

# SCORECARD

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## Default Definition and Data Preparation

Following Basel II principles

*"A default is considered to have occurred when:*

*the banking institution considers that an obligor is unlikely to repay in full its credit obligations to the banking group,*

*without recourse by the banking institution to actions such as realising security;*

*or the obligor has breached its contractual repayment schedule and is past due for more than 90 days on any material credit obligation to the banking group"*

From an IFRS 9 perspective, Section B5.5.37 of IASB (2014) does not directly define default, but requires entities to align with internal credit risk management

From a FASB (2016) standpoint,

*"Estimating expected credit losses is highly judgmental and generally will require an entity to make specific judgments.*

*Those judgments may include any of the following: a. The definition of default for default-based statistics ..."*

As standard practice, one may consider the following definition:

**Quantitative indicators.**

90 days past due (DPD) or 3 months in arrears (MIA) are common default triggers. A counter is put in place to account for delays or arrears balance

**Qualitative indicators.**

Bankruptcy

Balance due after maturity/expiry

Others (Forbearance)



## Default Definition and Data Preparation

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**Qualitative indicators.**

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Formula Bar



### Data Preparation

To build a PD base, we need an account to be non-defaulted /up-to-date/ Current status in the beginning of the year and default at least once within the year.

Let's consider the following account. The time points correspond to month beginnings.

■ up-to-date   
 ■ Default   
 ■ Cure   
 ■ Write-off

	Year 1												Year 2												Year 3												Year 4											
months	1	2	3	4	5	6	7	8	9	10	11	12	1	2	3	4	5	6	7	8	9	10	11	12	1	2	3	4	5	6	7	8	9	10	11	12	1	2	3	4	5	6	7	8	9	10	11	12
Events																																																

#### Under Instant Cure method

- ✓ for Y1 : Account is up-to-date in the beginning and has defaulted in the year.  
So, it will enter in PD base for year 1.
- ✓ for Y2 : Since, account cures instantly, it will be in up-to-date status in the beginning of year 2.  
The Account does default in year 2 as well.  
So, it will enter in PD base for year 2.
- ✗ for Y3 : Since the account does not cure in year 2, the status of the account in the beginning of year 3 will be Defaulted.  
So, it will not enter in the PD base for year 3.
- ✗ for Y4 : Since, the account is already written off in year 3, it won't enter in PD base for year 4.

#### Under Probationary period method

- ✓ for Y1 : Account is up-to-date in the beginning and has defaulted in the year.  
So, it will enter in PD base for year 1.
- ✗ for Y2 : Since, account cures on month 10, it will be under probation till month 3 of Year2 and will be in Defaulted status in this period. Therefore, the Account Status in the beginning of year 2 will be Defaulted.  
So, it will not enter in PD base for year 2.
- ✗ for Y3 : Since the account does not cure in year 2, the status of the account in the beginning of year 3 will be Defaulted.  
So, it will not enter in the PD base for year 3.
- ✗ for Y4 : Since, the account is already written off in year 3, it won't enter in PD base for year 4.

### Default Definition (Bad flag creation) and Data Preparation

#### Bad Flag creation

Default Event will be set to 1 if one or more of the following three conditions is TRUE.

Account is at least in 3m arrears (arrears\_event = 1)

Account is declared bankrupt (bankruptcy\_event = 1)

Account has residual outstanding balance after maturity (term\_expiry\_event = 1)

#### Train , Test split

The observations are randomly split based on a desired ratio (Training Set & Testing Set)

We will use rand() function to categorize observations into training and testing (it will be an approximate split)

It is important to ensure default rates are comparable between Training and Testing sets.

Sl	id	vintage_ye	monthly_installme	loan_balanc	bureau_sco	num_bankrupt_i	time_since_bankrup	num_x	time_since_c	ccj_amou	num_bankrup	num_i	min_months_since_bankrup	pl_fl	regi	ltv	arrears_montl	origination_da	ma
1	6670001	2005	746.7	131304.44	541	0	0	0	0	0	0	0	0	1	r_a	0.7586	0	14-09-2005	3
2	9131199	2006	887.4	115486.51	441	0	0	0	0	0	0	0	0	1	r_b	0.6973	0	20-01-2006	3
3	4963167	2004	1008.5	128381.73	282	0	0	1	36	459	0	0	0	0	r_c	0.6959	2.188230045	21-12-2004	3
4	3918582	2005	458.23	35482.96	461	0	0	0	0	0	0	0	0	0	r_d	0.1099	0	21-06-2005	3
5	5949777	2006	431.2	77086.31	466	0	0	0	0	0	0	0	0	1	r_e	0.3776	0	19-07-2006	3
6	1868971	2005	228.86	40380.63	470	0	0	0	0	0	0	0	0	0	r_c	0.2192	0	13-09-2005	3
7	8656464	2004	370.21	44978.8	515	0	0	0	0	0	0	0	0	1	r_c	0.4727	0	29-07-2004	3
8	2347301	2005	1665.05	440127.97	487	0	0	0	0	0	0	0	0	0	r_f	0.5215	0	27-09-2005	3
9	7372573	2007	397.1	100918.22	NA	NA	NA	NA	NA	NA	NA	NA	NA	1	r_g	0.9995	1.775698816	31-01-2007	3
10	7843579	2004	615.51	77337.43	307	0	0	0	0	0	0	0	0	0	r_h	0.4302	0	16-12-2004	3
11	4066165	2005	471.44	125415.07	367	0	0	0	0	0	0	0	0	0	r_c	0.8256	0.607924656	06-10-2005	3
12	3188782	2007	334.7	83965.1	328	0	0	0	0	0	0	0	0	1	r_a	1.078	0	23-04-2007	3
13	3581494	2006	771.3	194978.99	518	0	0	0	0	0	0	0	0	1	r_h	0.862	0	22-06-2006	3
14	8028525	2005	363	56273.26	428	0	0	0	0	0	0	0	0	1	r_a	0.6885	0	14-12-2005	3
15	5253590	2003	321.16	80971.8	472	0	0	0	0	0	0	0	0	1	r_d	0.7259	0	29-10-2003	3
16	3510252	2007	437.9	59906.35	427	0	0	0	0	0	0	0	0	1	r_i	0.709	0	06-03-2007	3
17	7042373	2006	189.7	191292.23	430	0	0	0	0	0	0	0	0	0	r_d	0.8023	0	16-01-2006	3
18	6838892	2006	372.32	98419.41	426	0	0	0	0	0	0	0	0	0	r_e	0.2471	0	24-04-2006	3
19	3691330	2007	976.02	257951.62	458	0	0	0	0	0	0	0	0	0	r_a	0.8819	0	07-03-2007	3
20	1108986	2003	370	13120.04	537	0	0	0	0	0	0	0	0	0	r_g	0.1028	0	14-11-2003	3
21	1567700	2006	1002.99	113546.28	180	0	0	0	0	0	0	0	0	1	r_e	0.3749	0	24-04-2006	3
22	8007790	2005	777.2	119226.81	494	0	0	0	0	0	0	0	0	1	r_g	0.7808	0	16-05-2005	3
23	4149143	2005	527.46	139325.95	365	1	56	1	56	0	0	1	0	0	r_d	0.6523	0	25-04-2005	3
24	1848036	2006	505.7	127972.39	502	0	0	0	0	0	0	0	0	1	r_d	0.6869	0	25-05-2006	3
25	3966099	2006	1286.8	340015.6	378	0	0	0	0	0	0	0	0	0	r_l	0.7559	0	20-12-2006	3
26	8534650	2007	574.11	94911.49	444	0	0	0	0	0	0	0	0	0	r_d	0.2331	0	24-05-2007	3
27	8452715	2006	762.84	104257.5	417	0	0	0	0	0	0	0	0	0	r_d	0.512	0	09-11-2006	3
28	4093539	2007	388.9	85946.99	213	0	0	0	0	0	0	0	0	1	r_h	0.8805	0	22-03-2007	3
29	3337583	2006	591.27	164732.04	494	0	0	0	0	0	0	0	0	0	r_b	0.5028	0	21-11-2006	3
30	8033354	2006	565.4	139603.15	160	0	0	0	0	0	0	0	0	1	r_d	0.7772	0	08-05-2006	3
31	1832358	2006	761.06	188346.73	278	0	0	0	0	0	0	0	0	0	r_e	0.2454	0	02-11-2006	3
32	1909666	2004	402.66	57664.72	363	0	0	0	0	0	0	0	0	1	r_c	0.6812	0	05-04-2004	3
33	8438164	2005	152.21	16658.53	539	0	0	0	0	0	0	0	0	0	r_i	0.1736	0	31-08-2005	3
34	9023854	2007	410.6	88083.64	227	0	0	0	0	0	0	0	0	0	r_d	0.2409	0	04-04-2007	3
35	5252710	2006	218.2	125401.41	406	0	0	0	0	0	0	0	0	0	r_h	0.9391	0	23-02-2006	2
36	2425429	2005	226	29211.8	469	0	0	0	0	0	0	0	0	0	r_g	0.4817	0	27-10-2005	3
37	7134595	2007	721.74	99138.37	119	0	0	0	0	0	0	0	0	1	r_e	0.1854	0	22-05-2007	3
38	6063761	2005	641.37	81090.98	518	0	0	0	0	0	0	0	0	0	r_g	0.6634	0	30-03-2005	3
39	5705263	2005	551.16	95579.7	561	0	0	0	0	0	0	0	0	0	r_e	0.276	0	20-06-2005	3
40	5130189	2002	179.2	13311.42	361	0	0	0	0	0	0	0	0	0	r_m	0.1167	0	19-12-2002	3
41	7172370	2005	771.56	172139.71	514	0	0	0	0	0	0	0	0	0	r_b	0.8239	0	10-08-2005	3
42	2451709	2006	445.4	79204.01	473	0	0	0	0	0	0	0	0	1	r_c	0.8025	0	18-07-2006	3



