

Binary Trees

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- General trees & binary trees
- Binary search trees (BST)
- Operations on BST (Conceptual)
 - Find
 - Traverse
 - Insert
 - Delete

Introduction

- Trees are one of the fundamental data structures
- Many real-world phenomena cannot be represented in the data structures we've had so far

Array & Linked List

● Array

- Easy to search
 - $O(\log 2n)$ – Binary search
- Slow Insertion & Deletion

● Linked List

- Easy to insert, delete
- But slow in searching, deleting the given item, ...

Trees

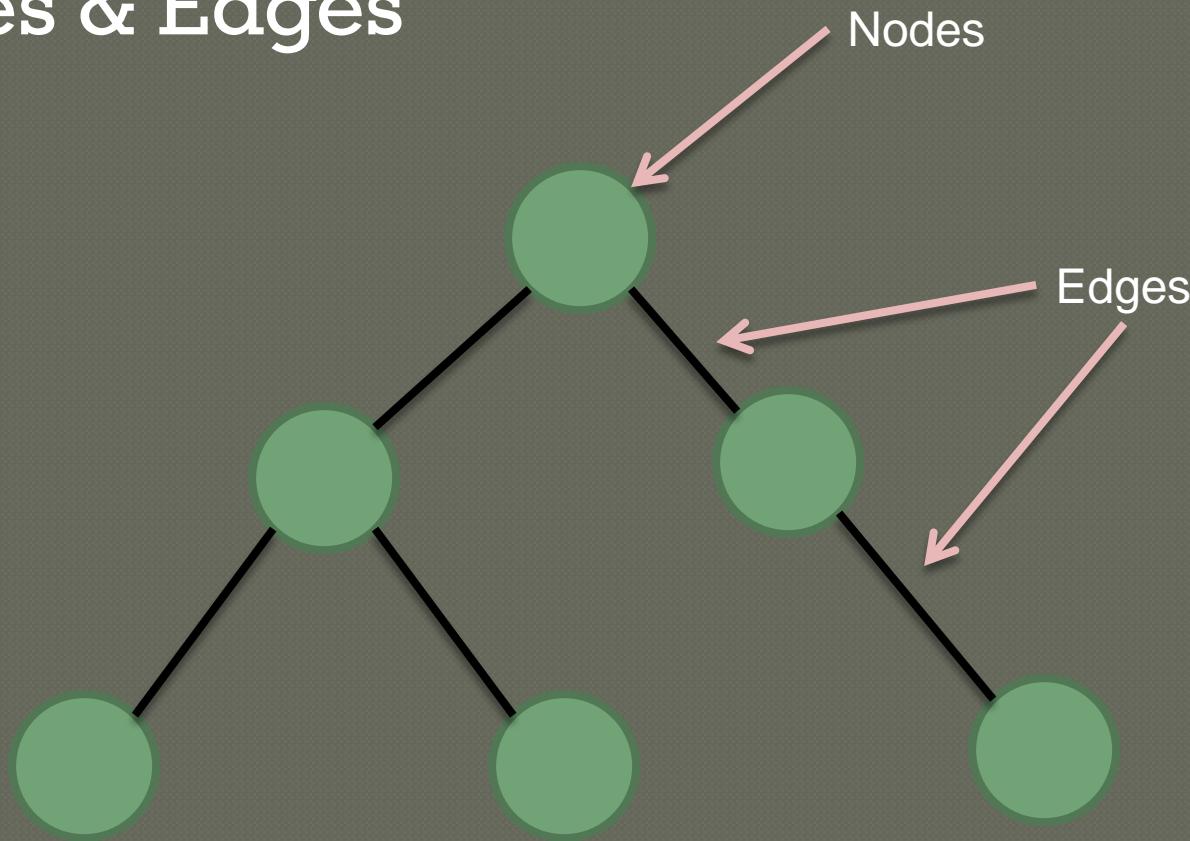
Is a data structure with

- ◎ Quick Insertion
 - ◎ Quick Deletion
 - ◎ Quick Searching
- Interesting data structures

What is a Tree?

