

Pref quals for high quality triangle mesh

- Close to EQUILATERAL triangles - Vertex close to 60° - Angles close to 60°

Manifolds

- Every edge is shared by exactly 2 triangles - There is a single complete loop of triangles around each vertex

Manifolds with Boundary

- Every edge is shared by 1 or 2 triangles - Vertex connect to a single edge connected triangle loop (can not connect 2 different groups of triangles) - Every manifold is also a manifold with boundary

Texture Wrapping

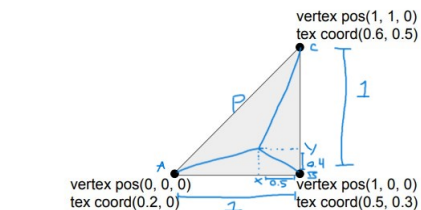
GL_CLAMP_TO_EDGE = take outer most pixels and repeat until the edge is reached

GL_REPEAT = repeat the image in a grid with all oriented the same way

GL_MIRRORED_REPEAT = repeat image in a grid with all mirrored along axis between original and new

Barycentric interpolation of texture coords

Ex. For texture position (0.5, 0.4, 0)



$$S_{ABC} = \frac{AB \cdot AC}{2} = \frac{1 \cdot 1}{2} = 0.5$$

$$S_{PAB} = \frac{AB \cdot PX}{2} = \frac{1 \cdot 0.4}{2} = 0.2$$

$$S_{PBC} = \frac{BC \cdot PY}{2} = \frac{1 \cdot 0.5}{2} = 0.25$$

So $P = \alpha A + \beta B + \gamma C$ Where α, β, γ are the barycentric coords of P

$$\alpha = \frac{S_{PBC}}{S_{ABC}} = \frac{0.25}{0.5} = 0.5$$

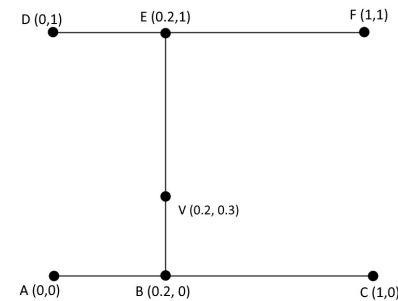
$$\gamma = \frac{S_{PAB}}{S_{ABC}} = \frac{0.2}{0.5} = 0.4$$

$$\beta = 1 - \alpha - \gamma = 1 - 0.5 - 0.4 = 0.1$$

$$\begin{aligned} \text{So } P &= 0.5A + 0.1B + 0.4C \\ &= 0.5(0.2, 0) + 0.1(0.5, 0.3) + 0.4(0.6, 0.5) \\ &= (0.1, 0) + (0.05, 0.03) + (0.24, 0.2) \\ &= (0.39, 0.23) \end{aligned}$$

Bilinear texture filtering

Ex. For vertex v's texture coord (0.2, 0.3)



Color of E:

$$E = 0.8C + 0.2D = 0.8(1, 0, 0) + 0.2(0, 0, 0) = (0.8, 0, 0)$$

Color of B:

$$B = 0.8A + 0.2C = 0.8(0, 1, 0) + 0.2(0, 0, 1) = (0, 0.8, 0.2)$$

Color of V:

$$V = 0.7B + 0.3E = 0.7(0, 0.8, 0.2) + 0.3(0.8, 0, 0) = (0.24, 0.56, 0.14)$$

Level of mipmap

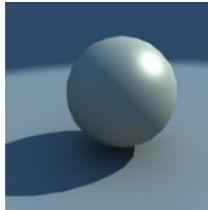
mipmap level = $\log_2 D$ where D = length of longest edge

Just approximate the size of the longest edge and use calculator

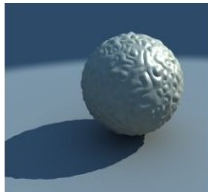
$$\log_2(x) = \log(x)/\log(2)$$

Types of maps

Nothing:



Displacement map:



Bump map:



Properties of light sources

Point Light - Illuminate in all directions and attenuated with distance
Directional Light - The light rays are nearly parallel to each other and there is no attenuation with distance

Spot Light - illuminates in a specific direction and attenuated with distance

Ambient Light - Tries to approximate global illumination and has a constant irradiance at every location and in all directions

Specular Exponent

Smaller specular exponent = larger shiny/white area

Larger specular exponent = smaller shiny/white area

Properties of Curves

Single Polynomial - Interpolation, C^2 continuity, Locality
Natural Cubic Spline - Interpolation, C^2 continuity, Locality
Hermite Cubic Spline - Interpolation, C^2 continuity, C^1 , Locality
Vardinal/Catmull-Rom - Interpolation, C^2 continuity, C^1 , Locality

Hermite vs Vardinal cubic Splines

Hermite - Users have to specify first derivatives of all control points

Cardinal - First derivatives are calculated from the neighbor control points

Terminology

Radiant Flux Φ - Power with units in W or J/s

Irradiance E - Power per unit area with unit in $\frac{W}{m^2}$

Radiance L - Power per unit area per direction with unit in $\frac{W}{m^2 \cdot sr}$

Radiant Intensity I - Power per direction with unit in $\frac{W}{sr}$

Acronyms

BRDF - Bidirectional Reflectance Distribution Function

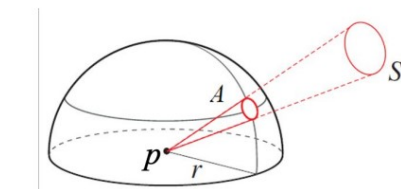
AABB - Axis-Aligned Bounding Box

BVH - Bounding Volume Hierachy

BSP - Binary Space Partition

Hemisphere Projection

Object has area $S=100$, and it is projected onto hemisphere with radius $r=3$, the projected area is $A=45$. What is the solid angle of this object with respect to the point p?