PEAKS2TAILS

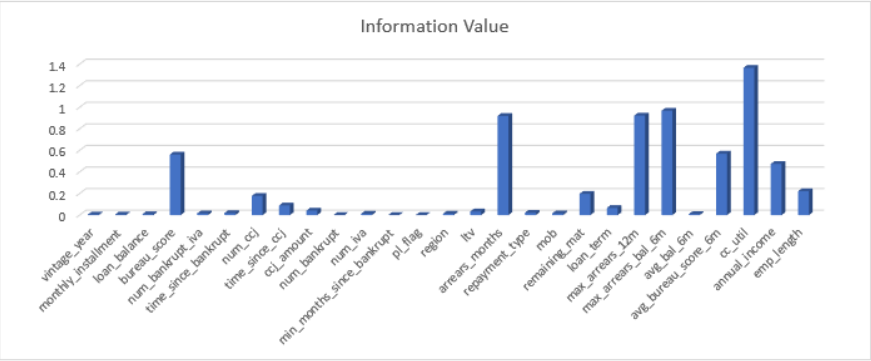
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	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P				
1																				
2																				
3		Testing Set			Gross Default rate		5.49%													
4																				
5		SL	Default	id	vintage_year	monthly_installment	loan_balance	bureau_score	num_bankrupt_iva	time_since_bankrupt	num_ccj	time_since_ccj	ccj_amount	num_bankrupt	num_iva	min_months_since_bankrupt	pl_flag	region	ltv	arrears
6		1	0	6670001	2005	746.7	131304.44	541	0	0	0	0	0	0	0	0	1	r_a	0.7586	
7		2	0	9131199	2006	887.4	115486.51	441	0	0	0	0	0	0	0	0	1	r_b	0.6973	
8		3	1	4963167	2004	1008.5	128381.73	282	0	0	1	36	459	0	0	0	0	r_c	0.6959	2.18
9		5	0	5949777	2006	431.2	77086.31	466	0	0	0	0	0	0	0	0	1	r_e	0.3776	
10		11	0	4066165	2005	471.44	125415.07	367	0	0	0	0	0	0	0	0	0	r_c	0.8256	0.60
11		19	0	3691330	2007	976.02	257951.62	458	0	0	0	0	0	0	0	0	0	r_a	0.8819	
12		23	0	4149143	2005	527.46	139325.95	365	1	56	1	56	0	0	1	0	0	r_d	0.6523	
13		24	0	1848036	2006	505.7	127972.39	502	0	0	0	0	0	0	0	0	1	r_d	0.6869	
14		27	0	8452715	2006	762.84	104257.5	417	0	0	0	0	0	0	0	0	0	r_d	0.512	
15		30	0	8033354	2006	565.4	139603.15	160	0	0	0	0	0	0	0	0	1	r_d	0.7772	
16		34	0	9023854	2007	410.6	88083.64	227	0	0	0	0	0	0	0	0	0	r_d	0.2409	
17		36	0	2425429	2005	226	29211.8	469	0	0	0	0	0	0	0	0	0	r_g	0.4817	
18		39	0	5705263	2005	551.16	95579.7	561	0	0	0	0	0	0	0	0	0	r_e	0.276	
19		48	0	6317615	2007	448.49	81019.68	195	0	0	0	0	0	0	0	0	1	r_c	0.8336	
20		53	0	3682722	2004	703.4	185883.99	505	0	0	0	0	0	0	0	0	0	r_f	0.5197	
21		56	0	2429741	2006	661.81	67241.82	499	0	0	0	0	0	0	0	0	0	r_e	0.2828	
22		60	0	7555242	2005	790.86	101770.69	268	0	0	0	0	0	0	0	0	1	r_l	0.6281	
23		61	0	8431952	2005	325.9	37927.29	350	0	0	0	0	0	0	0	0	1	r_c	0.4715	
24		62	0	4221098	2006	1537.11	209038.72	208	0	0	1	16	8822	0	0	0	0	r_i	0.4537	1.7
25		63	0	5099527	2006	262.15	35837.51	520	0	0	0	0	0	0	0	0	0	r_c	0.2252	
26		66	0	9601371	2005	569.87	143047.4	411	1	42	1	42	0	0	1	0	0	r_e	0.4379	
27		68	0	7171719	2004	703.8	53883.7	540	0	0	0	0	0	0	0	0	1	r_l	0.3695	
28		72	0	6444874	2007	234.4	58669.11	454	0	0	0	0	0	0	0	0	1	r_i	0.9577	
29		74	0	3126447	2006	750.56	122569.63	352	0	0	0	0	0	0	0	0	0	r_c	0.7675	
30		77	0	5512049	2005	300.78	53486.58	NA	NA	NA	NA	NA	NA	NA	NA	NA	1	r_g	0.8612	
31		86	0	3743439	2007	881.43	161787.35	NA	NA	NA	NA	NA	NA	NA	NA	NA	0	r_h	0.6758	
32		91	0	7889331	2006	678.3	171327.29	348	0	0	1	69	9550	0	0	0	0	r_f	0.6167	
33		94	0	7666011	2006	987.36	161265.41	563	0	0	0	0	0	0	0	0	0	r_d	0.6905	
34		96	0	4193714	2003	907.54	87202.81	318	0	0	0	0	0	0	0	0	0	r_h	0.7002	
35		103	0	1873590	2006	359.99	95121.12	306	0	0	0	0	0	0	0	0	0	r_e	0.3945	
36		105	0	4049563	2004	79.77	21084.66	542	0	0	0	0	0	0	0	0	0	r_i	0.1392	
37		108	0	2957269	2006	859.94	114286.13	343	1	63	0	0	0	1	0	63	0	r_c	0.7679	
38		109	0	3096903	2005	459.5	115783.16	343	0	0	0	0	0	0	0	0	1	r_a	0.8563	
39		112	0	9579301	2006	387.7	98962.7	205	0	0	0	0	0	0	0	0	1	r_l	0.898	
40		113	0	7089380	2005	479.65	61028.24	539	0	0	0	0	0	0	0	0	1	r_e	0.3369	
41		118	0	4561644	2005	609.57	77198.25	448	0	0	0	0	0	0	0	0	0	r_g	0.7519	
42		130	0	8796368	2004	934.1	200980.8	247	0	0	1	38	3666	0	0	0	0	r_g	1.0034	1.46
43		137	0	4913838	2006	871.04	113306.69	392	0	0	0	0	0	0	0	0	1	r_g	0.7759	
44		141	0	7858458	2006	466	73609.61	517	0	0	0	0	0	0	0	0	1	r_e	0.2444	
45		145	0	5737866	2006	522.6	88533.76	229	0	0	0	0	0	0	0	0	1	r_c	0.768	0.78
46		152	0	3903550	2007	436.33	60920.46	453	0	0	0	0	0	0	0	0	0	r_i	0.7665	
47		153	0	5818601	2006	824.2	131124.79	291	0	0	0	0	0	0	0	0	1	r_d	0.6516	



