Lab 1: Computation & Data Representations

Due Date: Thursday 2/2/2017 11:59PM

This lab covers the first two lectures. Feel free to refer to my lecture notes (posted on the course page) and the recommended textbook (Patt & Patel) Chapters 1 and 2. Be sure to go to your labs on Friday to get assistance from the TAs. When you encounter a number written x_y you should read it as "x in base y." For example, 2_{10} means "2 base 10" (decimal 2) and 10_2 means "10 base 2" (binary 10, same thing as decimal 2). Numbers without a subscript are assumed to be in decimal.

If you're unsure about a result, be sure to explain your thinking. In general, you should show your work. A well-reasoned but wrong answer (for example with a minor error) will receive more points than a wrong answer with no context at all.

Problems (100 points total)

- 1. For the following, use no more than 3 sentences in your answer.
 - a) Succinctly explain Turing's thesis.
 - b) What are the components of a Turing machine?
- 2. Explain some advantages digital computers have over analog computers.
- 3. How would one write 9_{10} in *unary* (base one)?
- 4. Write out the following numbers in terms of powers of 2. Omit the powers of 2 that are not present. For example, 43_{10} would be written as:

$$(1 \times 2^5) + (1 \times 2^3) + (1 \times 2^1) + (1 \times 2^0)$$

- a) 32
- b) 15
- c) 65
- d) 10
- 5. Convert 11101_2 to decimal. Assume it is unsigned.
- 6. Solve for x in

$$2^x = 00100000_2$$

7. Convert 01011001_2 to decimal. Assume unsigned again.

- 8. a) Given a 4-bit string of binary digits, how many unique binary strings are there?
 - b) What's the largest *unsigned* integer we can represent with this many bits?
 - c) How many unique binary strings for an n-bit string?
 - d) And the largest unsigned integer with n bits?
- 9. Add 20 and 35 *in binary* (give the answer in binary). Assume 8-bit unsigned integers. Show your work.
- 10. Subtract 20 from 87 in binary. Again, 8-bit unsigned.
- 11. Take the *one's complement* of 01110101_2 . Give the result in binary and in decimal.
- 12. a) We have a 7-bit signed, *two's complement* integer. What are the maximum (most positive) and minimum (most negative) values we can represent with it?
 - b) For an *n*-bit signed, 2's complement int, what are the most positive and negative numbers we can represent?
- 13. Fill in the rows in the following table. The first row is an example for your reference. Put an X when the number cannot be represented. Assume 6 bits.

Number	Signed Magnitude	One's Comp.	Two's Comp	Unsigned
-10	101010	110101	110110	X
-6				
7				
-1				
10				
-32				
31				

14. Subtract 10_{10} from 7_{10} (7-10) in binary using 6-bit, signed, 2's complement integers. **Hint**: x-y=x+(-y).

Hand-in Instructions

Make sure to put your name on your submission. Submissions without names will be given zero points!

Physical: If you're submitting a written copy, hand it to one of the TAs or to the instructor. You can also leave it in the instructor's mailbox in the CS department office, but make sure to get it time stamped when you do (see the "Submitting Work" section of the syllabus).

Digital: If you would like to submit an electronic copy, note that I will only accept PDF files (no Word docs please). Again, see the "Submitting Work" section of the syllabus. Please do not take a poorly lit picture of your assignment. Your grade will suffer commensurately with our inability to read your work. Once you have a PDF, you should submit it on fourier. You should name your file yourid-labl.pdf where yourid is the thing in front of the @hawk.iit.edu in your e-mail address.

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