$$\text{solid angle} = \frac{A}{r^2} = \frac{45}{9} = 5$$

Rendering Equation

$$L(P, \omega_o) = L_e(P, \omega_o) + \int_{\Omega} f_r(P, \omega_i, \omega_o) L_i(P, \omega_i) \cos \Theta_i d\omega_i$$

L_e = emitting light radiance

f_r = reflection of incoming light

ω_i = incoming direction

ω_o = outgoing direction

L_i = incoming light radiance

Reflection models

Phong - Uses the angle between the view and reflection vector for computing specular reflection

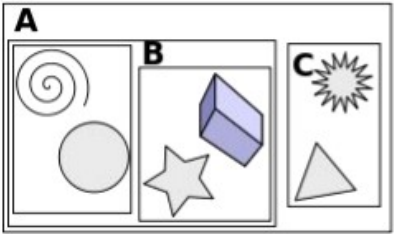
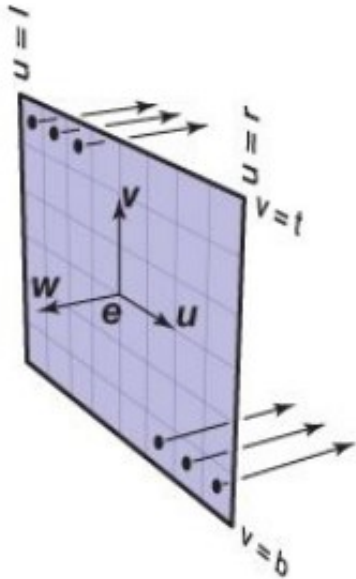
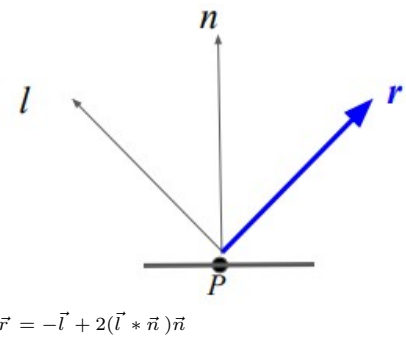
Blinn-Phong - Uses the angle between the normal and halfway vector for computing specular reflection

Shading models

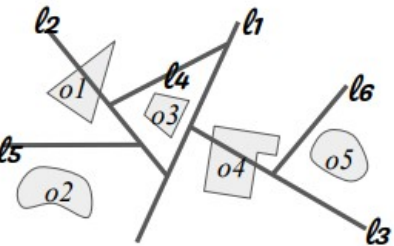
Gouraud - Uses pervertex color computation

Phong - Uses perfragment color computation

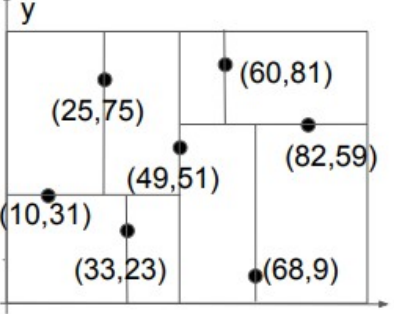
Mirrored reflection calculation



BSP:

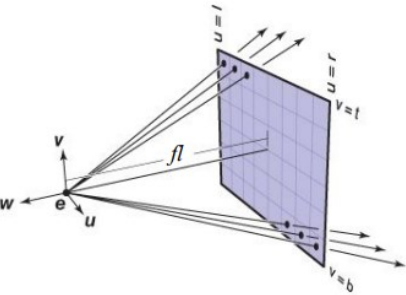


KD tree:



Ray tracing Modes

Perspective:



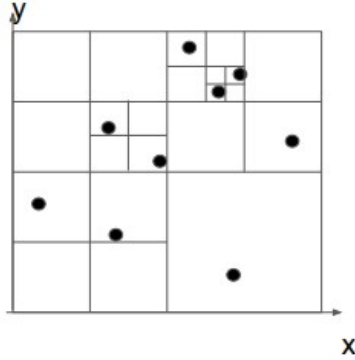
Orthographic:

Raytracing Calculation

Ray $r = o + t d$, where $o(2,3,4)$, $d(-1, 0, 0)$, what is the t value when it intersects with plane $y=3x$?
 $r = o + t d = (2, 3, 4) + t(-1, 0, 0) = (2 - t, 3, 4)$
 $y = 3x \rightarrow 3 = 3(2 - t) \rightarrow y/3 = 2 - t \rightarrow 1 = 2 - t \rightarrow t = 1$

Data structures

Quad-tree:

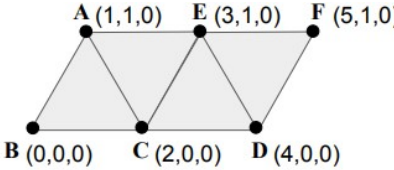


BVH:

Data structure Applications

- Quad - Image Compression
- BVH - Ray Tracing
- BSP - Painter's Algo
- KD tree - Nearest Neighbor Search

Triangle Mesh Representation



vertices = $[(1, 1, 0), (0, 0, 0), (2, 0, 0), (4, 0, 0), (3, 1, 0), (5, 1, 0)]$
triangles = $[(0, 1, 2), (0, 2, 4), (4, 2, 3), (4, 3, 5)]$