Chapter 9

Introduction to Graphs

Discrete Structures for Computing

TÀI LIÊU SƯU TẬP

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le Faculty of Computer Science and Engineering University of Technology - VNUHCM {htnguyen;trtanh}@hcmut.edu.vn

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs

Graph Isomorphism

Exercise Graph

Contents

1 Graph definitions

Terminology Special Graphs

Representing Graphs and Graph Isomorphism Representing Graphs Graph Isomorphism

Exercise

Graph Bipartie graph Isomorphism

'ÀI LIÊU SƯU TẬP

BỞI HCMUT-CNCP

Introduction to Graphs

Huvnh Tuong Nguyen Tran Tuan Anh. Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs and Graph

Isomorphism Representing Graphs

Graph Isomorphism

Exercise

Granh

Bipartie graph

Isomorphism

Course outcomes

	Course learning outcomes \(\(\)
	1/401.24CV
L.O.1	Understanding of logic and discrete structures
	L.O.1.1 – Describe definition of propositional and predicate logic
	L.O.1.2 – Define basic discrete structures: set, mapping, graphs
	4
L.O.2	Represent and model practical problems with discrete structures
	L.O.2.1 – Logically describe some problems arising in Computing
	L.O.2.2 – Use proving methods: direct, contrapositive, induction
	L.O.2.3 – Explain problem modeling using discrete structures
L.O.3	Understanding of basic probability and random variables
	L.O.3.1 – Define basic probability theory
	L.O.3.2 – Explain discrete random variables
	ΤΔΙΤΙΕΠΙΝΙΤΑΡ
L.O.4	Compute quantities of discrete structures and probabilities
	L.O.4.1 – Operate (compute/ optimize) on discrete structures
	L.O.4.2 – Compute probabilities of various events, conditional
	ones, Bayes theorem

Introduction to Graphs

Huynh Tuong Nguyen Tran Tuan Anh, Nguye Ngoc Le



Graph definitions

Terminology Special Graphs

Representing Graphs and Graph

Isomorphism Representing Graphs Graph Isomorphism

Exercise

Graph

Bipartie graph

Motivations

The need of the graph

- Representation/Storing
- Searching/sorting
- Optimization

Its applications

- Electric circuit/board
- Chemical structure
- Networking
- Map, geometry, ...
- Graph theory is useful for analysing "things that are connected to other things".
- Some difficult problems become easy when represented using a graph.

Introduction to Graphs

Huvnh Tuong Nguyen. Tran Tuan Anh. Nguye Ngoc Le



Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Granh

Graph

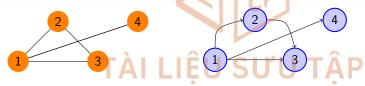
just only one type : or un or directed

Definition

A graph $(d\hat{o} thi)$ G is a pair of (V, E), which are:

- V nonempty set of vertices (nodes) (dinh)
- E set of edges (cạnh)

A graph captures abstract relationships between vertices.



Undirected graph

BOI HCMU Directed graph

$$1 -> 2 = 2 -> 1$$

Introduction to Graphs

Huynh Tuong Nguyen Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs

Graph Isomorphism

Exercise

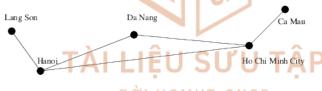
Graph

Undirected Graph (Đồ thị vô hướng)

Definition (Simple graph (đơn đồ thị))

- Each edge connects two different vertices, and
- No two edges connect the same pair of vertices

An edge between two vertices u and v is denoted as $\{u, v\}$



BỞI HCMUT-CNCP

BACHKHOACNCP.COM

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Graph

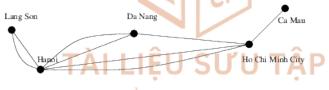
Undirected Graph

KHOACNC

Definition (Multigraph (đa đồ thị))

Graphs that may have multiple edges connecting the same vertices.

An unordered pair of vertices $\{u,v\}$ are called multiplicity m ($b\hat{\rho}i$ m) if it has m different edges between.



