







DATA SCIENCE

Variational autoencoders.



In my introductory post on autoencoders, I discussed various models (undercomplete, sparse, denoising, contractive) which take data as input and discover some latent state representation of that data. More specifically, our input data is converted into an *encoding vector* where each dimension represents some learned attribute about the data. The most important detail to grasp here is that our encoder network is outputting a *single value* for each encoding dimension. The decoder network then subsequently takes these values and attempts to recreate the original input.

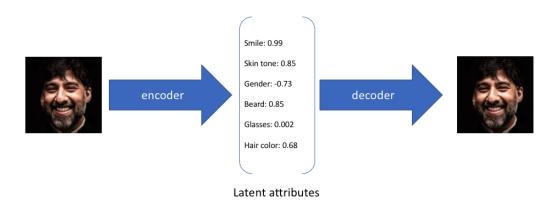
A variational autoencoder (VAE) provides a *probabilistic* manner for describing an observation in latent space. Thus, rather than building an encoder which outputs a single value to describe each latent state attribute, we'll formulate our encoder to describe a probability distribution for each latent attribute.

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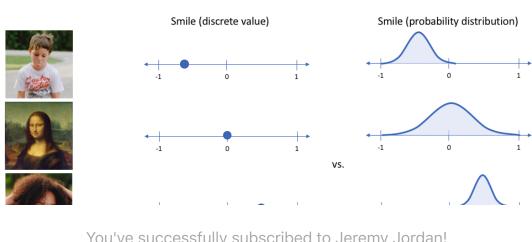
on a large dataset of faces with a encoding dimension of 6. An ideal

whether or not the person is wearing glasses, etc. in an attempt to describe an observation in some compressed representation.

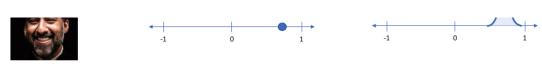




In the example above, we've described the input image in terms of its latent attributes using a single value to describe each attribute. However, we may prefer to represent each latent attribute as a range of possible values. For instance, what single value would you assign for the smile attribute if you feed in a photo of the Mona Lisa? Using a variational autoencoder, we can describe latent attributes in probabilistic terms.

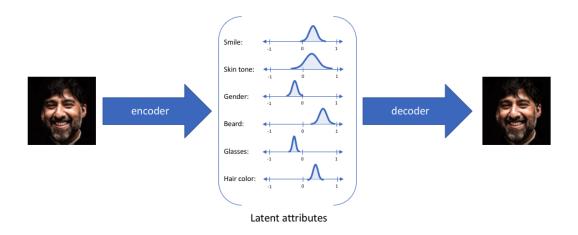


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With this approach, we'll now represent *each latent attribute* for a given input as a probability distribution. When decoding from the latent state, we'll randomly sample from each latent state distribution to generate a vector as input for our decoder model.



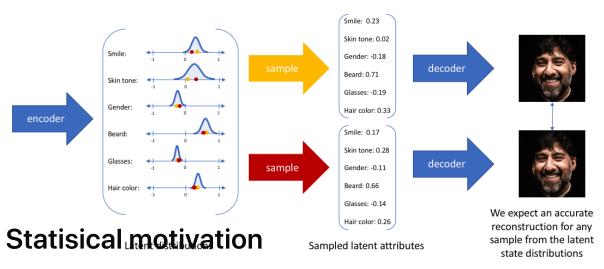


Note: For variational autoencoders, the encoder model is sometimes referred to as the **recognition model** whereas the decoder model is sometimes referred to as the **generative model**.

By constructing our encoder model to output a range of possible values (a statistical distribution) from which we'll randomly sample to feed into our decoder model, we're essentially enforcing a continuous, smooth latent space representation. For any sampling of the latent distributions, we're expecting our decoder model to be able to accurately reconstruct the input. Thus, values which are nearby to one another in latent space should correspond with very similar reconstructions.

5/17/2021 Variational autoencoders.