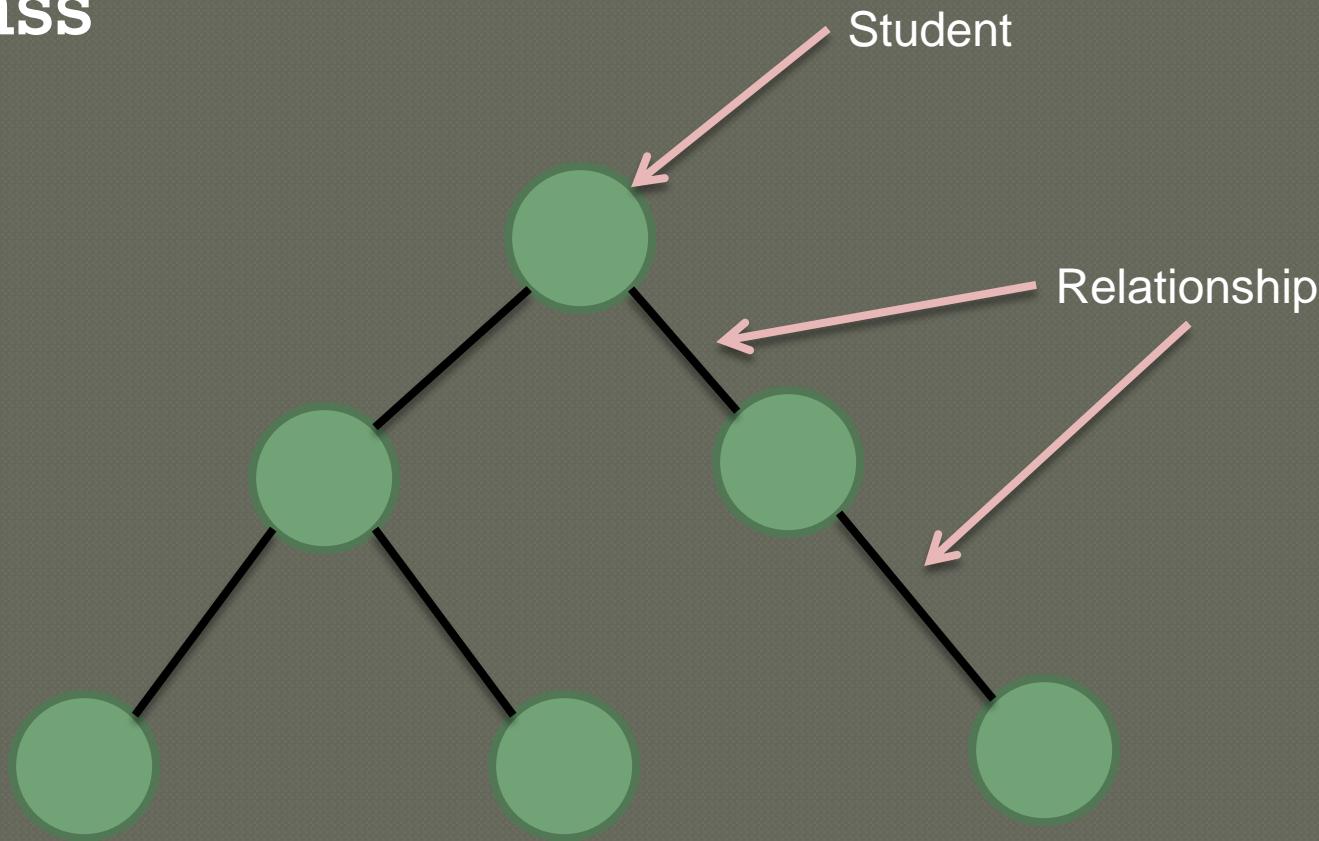
A tree consists of

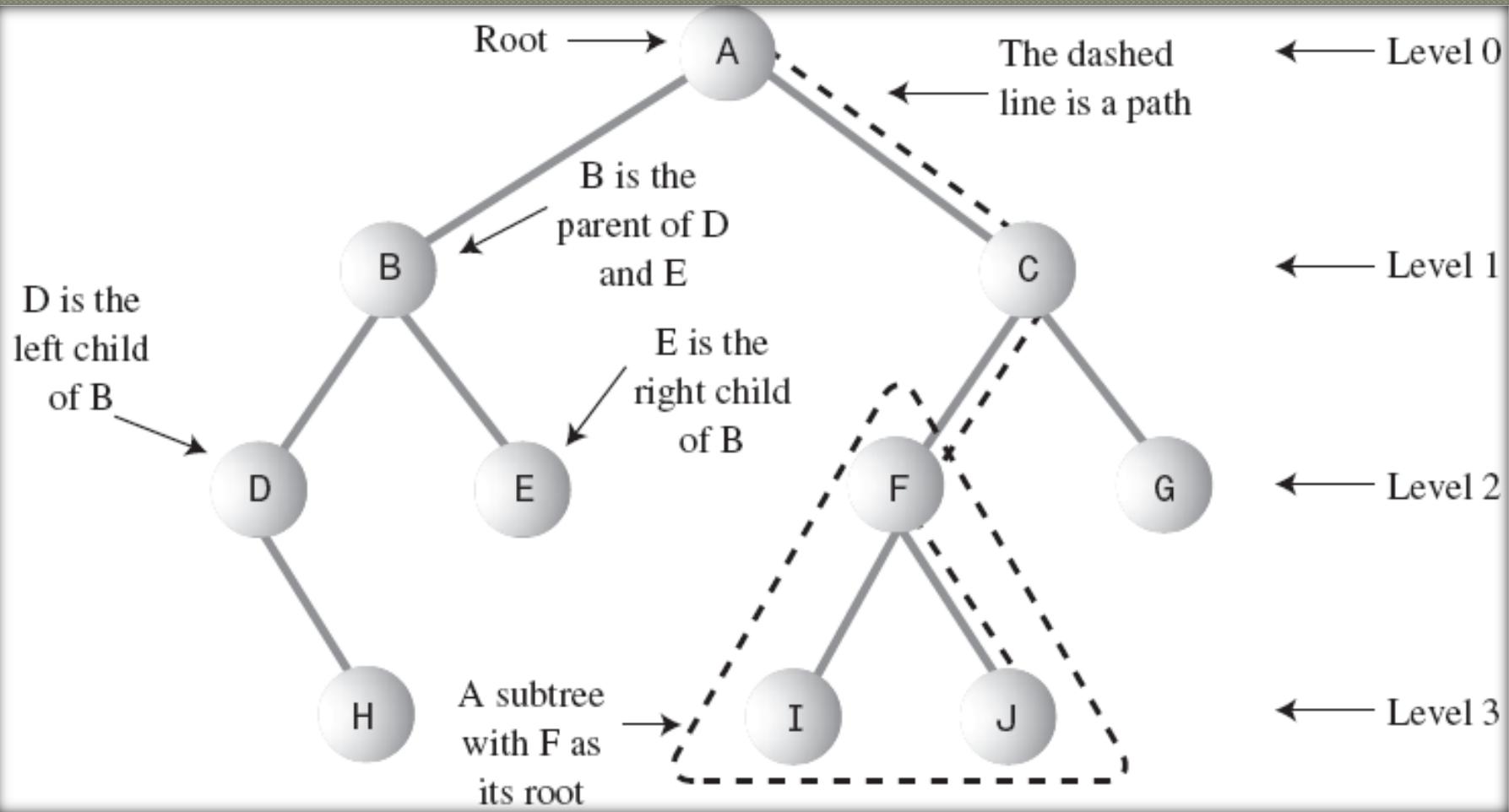
- Nodes & Edges



Trees as tool

- Describe relationships between students in class





Trees terminology

Path, Root, Parent, Child, Leaf, Subtree