BỞI HCMUT-CNCP

BACHKHOACNCP.COM

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs and Graph

Isomorphism

Representing Graphs

Graph Isomorphism

Exercise

Graph

Undirected Graph

KHOACNC

Definition (Pseudograph (giả đồ thị))

Are multigraphs that have

• loops (khuyên) – edges that connect a vertex to itself



BỞI HCMUT-CNCP

BACHKHOACNCP.COM

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs and Graph

Isomorphism

Representing Graphs

Graph Isomorphism

Exercise

Graph

Directed Graph

Definition (Directed Graph (đồ thị có hướng))

A directed graph G is a pair of (V, E), in which:

- V nonempty set of vertices
- E set of directed edges (cạnh có hướng, arcs)

A directed edge start at u and end at v is denoted as (u, v).



BACHKHOACNCP.COM

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Graph

Terminologies For Undirected Graph

Neighborhood

In an undirected graph G = (V, E),

- two vertices u and $v \in V$ are called adjacent ($li\hat{e}n \ k\hat{e}$) if they are end-points ($di\hat{e}m \ d\hat{a}u \ m\acute{u}t$) of edge $e \in E$, and
- e is incident with (cạnh liên thuộc) u and v
- e is said to **connect** (canh $n\delta i$) u and v;

The degree of a vertex

The degree of a vertex ($b\hat{q}c$ $c\hat{u}a$ $m\hat{q}t$ $d\hat{l}nh$), denoted by deg(v) is the number of edges incident with it, except that a loop contributes twice to the degree of that vertex.

- isolated vertex (đỉnh cô lập): vertex of degree 0
- pendant vertex (*dinh treo*): vertex of degree 1

loop = twice => caculate the edges in v

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs

Graph Isomorphism

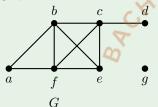
Exercise

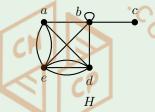
Graph

Example

Example

What are the degrees and neighborhoods of the vertices in these graphs?





Solution

In G, deg(a) = 2, deg(b) = deg(c) = deg(f) = 4, deg(d) = 1, ... Neiborhoods of these vertices are

$$N(a) = \{b, f\}, N(b) = \{a, c, e, f\}, CMUT-CNCP$$

In
$$H$$
, $deg(a) = 4$, $deg(b) = deg(e) = 6$, $deg(c) = 1$, . . .

Neiborhoods of these vertices are

$$N(a) = \{b, d, e\}, N(b) = \{a, b, c, d, e\}, \dots$$

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs Graph Isomorphism

Graph Isomorphism

Exercise Graph

Grapn

Basic Theorems

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Theorem (The Handshaking Theorem)

Let G = (V, E) be an undirected graph with m edges. Then

$$2m = \sum_{v \in V} deg(v)$$

(Note that this applies even if multiple edges and loops are present.)

Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs

Graph Isomorphism

Exercise

Graph

Bipartie graph Isomorphism

Theorem

An undirected graph has an even number of odd-degree vertices.

BACHKHOACNCP.COM

TÀI LIEU SƯU TÀI

If the number of vertices in an undirected graph is an odd number, then there exists an even-degree vertex.

If the number of vertices in an undirected graph is an odd number, then the number of vertices with even degree is odd.

If the number of vertices in an undirected graph is an even number, then the number of vertices with even degree is even.

BÓI HCMUT-CNCP

Introduction to Graphs

Huynh Tuong Nguyen Tran Tuan Anh. Nguye Ngoc Le



Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs

Graph Isomorphism

Exercise

Granh

Terminologies for Directed Graph

Neighborhood

In an directed graph G = (V, E), $\bigcap A \cap \bigwedge$

- u is said to be adjacent to (nối tới) v and v is said to be adjacent from (được nối từ) u if (u, v) is an arc of G, and
- u is called **initial vertex** (dinh d $\hat{a}u$) of (u,v)
- ullet v is called **terminal** $(\emph{d}\emph{i}\emph{n}\emph{h}\ \emph{cu\'o}\emph{i})$ or **end vertex** of (u,v)
- the initial vertex and terminal vertex of a loop are the same.

