

Master Theorem Practice

$$T(n) = 3T\left(\frac{n}{9}\right) + \sqrt{n}$$

$$a = 3, b = 9, f(n) = n \quad n^{\log_b a} = n^{\log_9 3} = n^{\frac{1}{2}} \quad \text{Case: Case 2 Result: } \Theta(n^{\frac{1}{2}} \log n)$$

$$T(n) = 4T\left(\frac{n}{2}\right) + n^3$$

$$a = 4, b = 2, f(n) = n^3 \quad n^{\log_b a} = n^{\log_2 4} = n^2 \quad \text{Case: Case 3 Result: } \Theta(n^3)$$

$$5T\left(\frac{n}{4}\right) + n \log n$$

$$a = 5, b = 4, f(n) = n \log n \quad n^{\log_b a} = n^{\log_4 5} \quad \text{Case: Case 1 Result: } \Theta(n^{\log_4 5})$$