	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y
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Variables	IV
vintage_year	0.00475
monthly_installment	0.00514
loan_balance	0.00845
bureau_score	0.56076
num_bankrupt_iva	0.01517
time_since_bankrupt	0.0182
num_ccj	0.17735
time_since_ccj	0.08907
ccj_amount	0.04142
num_bankrupt	0.001
num_iva	0.01172
min_months_since_bankrupt	0.00083
pl_flag	0.00025
region	0.01221
ltv	0.03341
arrears_months	0.9191
repayment_type	0.02158
mob	0.01549
remaining_mat	0.19698
loan_term	0.0665
max_arrears_12m	0.92283
max_arrears_bal_6m	0.96793
avg_bal_6m	0.0091
avg_bureau_score_6m	0.56911
cc_util	1.36593
annual_income	0.47443
emp_length	0.22107
months_since_recent_cc_delinq	0.37367

**Most Prominent variables (IV > 0.4)**

bureau\_score  
 arrears\_months (dropped since it is repeated)  
 max\_arrears\_12m  
 max\_arrears\_bal\_6m  
 avg\_bureau\_score\_6m (dropped since it is repeated)  
 cc\_util  
 annual\_income

**Medium Important** (included as part of expert judgement)

num\_ccj  
 emp\_length  
 months\_since\_recent\_cc\_delinq

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
1																
2																
3		WOE Transformed (Training Set)														
4																
5		Default	bureau_score	max_arrears_12m	max_arrears_bal_6m	cc_util	annual_income	num_ccj	emp_length	months_since_recent_cc_delinq						
6		0	0.848988348	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.519371295	-0.379586857						
7		1	0.848988348	0.446897907	0.605966823	-0.7399926	0.324421315	0.182549	-0.382216378	-0.359844634						
8		0	1.075105467	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.88879147	1.036190088						
9		0	0.848988348	0.446897907	0.605966823	1.14072133	0.056834275	0.182549	-0.180192003	-0.359844634						
10		1	-0.232100523	-1.708298136	-1.371963137	-1.9129446	-0.641267459	-0.2321	-0.306787205	-0.359844634						
11		0	-0.100424502	0.446897907	0.605966823	1.14072133	-0.641267459	0.182549	-0.860408385	1.036190088						
12		0	-0.100424502	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.627726273	1.036190088						
13		0	1.075105467	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	-0.180192003	-0.359844634						
14		0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.439573656	-0.359844634						
15		0	0.848988348	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.520370796	-0.379586857						
16		0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.519371295	-0.379586857						
17		0	0.848988348	0.446897907	0.605966823	-0.7399926	-0.641267459	0.182549	-0.306787205	-0.359844634						
18		0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.211585475	-0.359844634						
19		0	1.075105467	0.446897907	0.605966823	-0.7399926	0.324421315	0.182549	0.211585475	-0.359844634						
20		0	-1.178027211	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.627726273	-0.379586857						
21		0	0.848988348	0.446897907	0.605966823	-1.9129446	0.056834275	0.182549	0.519371295	1.036190088						
22		0	-0.100424502	0.446897907	0.605966823	-0.7399926	0.324421315	0.182549	-0.306787205	-0.359844634						
23		0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.439573656	-0.379586857						
24		0	-0.684965808	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.519371295	1.036190088						
25		0	0.848988348	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.211585475	-0.359844634						
26		0	-0.684965808	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.211585475	1.036190088						
27		0	-0.100424502	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.520370796	-0.359844634						
28		0	1.075105467	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.211585475	-0.379586857						
29		1	0.848988348	0.446897907	0.605966823	1.14072133	-0.641267459	0.182549	-0.382216378	1.036190088						
30		0	-1.178027211	0.446897907	0.605966823	-1.9129446	0.659648047	0.182549	0.520370796	-0.379586857						
31		0	1.075105467	0.446897907	0.605966823	1.14072133	-0.641267459	0.182549	0.211585475	-0.379586857						
32		0	-0.100424502	0.446897907	0.605966823	-0.7399926	0.056834275	0.182549	0.211585475	-0.379586857						
33		0	1.075105467	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	-0.306787205	-0.359844634						
34		0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.439573656	-0.359844634						
35		0	-0.100424502	0.446897907	0.605966823	1.14072133	-0.641267459	0.182549	0.211585475	-0.379586857						
36		0	-0.100424502	0.446897907	0.605966823	-1.9129446	-0.641267459	-0.84072	-0.382216378	-0.359844634						
37		0	-0.100424502	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	-0.180192003	1.036190088						
38		0	-0.100424502	0.446897907	0.605966823	-0.7399926	0.659648047	0.182549	0.520370796	-0.379586857						
39		0	-0.100424502	0.446897907	-1.371963137	1.14072133	0.324421315	-0.84072	0.520370796	-0.379586857						
40		0	-0.100424502	0.446897907	0.605966823	1.14072133	0.056834275	0.182549	0.627726273	1.036190088						
41		0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.439573656	-0.359844634						
42		0	-1.178027211	-1.708298136	-1.371963137	-1.9129446	0.324421315	-0.9376	-0.306787205	-0.379586857						
43		0	-0.684965808	0.446897907	0.605966823	1.14072133	-0.641267459	-0.84072	-0.860408385	1.036190088						
44		0	-0.100424502	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.88879147	1.036190088						
45		0	-0.684965808	-2.643118019	0.605966823	1.14072133	0.324421315	-0.84072	0.519371295	-0.379586857						
46		0	0.848988348	0.446897907	0.605966823	-0.7399926	0.324421315	0.182549	-0.382216378	-0.379586857						
47		0	-0.100424502	0.446897907	0.605966823	-1.9129446	-0.641267459	0.182549	-0.382216378	-0.359844634						
48		0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.519371295	1.036190088						

