Before you start:

Homework Files

You can download the starter files for coding as well as this *tex* file (you only need to modify *homework3.tex*) on canvas and do your homework with latex. Or you can scan your handwriting, convert to pdf file, and upload it to canvas before the due date. If you choose to write down your answers by hand, you can directly download the pdf file on canvas which provides more blank space for solution box.

Submission Form

For homework 3, there are only one part of submission, which is a pdf file as your solution named as VE281_HW3_[Your Student ID]_[Your name].pdf uploaded to canvas. Estimated time used for this homework: **3-4 hours.**

Great credits to 2020FA VE281 TA Group and enormous thanks to 2021SU VE281 TA Roihn!!!

Student Info (0 point) 0

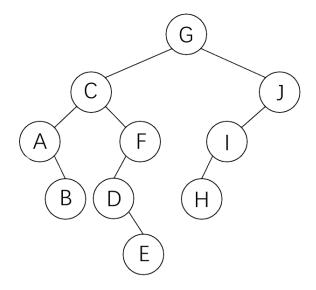
Your name and student id:

Solution:

Tree Traversal (27 points)

Given A Tree (16 points)

Given a binary tree below, please write out the following traversals:



(a) Pre-order depth-first traversal. (4 points)

Solution:

(b) Post-order depth-first traversal. (4 points)

Solution:

(c) In-order depth-first traversal. (4 points)

Solution:

(d) Level-order traversal. (4 points)

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1.2 Draw The Tree (11 points)

a) Now we have a specific binary tree, but we only know some of its traversals. Its pre-order traversal is: FBADCEGIH, and its in-order traversal is: ABCDEFGHI. Then please draw out the binary tree and show its post-order traversal. (4 points)

Solution:

前序第一个F为根节点,则看中序中F左边为左子树,右边为右子树 然后,ABCDE中前序中B为第一个,为左子树根节点,如此

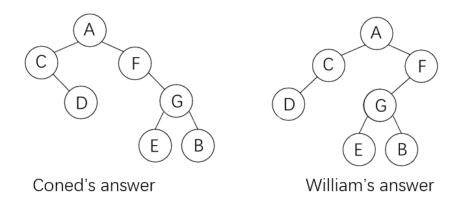
b) Now we have a specific binary tree, but we only know some of its traversals. Its post-order traversal is: FEKLJIHG, and its in-order traversal is: EFGHIKJL. Then please draw out the binary tree and show its pre-order traversal. (4 points)

Solution:

后序最后一个G为根节点,则看中序中G左边为左子树,右边为右子树 然后,EF中后序中E为最后一个,为左子树根节点,如此

c) Now students are required to draw out the binary tree according to the given traversals: Its pre-order traversal is: ACDFGEB, and its post-order traversal is: DCEBGFA. Then please draw out the binary tree and show its pre-order traversal.

William and Coned both provide their plot of the unknown trees.



Their answers are totally different, but seem to be both correct. Can you explain why such a case happens? (3 points)

Solution:			

2 True or False (20 points)

Please judge whether the following statements are **TRUE** or **FALSE**. You can briefly state your reason if you would like to get partial points. No deduction if the solution is right without explanation. Each question takes 2 points.

a) A complete tree is a tree where every node has either 0 or 2 children.

Solution:			

b) A complete tree is a tree where every level except the last is necessarily filled, and in the last level, nodes are filled in from left to right.

	Solution:
c)	Heapsort has worst-case $\Theta(n \log n)$ time complexity.
	Solution:
d)	Percolate-up has an average-case time complexity of $\Theta(\log n)$.
	Solution:
e)	Dequeue is done by simply removing the root.
	Solution:
f)	Enqueue in a min-heap is done by inserting the element at the end, and then calling percolate-up.
	Solution:
g)	[1, 13, 17, 23, 14, 16, 20, 35] is a representation of a min-heap.
	Solution:
h)	[83, 47, 9, 22, 15, 7, 1, 20] is a representation of a max-heap .
	Solution:

i) Proceeding from the bottom of the heap to the top, while repeatedly calling percolateDown()

can initialize a min-heap.

	Solution:
	roceeding from the top of the heap to the bottom, while repeatedly calling percolateUp() car ot initialize a min-heap.
	Solution:
3	Min Heap (23 points)
Cons	sider a min-heap represented by the following array:
	$\{2, 3, 8, 16, 46, 34, 42, 35, 26\}$
the r	the following operations, tell how many percolations (either up or down) are needed and show result of the heap after each percolation in either tree form or array form. The value of 1 into this min-heap. (4 points)
	Solution:
) A	fter a), push the value of 5 into this min-heap. (4 points) Solution:

c) After b), update element 2 to have a value of 37 (Suppose you have the access to each element).

(5 points)

	Solution:
d)	After c), remove the min element from the heap. (5 points)
	Solution:
e)	After d), update element 26 to have a value of 4 (Suppose you have the access to each element) (5 points)
	Solution:

4 Binary Search Tree (30 points)

4.1 Simple simulation (16 points)

Perform the following operations to construct a binary search tree. Show the result of the BST after each operation in either tree form or array form.

a)	a) Insert 24, 29, 22, 25, 19, 32, 15, 37 (3 points)						
	Solution:						
b)	Delete 22 (3 points)						
	Solution:						
c)	Delete 29 (3 points)						
	Solution:						

d) Insert 22 (3 points)

	Solution:
,	What is the in-order predecessor of node 25? What is the in-order successor of node 32? (4 points)
	Solution:
4.2	2 Better than linear selection? (14 points)
eith	the learning the application of the BST, Coned thinks that with BST, rank search can be done her in a faster way or with less space compared with the linear selection algorithms introduced the lecture.
	Compare BST rank search with deterministic selection algorithm in terms of time complexity and space usage briefly. Assume that for each node, a variable <i>leftsize</i> is maintained as introduced in the lecture. (8 points)
	Solution:

b)	William, our master of algorithm, has a different idea again. He states that for the linear selection
	algorithm, the input can be arbitrary array while for BST rank search, you have to first build
	up a binary search tree, which will also take some time. Therefore, the average time complexity
	of BST rank search is not better than $O(n)$. Is he right? (6 points)
	Assume that we are working on a fixed array.

Solution:			

Reference

Assignment 3, VE281, FA2020, UMJI-SJTU. Homework 2, VE281, SU2021, UMJI-SJTU.