

Assignment-2

O-1

i) $\begin{array}{r} 1101.10110011 \\ \hline 0 \quad 8 \quad 3 \end{array}$

\therefore Hexadecimal equivalent $\Rightarrow D.B3$

ii) $\begin{array}{r} 0010100110100101.10001100 \\ \hline 2 \quad 9 \quad A \quad 5 \quad 8 \quad C \end{array}$

\therefore Hexadecimal equivalent $\Rightarrow 29A5.8C$

O-2

i) $28D$
 $101011101.$

\therefore Binary equivalent $\Rightarrow 101011101$

ii) $5A3.CE2$

1011010011.11001100010

\therefore Binary equivalent $\Rightarrow 1011010011.11001100010$

O-3

$(475.25)_8 =$

$$4 \times 8^2 + 7 \times 8^1 + 5 \times 8^0 + 2 \times \frac{1}{8^1} + 5 \times \frac{1}{8^2}$$

$$256 + 56 + 5 + 0.25 + 0.078125$$

$$= 317.328125$$

Q-4

$$(1 \ 2 \ 3 \ 4)_8$$

Converting it to decimal \Rightarrow

$$1 \times 8^3 + 2 \times 8^2 + 3 \times 8^1 + 4 \times 8^0$$

$$\Rightarrow 512 + 128 + 24 + 4$$

$$\Rightarrow 640 + 28$$

$$\Rightarrow (668)_2$$

Converting decimal to hexadecimal \Rightarrow

$$\begin{array}{r} 16 | 658 \\ 16 | 41 \\ \hline & 2 \end{array} \quad \begin{array}{r} 16 | 658 \\ 16 | 41 \\ \hline & 9 \end{array}$$

↑

\therefore Hexadecimal equivalent $\Rightarrow 29C$.

Q-5

$$(A \ B6.13)_{16}$$

Converting it to binary \Rightarrow

$$(101010110110, 00010011)_2$$

Converting binary to octal \Rightarrow

$$\underline{101010110110}, \underline{00010011}$$

$$(5266.046)_8$$

∴ Octal equivalent $\Rightarrow 5266.046$

O-6

$$(4570. F8)_{11}$$

Converting it to binary \Rightarrow

$$(10001010111\boxed{0}, 1111000)_2$$

Converting binary to octal \Rightarrow

$$\begin{array}{ccccccccc} \underline{1} & \underline{0} & \underline{0} & \underline{0} & \underline{1} & \underline{0} & \underline{1} & \underline{1} & \underline{1} \\ 4 & 2 & 5 & 7 & 5 & 7 & 6 & 0 \end{array}$$

∴ Octal equivalent $\Rightarrow 42575.760$

O-7

a)

$$(16)_{10} = (10000)_2$$

$$(10)_{10} = (1010)_2$$

$$\text{Now, } (16)_{10} - (10)_{10} = (10000)_2 - (01010)_2$$

$$\text{Taking } 2^{\text{'s}} \text{ complement of } (01010)_2 = 10110$$

$$\therefore \text{Difference} \Rightarrow (10000)_2 + (10110)_2$$

$$\begin{array}{r}
 & 1 & 0 & 0 & 0 & 0 \\
 + & 1 & 0 & & 1 & 0 \\
 \hline
 & 0 & 0 & 1 & 1 & 0
 \end{array}$$

carry

Drop the carry or Drop MSB \Rightarrow 110 is the required solution.

\therefore Required difference $\Rightarrow (110)_2 = (6)_{10}$ and result is positive.

6)

$$(22)_{10} = (10110)_2$$

$$(10)_{10} = (1010)_2$$

$$\text{Now, } (22)_{10} - (10)_{10} = (10110)_2 - (01010)_2$$

Taking 2's complement of $(01010)_2 = 10110$

$$\therefore \text{Difference} = (10110) + (10110)$$

$$\begin{array}{r}
 & 1 & 0 & 1 & 1 & 0 \\
 + & 1 & 0 & & 1 & 0 \\
 \hline
 & 0 & 1 & 1 & 0 & 0
 \end{array}$$

carry

Drop the carry or Drop MSB \Rightarrow 1100 is the required solution.