, Visiting, Traversing, Levels, Keys

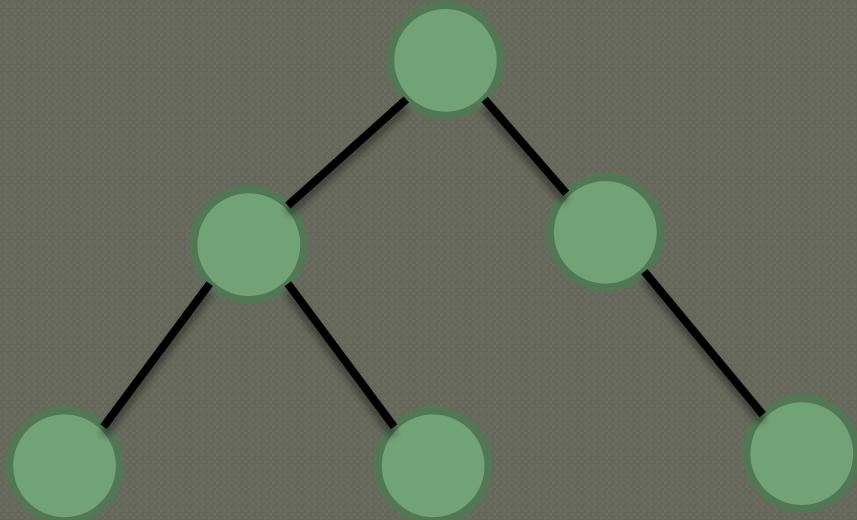
Properties of Trees

- Have one and only one Root
- One and only one Path from root to any other node
 - → Only one parent
 - → No circles
- Example
 - File hierarchy

