



deeplearning.ai

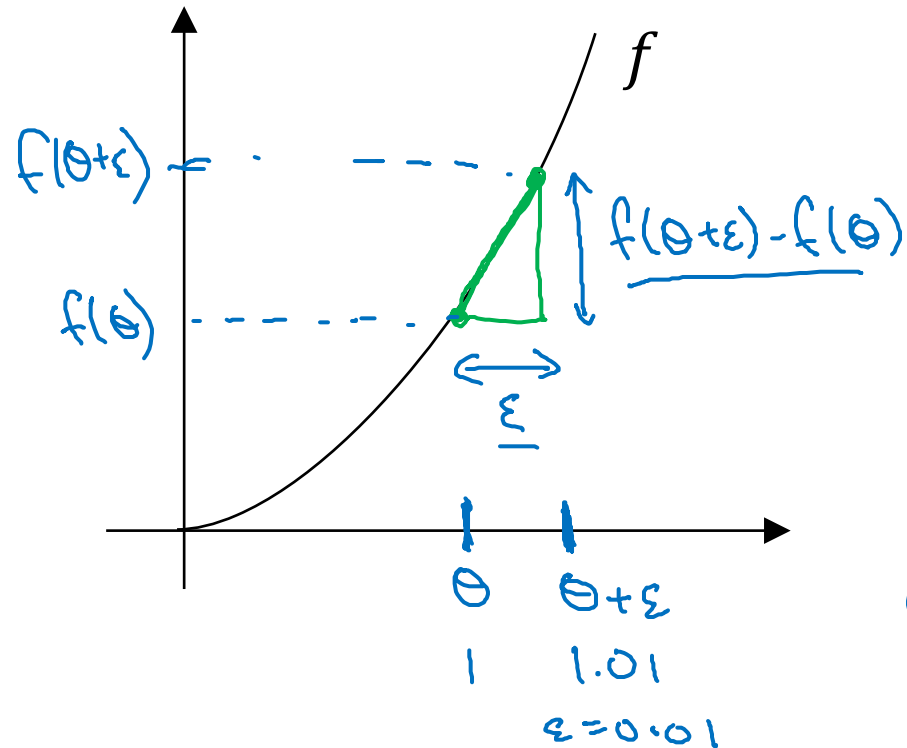
# Setting up your optimization problem

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## Numerical approximation of gradients

# Checking your derivative computation

I  $f(\theta) = \theta^3$   
 $\theta \in \mathbb{R}.$



$$g(\theta) = \frac{d}{d\theta} f(\theta) = f'(\theta)$$

$g(\theta) = 3\theta^2$

$\frac{dw}{db}$

$g(\theta) = 3 \cdot (1)^2 = 3$   
 when  $\theta = 1$

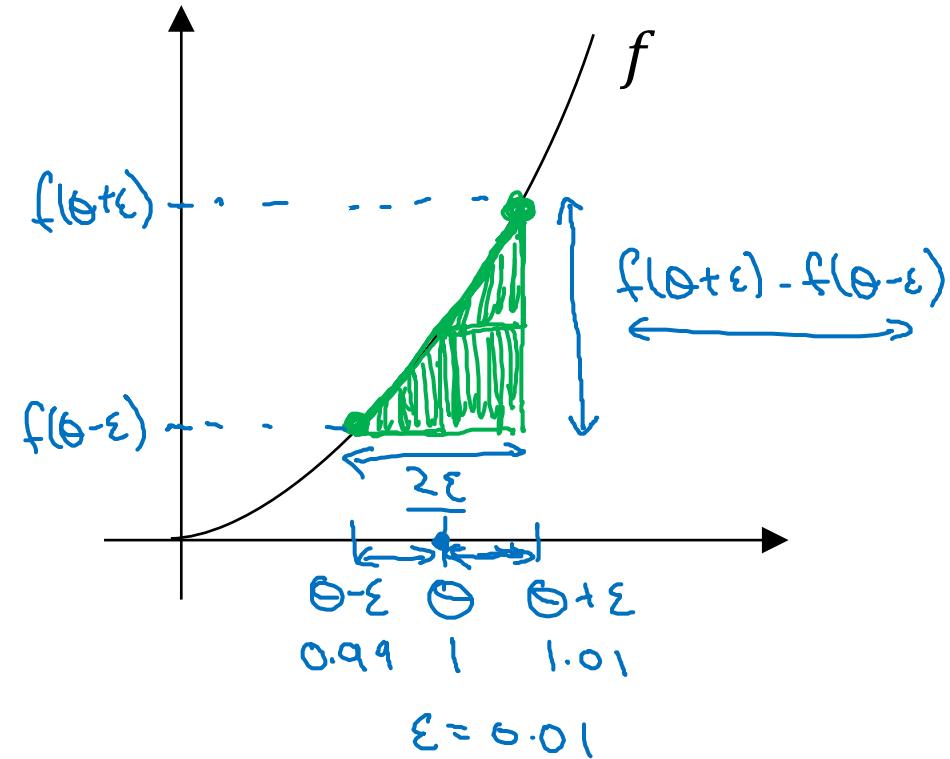
$$\frac{f(\theta + \epsilon) - f(\theta)}{\epsilon} \approx g(\theta)$$

$$\frac{(1.01)^3 - 1^3}{0.01} = \frac{3.0301}{0.01} = 3.0301 \approx 3$$

Annotations:  $\theta = 1$ ,  $\theta + \epsilon = 1.01$ ,  $\epsilon = 0.01$ . The calculation shows  $3.1$  and  $3.2$  as intermediate steps.

# Checking your derivative computation

$$\underline{f(\theta) = \theta^3}$$



$$\left[ \frac{f(\theta + \epsilon) - f(\theta - \epsilon)}{2\epsilon} \approx \underline{g(\theta)} \right]$$

$$\frac{(1.01)^3 - (0.99)^3}{2(0.01)} = 3.0001 \approx 3$$

$$g(\theta) = 3\theta^2 = 3$$

approx error: 0.0001

(prev slide: 3.0301. error: 0.03)

$$\left\{ \begin{array}{l} f'(\theta) = \lim_{\epsilon \rightarrow 0} \frac{f(\theta + \epsilon) - f(\theta - \epsilon)}{2\epsilon} \quad \begin{array}{l} O(\epsilon^2) \\ 0.01 \\ \underline{0.0001} \end{array} \quad \left| \quad \frac{f(\theta + \epsilon) - f(\theta)}{\epsilon} \quad \begin{array}{l} \text{error: } O(\epsilon) \\ 0.01 \end{array} \end{array} \right.$$