

# Recurrent Neural Networks

LSTM (long short term memory) unit

## GRU and LSTM

### GRU

#### LSTM

$$\underbrace{\tilde{c}^{< t>}}_{c} = \tanh(W_{c}[\Gamma_{r} * \underline{c^{< t-1>}}, x^{< t>}] + b_{c}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \tanh(W_{c}[\Gamma_{r} * \underline{c^{< t-1>}}, x^{< t>}] + b_{c}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \tanh(W_{c}[\Gamma_{r} * \underline{c^{< t-1>}}, x^{< t>}] + b_{c}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t>}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t>}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t}}_{c} = \sigma(W_{u}[c^{< t-1>}, x^{< t}] + b_{u}) \qquad \underbrace{\tilde{c}^{< t}}_{c} = \sigma(W_{u}[c^{< t-1>},$$

## LSTM units

#### **GRU**

$$\tilde{c}^{< t>} = \tanh(W_c[\Gamma_r * c^{< t-1>}, x^{< t>}] + b_c)$$

$$\tilde{c}^{} = \tanh(W_c[a^{}, x^{}] + b_c)$$

$$\Gamma_u = \sigma(W_u[c^{}, x^{}] + b_u)$$

$$\Gamma_u = \sigma(W_u[a^{< t-1>}, x^{< t>}] + b_u)$$

$$\Gamma_r = \sigma(W_r[c^{< t-1>}, x^{< t>}] + b_r)$$

$$\Gamma_f = \sigma(W_f[a^{< t-1>}, x^{< t>}] + b_f)$$

$$c^{} = \Gamma_u * \tilde{c}^{} + (1 - \Gamma_u) * c^{}$$

$$\Gamma_o = \sigma(W_o[a^{< t-1>}, x^{< t>}] + b_o)$$

$$a^{< t>} = c^{< t>}$$

$$c^{< t>} = \Gamma_u * \tilde{c}^{< t>} + \Gamma_f * c^{< t-1>}$$

$$a^{< t>} = \Gamma_o * c^{< t>}$$

[Hochreiter & Schmidhuber 1997. Long short-term memory]

## LSTM in pictures