The degree of a vertex

In a graph G with directed edges:

- in-degree (bậc vào) of a vertex v, denoted by $\deg^-(v)$, is the number of arcs with v as their terminal vertex.
- out-degree (bậc ra) of a vertex v, denoted by $\deg^+(v)$, is the number of arcs with v as their initial vertex.

Note: a loop at a vertex contributes 1 to both the in-degree and the out-degree of this vertex.

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Graph

Bipartie graph

Isomorphism

Basic Theorem

Introduction to Graphs

Huynh Tuong Nguyen Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs

Graph Isomorphism

Exercise

Graph

Bipartie graph Isomorphism

Chr

Theorem

Let G = (V, E) be a graph with directed edges. Then

$$\sum_{v \in V} \deg^-(v) = \sum_{v \in V} \deg^+(v) = |E|. = \text{sum of edges}$$

TÀI LIỆU SƯU TẬP

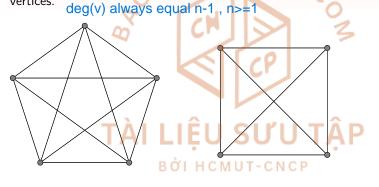
BỞI HCMUT-CNCP

BACHKHOACNCP.COM

Complete Graphs

 K_5

A complete graph $(d\hat{o} thi d\hat{a} y d\hat{u})$ on n vertices, K_n , is a simple graph that contains exactly one edge between each pair of distinct vertices.



 K_4 BACHKHOACNCP.COM

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs

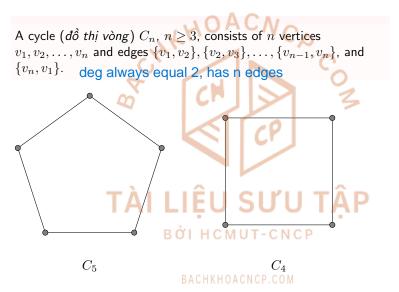
and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Graph





Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs

Graph Isomorphism

Exercise

Grapn

Wheels

We obtain a wheel ($d\hat{o}$ thị hình bánh xe) W_n when we add an additional vertex to a cycle C_n , for $n \geq 3$, and connect this new vertex to each of the n vertices in C_n . deg tt = ndeg xung quanh = 3 has 2n edges BỞI HCMUT-CNCP W_5 W_{4}

Introduction to Graphs

Huynh Tuong Nguyen Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs

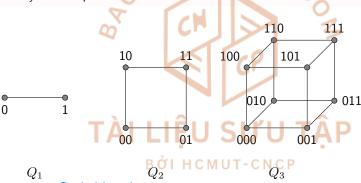
Graph Isomorphism

Exercise

Grapn

n-cube

An n-dimensional hypercube ($kh\delta i n chiều$), Q_n , is a graph that has vertices representing the 2^n bit strings of length n. Two vertices are adjacent iff the bit strings that they represent differ in exactly one bit position.



Qn is bipartite

has 16 vertices and 16*4/2 edges What's about Q_4 ?

Introduction to Graphs

Huvnh Tuong Nguyen Tran Tuan Anh. Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs

and Graph Isomorphism Representing Graphs

Graph Isomorphism

Exercise Granh

Bipartie graph

Isomorphism

Applications of Special Graphs

• Local networks topologies

- Star, ring, hybrid
- Parallel processing
 - Linear array
 - Mesh network



BACHKHOACNCP.COM

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Graph



Exercise (5)

Give the number of edges in function of number of vertices in a complete graph K_n . (n-1)*n/2

Exercise (6)

Give an undirected simple graph G=(V,E) with |V|=n, show that

- **6** there does not exist simultaneously both a vertex of degree 0 and a vertex of degree (n-1) with $n \ge 2$,
- deduce that there are at least two vertices of the same degree.
 0+1+2+ +n-1

Exercise (7)

BOI HCMUT-CNCP

Is it possible that each person has exactly 3 friends in the same group of 9 people? 3*9=27 kg chia het cho 2 M

Introduction to Graphs

Huynh Tuong Nguyen Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs and Graph

