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1 import numpy as np
2 # Setting the random seed, feel free to change it and see different solutions.
3 np.random.seed(42)
4
5 def stepFunction(t):
6     if t >= 0:
7         return 1
8     return 0
9
10 def prediction(X, W, b):
11     return stepFunction((np.matmul(X,W)+b)[0])
12
13 # TODO: Fill in the code below to implement the perceptron trick.
14 # The function should receive as inputs the data X, the labels y,
15 # the weights W (as an array), and the bias b,
16 # update the weights and bias W, b, according to the perceptron algorithm,
17 # and return W and b.
18 def perceptronStep(X, y, W, b, learn_rate = 0.01):
19     # Fill in code
20     # X = the array of 100 rows, 2 columns -
21     #     first col: x1 coord,
22     #     second col: x2 coord
23     # y = the label 0 or 1, 0 => fail, 1 => pass
24     # W => the initial set of weights
25     # b => some initial bias
26     for i in range(len(X)):
27         pred = prediction(X[i], W, b);
28         # print (pred)
29         if (pred == 1 and y[i] != 1):
30             # we need to move the line up
31             W[0] = W[0] - X[i][0]*learn_rate
32             W[1] = W[1] - X[i][1]*learn_rate
33             b -= learn_rate
34
35         elif (pred == 0 and y[i] != 0):
36             # we need to move the line down
37             W[0] = W[0] + X[i][0]*learn_rate
38             W[1] = W[1] + X[i][1]*learn_rate
39             b += learn_rate
40
41     return W, b
42
43 # This function runs the perceptron algorithm repeatedly on the dataset,
44 # and returns a few of the boundary lines obtained in the iterations,
45 # for plotting purposes.
46 # Feel free to play with the learning rate and the num_epochs,
47 # and see your results plotted below.
48 def trainPerceptronAlgorithm(X, y, learn_rate = 0.01, num_epochs = 25):
49     x_min, x_max = min(X.T[0]), max(X.T[0])
50     y_min, y_max = min(X.T[1]), max(X.T[1])
51     W = np.array(np.random.rand(2,1))
52     b = np.random.rand(1)[0] + x_max
53     # These are the solution lines that get plotted below.
54     boundary_lines = []
55     for i in range(num_epochs):
56         # In each epoch, we apply the perceptron step.
57         W, b = perceptronStep(X, y, W, b, learn_rate)
58         boundary_lines.append((-W[0]/W[1], -b/W[1]))
59     return boundary_lines
60

```