

**Group A**  
*[Answer all the questions]*

**1. Answer any FIVE**

**5x2=10**

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- a) Define sampling and quantization.
- b) What do you understand by object space and image space?
- c) In the RGB model, what color do we have along the diagonal running from the origin to the (1,1,1) point?
- d) Give an example of such a string that stays the same even after compressing using Run-Length Encoding.
- e) Find the perspective projection onto the view plane  $z=d$  where the center of the projection is the origin(0,0,0).
- f) During Scan-Conversion, which one of the following two will produce less aliasing effect? Why?  
 $(x',y') = \text{Floor}(x + 0.5, y + 0.5)$  or  $(x',y') = \text{Floor}(x, y)$
- g) Can we use exactly the same Midpoint Ellipse algorithm for scan converting a circle? Why or why not?
- h) How can you detect any vertices in a polygon as a monotonously increasing point?

**2. Answer any FOUR**

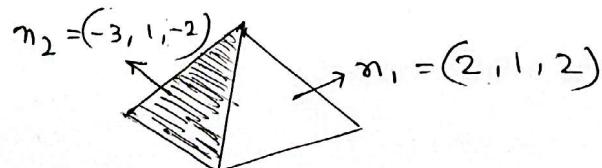
**4x5=20**

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- a) Find the coordinates of the color that remains the same both in RGB and CMY models, using the necessary calculation.
- b) What is the total storage required for an image of  $512 \times 640$  that uses a lookup table containing 1024 colors and each color containing 3 bits for Red, 4 bits for Green, and 5 bits for Blue?
- c) Mathematically how do you determine whether a surface is back facing or front facing? The normal  $n_1$  and  $n_2$  of two surfaces and the view point V is shown in the following figure. Determine which surface is back facing.



- d) What are the shortcomings of direct use of the equation and DDA algorithm for scan converting a line? How does Bresenham's line algorithm overcome these?
- e) Write the basic steps of scan converting an ellipse rotated  $\theta^\circ$  counter-clockwise and centered at  $(h,k)$  point.
- f) Briefly discuss 3 types of anti-aliasing techniques.

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**3. Answer any TWO**

**2x10=20**

5+5

- a) Let's assume we've cut out a sub-image from the center of an image. The initial image has an aspect ratio of 4:5 and contains 327,680 pixels. The aspect ratio of the sub-image is inverse of the initial image and the sub-image contains  $\frac{1}{4}$  th of the total pixels of the initial one.
  - i) Find the lower-left corner of the sub-image (the upper-left corner of the initial image is the origin).
  - ii) What is the maximum size of the sub-image that could be cut out from the center, in the same manner, having an inverse aspect ratio of the initial image?

- b) i) Indicate which raster locations would be chosen by Bresenham's algorithm when scan converting a line from pixel coordinate from (4,5) to (11,9). 8+2  
ii) Plot the rastered pixels.

- c) The coordinates of the vertices of a polygon are shown in the figure 6+4  
i) Write the initial edge list for the polygon.  
ii) State which edges will be active on scan lines =6,7,8,9 and 10.

y	1	2	3	4	5	6	7	8	9	10	x
10				V <sub>6</sub>		E <sub>5</sub>		V <sub>5</sub>			
9				( )	( )	( )	( )	( )	( )		
8		E <sub>6</sub>	( )					( )	E <sub>4</sub>		
7	V <sub>8</sub>	( )	( )	( )	V <sub>7</sub>		V <sub>4</sub>	( )	( )		
6		( )	E <sub>7</sub>					E <sub>3</sub>	( )		
5	E <sub>8</sub>	( )							( )		
4		( )	( )	( )	( )	( )	( )	( )	( )		
3		V <sub>1</sub>		E <sub>1</sub>				V <sub>2</sub>			
2											
1											
0	1	2	3	4	5	6	7	8	9	10	x