Isomorphism Representing Graphs

Graph Isomorphism

Exercise

Graph

Bipartite Graphs

Definition

A simple graph G is called bipartite $(d\hat{o})$ thi phân $d\hat{o}i)$ if its vertex set V can be partitioned into two disjoint sets V_1 and V_2 such that every edge in the graph connects a vertex in V_1 and a vertex in V_2 (so that no edge in G connects either two vertices in V_1 or two vertices in V_2) neu do thi con la tam giac thi ko phan doi

Example

 C_6 is bipartite

Cn is bipartie if n is even



Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs and Graph

and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Graph

Complete Bipartite Graphs

Definition

A complete bipartite $K_{m,n}$ is a graph that

- has its vertex set partitioned into two subsets of m and n vertices, respectively,
- with an edge between two vertices iff one vertex is in the first subset and the other is in the second one



 $K_{3,3}$

moi dinh dc noi voi all dinh o subset kia

Introduction to Graphs

Huvnh Tuong Nguyen Tran Tuan Anh. Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs and Graph

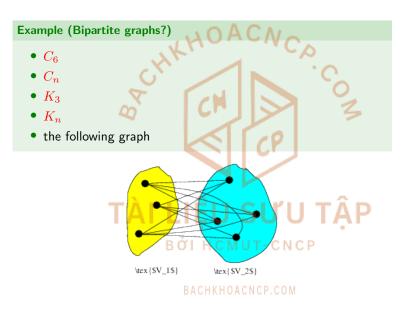
Isomorphism Representing Graphs

Graph Isomorphism

Exercise

Granh

Bipartite graphs



Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs

and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Graph

New Graph From Old

Definition

A subgraph $(d\hat{o} \ thi \ con)$ of a graph G = (V, E) is a graph H = (W, F) where $W \subseteq V$ and $F \subseteq E$.

Definition

 G_1

The union $(h\phi p)$ of two simple graphs $G_1=(V_1,E_1)$ and $G_2=(V_2,E_2)$ is a simple graph with vertex set $V_1\cup V_2$ and edge set $E_1\cup E_2$. The union of G_1 and G_2 is denoted by $G_1\cup G_2$.



 G_2

 $G_1 \cup G_2$

BACHKHOACNCP.COM

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

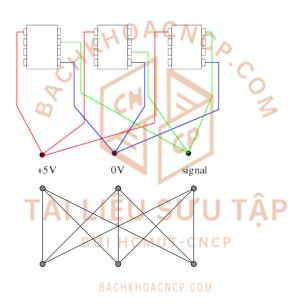
Representing Graphs and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Graph

Planar Graphs



Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs

and Graph Isomorphism

Representing Graphs Graph Isomorphism

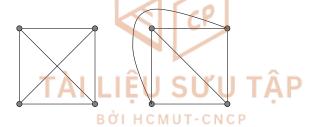
Exercise

Graph

Planar Graphs

Definition

- A graph is called planar (phẳng) if it can be drawn in the plane without any edges crossing.
- Such a drawing is called planar representation (biểu diễn phẳng) of the graph.



 K_4 K_4 with no crossing

Introduction to Graphs

Huynh Tuong Nguyen Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs

Graph Isomorphism

Exercise

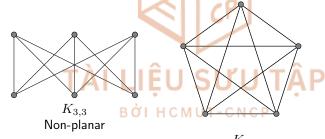
Graph

Important Corollaries

Corollary

- If G is a connected planar simple graph with e edges and v vertices where $v \geq 3$, then $e \leq 3v 6$.
- If G is a connected planar simple graph with e edges and v vertices where $v \ge 3$, and no circuits of length 3, then $e \le 2v 4$.

ko chu trinh 3 canh



 K_{5} BACHKHOACN Non-planar

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Contents

Graph definitions

Terminology

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Graph

Elementary Subdivision

Definition

- Given a planar graph G, an elementary subdivision (phân chia sơ cấp) is removing an edge $\{u,v\}$ and adding a new vertex w together with edges $\{u,w\}$ and $\{w,v\}$.
- Graphs $G_1 = (V_1, E_1)$ and $G_2 = (V_2, E_2)$ are called homeomorphic $(d\hat{o}ng\ ph\hat{o}i)$ if they can obtained from the same graph by a sequence of elementary subdivisions.



