or operator like * , + [do not represent the parentheses] [4 Marks]
- If $x=10$ and $y=2$, evaluate the expression [2 Marks]
- Translate the expression into postfix [4 Marks]
- Show how to use the expression tree to generate postfix translation of the given expression [4 Marks]
- Using stack show step by step how to evaluate this expression [4 Marks]

Question 3 [16 Marks]

It is required to count the nodes of a binary search tree of integer values.

- Write down a class for the single node of the binary search tree [4 Marks]
- Write down a recursive function in C++ to find the total number of nodes [4 Marks]
- Write down an iterative function in C++ to find the total number of nodes [4 Marks]
- Compare recursion with iteration in terms of (i) big O and (ii) simplicity [4 Marks]

Question 4 [20 Marks]

Write C++ code or an algorithm to

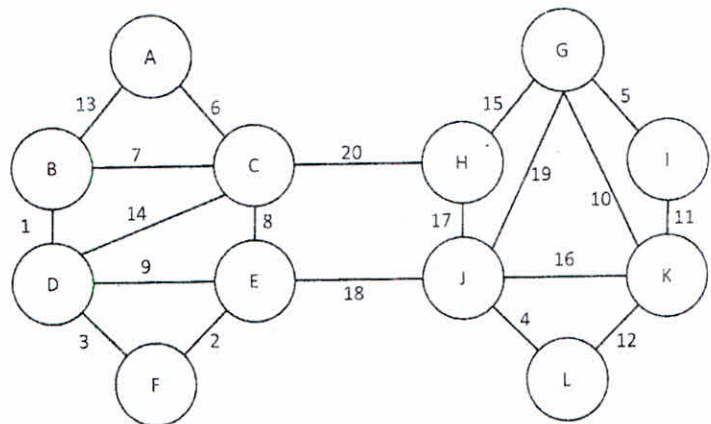
- Check if a given array is a heap or not [5 Marks]
- Add the values inside the nodes of a linked list of integers [5 Marks]
- Print a linked list content in a reverse order [5 Marks]
- Print a binary tree in postorder [5 Marks]

Question 5 [24 Marks]

Given the following undirected graph

- Represent this graph using matrix or linked list [4 Marks] and justify your choice [2 Marks]

- Using Prim algorithm, show step by step how to find Minimum spanning tree for the given graph [6 marks]



- Starting from node A, Traverse this graph using breadth first search (BFS), show the order of the nodes visited and the queue contents (assume nodes appear alphabetically i.e. A→B→C→D→E→F→G→H→I→J→K→L) mark the node once you add it to the queue, do not add already visited/visited nodes [6 marks]
- Using Dijkstra algorithm, find the shortest path starting from node B and ending at node K [6 marks]

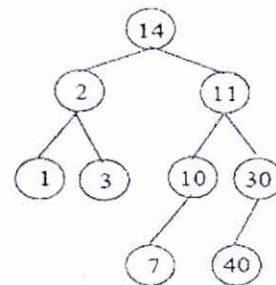
Question 6 [18 Marks]

Complete the following statements with short answers or choose one answer from between parentheses. In your answer sheet write the short answer and the question number.

- a) In a single linked list, the operation of deleting the last node has big O of _____
- b) Perfect hash table should have find operation with big O of _____
- c) Two different binary search trees (with the same elements but different arrangement) have the same _____ traverse
- d) Suppose that a heap containing 85 elements and it is stored in an array. The heap root is in index 0, the left child of node with index 5 is _____ and the parent of the child with index 37 is at index _____ the first leaf node is found at index _____.
- e) The largest value of a binary search tree is always stored at _____
- f) A complete directed graph with 8 vertices has _____ edges.
- g) The height L of a balanced full binary tree with 15 nodes is _____.
- h) A hash table with the hash function $h(i) = i - \text{Offset}$, where offset is a constant is has a disadvantage of _____

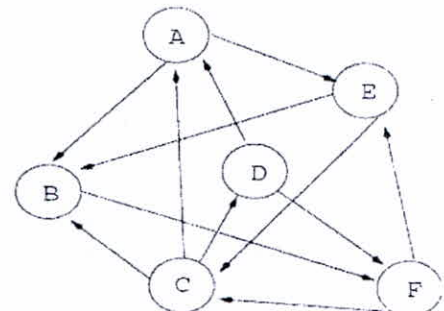
i) Given the following binary tree

The depth of the node with value 11 is _____
This binary tree is (left justified, balanced, heap, binary search tree)



j) Given the following graph:

- This is a (connected, complete, connected and complete) graph it is (directed, undirected) graph
- Draw its linked-list representation (store the vertices in alphabetical order).
- Draw one possible spanning tree starting from node A



GOOD LUCK