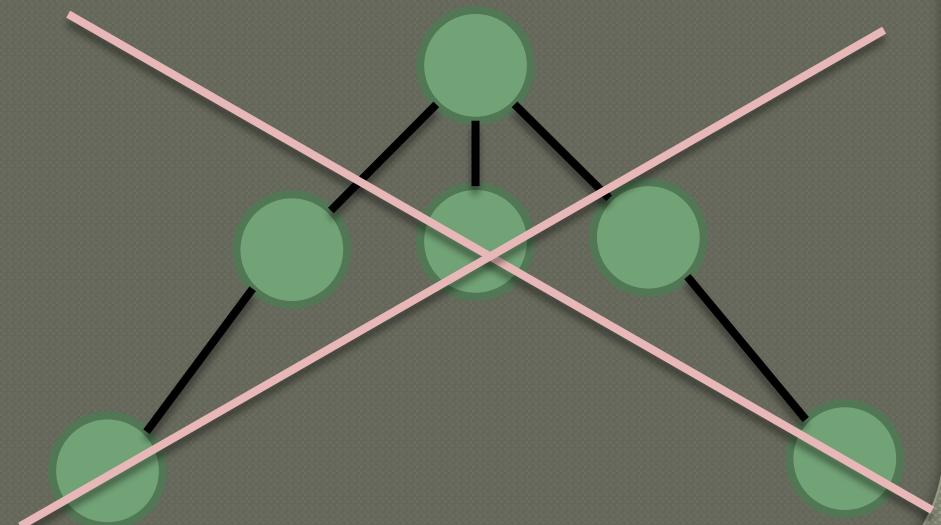
Binary tree

- Is a tree and
- every node have at most two children

Binary tree

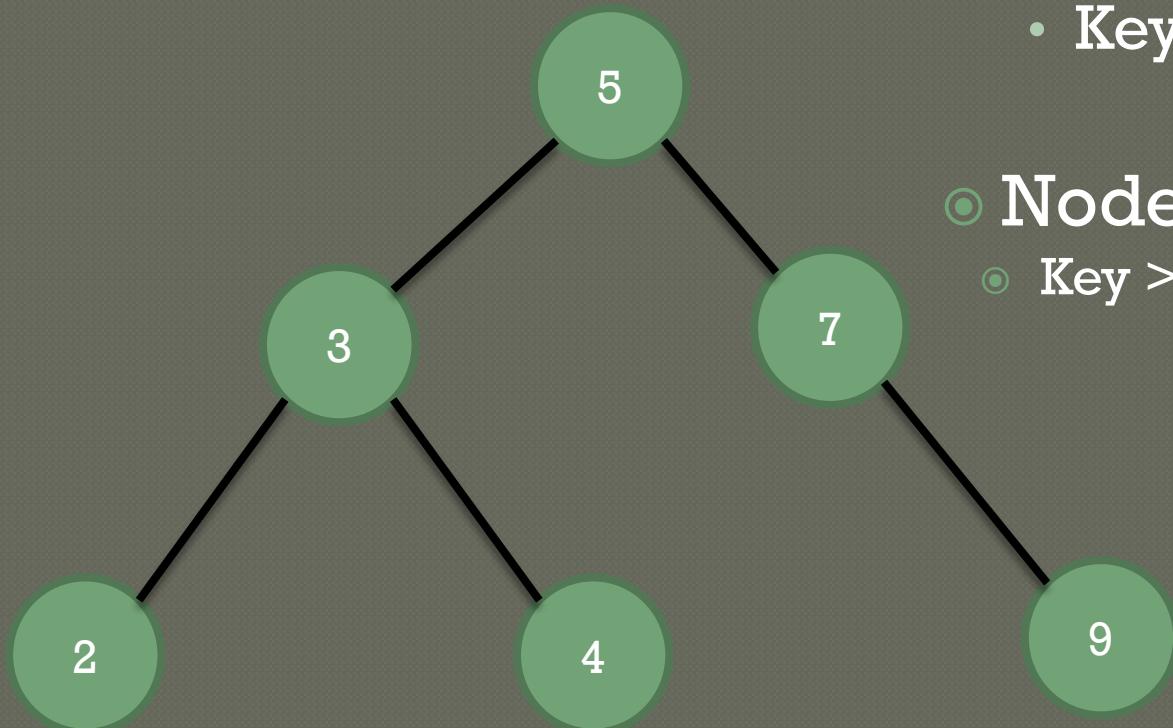


Not a binary tree



