

Group A
[Answer all the questions]

1. Answer any FIVE

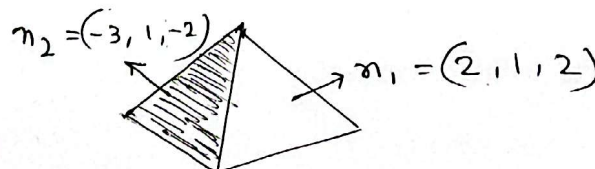
5x2=10

- a) Define sampling and quantization.
- b) What do you understand by object space and image space?
- c) In the RGB model, what color do we have along the diagonal running from the origin to the (1,1,1) point?
- d) Give an example of such a string that stays the same even after compressing using Run-Length Encoding.
- e) Find the perspective projection onto the view plane $z=d$ where the center of the projection is the origin(0,0,0).
- f) During Scan-Conversion, which one of the following two will produce less aliasing effect? Why?
 $(x', y') = \text{Floor}(x + 0.5, y + 0.5)$ or $(x', y') = \text{Floor}(x, y)$
- g) Can we use exactly the same Midpoint Ellipse algorithm for scan converting a circle? Why or why not?
- h) How can you detect any vertices in a polygon as a monotonously increasing point?

2. Answer any FOUR

4x5=20

- a) Find the coordinates of the color that remains the same both in RGB and CMY models, using the necessary calculation. 5
- b) What is the total storage required for an image of 512×640 that uses a lookup table containing 1024 colors and each color containing 3 bits for Red, 4 bits for Green, and 5 bits for Blue? 5
- c) Mathematically how do you determine whether a surface is back facing or front facing? The normal n_1 and n_2 of two surfaces and the view point V is shown in the following figure. Determine which surface is back facing. 5



- d) What are the shortcomings of direct use of the equation and DDA algorithm for scan converting a line? How does Bresenham's line algorithm overcome these? 5
- e) Write the basic steps of scan converting an ellipse rotated θ° counter-clockwise and centered at (h, k) point. 5
- f) Briefly discuss 3 types of anti-aliasing techniques. 5

3. Answer any TWO

2x10=20

- a) Let's assume we've cut out a sub-image from the center of an image. The initial image has an aspect ratio of 4:5 and contains 327,680 pixels. The aspect ratio of the sub-image is inverse of the initial image and the sub-image contains $\frac{1}{4}$ th of the total pixels of the initial one. 5+5
 - i) Find the lower-left corner of the sub-image (the upper-left corner of the initial image is the origin).
 - ii) What is the maximum size of the sub-image that could be cut out from the center, in the same manner, having an inverse aspect ratio of the initial image?

- b) i) Indicate which raster locations would be chosen by Bresenham's algorithm when scan converting a line from pixel coordinate from (4,5) to (11,9). 8+2
 ii) Plot the rastered pixels.
- c) The coordinates of the vertices of a polygon are shown in the figure 6+4
 i) Write the initial edge list for the polygon.
 ii) State which edges will be active on scan lines = 6,7,8,9 and 10.

y												
10				V ₆		E ₅		V ₅				
9				⊙	⊙	⊙	⊙	⊙				
8			E ₆	⊙				⊙	E ₄			
7	V ₈	⊙	⊙	⊙	V ₇		V ₄	⊙	⊙			
6		⊙	E ₇					E ₃	⊙			
5	E ₈	⊙							⊙			
4		⊙	⊙	⊙	⊙	⊙	⊙	⊙	⊙			
3		V ₁			E ₁				V ₂			
2												
1												
	0	1	2	3	4	5	6	7	8	9	10	x

Group B

[Answer all the questions]

5x2=10

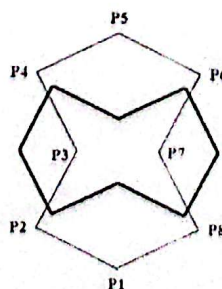
4. Answer any FIVE

- a) Mirroring against which line reverses the coordinates i.e. $M_L(x, y) = (y, x)$? $\frac{y_2 - y_1}{x_2 - x_1} = \frac{y - y_1}{x - x_1}$
 b) What is the transformation matrix for translating an object's center from (2,3) to (6,5)?
 c) Find the transformation for mirror reflection of a point P(x,y,z) with respect to the xy plane. Use suitable figures.
 d) During line clipping, which would need less computation between Cohen-Sutherland and Midpoint Subdivision in the worst case? Why?
 e) Is the point (2,3) to the left or to the right of the directed line segment from (-3,0) to (0,-3)?
 f) What is the relationship among the rotations R_θ , $R_{-\theta}$, R_0 ?
 g) After scaling with respect to any arbitrary point (x,y,z), which point isn't transformed to a new position?
 h) What is isometric projection?