\therefore Required difference $\Rightarrow (1100)_2 = (12)_{10}$ and result is positive.

Q - 8

a) $43 - 57$

$$(43)_{10} = (101011)_2$$

$$(57)_{10} = (111001)_2$$

1's complement of $(111001)_2 = 000110$

positive.

Now, $(101011)_2 + (000110)_2$

$$\begin{array}{r} 101011 \\ 000110 \\ \hline 110001 \end{array}$$

Since, there is no carry generated \Rightarrow Result is negative.

Taking 1's complement of $(10001)_2 = (001110)_2$ is the required solution = 14

\therefore Required result \Rightarrow 14 in negative.

b) $8 - 10$

$$(8)_{10} = (1000)_2$$

$$(10)_{10} = (1010)_2$$

1's complement of $(1010)_2 = 0101$

Now, $(1000)_2 + (0101)_2$

$$\begin{array}{r} 1000 \\ + 0101 \\ \hline 1101 \end{array}$$

Since, no carry is generated \Rightarrow Result is negative.

Taking 1's complement of $(1101)_2 = (0010)_2$, which is the required result = 2.

\therefore Required result = 2 in negative.

C) $8.75 - 10.624$

$$(8.75)_{10} = (1000.11)_2$$

$$(10.624)_{10} = (1010.10011)_2$$

$$(1010.10011)_2, \text{ one's complement} \Rightarrow (0101.011000)_2$$

Now, $(1000.11)_2 + (0101.011000)_2$

$$\begin{array}{r} 1000.110000 \\ + 0101.011000 \\ \hline 1110.001000 \end{array}$$

Since, there is no carry \Rightarrow Result is negative.

Taking 1's complement of $(1110.001000)_2 = (0001.110111)_2$, which is the required result = -1.874

\therefore Required result = -1.874 in negative.

d) $11.125 - 16.875$

$$(11.125)_{10} = (1011.001)_2$$

$$(16.875)_{10} = (10000.111)_2$$

One's complement of $(10000.111)_2 = (01111.000)_2$

Now, $(1011.001)_2 + (01111.000)_2$

$$\begin{array}{r} 01011.001 \\ + 01111.000 \\ \hline 11010.001 \end{array}$$

Since, there is no carry \Rightarrow result is negative

Taking 1's complement of $(11010.001)_2 = (00101.110)_2$

\therefore Required solution $\Rightarrow (00101.110)_2 = 5.75$ in negative.

O-9

a) 1010 , 2's complement \Rightarrow

$$\begin{array}{r} 0101 \\ + 1 \\ \hline 0110 \end{array}$$

\therefore 2's complement $\Rightarrow 0110$.

b) 1111 , 2's complement \Rightarrow

$$\begin{array}{r} 0000 \\ + 1 \\ \hline 0001 \end{array}$$

\therefore 2's complement $\Rightarrow 0001$.

C) 11.01 , 2's complement = $\begin{array}{r} 00.10 \\ + \quad 1 \\ \hline 00.11 \end{array}$

\therefore 2's complement = 00.11

0-11

a) 7-22

$$(7)_{10} = (111)_2$$

$$(22)_{10} = (10110)_2$$

$$\text{2's complement of } (10110)_2 = \begin{array}{r} 01001 \\ + \quad 1 \\ \hline 01010 \end{array}$$

$$\text{Now } (111)_2 + (01010)_2 \Rightarrow$$

$$\begin{array}{r} 00111 \\ + 01010 \\ \hline 10001 \end{array}$$

Since, there is no carry, hence the result is negative.

$$\text{2's complement of } (10001)_2 = \begin{array}{r} 01110 \\ + \quad 1 \\ \hline 01111 \end{array}$$

$$\therefore \text{Required result} = (01111)_2 = 15 \text{ in negative.}$$

6)