### WOE Transformed (Training Set)

Default	bureau_score	max_arrears_12m	max_arrears_bal_6m	cc_util	annual_income	num_ccj	emp_length	months_since_recent_cc_delinq
0	0.848988348	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.519371295	-0.379586857
1	0.848988348	0.446897907	0.605966823	-0.7399926	0.324421315	0.182549	-0.382216378	-0.359844634
0	1.075105467	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.88879147	1.036190088
0	0.848988348	0.446897907	0.605966823	1.14072133	0.056834275	0.182549	-0.180192003	-0.359844634
1	-0.232100523	-1.708298136	-1.371963137	-1.9129446	-0.641267459	-0.2321	-0.306787205	-0.359844634
0	-0.100424502	0.446897907	0.605966823	1.14072133	-0.641267459	0.182549	-0.860408385	1.036190088
0	-0.100424502	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.627726273	1.036190088
0	1.075105467	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	-0.180192003	-0.359844634
0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.439573656	-0.359844634
0	0.848988348	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.520370796	-0.379586857
0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.519371295	-0.379586857
0	0.848988348	0.446897907	0.605966823	-0.7399926	-0.641267459	0.182549	-0.306787205	-0.359844634
0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.211585475	-0.359844634
0	1.075105467	0.446897907	0.605966823	-0.7399926	0.324421315	0.182549	0.211585475	-0.359844634
0	-1.178027211	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.627726273	-0.379586857
0	0.848988348	0.446897907	0.605966823	-1.9129446	0.056834275	0.182549	0.519371295	1.036190088
0	-0.100424502	0.446897907	0.605966823	-0.7399926	0.324421315	0.182549	-0.306787205	-0.359844634
0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.439573656	-0.379586857
0	-0.684965808	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.519371295	1.036190088
0	0.848988348	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.211585475	-0.359844634
0	-0.684965808	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.211585475	1.036190088
0	-0.100424502	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.520370796	-0.359844634
0	1.075105467	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	0.211585475	-0.379586857
1	0.848988348	0.446897907	0.605966823	1.14072133	-0.641267459	0.182549	-0.382216378	1.036190088
0	-1.178027211	0.446897907	0.605966823	-1.9129446	0.659648047	0.182549	0.520370796	-0.379586857
0	1.075105467	0.446897907	0.605966823	1.14072133	-0.641267459	0.182549	0.211585475	-0.379586857
0	-0.100424502	0.446897907	0.605966823	-0.7399926	0.056834275	0.182549	0.211585475	-0.379586857
0	1.075105467	0.446897907	0.605966823	1.14072133	0.324421315	0.182549	-0.306787205	-0.359844634
0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.439573656	-0.359844634
0	-0.100424502	0.446897907	0.605966823	1.14072133	-0.641267459	0.182549	0.211585475	-0.379586857
0	-0.100424502	0.446897907	0.605966823	-1.9129446	-0.641267459	-0.84072	-0.382216378	-0.359844634
0	-0.100424502	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	-0.180192003	1.036190088
0	-0.100424502	0.446897907	0.605966823	-0.7399926	0.659648047	0.182549	0.520370796	-0.379586857
0	-0.100424502	0.446897907	-1.371963137	1.14072133	0.324421315	-0.84072	0.520370796	-0.379586857
0	-0.100424502	0.446897907	0.605966823	1.14072133	0.056834275	0.182549	0.627726273	1.036190088
0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.439573656	-0.359844634
0	-1.178027211	-1.708298136	-1.371963137	-1.9129446	0.324421315	-0.9376	-0.306787205	-0.379586857
0	-0.684965808	0.446897907	0.605966823	1.14072133	-0.641267459	-0.84072	-0.860408385	1.036190088
0	-0.100424502	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.88879147	1.036190088
0	-0.684965808	-2.643118019	0.605966823	1.14072133	0.324421315	-0.84072	0.519371295	-0.379586857
0	0.848988348	0.446897907	0.605966823	-0.7399926	0.324421315	0.182549	-0.382216378	-0.379586857
0	-0.100424502	0.446897907	0.605966823	-1.9129446	-0.641267459	0.182549	-0.382216378	-0.359844634
0	0.848988348	0.446897907	0.605966823	1.14072133	0.659648047	0.182549	0.519371295	1.036190088



### Multivariate Analysis

	bureau_score	max_arrears_12m	max_arrears_bal_6m	cc_util	annual_income	num_ccj	emp_length	months_since_recent_cc_delinq
bureau_score	1	0.266246184	0.321168348	0.054	0.022599645	0.35108	0.005446495	0.024246518
max_arrears_12m	0.266246184	1	0.701763068	0.1096	0.065276107	0.19883	0.032128934	0.042527845
max_arrears_bal_6m	0.321168348	0.701763068	1	0.0988	0.059666063	0.213646	0.0299829	0.032641582
cc_util	0.054001383	0.109595561	0.098803204	1	0.061351839	0.040001	0.03022804	0.302193037
annual_income	0.022599645	0.065276107	0.059666063	0.06135	1	0.02938	0.512690878	0.036437727
num_ccj	0.351080139	0.198830077	0.213646372	0.04	0.029380478	1	0.017346211	0.01929747
emp_length	0.005446495	0.032128934	0.0299829	0.03023	0.512690878	0.017346	1	0.008514278
months_since_recent_cc_delinq	0.024246518	0.042527845	0.032641582	0.30219	0.036437727	0.019297	0.008514278	1

max\_arrears\_bal\_6m will be dropped as it is highly correlated with max\_arrears\_12m

### The Final Selection of variables

bureau\_score  
 max\_arrears\_12m  
 cc\_util  
 annual\_income  
 num\_ccj  
 emp\_length  
 months\_since\_recent\_cc\_delinq



PEAKS<sup>2</sup>TAILS[illegible]

 $\min AIC$ 

6131.777902

	-2.911680374	-0.999998675				-2.91168	-1.000001147				-2.91168	-1.000001073			
Default	Intercept	bureau_score	P(1)	ylnP(1) + (1-y)ln(1-P(1))		Default	Intercept	max_arrears_12m	P(1)	ylnP(1) + (1-y)ln(1-P(1))	Default	Intercept	cc_util	P(1)	ylnP(1) + (1-y)ln(1-P(1))
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
1	-2.911680374	0.848988348	0.022739	-3.783669222		1	-2.91168	0.446897907	0.033615	-3.392770773	1	-2.91168	-0.739992552	0.102322	-2.279632819
0	-2.911680374	1.075105467	0.018221	-0.018389175		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
1	-2.911680374	-0.232100523	0.064189	-2.745922002		1	-2.91168	-1.708298136	0.230875	-1.465880223	1	-2.91168	-1.912944649	0.26919	-1.312337691
0	-2.911680374	-0.100424502	0.056719	-0.058390997		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	-0.100424502	0.056719	-0.058390997		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	1.075105467	0.018221	-0.018389175		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168	0.446897907	0.033615	-0.034193395	0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.911680374	0.848988348	0.022739	-0.023001624		0	-2.91168								



