# METHOD TO ESTIMATE THE MEAN AND VARIANCE OF THE SPE PEAK

Khalid Gameil

### **SUMMARY OF PAPER**

- Take the mean and the variance of the ADC spectrum of the PMT with the laser light on and off
- Estimate the mean number of laser-induced photoelectrons produced in each trigger (referred to as the occupancy in the paper)

### THEORY SUMMARY

$$E[\psi] = \frac{E[T] - E[B]}{E[L]}$$

$$V[\psi] = \frac{V[T] - V[B] - E^2[\psi]V[L]}{E[L]}$$

- E[T] and V[T] = mean and variance signal distribution (i.e the distribution with the laser on)
- E[B] and V[B] = mean and variance of the background distribution (i.e the distribution with the laser off)
- E[L] and V[L] = mean and variance of the number of photoelectrons produced by the laser light

### THEORY PART 1/3

• The probability distribution of the total integrated charge (T(q)) is the convolution of the background distribution (B(q)) and the signal distribution (S(q))

$$T(q) = (B * S)(q)$$

• Moments of distribution (additive):

Mean: E[T] = E[B] + E[S]

Variance: V[T] = V[B] + V[S]

• Signal charge distribution is summation of each signal charge distribution corresponding to p=(0,1,2..) photoelectrons  $(S_p(q))$  and the discrete probability distribution of the photoelectrons produced by a laser light pulse (L(p))

# THEORY PART 2/3: SINGLE PHOTO-ELECTRON MEAN

- The signal charge distribution for p=1:  $S_1(q) = \psi(q)$
- The signal charge distribution for p:  $S_p(q) = (\psi(q))^p$
- The mean and variance of  $S_p(q)$  is:

$$E[\psi^p] = pE[\psi]$$

$$V[\psi^p] = pV[\psi]$$

• Therefore the signal charge distribution moments are:

$$E[s] = E[\psi]E[L]$$

$$V[\mathfrak{g}] = V[\mathfrak{g}] F[I] + F^2[\mathfrak{g}]V[I]$$

### THEORY PART 3/3: PARAMETER ESTIMATION

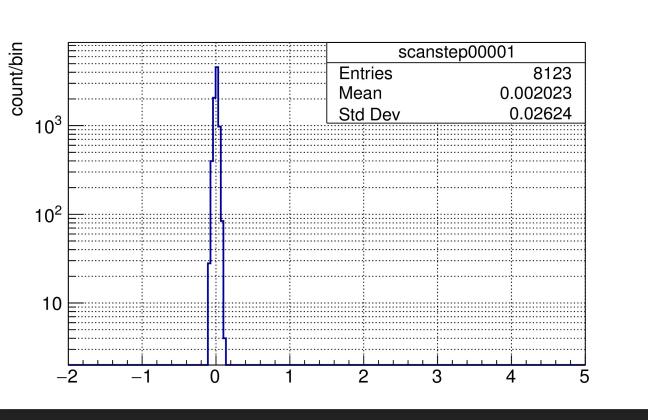
- E[T] and V[T] come as a the mean and variance of the signal distribution (i.e the distribution with the laser on)
- E[B] and V[B] come as a the mean and variance of the background distribution (i.e the distribution with the laser off)
- E[L] and V[L] represent the mean and variance of the number of photoelectrons produced by the laser light. If it is assumed that L(p) is represented by a Poisson distribution (which is valid for autenuated light) then:

$$L(p) = \frac{\lambda^p e^{-\lambda}}{p!} \lambda = E[L] = V[L]$$

• The occupancy can be estimated by the number of sample triggers 0-pe trigger over the total number of triggers

# PARAMETER ESTIMATION 1/2: T AND B

Background spectrum with laser light turned off.



mV

Signal spectrum with laser light turned on.