13-27

$$(13)_{10} = (1101)_2$$

$$(27)_{10} = (11011)_2$$

2's complement of $(11011)_2 \Rightarrow$

$$\begin{array}{r} (00100)_2 \\ + 1 \\ \hline 00101 \end{array}$$

Now, $(1101)_2 + (00101)_2$

$$\begin{array}{r} 0 \ 1 \ 1 \ 0 \ 1 \\ 0 \ 0 \ 1 \ 0 \ 1 \\ \hline 1 \ 0 \ 0 \ 1 \ 0 \end{array}$$

Since, there is no carry \Rightarrow result is negative.

2's complement of $(10010)_2 = (01101)_2$

$$\begin{array}{r} (01101)_2 \\ + 1 \\ \hline 1110 \end{array}$$

Required result $\Rightarrow (1110)_2 = -14$ in negative.

(C)

10 - 28

FS-81 (J)

$$(10)_{10} = (1010)_2$$

$$(28)_{10} = (11100)_2$$

2's complement of $(11100)_2$ = $\begin{array}{r} 00011 \\ + \\ \underline{00100} \end{array}$

Now, $(1010)_2 + (00100)_2$

$$\begin{array}{r} 01010 \\ + 00100 \\ \hline \underline{01110} \end{array}$$

Since, there is no carry, \Rightarrow result is negative.

2's complement of $(01110)_2 \Rightarrow \begin{array}{r} 10001 \\ + 1 \\ \hline \underline{10010} \end{array}$

Required result = $(10010)_2 = 18$ in negative.

d) $16.5 - 24.75$

$$(16.5)_{10} = (10000.1)_2$$

$$(24.75)_{10} = (11000.11)_2$$

2^r complement of $(11000.11)_2 = 00111.00$

$$\begin{array}{r} + \\ \hline 00111.01 \end{array}$$

Now, $(10000.1)_2 + (00111.01)_2 \Rightarrow$

$$\begin{array}{r} 10000.10 \\ 00111.01 \\ \hline 10111.11 \end{array}$$

Since, there is no carry, \Rightarrow result is negative.

2^r complement of $(10111.11)_2 = 01000.00$

$$\begin{array}{r} + \\ \hline 01000.01 \end{array}$$

\therefore Required result $\Rightarrow (01000.01)_2 = 8.25$ in negative.

Q-12

a) $(1011)_2$

$$\text{Ex-3} \Rightarrow \begin{array}{r} 1011 \\ 0011 \\ \hline 1110 \end{array}$$

$$\therefore \text{Required Ex-3 code} = (1110)_{\text{Ex-3}}$$

b) $(436)_8$

$$(436)_8 = (280)_{10}$$

$$\begin{array}{r} 2 & 8 & 0 \\ +3 & +3 & +3 \\ \hline 5 & 11 & 3 \\ \hline 0101 & 1011 & 0011 \end{array}$$

$$\therefore \text{Ex-3 code} \Rightarrow (010110110011)_{\text{Ex-3}}$$

c) $(3A)_{16}$

$$(3A)_{16} = (58)_{10}$$

$$\begin{array}{r} 5 & 8 \\ +3 & +3 \\ \hline 8 & 11 \\ \hline 1000 & 1011 \end{array}$$

$$\therefore \text{Ex-3 code} \Rightarrow (10001011)_{\text{Ex-3}}$$

d) $(1100,011)_2$

$$(1100,011)_2 = 12,375$$

$$\begin{array}{cccccc}
 & 1 & 2 & . & 3 & 7 \ 5 \\
 +3 & & +3 & & +3 & +3 \\
 \hline
 4 & & 5 & & 6 & 8 \\
 0100 & 0101 & 0110 & 1010 & 1000
 \end{array}$$