 $\min AIC$ 

6131.777902

	-2.91168	-1.000001073		
Default	Intercept	cc_util	P(1)	ylnP(1) + (1-y)ln(1-P(1))
0	-2.91168	1.14072133	0.017084	-0.017231208
1	-2.91168	-0.739992552	0.102322	-2.279632819
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
1	-2.91168	-1.912944649	0.26919	-1.312337691
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	-0.739992552	0.102322	-0.107943594
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	-0.739992552	0.102322	-0.107943594
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	-1.912944649	0.26919	-0.313601822
0	-2.91168	-0.739992552	0.102322	-0.107943594
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
1	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	-1.912944649	0.26919	-0.313601822
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	-0.739992552	0.102322	-0.107943594
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	-1.912944649	0.26919	-0.313601822
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	-0.739992552	0.102322	-0.107943594
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
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0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	-1.912944649	0.26919	-0.313601822
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	-0.739992552	0.102322	-0.107943594
0	-2.91168	1.14072133	0.017084	-0.017231208
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0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	-1.912944649	0.26919	-0.313601822
0	-2.91168	1.14072133	0.017084	-0.017231208
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0	-2.91168	-1.912944649	0.26919	-0.313601822
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0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208
0	-2.91168	1.14072133	0.017084	-0.017231208

### Stepwise Regression (3 variables)

3 variables selected so far are :

cc\_util, max\_arrears\_12m, annual\_income

**min AIC**  
5019.264266

**min AIC**  
5324.541447

	-2.91237698	-0.981180025	-0.958784912	-0.985164084		
Default	Intercept	cc_util	max_arrears_12m	annual_income	P(1)	ylnP(1) + (1-y)ln(1-P(1))
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
1	-2.91237698	-0.739992552	0.446897907	0.324421315	0.050479	-2.986195999
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.056834275	0.010813	-0.010872256
1	-2.91237698	-1.912944649	-1.708298136	-0.641267459	0.774555	-0.255467104
0	-2.91237698	1.14072133	0.446897907	-0.641267459	0.021283	-0.021512294
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	-0.739992552	0.446897907	-0.641267459	0.120996	-0.128965297
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	-0.739992552	0.446897907	0.324421315	0.050479	-0.051797732
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	-1.912944649	0.446897907	0.056834275	0.179476	-0.197811707
0	-2.91237698	-0.739992552	0.446897907	0.324421315	0.050479	-0.051797732
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
1	-2.91237698	1.14072133	0.446897907	-0.641267459	0.021283	-3.849867559
0	-2.91237698	-1.912944649	0.446897907	0.659648047	0.107765	-0.114025964
0	-2.91237698	1.14072133	0.446897907	-0.641267459	0.021283	-0.021512294
0	-2.91237698	-0.739992552	0.446897907	0.056834275	0.06472	-0.066908977
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	-0.641267459	0.021283	-0.021512294
0	-2.91237698	-1.912944649	0.446897907	-0.641267459	0.303189	-0.361240653
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	-0.739992552	0.446897907	0.659648047	0.036804	-0.037498312
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	1.14072133	0.446897907	0.056834275	0.010813	-0.010872256
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	-1.912944649	-1.708298136	0.324421315	0.570244	-0.844538594
0	-2.91237698	1.14072133	0.446897907	-0.641267459	0.021283	-0.021512294
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116

	-2.9067	-0.981943205	-0.917025532	-0.482702242		
Default	Intercept	cc_util	max_arrears_12m	num_ccj	P(1)	ylnP(1) + (1-y)ln(1-P(1))
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
1	-2.9067	-0.739992552	0.446897907	0.182549259	0.064284	-2.744443629
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
1	-2.9067	-1.912944649	-1.708298136	-0.232100523	0.657077	-0.419954432
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-0.739992552	0.446897907	0.182549259	0.064284	-0.066443328
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-0.739992552	0.446897907	0.182549259	0.064284	-0.066443328
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-1.912944649	0.446897907	0.182549259	0.178546	-0.196679643
0	-2.9067	-0.739992552	0.446897907	0.182549259	0.064284	-0.066443328
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
1	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-4.53553359
0	-2.9067	-1.912944649	0.446897907	0.182549259	0.178546	-0.196679643
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-0.739992552	0.446897907	0.182549259	0.064284	-0.066443328
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-1.912944649	0.446897907	-0.840719323	0.26264	-0.304678526
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-0.739992552	0.446897907	0.182549259	0.064284	-0.066443328
0	-2.9067	1.14072133	0.446897907	-0.840719323	0.01745	-0.017603891
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-1.912944649	-1.708298136	-0.937598024	0.729254	-1.306573045
0	-2.9067	1.14072133	0.446897907	-0.840719323	0.01745	-0.017603891
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071



## Stepwise Regression (3 variables)

3 variables selected so far are :

cc\_util, max\_arrears\_12m, annual\_income

min AIC

5019.264266

min AIC

5324.541447

	-2.91237698	-0.981180025	-0.958784912	-0.985164084		
Default	Intercept	cc_util	max_arrears_12m	annual_income	P(1)	ylnP(1) + (1-y)ln(1-P(1))
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
1	-2.91237698	-0.739992552	0.446897907	0.324421315	0.050479	-2.986195999
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.056834275	0.010813	-0.010872256
1	-2.91237698	-1.912944649	-1.708298136	-0.641267459	0.774555	-0.255467104
0	-2.91237698	1.14072133	0.446897907	-0.641267459	0.021283	-0.021512294
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	-0.739992552	0.446897907	-0.641267459	0.120996	-0.128965297
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	-0.739992552	0.446897907	0.324421315	0.050479	-0.051797732
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	-1.912944649	0.446897907	0.056834275	0.179476	-0.197811707
0	-2.91237698	-0.739992552	0.446897907	0.324421315	0.050479	-0.051797732
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
1	-2.91237698	1.14072133	0.446897907	-0.641267459	0.021283	-3.849867559
0	-2.91237698	-1.912944649	0.446897907	0.659648047	0.107765	-0.114025964
0	-2.91237698	1.14072133	0.446897907	-0.641267459	0.021283	-0.021512294
0	-2.91237698	-0.739992552	0.446897907	0.056834275	0.06472	-0.066908977
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	1.14072133	0.446897907	-0.641267459	0.021283	-0.021512294
0	-2.91237698	-1.912944649	0.446897907	-0.641267459	0.303189	-0.361240653
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	-0.739992552	0.446897907	0.659648047	0.036804	-0.037498312
0	-2.91237698	1.14072133	0.446897907	0.324421315	0.008328	-0.008363304
0	-2.91237698	1.14072133	0.446897907	0.056834275	0.010813	-0.010872256
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116
0	-2.91237698	-1.912944649	-1.708298136	0.324421315	0.570244	-0.844538594
0	-2.91237698	1.14072133	0.446897907	-0.641267459	0.021283	-0.021512294
0	-2.91237698	1.14072133	0.446897907	0.659648047	0.006	-0.006018116