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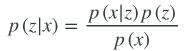


Suppose that there exists some hidden variable z which generates an observation x.



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other words, we'd like to compute p(z|x).



Unfortunately, computing p(x) is quite difficult.

$$p(x) = \int p(x|z) p(z) dz$$

This usually turns out to be an intractable distribution. However, we can apply varitational inference to estimate this value.

Let's approximate p(z|x) by another distribution q(z|x) which we'll define such that it has a tractable distribution. If we can define the parameters of q(z|x) such that it is very similar to p(z|x), we can use it to perform approximate inference of the intractable distribution.

Recall that the KL divergence is a measure of difference between two probability distributions. Thus, if we wanted to ensure that q(z|x) was similar to p(z|x), we could minimize the KL divergence between the two distributions.

$$\min KL(q(z|x)||p(z|x))$$

Dr. Ali Ghodsi goes through a full derivation here, but the result gives us that we can minimize the above expression by maximizing the following:

$$E_{q(z|x)}\log p(x|z) - KL(q(z|x)||p(z))$$

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term ensures that our learned distribution q is similar to the true prior

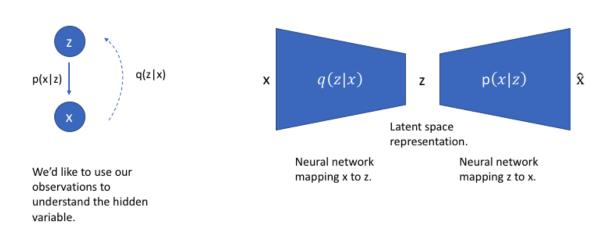






To revisit our graphical model, we can use q to infer the possible hidden variables (ie. latent state) which was used to generate an observation. We can further construct this model into a neural network architecture where the encoder model learns a mapping from x to z and the decoder model learns a mapping from z back to x.





Our loss function for this network will consist of two terms, one which penalizes reconstruction error (which can be thought of maximizing the reconstruction likelihood as discussed earlier) and a second term which encourages our learned distribution q(z|x) to be similar to the true prior distribution p(z), which we'll assume follows a unit Gaussian distribution, for each dimension j of the latent space.

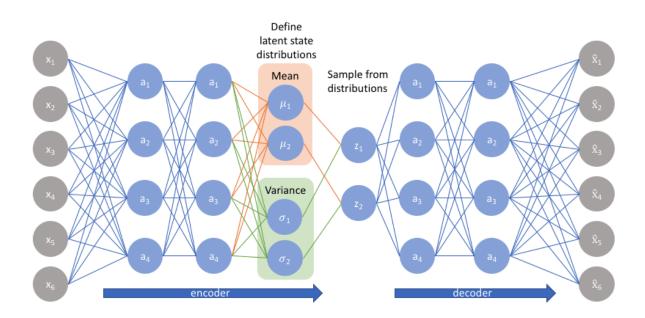
$$\mathcal{L}(x,\hat{x}) + \sum_{j} KL(q_{j}(z|x)||p(z))$$

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variational autoencoder structure. In this section, I'll provide the practical implementation details for building such a model yourself.

standard autoencoder, the encoder model of a VAE will output parameters describing a distribution for each dimension in the latent space. Since we're assuming that our prior follows a normal distribution, we'll output *two* vectors describing the mean and variance of the latent state distributions. If we were to build a true multivariate Gaussian model, we'd need to define a covariance matrix describing how each of the dimensions are correlated. However, we'll make a simplifying assumption that our covariance matrix only has nonzero values on the diagonal, allowing us to describe this information in a simple vector.

Our decoder model will then generate a latent vector by sampling from these defined distributions and proceed to develop a reconstruction of the original input.



