

<b>Đã bắt đầu vào lúc</b>	Thứ bảy, 19 Tháng mười một 2022, 10:17 AM
<b>Tình trạng</b>	Đã hoàn thành
<b>Hoàn thành vào lúc</b>	Thứ ba, 29 Tháng mười một 2022, 9:09 PM
<b>Thời gian thực hiện</b>	10 ngày 10 giờ
<b>Điểm</b>	3,00/3,00
<b>Điểm</b>	<b>10,00</b> của 10,00 (100%)



**Câu hỏi 1**

Chính xác

Điểm 1,00 của 1,00

Given class SplayTree definition:



```

class SplayTree {
    struct Node {
        int val;
        Node* pLeft;
        Node* pRight;
        Node* pParent;
        Node(int val = 0, Node* l = nullptr, Node* r = nullptr, Node* par = nullptr) : val(val), pLeft(l), pRight(r), pParent(par)
    }
};

Node* root;

// print the tree structure for local testing
void printBinaryTree(string prefix, const Node* root, bool isLeft, bool hasRightSibling) {
    if (!root && isLeft && hasRightSibling) {
        cout << prefix << "└─\n";
    }
    if (!root) return;
    cout << prefix;
    if (isLeft && hasRightSibling)
        cout << "└─";
    else
        cout << "┌─";
    cout << root->val << '\n';
    printBinaryTree(prefix + (isLeft && hasRightSibling ? "| " : " "), root->pLeft, true, root->pRight);
    printBinaryTree(prefix + (isLeft && hasRightSibling ? "| " : " "), root->pRight, false, root->pRight);
}

void printPreorder(Node* p) {
    if (!p) {
        return;
    }
    cout << p->val << ' ';
    printPreorder(p->pLeft);
    printPreorder(p->pRight);
}

public:
    SplayTree() {
        root = nullptr;
    }
    ~SplayTree() {
        // Ignore deleting all nodes in the tree
    }

    void printBinaryTree() {
        printBinaryTree("", root, false, false);
    }

    void printPreorder() {
        printPreorder(root);
        cout << "\n";
    }

    void splay(Node* p) {
        // To Do
    }

    void insert(int val) {
        // To Do
    }
};

```

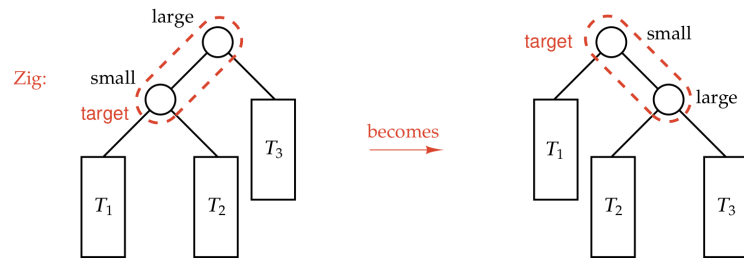
Implement the following method:

1. void splay(Node\* p): bottom-up splaying a Node

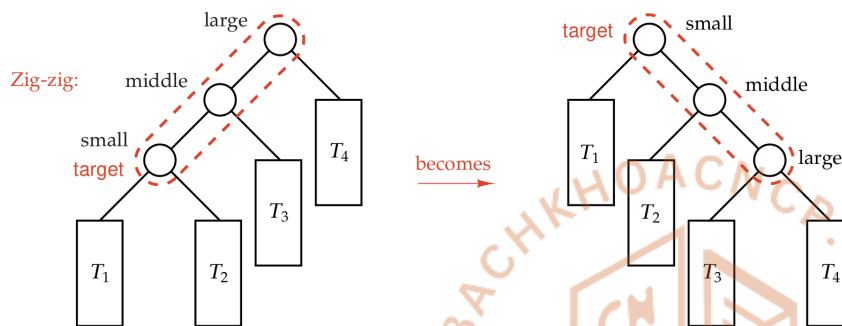
When a splay operation is performed on Node p, it will be moved to the root. To perform a splay operation we carry out a sequence of splay steps, each of which moves p closer to the root.