$$\therefore EX-3 \text{ code} \Rightarrow (01000101011010101000)_{EX-3}$$

Q-13

a) $46 + 33$

$$(46)_{10} \Rightarrow$$

$$\begin{array}{ccc}
 4 & & 6 \\
 +3 & & +3 \\
 \hline
 7 & & 9 \\
 0111 & & 1001
 \end{array}$$

$$(46)_{10} = (0111\ 1001)_{EX-3}$$

$$(33)_{10} \Rightarrow$$

$$\begin{array}{ccc}
 3 & & 3 \\
 +3 & & +3 \\
 \hline
 6 & & 6 \\
 0110 & & 0110
 \end{array}$$

$$(33)_{10} = (01100110)_{EX-3}$$

Adding \Rightarrow

$$\begin{array}{r} 0111 \\ 0110 \\ \hline 1101 \end{array} \quad \begin{array}{r} 1001 \\ 0110 \\ \hline 1111 \end{array}$$

Now subtracting EX-3 \Rightarrow

$$\begin{array}{r} 1101 \\ 0011 \\ \hline 1010 \end{array} \quad \begin{array}{r} 1111 \\ 0011 \\ \hline 1100 \end{array}$$

\therefore Required EX-3 code $\Rightarrow (10101100)_{EX-3}$

b) $72.6 + 15.2$

$$(72.6)_{10} \Rightarrow$$

$$\begin{array}{r} 7 & 2 & . & 6 \\ + 3 & + 3 & & + 3 \\ \hline 10 & 5 & & 9 \\ 1010 & 0101 & & 1001 \end{array}$$

$$(72.6)_{10} = (10100101.1001)_{EX-3}$$

$$(15.2)_{10} \Rightarrow$$

$$\begin{array}{r} 1 & 5 & . & 2 \\ + 3 & + 3 & & + 3 \\ \hline 4 & 8 & & 5 \\ 0100 & 1000 & & 0101 \end{array}$$

$$(15.2)_{10} = (01001000.0101)_{EX-3}$$

Adding \Rightarrow

$$\begin{array}{r} 1010 \\ 0100 \\ \hline 1110 \end{array} \quad \begin{array}{r} 0101 \\ 1000 \\ \hline 1101 \end{array} \quad \begin{array}{r} 1001 \\ 0101 \\ \hline 1101 \end{array}$$

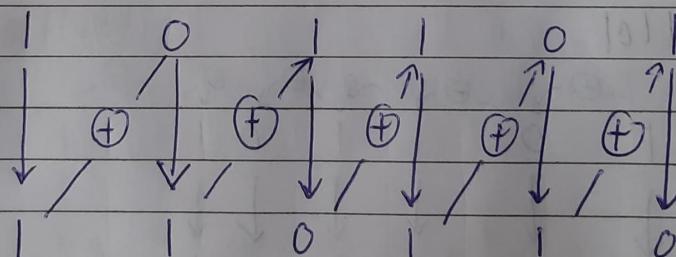
Now, subtracting EX-3 \Rightarrow

$$\begin{array}{r} 1110 \\ 0011 \\ \hline 1011 \end{array} \quad \begin{array}{r} 1101 \\ 0011 \\ \hline 1010 \end{array} \quad \begin{array}{r} 1101 \\ 0011 \\ \hline 1010 \end{array}$$

\therefore Required EX-3 code $\Rightarrow (10111010.1010)_{EX-3}$

Q-14

a) 101101



\therefore Required binary equivalent $\Rightarrow (110110)_2$

b) 1010111

$$\begin{array}{cccccccccc}
 & 1 & 0 & 1 & 0 & 1 & 1 & 1 \\
 & \downarrow \\
 1 & , & \oplus' \\
 & 1 & 1 & 0 & 0 & 1 & 0 & 1 & 0 &
 \end{array}$$

\therefore Required binary equivalent $\Rightarrow (11001010)_2$

c) 101011

$$\begin{array}{ccccccc}
 & 1 & 0 & 1 & 0 & 1 & 1 \\
 & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\
 1 & , & \oplus' & , & \oplus' & , & \oplus' \\
 & 1 & 1 & 0 & 0 & 1 & 0
 \end{array}$$

