## Find the number of integer solutions

$$\begin{array}{l} X + Y + Z + U + V + W = 23 \\ X \geq 2, \, Y \geq 0, \, Z \geq 6, \, U \geq 10, \, V \geq 8, \, W \geq \text{--}7 \end{array}$$

Number of Solutions:

$$\begin{array}{l} X \, + \, Y \, + \, Z \, + \, U \, = \, 6 \\ X \, \geq \, \text{-8}, \, Y \, \geq \, 7, \, Z \, \geq \, 10, \, U \, \geq \, \text{-6} \end{array}$$

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U + V + W = \text{-}19 \\ X \geq 1, \, Y \geq 0, \, Z \geq \text{-}3, \, U \geq \text{-}1, \, V \geq \text{-}9, \, W \geq \text{-}9 \end{array}$$

Number of Solutions:

$$X + Y + Z + U = 19$$
  
 $X \ge 7, Y \ge -1, Z \ge -3, U \ge 9$ 

Number of Solutions:

$$\begin{array}{l} X+Y+Z=25 \\ X\geq 10,\,Y\geq \mbox{-}2,\,Z\geq 10 \end{array}$$

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U = 5 \\ X \geq \text{--}2, \, Y \geq \text{--}1, \, Z \geq 6, \, U \geq \text{--}3 \\ \end{array}$$

$$X + Y + Z = 3$$
  
 $X \ge -5, Y \ge -4, Z \ge 7$ 

$$\begin{array}{l} X + Y + Z + U + V + W = \text{-}24 \\ X \geq 2, \, Y \geq \text{-}10, \, Z \geq \text{-}4, \, U \geq \text{-}9, \, V \geq \text{-}3, \, W \geq \text{-}5 \end{array}$$

Number of Solutions:

$$X + Y + Z + U = -9$$
  
 $X \ge 2, Y \ge -2, Z \ge -5, U \ge -7$ 

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U + V + W = 15 \\ X \geq 1, \, Y \geq 4, \, Z \geq 6, \, U \geq 7, \, V \geq \text{-}6, \, W \geq 2 \end{array}$$

Number of Solutions:

$$X + Y + Z + U = 14$$
  
 $X \ge -3, Y \ge 4, Z \ge 3, U \ge 3$ 

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U = \text{-}21 \\ X \geq \text{-}5, \, Y \geq \text{-}9, \, Z \geq \text{-}10, \, U \geq 0 \end{array}$$

$$\begin{array}{l} X + Y + Z + U + V + W = 6 \\ X \geq 2, \, Y \geq \mbox{-7}, \, Z \geq 1, \, U \geq 2, \, V \geq 6, \, W \geq \mbox{-3} \end{array}$$

$$\begin{array}{l} X \, + \, Y \, + \, Z \, + \, U \, = \, 9 \\ X \, \geq \, 0, \, Y \, \geq \, 5, \, Z \, \geq \, \text{--}2, \, U \, \geq \, 0 \end{array}$$

Number of Solutions:

$$X + Y + Z + U = 10$$
  
 $X \ge 8, Y \ge -6, Z \ge -4, U \ge 9$ 

Number of Solutions:

$$\begin{array}{l} X \, + \, Y \, + \, Z \, + \, U \, = \, 0 \\ X \, \geq \, 5, \, Y \, \geq \, \text{--8}, \, Z \, \geq \, 5, \, U \, \geq \, \text{--7} \end{array}$$

Number of Solutions:

$$X + Y + Z + U = 7$$
  
 $X \ge -7, Y \ge 5, Z \ge 4, U \ge 1$ 

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U + V = \text{-}29 \\ X \geq \text{-}1, \, Y \geq \text{-}8, \, Z \geq \text{-}4, \, U \geq \text{-}10, \, V \geq \text{-}9 \end{array}$$

$$\begin{array}{l} X+Y+Z=23 \\ X\geq 5,\,Y\geq 10,\,Z\geq 4 \end{array}$$

$$X + Y + Z = 7$$
  
 $X \ge 3, Y \ge 1, Z \ge -5$ 

Number of Solutions:

$$X + Y + Z = -4$$
  
 $X \ge -9, Y \ge 6, Z \ge -9$ 

Number of Solutions:

$$\begin{array}{l} X+Y+Z+U=5 \\ X\geq 4,\,Y\geq 1,\,Z\geq \text{--}1,\,U\geq \text{--}6 \end{array}$$

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U + V + W = 31 \\ X \geq 7, \, Y \geq 1, \, Z \geq \text{--}2, \, U \geq 9, \, V \geq 7, \, W \geq 8 \end{array}$$