The three types of splay steps are:

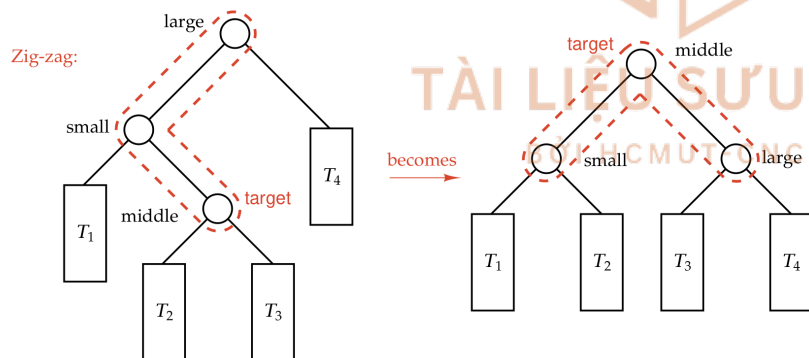
- Zig step



- Zig-zig step:



- Zig-zag step:



Note: there are also zag, zag-zag and zag-zig step but we don't show them here

2. void insert(int val):

To insert a value val into a splay tree:

- + Insert val as with a normal binary search tree.
- + When the new value is inserted, a splay operation is performed. As a result, the newly inserted node becomes the root of the tree.

Note: In a splay tree, the values in the left subtree  $\leq$  root's value  $\leq$  the values in the right subtree. In this exercise, when inserting a duplicate value, you have to insert it to the right subtree to pass the testcases.

Constraint of testcases:

- + number of operation  $\leq 10^4$
- +  $1 \leq \text{val} \leq 10^5$

For example:

Test	Input	Result
<pre>SplayTree tree; int query; cin &gt;&gt; query; for(int i = 0; i &lt; query; i++) {     string op;     int val;     cin &gt;&gt; op &gt;&gt; val;     if (op == "insert")         tree.insert(val); } // print preorder traversal of the tree tree.printPreorder(); // print structure of the tree tree.printBinaryTree();</pre>	<pre>6 insert 50 insert 70 insert 30 insert 80 insert 100 insert 90</pre>	<pre>90 80 30 70 50 100 └─90   └─80     └─30       └─70         └─50           └─100</pre>
<pre>SplayTree tree; int query; cin &gt;&gt; query; for(int i = 0; i &lt; query; i++) {     string op;     int val;     cin &gt;&gt; op &gt;&gt; val;     if (op == "insert")         tree.insert(val); } // print preorder traversal of the tree tree.printPreorder(); // print structure of the tree tree.printBinaryTree();</pre>	<pre>6 insert 95 insert 200 insert 80 insert 100 insert 200 insert 95</pre>	<pre>95 95 80 200 100 200 └─95   └─95     └─80       └─200         └─100           └─200</pre>

Answer: (penalty regime: 0 %)

Reset answer

```
1 // write your helper functions here
2 void rotateRight(Node *node)
3 {
4     Node *T=node->pLeft;
5     Node *B=T->pRight;
6     Node *D=node->pParent;
7     if(D)
8     {
9         if(D->pRight==node) D->pRight=T;
10        else D->pLeft=T;
11    }
12    if(B) {
13        B->pParent=node;
14    }
15    T->pParent=D;
16    T->pRight=node;
17
18    node->pParent =T;
19    node->pLeft=B;
20 }
21
22
23 void rotateLeft(Node *node)
24 {
25     Node *T=node->pRight;
26     Node *B=T->pLeft;
27     Node *D=node->pParent;
28     if(D)
29     {
30         if(D->pRight==node) D->pRight=T;
31         else D->pLeft=T;
32    }
33    if(B) {
34        B->pParent=node;
```