**Group B**  
[Answer all the questions]

5x2=10

**4. Answer any FIVE**

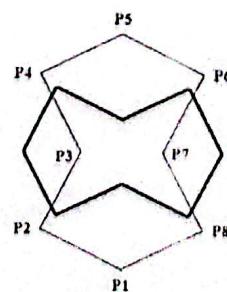
- a) Mirroring against which line reverses the coordinates i.e.  $M_L(x, y) = (y, x)$ ?  $\frac{y_2 - b_2}{x_2 - x_1} = \frac{y_1 - b_1}{x_1 - x_2}$   
b) What is the transformation matrix for translating an object's center from (2,3) to (6,5)?  
c) Find the transformation for mirror reflection of a point P(x,y,z) with respect to the xy plane. Use suitable figures.  
d) During line clipping, which would need less computation between Cohen-Sutherland and Midpoint Subdivision in the worst case? Why?  
e) Is the point (2,3) to the left or to the right of the directed line segment from (-3,0) to (0,-3)?  
f) What is the relationship among the rotations  $R_\theta R_{-\theta} R_\theta$ ?  
g) After scaling with respect to any arbitrary point (x,y,z), which point isn't transformed to a new position?  
h) What is isometric projection?

**5. Answer any FOUR**

4x5=20

- a) Which transformation is itself its inverse transformation? Provide mathematical proof. 1+4  
b) A rectangle is defined by its vertices in counter-clockwise(CCW) direction: 5  

$$V = \{(0,0), (0,4), (4,4), (4,0)\}$$
  
Find the coordinates, after rotating it by 45° CCW with respect to its center.  
c) Find the window to viewport mapped coordinates of a triangle  $\{(4,5), (4,8), (8,5)\}$  where  $wx_{min} = 10, wx_{max} = 80, wy_{min} = 20, wy_{max} = 100$  and  $vx_{min} = 30, vx_{max} = 60, vy_{min} = 50, vy_{max} = 80$  5  
d) Find the clipped polygon showing the chronological steps using the Weiler-Atherton algorithm. 5



The bolded one is the clipping polygon.

- e) Let's say, we performed  $\theta_x$  rotation about the x-axis and  $\theta_y$  rotation about y-axis.  
Does the order matter, i.e. is  $R_{\theta_x,I} \cdot R_{\theta_y,J} = R_{\theta_y,J} \cdot R_{\theta_x,I}$ ? Show mathematically.
- f) Describe 3 perspective projection anomalies.

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6. Answer any TWO

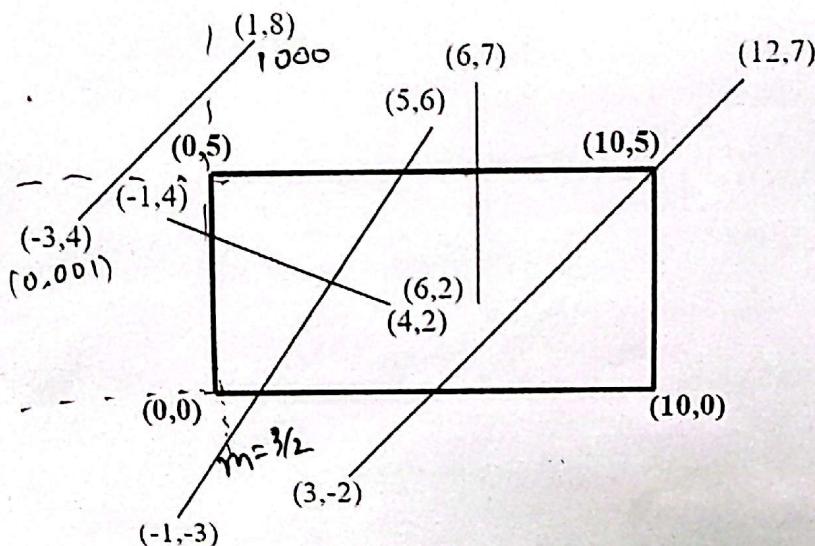
$2 \times 10 = 20$

- a) The matrix given below defines a transformation called a simultaneous shearing. The special case when  $b = 0$  is called shearing in the x-direction. When  $a = 0$ , we get shearing in the y-direction. Illustrate the effect of these shearing transformations on the square A(0, 0), B(1, 0), C(1, 1), and D(0, 1) when  $a = 2$  and  $b = 3$ .

$$\begin{bmatrix} 1 & a \\ b & 1 \end{bmatrix}$$

- b) You're given a rectangular window and some line segments to be clipped in the following figure. Apply the Cohen-Sutherland algorithm to clip these line segments using the window.

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Draw the final result after you're done.

*the line passes*

- c) Let's assume, we want to rotate a point,  $P(x,y,z)$  with respect to an arbitrary line,  $v = aI + bJ + cK$ . The line passes through a point  $Q(p, q, r)$ . Write the composite transformation of the rotation along that line showing the necessary details.

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