Binary search tree (BST)

Properties

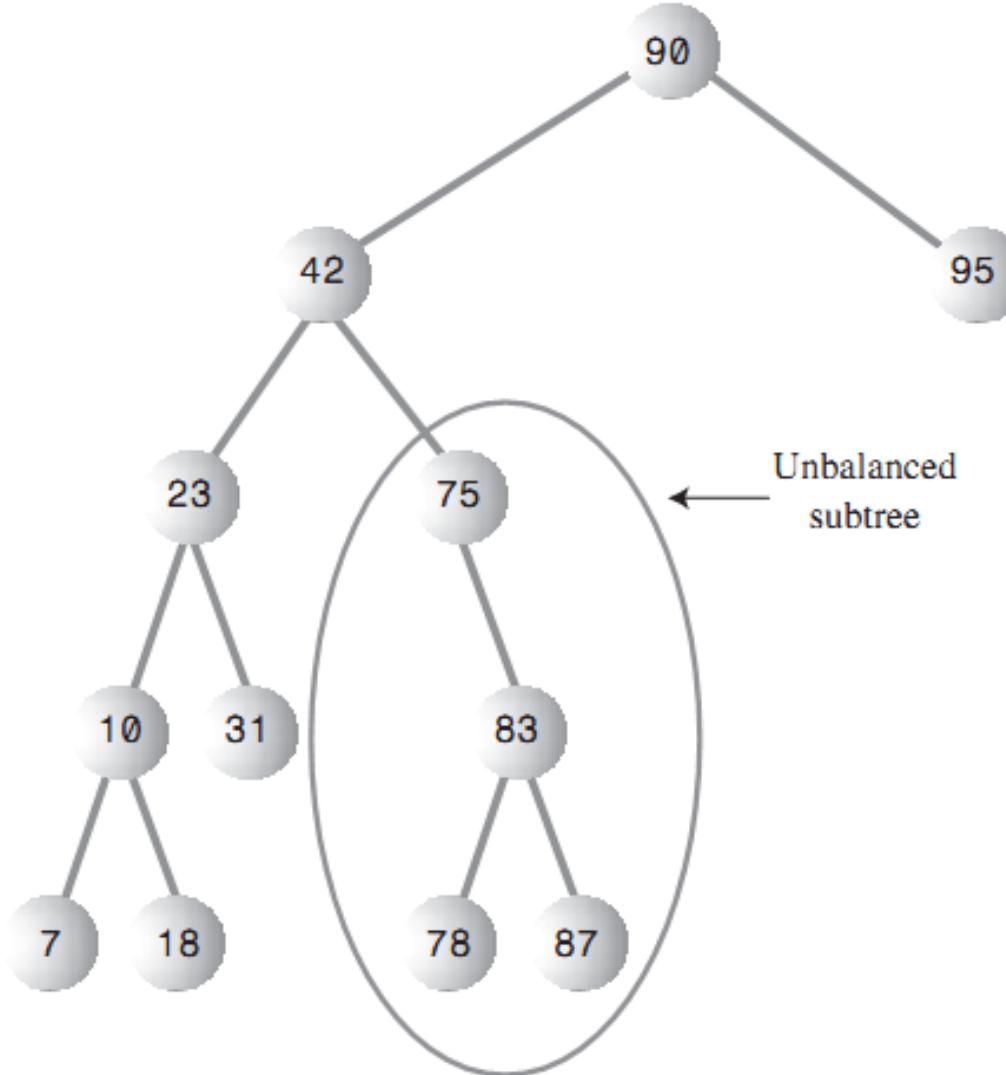


- ◎ Node's left child:
 - Key < Key of Parent
- ◎ Node's right child:
 - Key \geq Key of Parent

How Do BST Work?