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```

35     }
36     T->pParent=D;
37     T->pLeft=node;
38
39     node->pParent =T;
40     node->pRight =

```

	Test	Input	Expected	Got	
✓	<pre> SplayTree tree; int query; cin &gt;&gt; query; for(int i = 0; i &lt; query; i++) {     string op;     int val;     cin &gt;&gt; op &gt;&gt; val;     if (op == "insert")         tree.insert(val); } // print preorder traversal of the tree tree.printPreorder(); // print structure of the tree tree.printBinaryTree(); </pre>	<pre> 6 insert 50 insert 70 insert 30 insert 80 insert 100 insert 90 </pre>	<pre> 90 80 30 70 50 100 └─90   └─80     └─30       └─70         └─50           └─100 </pre>	<pre> 90 80 30 70 50 100 └─90   └─80     └─30       └─70         └─50           └─100 </pre>	✓
✓	<pre> SplayTree tree; int query; cin &gt;&gt; query; for(int i = 0; i &lt; query; i++) {     string op;     int val;     cin &gt;&gt; op &gt;&gt; val;     if (op == "insert")         tree.insert(val); } // print preorder traversal of the tree tree.printPreorder(); // print structure of the tree tree.printBinaryTree(); </pre>	<pre> 6 insert 95 insert 200 insert 80 insert 100 insert 200 insert 95 </pre>	<pre> 95 95 80 200 100 200 └─95   └─95     └─80       └─200         └─100           └─200 </pre>	<pre> 95 95 80 200 100 200 └─95   └─95     └─80       └─200         └─100           └─200 </pre>	✓

Passed all tests! ✓

Chính xác

Điểm cho bài nộp này: 1,00/1,00.

## Câu hỏi 2

Chính xác

Điểm 1,00 của 1,00

Given class SplayTree definition:

```
class SplayTree {
    struct Node {
        int val;
        Node* pLeft;
        Node* pRight;
        Node* pParent;
        Node(int val = 0, Node* l = nullptr, Node* r = nullptr, Node* par = nullptr) : val(val), pLeft(l), pRight(r), pParent(par)
    }
};
```

```
Node* root;
```

```
// print the tree structure for local testing
void printBinaryTree(string prefix, const Node* root, bool isLeft, bool hasRightSibling) {
    if (!root && isLeft && hasRightSibling) {
        cout << prefix << "├─\n";
    }
    if (!root) return;
    cout << prefix;
    if (isLeft && hasRightSibling)
        cout << "├─";
    else
        cout << "└─";
    cout << root->val << '\n';
    printBinaryTree(prefix + (isLeft && hasRightSibling ? "│" : " "), root->pLeft, true, root->pRight);
    printBinaryTree(prefix + (isLeft && hasRightSibling ? "│" : " "), root->pRight, false, root->pRight);
}
```

```
void printPreorder(Node* p) {
    if (!p) {
        return;
    }
    cout << p->val << ' ';
    printPreorder(p->pLeft);
    printPreorder(p->pRight);
}
```