	-2.9067	-0.981943205	-0.917025532	-0.482702242		
Default	Intercept	cc_util	max_arrears_12m	num_ccj	P(1)	ylnP(1) + (1-y)ln(1-P(1))
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
1	-2.9067	-0.739992552	0.446897907	0.182549259	0.064284	-2.744443629
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
1	-2.9067	-1.912944649	-1.708298136	-0.232100523	0.657077	-0.419954432
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-0.739992552	0.446897907	0.182549259	0.064284	-0.066443328
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-0.739992552	0.446897907	0.182549259	0.064284	-0.066443328
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-1.912944649	0.446897907	0.182549259	0.178546	-0.196679643
0	-2.9067	-0.739992552	0.446897907	0.182549259	0.064284	-0.066443328
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
1	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-4.53553359
0	-2.9067	-1.912944649	0.446897907	0.182549259	0.178546	-0.196679643
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-0.739992552	0.446897907	0.182549259	0.064284	-0.066443328
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-1.912944649	0.446897907	-0.840719323	0.26264	-0.304678526
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-0.739992552	0.446897907	0.182549259	0.064284	-0.066443328
0	-2.9067	1.14072133	0.446897907	-0.840719323	0.01745	-0.017603891
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071
0	-2.9067	-1.912944649	-1.708298136	-0.937598024	0.729254	-1.306573045
0	-2.9067	1.14072133	0.446897907	-0.840719323	0.01745	-0.017603891
0	-2.9067	1.14072133	0.446897907	0.182549259	0.010721	-0.010779071



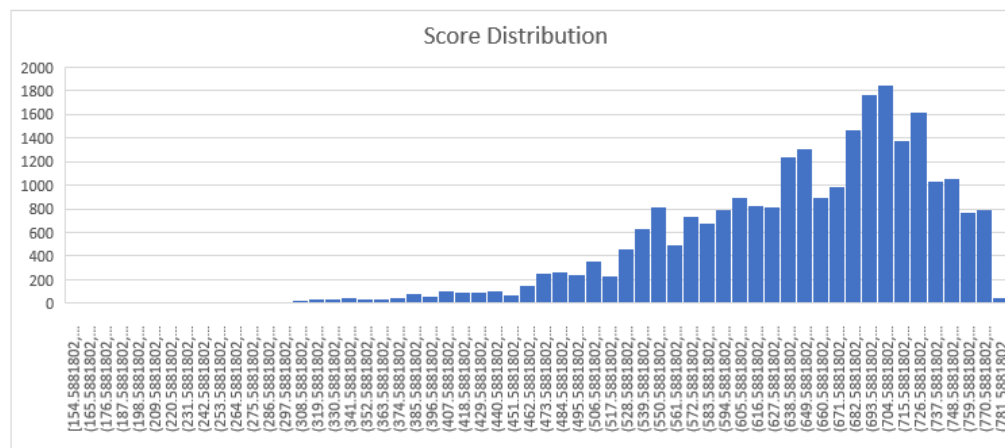
### Score Normalization

Goal is to score the entire data set  
Odds 72 : 1 is anchored at score 660 as per standard  
An increment of score 40 doubles the odds of not defaulting

So we have  
 $\ln(\text{odds}) = a + b * \text{Score}$   
 $\ln(72) = a + 660b$   
 $\ln(36) = a + 620b$

Solving  $b = 0.01732868$   
 $a = -7.16026236$

### Training + Testing Data Set



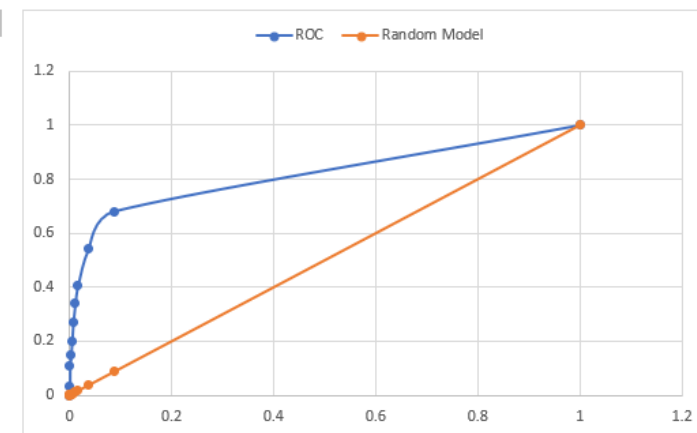
As expected, the score is concentrated at high scores indicating

Note that , we are able to derive scores from PD estimates  
If softwares produce score as direct output, it's easy to backtra

IRB in BASEL requires accounts to be mapped to a rating.  
IFRS/CECL does not require mapping to a rating

		-2.91589321	-0.652455435	-0.785562379	-0.924812	-0.865525003	-0.14029063	-0.337886572	-0.528973758			
	Default	Intercept	bureau_score	max_arrears_12m	cc_util	annual_income	num_ccj	emp_length	months_since_recent_cc_delinq	P(1)	ln(odds)	Score
22	0	-2.91589321	0.848988348	0.446897907	1.1407213	0.324421315	0.182549259	0.519371295	-0.379586857	0.005726	5.156941	710.7988
23	1	-2.91589321	0.848988348	0.446897907	-0.739993	0.324421315	0.182549259	-0.382216378	-0.359844634	0.042151	3.123443	593.45
24	0	-2.91589321	1.075105467	0.446897907	1.1407213	0.659648047	0.182549259	0.88879147	1.036190088	0.001549	6.468351	786.4773
25	0	-2.91589321	0.848988348	0.446897907	1.1407213	0.056834275	0.182549259	-0.180192003	-0.359844634	0.009019	4.699408	684.3955
26	1	-2.91589321	-0.232100523	-1.708298136	-1.912945	-0.641267459	-0.23210052	-0.306787205	-0.359844634	0.773509	-1.22823	342.3243
27	0	-2.91589321	-0.100424502	0.446897907	1.1407213	-0.641267459	0.182549259	-0.860408385	1.036190088	0.018264	3.984364	643.1319
28	0	-2.91589321	-0.100424502	0.446897907	1.1407213	0.659648047	0.182549259	0.627726273	1.036190088	0.003636	5.61316	737.1261
29	0	-2.91589321	1.075105467	0.446897907	1.1407213	0.659648047	0.182549259	-0.180192003	-0.359844634	0.004639	5.36869	723.0183
30	0	-2.91589321	0.848988348	0.446897907	1.1407213	0.659648047	0.182549259	0.439573656	-0.359844634	0.004361	5.430569	726.5892
31	0	-2.91589321	0.848988348	0.446897907	1.1407213	0.324421315	0.182549259	0.520370796	-0.379586857	0.005724	5.157279	710.8182
32	0	-2.91589321	0.848988348	0.446897907	1.1407213	0.659648047	0.182549259	0.519371295	-0.379586857	0.00429	5.447089	727.5425
33	0	-2.91589321	0.848988348	0.446897907	-0.739993	-0.641267459	0.182549259	-0.306787205	-0.359844634	0.090044	2.313101	546.687
34	0	-2.91589321	0.848988348	0.446897907	1.1407213	0.659648047	0.182549259	0.211585475	-0.359844634	0.004709	5.353535	722.1437
35	0	-2.91589321	1.075105467	0.446897907	-0.739993	0.324421315	0.182549259	0.211585475	-0.359844634	0.030131	3.471612	613.5421
36	0	-2.91589321	-1.178027211	0.446897907	1.1407213	0.324421315	0.182549259	0.627726273	-0.379586857	0.020412	3.871016	636.5908
37	0	-2.91589321	0.848988348	0.446897907	-1.912945	0.056834275	0.182549259	0.519371295	1.036190088	0.054672	2.850179	577.6806
38	0	-2.91589321	-0.100424502	0.446897907	-0.739993	0.324421315	0.182549259	-0.306787205	-0.359844634	0.073817	2.52948	559.1737
39	0	-2.91589321	0.848988348	0.446897907	1.1407213	0.659648047	0.182549259	0.439573656	-0.379586857	0.004407	5.420126	725.9866
40	0	-2.91589321	-0.684965808	0.446897907	1.1407213	0.324421315	0.182549259	0.519371295	1.036190088	0.007355	4.905014	696.2606
41	0	-2.91589321	0.848988348	0.446897907	1.1407213	0.324421315	0.182549259	0.211585475	-0.359844634	0.006284	5.063388	705.4
42	0	-2.91589321	-0.684965808	0.446897907	1.1407213	0.324421315	0.182549259	0.211585475	1.036190088	0.008154	4.801017	690.2591
43	0	-2.91589321	-0.100424502	0.446897907	1.1407213	0.659648047	0.182549259	0.520370796	-0.359844634	0.007857	4.83842	692.4176
44	0	-2.91589321	1.075105467	0.446897907	1.1407213	0.324421315	0.182549259	0.211585475	-0.379586857	0.005484	5.200476	713.311
45	1	-2.91589321	0.848988348	0.446897907	1.1407213	-0.641267459	0.182549259	-0.382216378	1.036190088	0.008448	4.765388	688.2031
46	0	-2.91589321	-1.178027211	0.446897907	-1.912945	0.659648047	0.182549259	0.520370796	-0.379586857	0.214027	1.300821	488.2705
47	0	-2.91589321	1.075105467	0.446897907	1.1407213	-0.641267459	0.182549259	0.311585475	-0.379586857	0.013558	4.264648	655.0773