5. Answer any FOUR

4x5=20

- a) Which transformation is itself its inverse transformation? Provide mathematical proof. 1+4
 b) A rectangle is defined by its vertices in counter-clockwise (CCW) direction:
 $V = \{(0,0), (0,4), (4,4), (4,0)\}$ 5
 Find the coordinates, after rotating it by 45° CCW with respect to its center.
 c) Find the window to viewport mapped coordinates of a triangle $\{(4,5), (4,8), (8,5)\}$ 5
 where $wx_{min} = 10, wx_{max} = 80, wy_{min} = 20, wy_{max} = 100$ and $vx_{min} = 30, vx_{max} = 60, vy_{min} = 50, vy_{max} = 80$
 d) Find the clipped polygon showing the chronological steps using the Weiler-Atherton algorithm. 5



The bolded one is the clipping polygon.

- e) Let's say, we performed θ_x rotation about the x-axis and θ_y rotation about y-axis. Does the order matter, i.e. is $R_{\theta_x, I} \cdot R_{\theta_y, J} = R_{\theta_y, J} \cdot R_{\theta_x, I}$? Show mathematically. 5
- f) Describe 3 perspective projection anomalies. 5

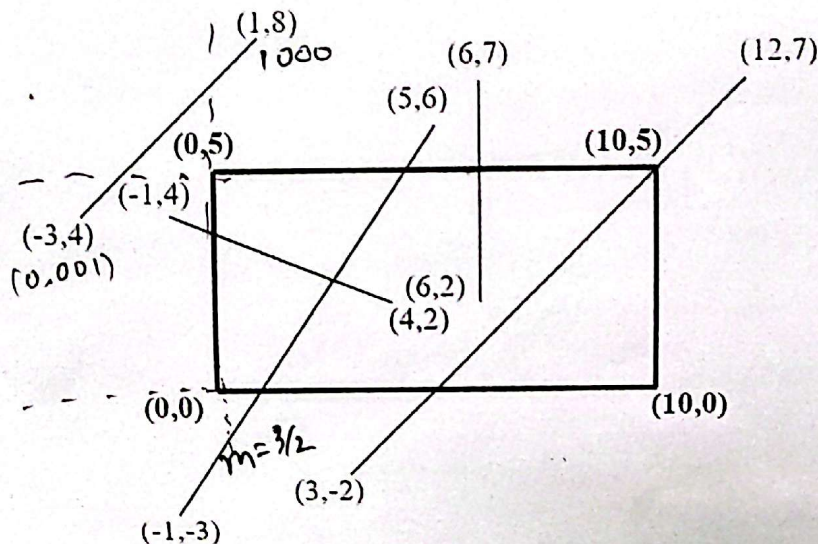
6. Answer any TWO

2x10=20

- a) The matrix given below defines a transformation called a simultaneous shearing. The special case when $b = 0$ is called shearing in the x-direction. When $a = 0$, we get shearing in the y-direction. Illustrate the effect of these shearing transformations on the square A(0, 0), B(1, 0), C(1, 1), and D(0, 1) when $a = 2$ and $b = 3$. 10

$$\begin{bmatrix} 1 & a \\ b & 1 \end{bmatrix}$$

- b) You're given a rectangular window and some line segments to be clipped in the following figure. Apply the Cohen-Sutherland algorithm to clip these line segments using the window. 10



Draw the final result after you're done.

- c) Let's assume, we want to rotate a point, $P(x,y,z)$ with respect to an arbitrary line, $v = aI + bJ + cK$. The line passes through a point $Q(p,q,r)$. Write the composite transformation of the rotation along that line showing the necessary details. 10