# FSBE III (Electrical) MATLAB-based Lab **assignment-3** for Control System Engineering

# Prob. 1:

Consider a system  $G_1(s) = 4 / (s^2 + 1.6s + 4)$  with another subsystem  $G_2(s)$  in cascade with it. Using MATLAB generate the Bode plots and obtain the stability margins for the overall system and compare them with that of  $G_1(s)$  in each case when  $G_2(s)$  is:

- i. A pure integrator  $G_2(s) = 1/s$
- ii. A real pole  $G_2(s) = 10/(2s+1)$
- iii. A real zero  $G_2(s) = (2s+1)$

Comment on the results. Obtain the Bode plots for  $G_1$  and  $G_1G_2$  on the same figure for each  $G_1G_2$  combination.

# Prob. 2:

Consider a unity-feedback system with open-loop transfer function G(s) = K/s(10s+1). Use **rltool** to find the value of gain K for the system to have a phase margin of greater than 40 degrees.

# Prob. 3:

A PI controller  $G_c(s) = K(1+0.1/s)$  is used to control the system G(s) = (s+5) / s(10s+1)Use **rltool** to find a value for K to give a closed-loop damping ratio of 0.5.

# Prob. 4:

Consider the second-order system  $G(s) = 1/(s^2+2\zeta s+1)$ . Write an M-file to plot the gain response of G(s) for  $\zeta = 0.2, 0.4, 0.6, 0.8, 1.0$  and 2.0 on the same figure window. Use your plots to state a trend between the maximum of the gain response and the damping ratio.

# Prob. 5:

Using the *Nichols*, ngrid('new') and logspace functions, obtain the Nichols chart with a grid for the following transfer functions, where  $0.1 \le \omega \le 10$ :

- a) G(s) = 1/(s+0.1)
- **b)**  $G(s) = 1/(s^2+2s+1)$
- c)  $G(s) = 24 / (s^3 + 9s^2 + 26s + 24)$

Determine the approximate phase and gain margins from the Nichols charts and label the charts accordingly.

### Prob. 6:

Control system for a paper making machine is a unity-feedback system having a controller  $G_c(s)=K(s+50)/(s+20)$  in cascade with the machine having the transfer function G(s)=1/s(s+10).

Using MATLAB, obtain a plot of the bandawidth of the closed-loop system as K varies in the interval  $1 \le K \le 50$ .

# Prob. 7:

For a unity-feedback control system having loop transfer function

$$G(s)H(s) = 10 / s(1+0.2s)(1+0.02s)$$

Using MATLAB, obtain the Nyquist plot with a selection of appropriate frequency range from the Bode plot. Determine GCF, PCF, GM and  $\Phi$ M from both the plots.

# Prob. 8:

For a unity-feedback control system having loop transfer function

$$G(s)H(s) = K / s(1+s)(s+5)$$

Determine the stability using Bode and root locus plots using MATLAB for (i) K = 10, (ii) K = 100.

# Prob. 9:

Use MATLAB to generate the Bode and root locus plots to determine the range of values of **K** for which a unity-feedback system having the following open-loop transfer functions would remain stable:

- a) G(s) = K/(s+2)(s+4)(s+5)
- **b)** G(s) = K/(1+0.2s)(1+0.02s)

# **Prob. 10:**

For a feedback control system having loop transfer function G(s)H(s) = 199 / s(s+1.71)(s+100) use MATLAB to obtain gain crossover frequency, phase margin, peak overshoot and settling time.

## **Prob. 11:**

Using MATLAB for a negative feedback control system having loop transfer function

$$G(s)H(s) = 4/s(s+1)(s+2)$$

a) Obtain Bode plot and find the gain crossover frequency and the phase margin.

- b) How should the gain be adjusted to obtain a  $\Phi M$  of  $50^{\circ}$ ?
- c) Using second-order correlations between time and frequency domain measures estimate the peak overshoot and settling time of the step response.
- d) Determine the **bandwidth** of the gain-compensated system.

# **Prob. 12:**

Using MATLAB for a unity-feedback control system having open-loop transfer function

$$G(s) = 5 / s(1+s)(s^2+2s+5)$$

- a) Obtain Bode plot and evaluate GCF, PCF, GM and  $\Phi M$  from it.
- b) Determine the open-loop gain to obtain gain margin of 10 dB.
- c) Determine the open-loop gain so that the gain crossover frequency becomes 1.27 rad/sec.
- d) Determine the open-loop gain to obtain phase margin of 45 degrees.

# Prob. 13:

Using MATLAB for a unity-feedback control system having open-loop transfer function

$$G(s) = K / s(10+s)(s+2)$$

Determine the value of K such that the system remains stable with (i)  $\Phi M \ge 45$  degrees and (ii) GCF as large as possible.