However, this sampling process requires some extra attention. When

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for a random sampling process. Fortunately, we can leverage a clever idea

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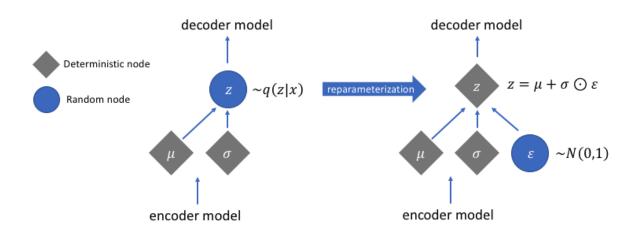




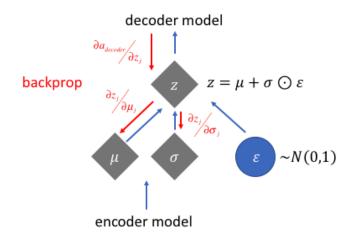
the latent distribution's mean μ and scale it by the latent distribution's variance σ .







With this reparameterization, we can now optimize the *parameters* of the distribution while still maintaining the ability to randomly sample from that distribution.

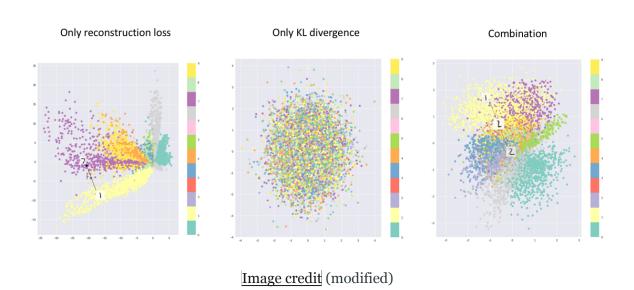


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exponentiate this value to get the latent distribution's variance.

Visualization of latent space
To understand the implications of a variational autoencoder model and how it differs from standard autoencoder architectures, it's useful to examine the latent space. This blog post introduces a great discussion on the topic, which I'll summarize in this section.

The main benefit of a variational autoencoder is that we're capable of learning *smooth* latent state representations of the input data. For standard autoencoders, we simply need to learn an encoding which allows us to reproduce the input. As you can see in the left-most figure, focusing only on reconstruction loss does allow us to separate out the classes (in this case, MNIST digits) which should allow our decoder model the ability to reproduce the original handwritten digit, but there's an uneven distribution of data within the latent space. In other words, there are areas in latent space which don't represent any of our observed data.



On the flip side if we only feets only on ensuring that the latent

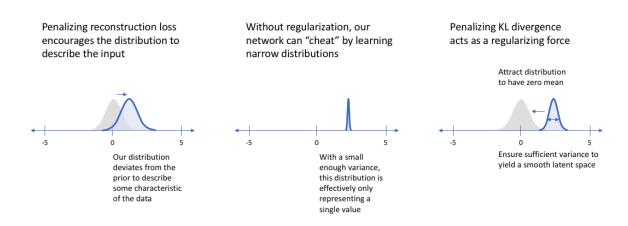
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Gaussian, which we subsequently sample from to describe the latent

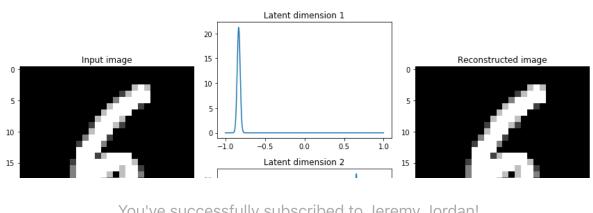
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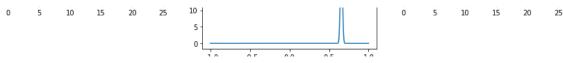
the same characteristics; in other words, we've failed to describe the Prisingled simultaneously, we're encouraged to describe the latent state for an observation with distributions close to the prior but deviating when necessary to describe salient features of the input.





When I'm constructing a variational autoencoder, I like to inspect the latent dimensions for a few samples from the data to see the characteristics of the distribution. I encourage you to do the same.





