PROGRAMMING IN HASKELL



Chapter 4 - Defining Functions

Conditional Expressions

As in most programming languages, functions can be defined using <u>conditional expressions</u>.

```
abs :: Int \rightarrow Int abs n = if n \ge 0 then n else -n
```

abs takes an integer n and returns n if it is non-negative and -n otherwise.

Conditional expressions can be nested:

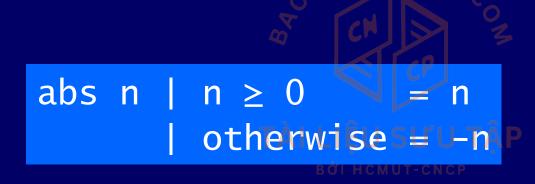
```
signum :: Int \rightarrow Int signum n = if n < 0 then -1 else if n = 0 then 0 else 1
```

Note:

In Haskell, conditional expressions must <u>always</u> have an else branch, which avoids any possible ambiguity problems with nested conditionals.

Guarded Equations

As an alternative to conditionals, functions can also be defined using guarded equations.



As previously, but using guarded equations.

Guarded equations can be used to make definitions involving multiple conditions easier to read:

Note:

■ The catch all condition <u>otherwise</u> is defined in the prelude by otherwise = True.

Pattern Matching

Many functions have a particularly clear definition using pattern matching on their arguments.

```
not :: Bool → Bool
not False = True
not True = False
```

not maps False to True, and True to False.

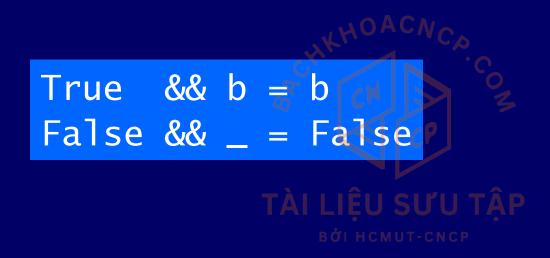
Functions can often be defined in many different ways using pattern matching. For example

```
(&&) :: Bool → Bool → Bool
True && True = True
True && False
False && True = False
False && False = False
```

can be defined more compactly by

```
True && True = True
_ && _ = False
```

However, the following definition is more efficient, because it avoids evaluating the second argument if the first argument is False:



Note:

■ The underscore symbol _ is a wildcard pattern that matches any argument value.

Patterns are matched <u>in order</u>. For example, the following definition always returns False:

Patterns may not <u>repeat</u> variables. For example, the following definition gives an error:

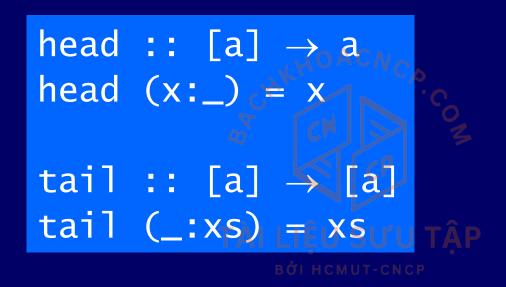
List Patterns

Internally, every non-empty list is constructed by repeated use of an operator (:) called "cons" that adds an element to the start of a list.

[1,2,3,4] TÀI LIỆU SƯU TẬP

Means 1:(2:(3:(4:[]))).

Functions on lists can be defined using x:xs patterns.



head and tail map any non-empty list to its first and remaining elements.

Note:

x:xs patterns only match non-empty lists:

```
> head []
*** Exception: empty list
```

x:xs patterns must be <u>parenthesised</u>, because application has priority over (:). For example, the following definition gives an error:

head
$$x: = x$$

Lambda Expressions

Functions can be constructed without naming the functions by using <u>lambda expressions</u>.



the nameless function that takes a number x and returns the result x + x.

Note:

The symbol λ is the Greek letter <u>lambda</u>, and is typed at the keyboard as a backslash \.

In mathematics, nameless functions are usually denoted using the \mapsto symbol, as in $x \mapsto x + x$.

BỞI HCMUT-CNCP

In Haskell, the use of the λ symbol for nameless functions comes from the <u>lambda calculus</u>, the theory of functions on which Haskell is based.

Why Are Lambda's Useful?

Lambda expressions can be used to give a formal meaning to functions defined using <u>currying</u>.

For example:

```
add :: Int \rightarrow Int \rightarrow Int add x y = x + y MULLEN FROM
```

means

```
add :: Int \rightarrow (Int \rightarrow Int)
add = \lambda x \rightarrow (\lambda y \rightarrow x + y)
```

Lambda expressions can be used to avoid naming functions that are only <u>referenced once</u>.

For example:

odds
$$n = map f [0..n-1]$$
where
$$t_{A}f_{L}X_{L} = x^{*}2_{A} + 1$$

can be simplified to

odds n = map
$$(\lambda x \to x^2 + 1)$$
 [0..n-1]

Operator Sections

An operator written <u>between</u> its two arguments can be converted into a curried function written <u>before</u> its two arguments by using parentheses.

For example:

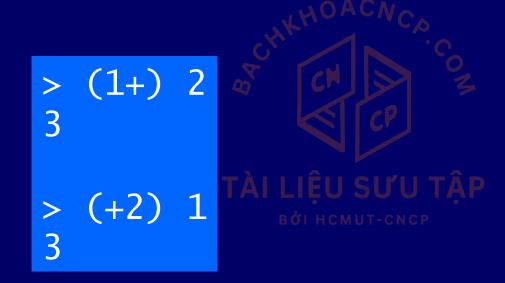
TÀI LIỆU SƯU TẬP

1+23(+) 1 23

BỞI HCMUT-CNCP

This convention also allows one of the arguments of the operator to be included in the parentheses.

For example:



In general, if \oplus is an operator then functions of the form (\oplus) , $(x\oplus)$ and $(\oplus y)$ are called <u>sections</u>.

Why Are Sections Useful?

Useful functions can sometimes be constructed in a simple way using sections. For example:

- (1+) successor function
- (1/) reciprocation function
- (*2) doubling function
- (/2) halving function

Exercises

- (1) Consider a function <u>safetail</u> that behaves in the same way as tail, except that safetail maps the empty list to the empty list, whereas tail gives an error in this case. Define safetail using:
 - (a) a conditional expression;
 - (b) guarded equations;
 - (c) pattern matching.

Hint: the library function null :: $[a] \rightarrow Bool$ can be used to test if a list is empty.

- (2) Give three possible definitions for the logical or operator (||) using pattern matching.
- (3) Redefine the following version of (&&) using conditionals rather than patterns:

```
True && True = True
_ && _ = False
```

BỞI HCMUT-CNCP

(4) Do the same for the following version:

```
True && b = b
False && _ = False
```