BACHKHOACNCP.COM

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs

and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Granh

Kuratowski's Theorem

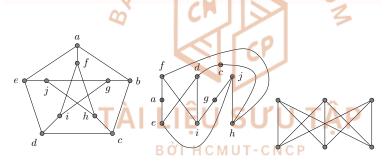
Introduction to Graphs

Huynh Tuong Nguyen Tran Tuan Anh, Nguye Ngoc Le



Theorem

A graph is nonplanar iff it contains a subgraph homeomorphic to $K_{3,3}$ or K_5 .



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs

and Graph Isomorphism Representing Graphs

Graph Isomorphism

Exercise

Graph

Bipartie graph Isomorphism

BACHKHOACNCP.COM

Exercise

Exercise • Is K_4 planar? • Is Q_3 planar? 110 100 101 010 011 000 001 BỞI HCMUT-CNCP K_4

Introduction to Graphs

Huynh Tuong Nguyen Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Graph

Bipartie graph

Isomorphism

Adjacency Lists (Danh sách kề)

b, c, e

a, d, e

a, c, d

c, e

Vertex

a

h

C

Ч

e

Adjacent vertices

Introduction to Graphs

Huynh Tuong Nguyen Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs and Graph Isomorphism

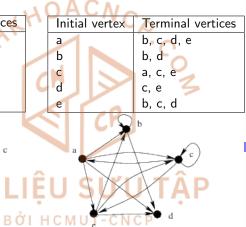
Representing Graphs

Graph Isomorphism

Exercise

Graph

Bipartie graph Isomorphism



BACHKHOACNCP.COM

Adjacency Matrices

Definition

- Matrix elements

$$a_{ij} = \begin{cases} 1 & \text{if } (v_i, v_j) \in E \\ 0 & \text{otherwise} \end{cases}$$

vo huong: doi xung qua duong cheo chinh



Introduction to Graphs

Huvnh Tuong Nguyen Tran Tuan Anh. Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs

Graph Isomorphism

Exercise

Granh

Bipartie graph

Isomorphism

Examples

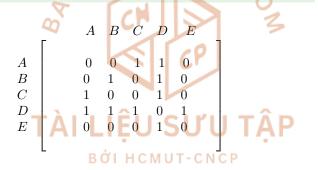
Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguye Ngoc Le



Example

Give the graph defined by the following adjacency matrix



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs

and Graph Isomorphism Representing Graphs

Graph Isomorphism

Graph Isomorphism

Exercise

Graph

Bipartie graph Isomorphism

BACHKHOACNCP.COM

Adjacency Matrices

HOACN

Example

Give the directed graph defined by the following adjacency matrix



BACHKHOACNCP.COM

Introduction to Graphs

Huynh Tuong Nguyen Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs

Graph Isomorphism

Exercise

Graph

Incidence Matrices

Definition

Incidence matrix (ma trận liên thuộc) M_G of G=(V,E)

- Dimension $|V| \times |E|$
- Matrix elements

 $m_{ij} = \begin{cases} 1 & \text{if } e_j \text{ is incident with} \\ 0 & \text{otherwise} \end{cases}$



Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyer Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs

Graph Isomorphism

Exercise

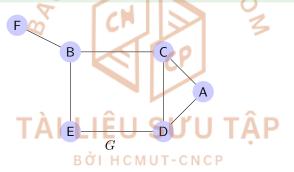
Graph

Examples

MOACNO

Example

Give incidence matrix according to the following graph



BACHKHOACNCP.COM

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyen Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs

Graph Isomorphism

Exercise

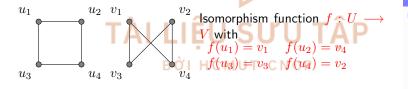
Graph

Graph Isomorphism

Definition

 $G_1=(V_1,E_1)$ and $G_2=(V_2,E_2)$ are **isomorphic** $(d\mathring{a}ng\ c\^{a}u)$ if there is a **one-to-one function** f from V_1 to V_2 with the property that a and b are adjacent in G_1 iif f(a) and f(b) are adjacent in G_2 , for all a and b in V_1 . Such a function f is called an **isomorphism** $(m\^{o}t\ d\mathring{a}ng\ c\^{a}u)$.