If we observe that the latent distributions appear to be very tight, we may decide to give higher weight to the KL divergence term with a parameter $\beta > 1$, encouraging the network to learn broader distributions. This simple insight has led to the growth of a new class of models disentangled variational autoencoders. As it turns out, by placing a larger emphasis on the KL divergence term we're also implicitly enforcing that the learned latent dimensions are uncorrelated (through our simplifying assumption of a diagonal covariance matrix).

$$\mathcal{L}(x,\hat{x}) + \beta \sum_{j} KL(q_{j}(z|x)||N(0,1))$$

Variational autoencoders as a generative model

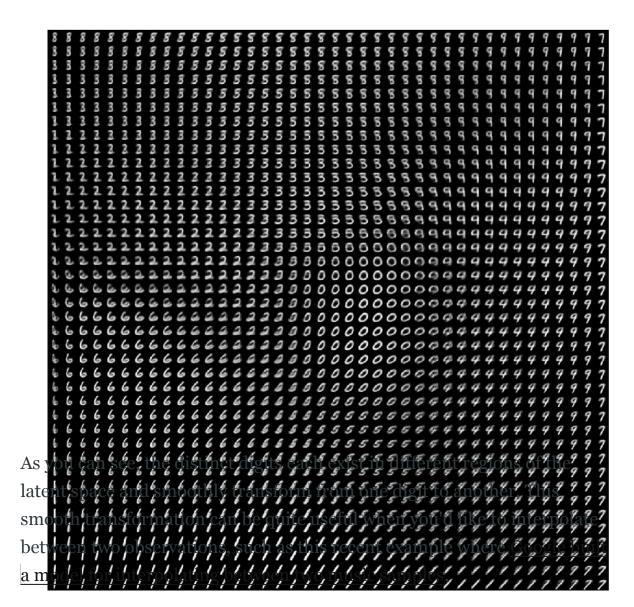
By sampling from the latent space, we can use the decoder network to form a generative model capable of creating new data similar to what was observed during training. Specifically, we'll sample from the prior distribution p(z) which we assumed follows a unit Gaussian distribution.

The figure below visualizes the data generated by the decoder network of a variational autoencoder trained on the MNIST handwritten digits dataset. Here, we've sampled a grid of values from a two-dimensional Gaussian and displayed the output of our decoder network.









MusicVAE: Melody 2-bar "Loop" Interpolation











Further reading

Lectures

- Ali Ghodsi: Deep Learning, Variational Autoencoder (Oct 12 2017)
- UC Berkley Deep Learning Decall Fall 2017 Day 6: Autoencoders and Representation Learning
- Stanford CS231n: Lecture on Variational Autoencoders

Blogs/videos

- Building Variational Auto-Encoders in TensorFlow (with great code examples)
- Building Autoencoders in Keras
- Variational Autoencoders Arxiv Insights
- Intuitively Understanding Variational Autoencoders
- Density Estimation: A Neurotically In-Depth Look At Variational
 Autoencoders
- Pyro: Variational Autoencoders
- Under the Hood of the Variational Autoencoder
- With Great Power Comes Poor Latent Codes: Representation
 Learning in VAEs
- Kullback-Leibler Divergence Explained
- Neural Discrete Representation Learning

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• Deep learning book (Chapter 20.10.3): Variational Autoencoders

- A tutorial on variational Bayesian inference
- Auto-Encoding Variational Bayes
- Tutorial on Variational Autoencoders

Papers on my reading list

- Neural Discrete Representation Learning
- Early Visual Concept Learning with Unsupervised Deep Learning
- Multimodal Unsupervised Image-to-Image Translation
 - Video from paper

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Common architectures in convolutional neural networks.

In this post, I'll discuss commonly used architectures for convolutional networks. As you'll see, almost all CNN architectures follow the same general design principles of successively applying convolutional layers to the input, periodically downsampling the spatial dimensions while increasing the number of feature maps.



DATA SCIENCE

Introduction to autoencoders.

Autoencoders are an unsupervised learning technique in which we leverage neural networks for the task of representation learning. Specifically, we'll design a neural network architecture such that we impose a bottleneck in the network which forces a compressed knowledge representation of the original input.



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