

XIV Algorithms & Data structures

Assignment 14

I	True	False
1.	True X	
2.	X	
3.	X	
4.		X
5.	X	
6.	X	
7.	X	
8.		X
9.		X
10.		X
11.	X	

II input: adjacency list of undirected graph $G=(V,E)$
output: array of all twodegrees of all vertices.

Algorithm

1. Create an array of length $|V|$, called degree
2. For each $v \in V$, store the length of adjacency row of v in the array. v_0 gets $\text{array}[0]$, this way, $\text{array}[i]$ contains the amount of neighbors v_i has.
3. ~~For each v~~ Create a new array of length $|V|$ initialized to 0. This array is called twodegree.
4. For each edge, ~~the endpoints of edge e are v_x and v_y~~ and for both endpoints, ~~add the degree~~ v_x and v_y . Add the degree of v_x to the twodegree of v_y , and the degree of v_y to the twodegree of v_x .

The complexity of this algorithm is:

1. $O(1)$
 2. $O(|V|)$ (for each $v \in V$)
 3. $O(1)$
 4. $O(|E|)$ (for each $e \in E$)
- Total = $O(|V| + |E|)$

III These bottleneck edges are in the all start in the min-cut of G . We need to thus need to run Ford-Fulkerson to calculate the min cut:

1. Run Ford-Fulkerson
2. Find the reachable set of vertices (min-cut)
3. All edges from such a reachable ~~edge~~^{vertex} to a non-reachable vertex are bottleneck edges.

IV We can extend the binary search tree by keeping track of how many keys are smaller than a key:

For a key x , we keep track of:

x .key

x .smaller

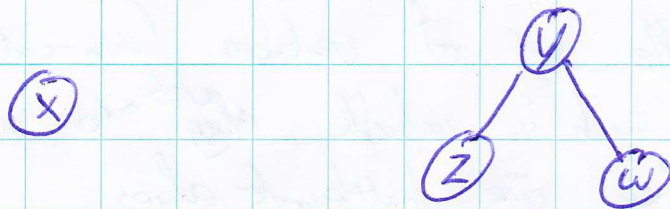
x .parent

x .left

x .right

For insertion, there are two possibilities:

Inserting x in tree:



② $x.key < y.key$:- y smaller @ $t=1$
 - insert x in Z

$x.key \geq y.key$: - insert x in w .
- $x.smallkey + 1$

For finding any node x for which there are k smaller keys, we can use this algorithm:

Algorithm: (using the same marks as above)

1. If $y_{\text{smaller}} == k$, return y
2. If $y_{\text{smaller}} < k$, ~~search~~ recursively use this algorithm to search $k - y_{\text{smaller}}$ at smaller keys in w . (y_{right})
3. If $y_{\text{smaller}} > k$, recursively use this algorithm to search k smaller keys in z (y_{left})

This algorithm works because for a node w , there are w smaller nodes in the tree plus the amount of smaller nodes the parent of w has. (because, if going up the right child of w is always larger than the child of w itself).

~~V For each item, we can calculate the value/weight ratio. This ratio will be used for adding items to the knapsack.~~

1. For a bottom-up approach, we use a 2D array k with $n+1$ columns and $W+1$ rows (n = amount of products).

Algorithm

KnapSack Algorithm (int w , int $val[]$, int n) {

int $k[n+1][w+1]$

for ($i=0; i \leq n; i++$) {

for ($we=0; we \leq w; we++$) {

if ($i==0$ and $we==0$) {

$k[i][we] = 0;$

else if ($weight[i-1] \leq we$) {

$k[i][we] = \max(val[i-1] + k[i-1][we - weight[i-1]],$

else $k[i][w] = k[i-1][w]$

either item a_i is in the knapsack or not.
 this way we can construct an algorithm:

$$K[i][w] = \begin{cases} 0 & \text{if } i = 0 \\ 0 & \text{if } w = 0 \\ \max(K[i-1][w], \text{val}[i-1] + K[i-1][w - \text{weight}[i-1]]) & \text{if } \text{weight}[i-1] \leq \text{remaining weight} \\ K[i-1][w] & \text{if } \text{weight}[i-1] > \text{remaining weight} \end{cases}$$

2. We can keep track of another ~~bool~~ array. This array indicates whether an item at place i is in the knapsack or not. This array will also keep track of the ~~prev~~ choice made:

```
struct Choice {
    prev previous = choice + null choice previous;
    bool in the file
}
```


KnapSack Algorithm (int w, int weight[], int val[], int n) {

int k[n+1][w+1];

choice C[n+1][w+1];

for (i=0; i<=n; i++) {

for (we=0; we<=w; we++) {

if (i==0 or we==0) {

k[i][we] = 0;

choice[i][we] = null;

else if (weight[i-1] <= we) {

k[i][we]

if (val[i-1] + k[i-1][we-weight[i-1]] >= k[i-1][we]) {

k[i][we] = val[i-1] + k[i-1][we-weight[i-1]];

C[i][we].in = true;

C[i][we].previous = C[i-1][we-weight[i-1]];

else {

k[i][we] = k[i-1][we];

C[i][we].in = false;

C[i][we].previous = C[i-1][we];

else {

k[i][we] = k[i-1][we];

C[i][we].in = false;

C[i][we].previous = C[i-1][we];

}

}

while

choice c = ([k]w]

while (c != null) {

print c if (c.in) {

print(~~loc~~) print(c);

}

}