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U + V + W = 4 \\ X \geq 5, \, Y \geq \mbox{-}4, \, Z \geq 6, \, U \geq \mbox{-}4, \, V \geq 2, \, W \geq \mbox{-}4 \end{array}$$

$$\begin{array}{l} X + Y + Z + U + V = 33 \\ X \geq 10, \, Y \geq \text{-2}, \, Z \geq 9, \, U \geq 7, \, V \geq 3 \end{array}$$

$$\begin{array}{l} X+Y+Z=24 \\ X\geq 0,\,Y\geq 9,\,Z\geq 8 \end{array}$$

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U + V = 9 \\ X \geq \text{-6}, \, Y \geq 3, \, Z \geq 5, \, U \geq 5, \, V \geq 0 \end{array}$$

Number of Solutions:

$$\begin{array}{l} X \, + \, Y \, + \, Z \, + \, U \, = \, 14 \\ X \, \geq \, 9, \, Y \, \geq \, \text{--7}, \, Z \, \geq \, 2, \, U \, \geq \, 3 \end{array}$$

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U + V + W = 15 \\ X \geq 10, \, Y \geq \mbox{-4}, \, Z \geq 4, \, U \geq 2, \, V \geq 7, \, W \geq \mbox{-5} \end{array}$$

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U + V = 23 \\ X \geq 0, \, Y \geq \mbox{-}2, \, Z \geq 2, \, U \geq 10, \, V \geq 10 \end{array}$$

$$\begin{array}{l} X + Y + Z + U + V = 5 \\ X \geq -8, \, Y \geq -1, \, Z \geq 7, \, U \geq 7, \, V \geq -6 \end{array}$$

$$\begin{array}{l} X + Y + Z + U + V = 17 \\ X \geq 9, \, Y \geq 7, \, Z \geq \text{--}1, \, U \geq \text{--}6, \, V \geq 2 \end{array}$$

Number of Solutions:

$$\begin{array}{l} X+Y+Z+U=5 \\ X\geq 1,\,Y\geq 1,\,Z\geq \mbox{-}1,\,U\geq \mbox{-}2 \end{array}$$

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U = 18 \\ X \geq 4, \, Y \geq \mbox{--}1, \, Z \geq 3, \, U \geq 5 \end{array}$$

Number of Solutions:

$$X + Y + Z + U + V = -2$$
  
 $X \ge -9, Y \ge 10, Z \ge -10, U \ge -4, V \ge 8$ 

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U + V = 19 \\ X \geq 10, \, Y \geq \mbox{-4}, \, Z \geq 3, \, U \geq 10, \, V \geq \mbox{-2} \end{array}$$

$$\begin{array}{l} X+Y+Z+U=6 \\ X\geq 7,\,Y\geq 5,\,Z\geq \text{-}9,\,U\geq \text{-}4 \end{array}$$

$$X + Y + Z + U = 18$$
  
 $X \ge 8, Y \ge -2, Z \ge 8, U \ge 1$ 

Number of Solutions:

$$\begin{split} X+Y+Z+U&=14\\ X\geq -1,\,Y\geq 8,\,Z\geq 2,\,U\geq -1 \end{split}$$

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U + V = 12 \\ X \geq -4, \, Y \geq 9, \, Z \geq -5, \, U \geq 6, \, V \geq 4 \end{array}$$

Number of Solutions:

$$X + Y + Z + U = 25$$
  
 $X \ge 5, Y \ge -1, Z \ge 8, U \ge 8$ 

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U + V = 31 \\ X \geq 8, \, Y \geq 0, \, Z \geq 7, \, U \geq 5, \, V \geq 5 \end{array}$$

$$\begin{array}{l} X + Y + Z + U + V = -9 \\ X \geq -5, \, Y \geq 8, \, Z \geq 3, \, U \geq -7, \, V \geq -10 \end{array}$$

$$\begin{array}{l} X + Y + Z + U + V + W = 5 \\ X \geq 9, \, Y \geq \text{--7}, \, Z \geq \text{--10}, \, U \geq 10, \, V \geq \text{--7}, \, W \geq 9 \end{array}$$

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U = -15 \\ X \geq -9, \, Y \geq 2, \, Z \geq -2, \, U \geq -9 \end{array}$$

Number of Solutions:

$$\begin{array}{l} X + Y + Z + U + V + W = 26 \\ X \geq \text{-3}, \, Y \geq 7, \, Z \geq 4, \, U \geq 8, \, V \geq 3, \, W \geq 3 \end{array}$$

Number of Solutions:

$$X + Y + Z + U + V = -6$$
  
 $X \ge -2, Y \ge 3, Z \ge -2, U \ge -4, V \ge -4$ 

Number of Solutions:

$$X + Y + Z = 6$$
  
 $X \ge -2, Y \ge 8, Z \ge -7$ 

$$\begin{array}{l} X+Y+Z+U=16 \\ X\geq 4,\,Y\geq 2,\,Z\geq 10,\,U\geq \text{--}7 \end{array}$$

$$\begin{array}{l} X + Y + Z + U + V + W = 6 \\ X \geq 2, \, Y \geq 2, \, Z \geq \text{--7}, \, U \geq \text{--2}, \, V \geq \text{--1}, \, W \geq 7 \end{array}$$