

$$\Delta X = \cos \beta \Delta 1 - \sin(\beta + \varphi) \Delta 2$$

$$\Delta y = \sin \beta \Delta 1 + \cos(\beta + \varphi) \Delta 2$$

$$\begin{cases} \cos \beta CM_1 k_1 - \sin(\beta + \varphi) CM_2 k_2 = 0 & \dots (1) \end{cases}$$

$$\begin{cases} \sin \beta CM_1 k_1 + \cos(\beta + \varphi) CM_2 k_2 = 222 & \dots (2) \end{cases}$$

$$\begin{cases} \sin \beta CM_1 k_1' + \cos(\beta + \varphi) CM_2 k_2' = 0 & \dots (3) \end{cases}$$

$$\begin{cases} \cos \beta CM_1 k_1' - \sin(\beta + \varphi) CM_2 k_2' = 222 & \dots (4) \end{cases}$$

由 (1)(3)

$$CM_1 k_1 \cos \beta = CM_2 k_2 \sin(\beta + \varphi)$$

$$CM_1 k_1' \sin \beta = -CM_2 k_2' \cos(\beta + \varphi)$$

相除

$$\frac{k_1}{k_1'} \cot \beta = -\frac{k_2}{k_2'} \tan(\beta + \varphi)$$

由 (2)(4)

$$CM_1 (k_1 \sin \beta - k_1' \cos \beta) +$$

$$CM_2 (k_2 \cos(\beta + \varphi) + k_2' \sin(\beta + \varphi)) = 0$$

$$\therefore \frac{CM_1}{CM_2} = -\frac{k_2 \cos(\beta + \varphi) + k_2' \sin(\beta + \varphi)}{k_1 \sin \beta - k_1' \cos \beta}$$

由 (1)(3)

$$CM_1 (k_1 \cos \beta + k_1' \sin \beta) +$$

$$CM_2 (-k_2 \sin(\beta + \varphi) + k_2' \cos(\beta + \varphi)) = 0$$

$$\therefore \frac{CM_1}{CM_2} = \frac{k_2 \sin(\beta + \varphi) - k_2' \cos(\beta + \varphi)}{k_1 \cos \beta + k_1' \sin \beta}$$

$$\cos 2 = k_1 \cos \beta + k_1' \sin \beta$$

$$\frac{k_2 \cos(\beta + \varphi) + k_2' \sin(\beta + \varphi)}{-k_1 \sin \beta + k_1' \cos \beta} = \frac{k_2 \sin(\beta + \varphi) - k_2' \cos(\beta + \varphi)}{k_1 \cos \beta + k_1' \sin \beta}$$

$$\begin{aligned} & k_1 k_2 \cos \beta \cos(\beta + \varphi) + k_1 k_2' \cos \beta \sin(\beta + \varphi) \\ & + k_1' k_2 \sin \beta \cos(\beta + \varphi) + k_1' k_2' \sin \beta \sin(\beta + \varphi) \\ & = -k_1 k_2 \sin \beta \sin(\beta + \varphi) + k_1 k_2' \sin \beta \cos(\beta + \varphi) \\ & + k_1' k_2 \cos \beta \sin(\beta + \varphi) - k_1' k_2' \cos \beta \cos(\beta + \varphi) \end{aligned}$$

$$\begin{aligned} \text{Eg: } & k_1 k_2 \cos(\beta - \beta - \varphi) + k_1 k_2' \sin(\beta + \varphi - \beta) \\ & + k_1' k_2 \sin(\beta - \beta - \varphi) + k_1' k_2' \cos(\beta + \varphi - \beta) = 0 \end{aligned}$$

$$k_1 k_2 \cos \varphi + k_1 k_2' \sin \varphi - k_1' k_2 \sin \varphi + k_1' k_2' \cos \varphi = 0$$

$$\therefore \cos \varphi (k_1 k_2 + k_1' k_2') = \sin \varphi (k_1' k_2 - k_1 k_2')$$

$$\therefore \tan \varphi = \frac{k_1 k_2 + k_1' k_2'}{k_1' k_2 - k_1 k_2'}$$

$$\frac{k_1}{k_1'} \cot \beta = - \frac{k_2}{k_2'} \tan(\beta + \varphi)$$

$$\tan(\beta + \varphi) = \frac{\tan \beta + \tan \varphi}{1 - \tan \beta \tan \varphi}$$

$$cm_2 = k_1 \cos \beta + k_1' \sin \beta$$

$$\frac{cm_2}{cm_1} = \frac{k_1 \cos \beta + k_1' \sin \beta}{k_2 \sin(\beta + \varphi) - k_2' \cos(\beta + \varphi)} = m$$

$$cm_1 = \frac{y}{k_1 \sin \beta + mk_2 \cos(\beta + \varphi)}$$

对于 X, Y 运动方向不同的两种情况

区别仅在于解方程时 ①+③, ②+④

结果变为

$$\tan \varphi = - \frac{k_1 k_2 + k_1' k_2'}{k_1' k_2 - k_1 k_2'}$$

β , cm_1 , cm_2 形式不变