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
7																	
8																	
9		Default	bureau_score	max_arrears_12m	cc_util	annual_income	num_ccj	emp_length	months_since_recent_cc_delinq	P(1)	Default (Pred)						
10		0	1.075105467	0.446897907	1.14072133	0.659648047	0.182549259	-0.382216378	1.036190088	0.002379	0						
11		0	0.848988348	0.446897907	-0.739992552	0.659648047	0.182549259	0.439573656	-0.379586857	0.024583	0						
12		1	-0.684965808	-2.643118019	-0.739992552	-0.641267459	-0.840719323	-0.382216378	-0.379586857	0.784928	0						
13		0	0.848988348	0.446897907	-1.912944649	0.659648047	0.182549259	0.439573656	-0.359844634	0.068721	0						
14		0	-0.100424502	-1.708298136	1.14072133	0.324421315	0.182549259	0.519371295	-0.379586857	0.054969	0						
15		0	0.848988348	0.446897907	1.14072133	-0.641267459	0.182549259	-0.860408385	1.036190088	0.009914	0						
16		0	-0.100424502	0.446897907	1.14072133	0.659648047	-0.840719323	0.627726273	-0.359844634	0.008739	0						
17		0	1.075105467	0.446897907	1.14072133	0.324421315	0.182549259	0.519371295	1.036190088	0.002344	0						
18		0	0.848988348	0.446897907	-3.025007735	0.659648047	0.182549259	0.211585475	-0.379586857	0.183836	0						
19		0	-1.178027211	0.446897907	-3.025007735	0.659648047	0.182549259	0.520370796	-0.379586857	0.432325	0						
20		0	-0.684965808	0.446897907	1.14072133	-0.641267459	0.182549259	-0.655185064	-0.379586857	0.051008	0						
21		0	0.848988348	0.446897907	1.14072133	0.659648047	0.182549259	0.520370796	-0.359844634	0.004245	0						
22		0	1.075105467	0.446897907	1.14072133	0.659648047	0.182549259	0.211585475	1.036190088	0.001947	0						
23		0	-1.178027211	0.446897907	1.14072133	0.324421315	0.182549259	-0.860408385	1.036190088	0.01603	0						
24		0	1.075105467	0.446897907	1.14072133	0.659648047	0.182549259	-0.306787205	-0.359844634	0.00484	0						
25		0	0.848988348	0.446897907	-1.912944649	0.324421315	0.182549259	0.519371295	-0.359844634	0.087598	0						
26		0	-0.684965808	0.446897907	1.14072133	0.324421315	0.182549259	-0.180192003	1.036190088	0.009298	0						
27		0	-0.100424502	0.446897907	1.14072133	-0.641267459	0.182549259	-0.306787205	1.036190088	0.015196	0						
28		0	-0.684965808	-2.643118019	1.14072133	0.324421315	-0.840719323	-0.306787205	1.036190088	0.113557	0						
29		0	1.075105467	0.446897907	-0.739992552	0.324421315	0.182549259	0.519371295	-0.379586857	0.027514	0						
30		0	0.848988348	0.446897907	1.14072133	-0.641267459	-0.840719323	-0.382216378	1.036190088	0.009739	0						
31		0	1.075105467	0.446897907	1.14072133	0.324421315	0.182549259	0.519371295	-0.379586857	0.004945	0						
32		0	0.848988348	0.446897907	1.14072133	0.659648047	0.182549259	0.88879147	1.036190088	0.001795	0						
33		0	-0.100424502	0.446897907	1.14072133	0.659648047	0.182549259	0.519371295	-0.359844634	0.00786	0						
34		0	-0.232100523	0.446897907	1.14072133	0.324421315	-0.232100523	-0.655185064	-0.359844634	0.017863	0						
35		0	-0.232100523	0.446897907	1.14072133	-0.641267459	-0.232100523	-0.180192003	1.036190088	0.016789	0						
36		0	-0.100424502	0.446897907	-0.739992552	0.324421315	-0.840719323	-0.860408385	-0.379586857	0.100795	0						
37		0	1.075105467	0.446897907	-0.739992552	0.324421315	0.182549259	-0.306787205	-0.359844634	0.035693	0						
38		0	-0.100424502	0.446897907	1.14072133	0.324421315	0.182549259	-0.180192003	-0.359844634	0.013235	0						
39		0	-0.100424502	0.446897907	1.14072133	-0.641267459	0.182549259	-0.306787205	1.036190088	0.015196	0						
40		0	1.075105467	0.446897907	-1.912944649	-0.641267459	0.182549259	-0.306787205	-0.379586857	0.203359	0						
41		0	-0.100424502	0.446897907	1.14072133	0.324421315	0.182549259	0.520370796	-0.359844634	0.010475	0						
42		0	-0.100424502	0.446897907	1.14072133	0.324421315	0.182549259	-0.306787205	1.036190088	0.006645	0						
43		0	-0.684965808	0.446897907	-1.912944649	0.324421315	0.182549259	0.627726273	-0.379586857	0.202838	0						
44		0	1.075105467	0.446897907	1.14072133	0.324421315	0.182549259	-0.655185064	1.036190088	0.003483	0						
45		0	0.848988348	0.446897907	-0.739992552	0.324421315	0.182549259	0.627726273	-0.379586857	0.030642	0						
46		0	-0.684965808	-2.643118019	1.14072133	-0.641267459	-0.840719323	-0.655185064	1.036190088	0.249484	0						
47		0	-0.100424502	0.446897907	1.14072133	0.324421315	0.182549259	0.439573656	1.036190088	0.005171	0						
48		0	1.075105467	0.446897907	-1.912944649	0.324421315	0.182549259	0.519371295	-0.359844634	0.076502	0						
49		0	-0.684965808	0.446897907	1.14072133	0.324421315	0.182549259	-0.382216378	-0.359844634	0.020595	0						
50		0	0.848988348	0.446897907	1.14072133	0.324421315	0.182549259	0.439573656	1.036190088	0.00279	0						
51		0	-0.684965808	0.446897907	1.14072133	-0.641267459	0.182549259	-0.180192003	1.036190088	0.02119	0						
52		0	1.075105467	0.446897907	-0.739992552	0.659648047	0.182549259	-0.180192003	-0.359844634	0.025847	0						
53		0	0.848988348	0.446897907	1.14072133	0.659648047	0.182549259	0.439573656	-0.359844634	0.004361	0						