```
public:
    SplayTree() {
        root = nullptr;
    }
```

```
~SplayTree() {
    // Ignore deleting all nodes in the tree
}
```

```
void printBinaryTree() {
    printBinaryTree("", root, false, false);
}
```

```
void printPreorder() {
    printPreorder(root);
    cout << "\n";
}
```

```
void splay(Node* p);
```

```
void insert(int val);
```

```
bool search(int val) {
    // To Do
}
};
```

Method splay and insert are already implemented

You have to implement the following method:

`bool search(int val)`: search for the value `val` in the tree.

The search operation in splay tree do the same thing as BST search. In addition, it also splays the node containing the value to the root.

- + If the search is successful, the node that is found will become the new root and the function return true.
- + Else, the last accessed node will be splayed and become the new root and the function return false.

Constraints of the testcases:

- + number of operation  $\leq 10^4$
- +  $1 \leq \text{val} \leq 10^5$

For example:

Test	Input	Result
<pre>SplayTree tree; int query; cin &gt;&gt; query; for(int i = 0; i &lt; query; i++) {     string op;     int val;     cin &gt;&gt; op &gt;&gt; val;     if (op == "insert")         tree.insert(val);     else if (op == "search")         cout &lt;&lt; (tree.search(val) ? "found" : "not found") &lt;&lt; '\n';     else if (op == "print")         tree.printPreorder(); } tree.printBinaryTree();</pre>	<pre>8 insert 95 insert 200 insert 80 search 100 insert 55 insert 100 search 95 print 0</pre>	<pre>not found found 95 55 80 100 200 └─95   └─55     └─┬─       └─80         └─100           └─200</pre>
<pre>SplayTree tree; int query; cin &gt;&gt; query; for(int i = 0; i &lt; query; i++) {     string op;     int val;     cin &gt;&gt; op &gt;&gt; val;     if (op == "insert")         tree.insert(val);     else if (op == "search")         cout &lt;&lt; (tree.search(val) ? "found" : "not found") &lt;&lt; '\n';     else if (op == "print")         tree.printPreorder(); } tree.printBinaryTree();</pre>	<pre>5 insert 100 insert 200 insert 300 insert 200 search 250</pre>	<pre>not found └─300   └─200     └─200       └─100</pre>



**Answer:** (penalty regime: 0 %)

Reset answer

```

1 // Write your helper functions here
2 bool searchRec(int val, Node*& node, Node*& par){
3     if(node == nullptr) {
4         if(par) splay(par);
5         return false;
6     }
7     if(val < node->val) return searchRec(val, node->pLeft, node);
8     if(val > node->val) return searchRec(val, node->pRight, node);
9     splay(node);
10    return true;
11 }
12 bool search(int val){
13     if(root == nullptr) return false;
14     return searchRec(val, root, root->pParent);
15 }

```



	Test	Input	Expected	Got	
✓	<pre> SplayTree tree; int query; cin &gt;&gt; query; for(int i = 0; i &lt; query; i++) {     string op;     int val;     cin &gt;&gt; op &gt;&gt; val;     if (op == "insert")         tree.insert(val);     else if (op == "search")         cout &lt;&lt; (tree.search(val) ? "found" : "not found") &lt;&lt; '\n';     else if (op == "print")         tree.printPreorder(); } tree.printBinaryTree(); </pre>	<pre> 8 insert 95 insert 200 insert 80 search 100 insert 55 insert 100 search 95 print 0 </pre>	<pre> not found found 95 55 80 100 200 └─95   └─55     └─       └─80         └─100           └─200 </pre>	<pre> not found found 95 55 80 100 200 └─95   └─55     └─       └─80         └─100           └─200 </pre>	✓

	Test	Input	Expected	Got	
✓	<pre> SplayTree tree; int query; cin &gt;&gt; query; for(int i = 0; i &lt; query; i++) {     string op;     int val;     cin &gt;&gt; op &gt;&gt; val;     if (op == "insert")         tree.insert(val);     else if (op == "search")         cout &lt;&lt; (tree.search(val) ? "found" : "not found") &lt;&lt; '\n';     else if (op == "print")         tree.printPreorder(); } tree.printBinaryTree(); </pre>	<pre> 5 insert 100 insert 200 insert 300 insert 200 search 250 </pre>	<pre> not found └─300    └─200       └─200          └─100 </pre>	<pre> not found └─300    └─200       └─200          └─100 </pre>	✓

Passed all tests! ✓

Chính xác

Điểm cho bài nộp này: 1,00/1,00.



### Câu hỏi 3

Chính xác

Điểm 1,00 của 1,00

Given class SplayTree definition:

```
class SplayTree {
    struct Node {
        int val;
        Node* pLeft;
        Node* pRight;
        Node* pParent;
        Node(int val = 0, Node* l = nullptr, Node* r = nullptr, Node* par = nullptr) : val(val), pLeft(l), pRight(r), pParent(par)
    }
};
Node* root;

// print the tree structure for local testing
void printBinaryTree(string prefix, const Node* root, bool isLeft, bool hasRightSibling) {
    if (!root && isLeft && hasRightSibling) {
        cout << prefix << "├─\n";
    }
    if (!root) return;
    cout << prefix;
    if (isLeft && hasRightSibling)
        cout << "├─";
    else
        cout << "└─";
    cout << root->val << '\n';
    printBinaryTree(prefix + (isLeft && hasRightSibling ? "├─" : "└─"), root->pLeft, true, root->pRight);
    printBinaryTree(prefix + (isLeft && hasRightSibling ? "├─" : "└─"), root->pRight, false, root->pRight);
}
```