(i.e. there is a one-to-one correspondence between vertices of the two graphs that preserves the adjacency relationship.)



Huynh Tuong Nguyen, Tran Tuan Anh, Nguye Ngoc Le

Introduction to Graphs



Contents

Graph definitions

Terminology Special Graphs

.....

Representing Graphs and Graph Isomorphism

Representing Graphs

Graph Isomorphism

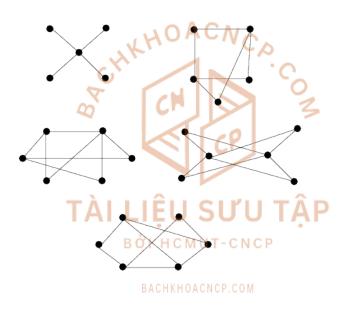
Exercise

Graph

Bipartie graph Isomorphism

BACHKHOACNCP.COM

Bipartie graph



Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs

and Graph Isomorphism

Representing Graphs Graph Isomorphism

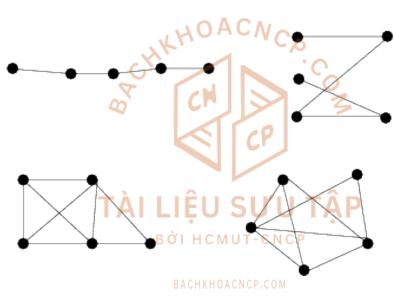
Exercise

Graph

Bipartie graph

Isomorphism

Isomorphism?



Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguyer Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

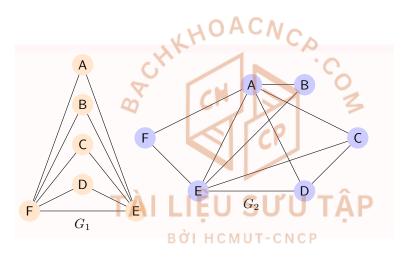
Representing Graphs and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Graph

Isomorphism?



BACHKHOACNCP.COM

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

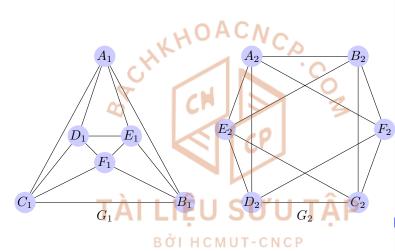
Representing Graphs and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Graph

Isomorphism?



Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs and Graph Isomorphism

Representing Graphs Graph Isomorphism

Exercise

Graph

Bipartie graph Isomorphism

BACHKHOACNCP.COM

Isomorphism

Introduction to Graphs

Huynh Tuong Nguyen, Tran Tuan Anh, Nguye Ngoc Le



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs and Graph Isomorphism

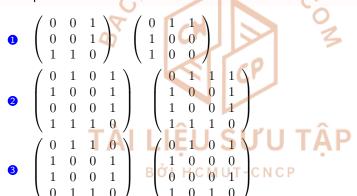
Representing Graphs Graph Isomorphism

Exercise

Graph

Bipartie graph

Are the simple graphs with the following adjacency matrices isomorphic ?



BACHKHOACNCP.COM

Isomorphism

Huvnh Tuong Nguyen Tran Tuan Anh. Nguye

Ngoc Le

Introduction to Graphs



Contents

Graph definitions

Terminology Special Graphs

Representing Graphs and Graph

Isomorphism Representing Graphs

Graph Isomorphism

Exercise

Granh

Bipartie graph Isomorphism

Determine whether the graphs (without loops) with the incidence matrices are isomorphic.

- $\left(\begin{array}{ccccc} 1 & 1 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 \\ 0 & 1 & 1 & 1 & 0 \end{array}\right) \quad \left($
- Extend the definition of isomorphism of simple graphs to undirected graphs containing loops and multiple edges.
- Define isomorphism of directed graphs