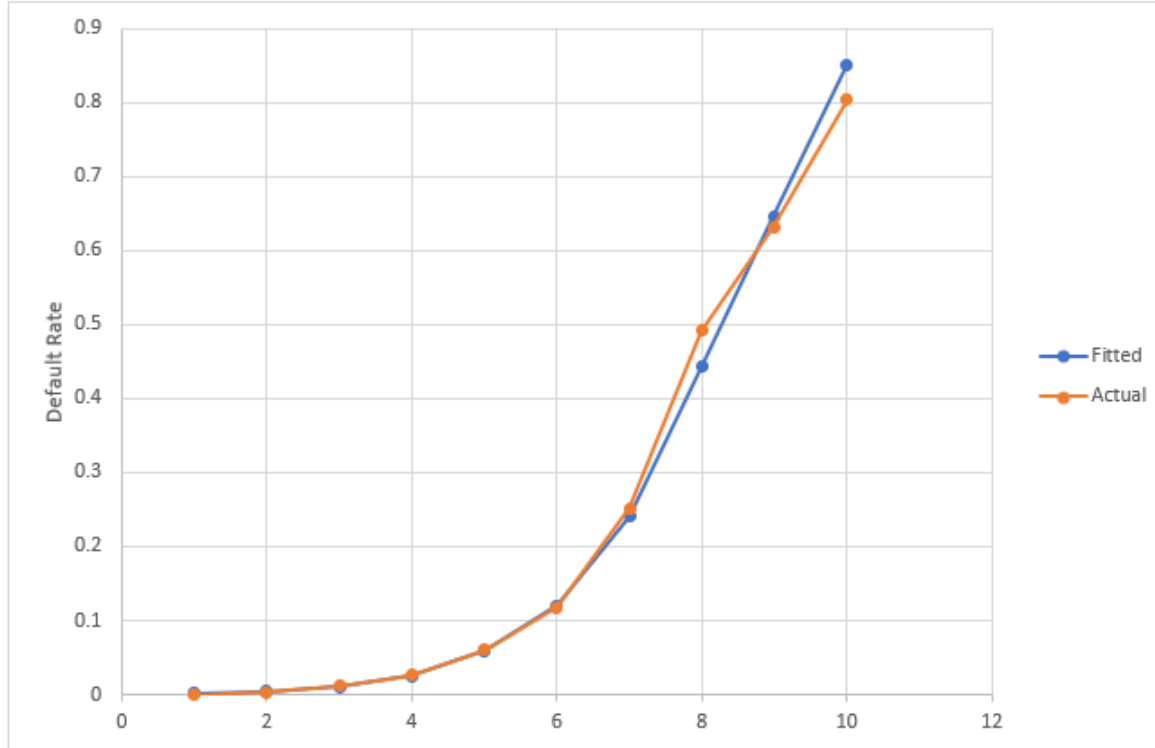
Cutoff	TPR	FPR	Random	area
0	1	1	1	0.76716276
0.1	0.6809	0.0872	0.0872	0.0305575
0.2	0.5414	0.0372	0.0372	0.0098118
0.3	0.4066	0.0165	0.0165	0.00205315
0.4	0.34	0.011	0.011	0.001219
0.5	0.2695	0.007	0.007	0.000538315
0.6	0.1986	0.0047	0.0047	0.000364875
0.7	0.1489	0.0026	0.0026	0.000242535
0.8	0.1064	0.0007	0.0007	0.000020565
0.9	0.0307	0.0004	0.0004	0.00000614
1	0	0	0	Total 0.81197664



### Calibration

In calibration, we test if the fitted PDs align with the Actual PDs.  
We will consider score bands and calculate average fitted PD and actual default rate.

Score Bands	fitted PD	Actual PD
750+	0.00228556	0
700-750	0.004769593	0.003525985
650-700	0.010531161	0.011509817
600-650	0.02488564	0.026638378
550-600	0.058764453	0.060295061
500-550	0.119951039	0.117940199
450-500	0.240974951	0.251732102
400-450	0.443401856	0.49187935
350-400	0.646351889	0.631799163
350-	0.851015006	0.803652968







### Low Default Portfolio

When portfolios have very low default occurrences (banks , sovereigns etc.), one needs special techniques to estimate PDs since history does not have enough data points.

#### Pluto and Tasche Method

If the average PD of a portfolio is p, the Probability that number of defaults observed in a portfolio of n accounts will be less than k is

$y = \text{BINOM.DIST}(k, n, p, \text{CUMULATIVE})$

Cum Binomial is related to Cum Beta distribution

$p = \text{BETA.INV}(1-y, k+1, n-k)$

y is the Confidence used to estimate p

#### Van Der Burgt Method

$$y(z) = \frac{1 - e^{-\theta \cdot z}}{1 - e^{-\theta}}$$

y is the cum % of defaults as a function of the cumulative % of debtors (z) in a rating class

$\theta$  is the Concavity parameter of CAP profile

First , one has to minimize the RMS (which is the Root Mean Square error between Default function and Actual Defaults)

$$RMS_{CAP} = \sqrt{\frac{1}{n_{class}} \sum_{j=1}^{n_{class}} \left( y_j - \frac{1 - e^{-\theta \cdot z_j}}{1 - e^{-\theta}} \right)^2}, \quad n_{class} \text{ is the number of rating classes}$$

After ,  $\theta$  is estimated , PD for each class can be found out from the following expression

$$PD_j = \frac{\theta \cdot \bar{DR}}{1 - e^{-\theta}} e^{-\theta z_j}, \quad \text{where, DR is the average default rate of the Portfolio}$$



### Pluto and Tasche Method

Assume our portfolio contains the following observations

Ratings	A	B	C	D	E	Total	C.I. ( $\gamma$ )
#Accounts	10	40	25	15	10	100	0.9
#Defaults	2	1	0	0	0	3	
PD	0.1158	0.0134	0.0042	0.007	0.0105		



### Van Der Burgt Method

Assume our portfolio contains the following observations

Ratings	A	B	C	D	E	Total	n <sub>class</sub>	5
#Accounts	10	40	25	15	10	100	θ	10.99331
#Defaults	2	1	0	0	0	3	DR	0.03
Cum Defaults	2	3	3	3	3			
Cum % y	0.6667	1	1	1	1			
Cum Accounts	10	50	75	90	100			
Cum % (z)	0.1	0.5	0.75	0.9	1			
y <sub>j</sub> - y(z)	-0.0003	0.0041	0.000245763	3.36644E-05	0			
Min : RMS	0.0018							
PD	0.1099	0.0014	8.65977E-05	1.66478E-05	5.54527E-06			