```
void printPreorder(Node* p) {
    if (!p) {
        return;
    }
    cout << p->val << ' ';
    printPreorder(p->pLeft);
    printPreorder(p->pRight);
}
```

public:

```
SplayTree() {
    root = nullptr;
}
```

```
~SplayTree() {
    // Ignore deleting all nodes in the tree
}
```

```
void printBinaryTree() {
    printBinaryTree("", root, false, false);
}
```

```
void printPreorder() {
    printPreorder(root);
    cout << "\n";
}
```

```
void splay(Node* p);
```

```
void insert(int val);
```

```
bool search(int val);
```

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```
Node* remove(int val) {
    // To Do
}
};
```

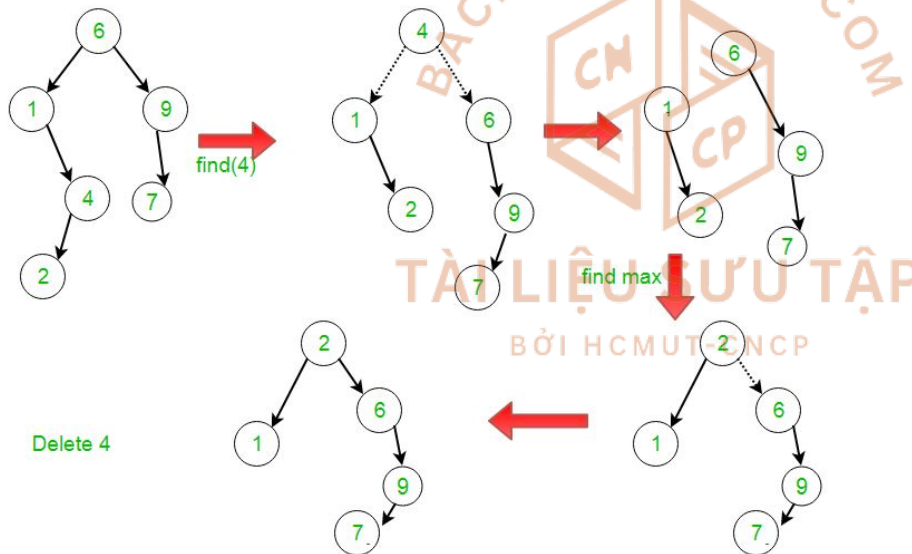
The methods splay, insert and search are already implemented.

Implement the following method:

Node\* remove(int val): remove the first Node with value equal to val from the tree and return it.

To perform remove operation on splay tree:

1. If root is NULL, return the root
2. Search for the first node containing the given value val and splay it. If val is present, the found node will become the root. Else the last accessed leaf node becomes the root.
3. If new root's value is not equal to val, return NULL as val is not present.
4. Else the value val is present, we remove root from the tree by the following steps:
  - 4.1 Split the tree into two tree: tree1 = root's left subtree and tree2 = root's right subtree
  - 4.2 If tree1 is NULL, tree2 is the new root
  - 4.3 Else, splay the leaf node with the largest value in tree1. tree1 will be a left skewed binary tree. Make tree2 the right subtree of tree1. tree1 becomes the new root
  - 4.4 Return the removed node.



Constraints of the testcases:

+ number of operations  $\leq 10^4$

+  $1 \leq \text{val} \leq 10^5$

**For example:**

Test	Input	Result
<pre> SplayTree tree; int query; cin &gt;&gt; query; for(int i = 0; i &lt; query; i++) {     string op;     int val;     cin &gt;&gt; op &gt;&gt; val;     if (op == "insert")         tree.insert(val);     else if (op == "remove")         cout &lt;&lt; (tree.remove(val) != nullptr ? "removed" : "not found") &lt;&lt; '\n';     else if (op == "search")         cout &lt;&lt; (tree.search(val) ? "found" : "not found") &lt;&lt; '\n';     else if (op == "print")         tree.printPreorder(); } tree.printBinaryTree(); </pre>	<pre> 7 insert 100 insert 300 insert 200 insert 50 insert 250 remove 200 print 0 </pre>	<pre> removed 100 50 250 300 └─100    └─50       └─250          └─300 </pre>
<pre> SplayTree tree; int query; cin &gt;&gt; query; for(int i = 0; i &lt; query; i++) {     string op;     int val;     cin &gt;&gt; op &gt;&gt; val;     if (op == "insert")         tree.insert(val);     else if (op == "remove")         cout &lt;&lt; (tree.remove(val) != nullptr ? "removed" : "not found") &lt;&lt; '\n';     else if (op == "search")         cout &lt;&lt; (tree.search(val) ? "found" : "not found") &lt;&lt; '\n';     else if (op == "print")         tree.printPreorder(); } tree.printBinaryTree(); </pre>	<pre> 7 insert 900 insert 1400 insert 100 insert 800 insert 750 remove 500 print 0 </pre>	<pre> not found 100 750 800 900 1400 └─100    └─750       └─800          └─900             └─1400 </pre>

Answer: (penalty regime: 0. %)

Reset answer

```

1 // Write your helper functions here
2
3 Node* remove(int val){
4     //TODO
5     if(root == nullptr) return nullptr;
6     search(val);
7     if(root->val == val){
8         if(!root->pLeft){
9             Node* tmp = root;
10            root = root->pRight;
11            if(root) root->pParent = nullptr;
12            return tmp;
13        }
14        Node* treeL = root->pLeft;
15        Node* treeR = root->pRight;
16        treeL->pParent = nullptr;
17        root->pLeft = root->pRight = nullptr;
18        Node* ans = root;
19        while(treeL->pRight) treeL = treeL->pRight;
20        splay(treeL);
21        treeL->pRight = treeR;
22        if(treeR) treeR->pParent = treeL;
23        return ans;
24    }
25    return nullptr;
26 }

```

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	Test	Input	Expected	Got	
✓	<pre> SplayTree tree; int query; cin &gt;&gt; query; for(int i = 0; i &lt; query; i++) {     string op;     int val;     cin &gt;&gt; op &gt;&gt; val;     if (op == "insert")         tree.insert(val);     else if (op == "remove")         cout &lt;&lt; (tree.remove(val) != nullptr ? "removed" : "not found") &lt;&lt; '\n';     else if (op == "search")         cout &lt;&lt; (tree.search(val) ? "found" : "not found") &lt;&lt; '\n';     else if (op == "print")         tree.printPreorder(); } tree.printBinaryTree(); </pre>	<pre> 7 insert 100 insert 300 insert 200 insert 50 insert 250 remove 200 print 0 </pre>	<pre> removed 100 50 250 300 └─100   └─50     └─250       └─300 </pre>	<pre> removed 100 50 250 300 └─100   └─50     └─250       └─300 </pre>	✓
✓	<pre> SplayTree tree; int query; cin &gt;&gt; query; for(int i = 0; i &lt; query; i++) {     string op;     int val;     cin &gt;&gt; op &gt;&gt; val;     if (op == "insert")         tree.insert(val);     else if (op == "remove")         cout &lt;&lt; (tree.remove(val) != nullptr ? "removed" : "not found") &lt;&lt; '\n';     else if (op == "search")         cout &lt;&lt; (tree.search(val) ? "found" : "not found") &lt;&lt; '\n';     else if (op == "print")         tree.printPreorder(); } tree.printBinaryTree(); </pre>	<pre> 7 insert 900 insert 1400 insert 100 insert 800 insert 750 remove 500 print 0 </pre>	<pre> not found 100 750 800 900 1400 └─100   └─750     └─800       └─900         └─ </pre>	<pre> not found 100 750 800 900 1400 └─100   └─750     └─800       └─900         └─ </pre>	✓

Passed all tests! ✓

Chính xác

Điểm cho bài nộp này: 1,00/1,00.

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