

### Unrestricted Grammar:-

⇒ A grammar  $G = (V, T, P, S)$  is called Unrestricted if all the productions are of the form

$$U \longrightarrow V$$

where  $U$  is in  $(V \cup T)^+$  and  $V$  is in  $(V \cup T)^*$ .

⇒ In unrestricted grammar, no conditions are imposed on the productions.

⇒ Any no. of variables and terminals can be on the left or right, and these can occur in any order.

⇒ There is only one restriction.  $\epsilon$  is not allowed as the left side of production.

eg:-

$$\begin{aligned} S &\longrightarrow S, B \\ S, &\longrightarrow aS, B \\ bB &\longrightarrow bbbB \\ aS, B &\longrightarrow aa \\ B &\longrightarrow \epsilon \end{aligned}$$

### Content Sensitive grammar:-

⇒ A grammar  $G = (V, T, P, S)$  is said to be content sensitive if all productions are of the form

$$x \longrightarrow y$$

where  $x, y \in (V \cup T)^+$  and  $|x| \leq |y|$

~~rule~~

$$\begin{aligned} \alpha &\longrightarrow \beta \\ \alpha, \beta &\in (V \cup T)^* \\ \alpha\alpha\beta &\longrightarrow \alpha\beta\gamma \end{aligned}$$

eg:  $\forall x A y \rightarrow \forall y V y$  is equivalent to  $A \rightarrow V$

can be applied in the situation where A occurs in a context of the string x on the left & the string y on the right.

### Chomsky hierarchy

- => Noam Chomsky, a founder of formal language theory, provided an initial classification into 4 language types: type 0, type 1, type 2, type 3.

For (UG) more powerful, less restricted.

$$\alpha \rightarrow \beta$$

$$\alpha \in (V+T)^+$$

$$\beta \in (V+T)^*$$

eg:

$$a A b \rightarrow b b$$

$$a A \rightarrow b b$$

only restriction.

$\Pi_1$  :- (CSG)  $A \rightarrow \epsilon$

$$\alpha \rightarrow \beta$$

$$|\alpha| \leq |\beta|$$

$$\alpha, \beta \in (V+T)^+$$

$$eg: a A b \rightarrow b b b$$

$$a A \rightarrow b b b$$

but  
 $a A b \rightarrow b b$   
 length 3      length 2  
 not allowed



T2:- CFG. PDA.

$$A \rightarrow \alpha$$

$$\alpha \in (V+T)^*$$

eg:-

$$A \rightarrow \epsilon$$

$$A \rightarrow BCD$$

Can have any variables ( $P, V$ ) on Rhs.

$$V \rightarrow (V+T)^*$$

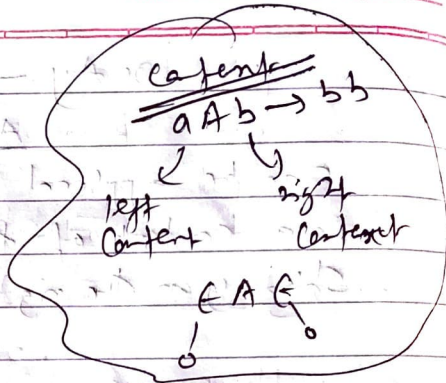


no content

content free



can have content



T3:- (RG) :- most restricted, less powerful (FA).

(RG)

Right linear

$$A \rightarrow xB / u$$

Left linear

$$A \rightarrow Bx / u$$

repetition on left

$\Rightarrow$  production contains atmost one nonterminal on the right hand side of its production.

$A, B \in V$   
 $x \in T^*$

$T \cup \epsilon$

eg:-

$S \rightarrow aS / b$   
 $S \rightarrow aS / c$  } RL

$S \rightarrow Sa / b$  } LL

$A \rightarrow \epsilon$

Linear grammar:-

There exist exactly one variable on L.H.S and at most one variable on R.H.S. is Linear grammar.

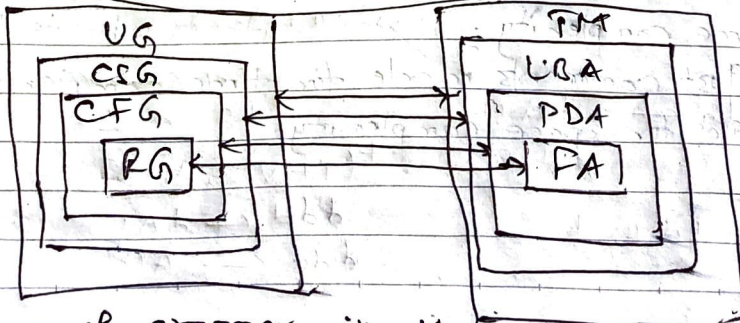
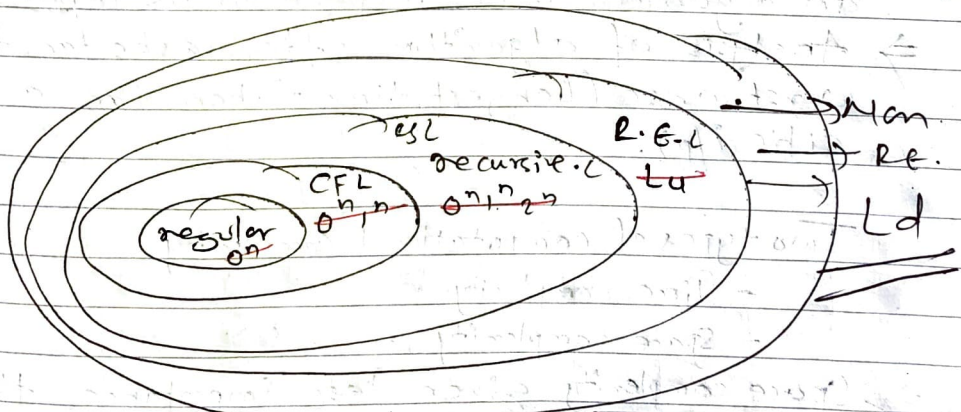


fig:- Types of grammar with their respective mathematical model.