\therefore Required binary equivalent $\Rightarrow (110010)_2$

Q-15

a) 101101

$$\begin{array}{cccccc}
 & \oplus' & \oplus' & \oplus' & \oplus' & \oplus' \\
 & 1 & 0 & 1 & 1 & 0 & 1 \\
 & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\
 1 & 1 & 1 & 0 & 1 & 1
 \end{array}$$

\therefore Required gray code = $(111011)_\text{gray}$.

b) 1010111

$$\begin{array}{ccccccccc}
 & -\oplus_1 & -\oplus_2 & -\oplus_3 & -\oplus_4 & -\oplus_5 & -\oplus_6 & -\oplus_7 \\
 | & 0 & 1 & 0 & 1 & 1 & 1 & 1 \\
 \downarrow & \downarrow \\
 | & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0
 \end{array}$$

\therefore Required gray code = $(11111000)_{gray}$

c) 101011

$$\begin{array}{ccccccc}
 & -\oplus_1 & -\oplus_2 & -\oplus_3 & -\oplus_4 & -\oplus_5 & -\oplus_6 \\
 | & 0 & 1 & 0 & 1 & 1 & 1 \\
 \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\
 | & 1 & 1 & 1 & 1 & 1 & 0
 \end{array}$$

\therefore Required gray code = $(111110)_{gray}$

Q-16

a) 11011001

$$\begin{array}{cccccccc}
 & -\oplus_1 & -\oplus_2 & -\oplus_3 & -\oplus_4 & -\oplus_5 & -\oplus_6 & -\oplus_7 \\
 | & 1 & 0 & 1 & 1 & 0 & 0 & 1 \\
 \downarrow & \downarrow \\
 | & 0 & 1 & 1 & 1 & 0 & 1 & 0 & 1
 \end{array}$$

\therefore Required gray code = $(0110101)_{gray}$

b) 1110101111

$$\begin{array}{cccccccccc}
 & \oplus_1 & \oplus_2 & \oplus_3 & \oplus_4 & \oplus_5 & \oplus_6 & \oplus_7 & \oplus_8 & \oplus_9 \\
 1 & 1 & 1 & 0 & 1 & 0 & 1 & 1 & 1 & 1 \\
 \downarrow & \downarrow \\
 1 & 0 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0
 \end{array}$$

\therefore Required gray code $\Rightarrow (1001111000)_{\text{gray}}$

c) 1011011111

$$\begin{array}{cccccccccc}
 & \oplus_1 & \oplus_2 & \oplus_3 & \oplus_4 & \oplus_5 & \oplus_6 & \oplus_7 & \oplus_8 & \oplus_9 \\
 1 & 0 & 1 & 1 & 0 & 1 & 1 & 1 & 1 & 1 \\
 \downarrow & \downarrow \\
 1 & 1 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 0
 \end{array}$$

\therefore Required gray code $\Rightarrow (111011000000)_{\text{gray}}$

Q-18

The weighted code are those that obey the position weighting principle, which states that the position of each number represent a specific weight. In weighted codes, each digit is assigned a specific weight according to its position.

These non-weighted code are not positionally weighted. In other words, codes that are not assigned with any weight to each digit position.

Q-19

Complements are used in the digital computers in order to simplify the subtraction operation and for the logical manipulations. For each radix- r system (radix r represents base of number system) there are two types of complements.

1) Radix Complement \rightarrow The radix complement is referred to as the r's complement.

2) Diminished Radix Complement \rightarrow The diminished radix complement is referred to as the $(r-1)$'s complement.

O-20 Alphanumeric codes, also called character codes, are binary codes used to represent alphanumeric data. The codes write alphanumeric data, including letters of the alphabet, numbers, mathematical symbols and punctuation marks, in a form that is understandable and processable by a computer. Using these codes, we can interface input-output devices such as keyboards, monitors, printers etc. with computer.