- Need to carry out basic tree operations such as
 - finding a node,
 - traversing a tree,
 - adding a node,
 - deleting a node, etc.
- This is what this chapter is all about

Unbalanced tree

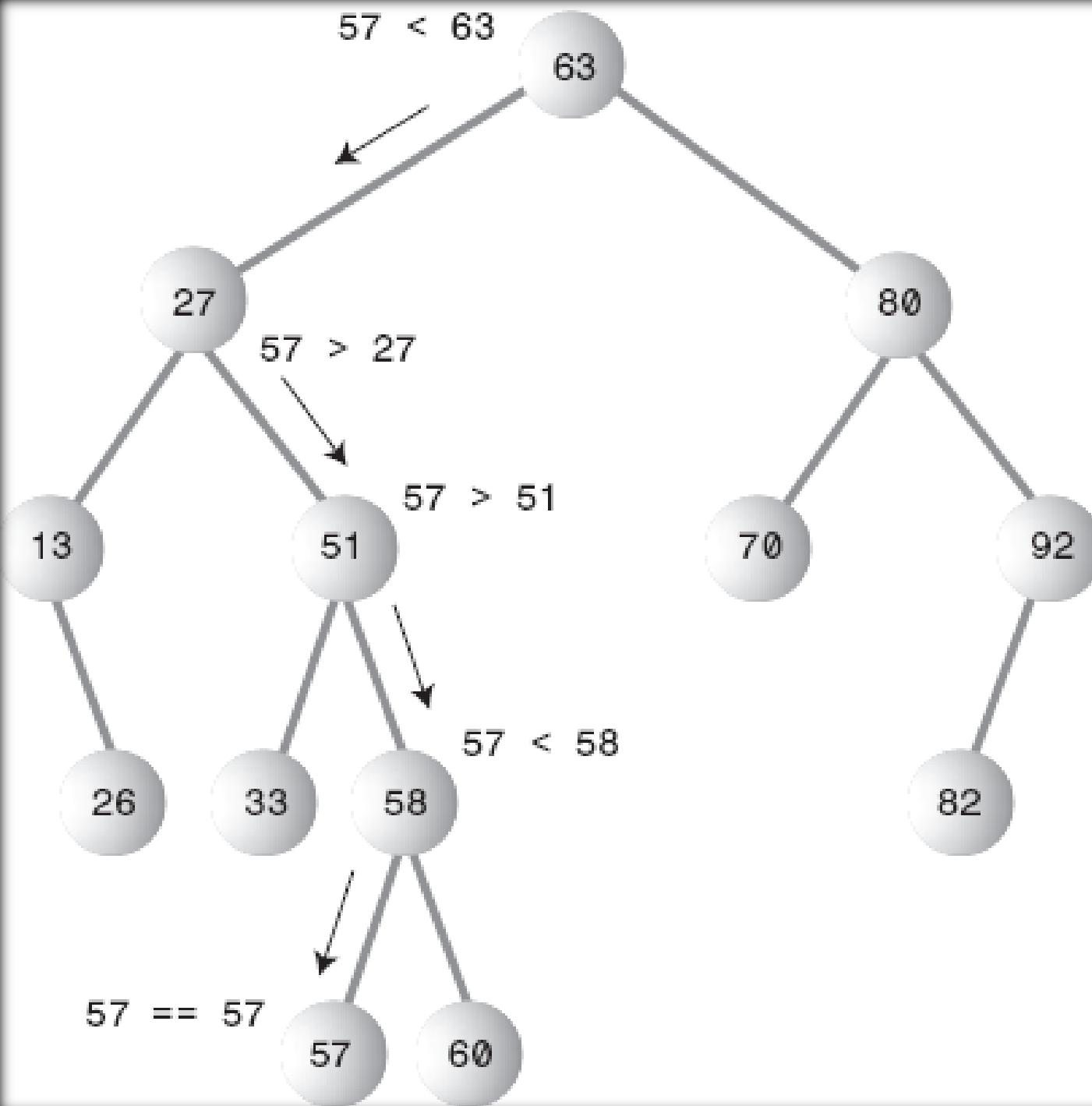


Unbalanced tree

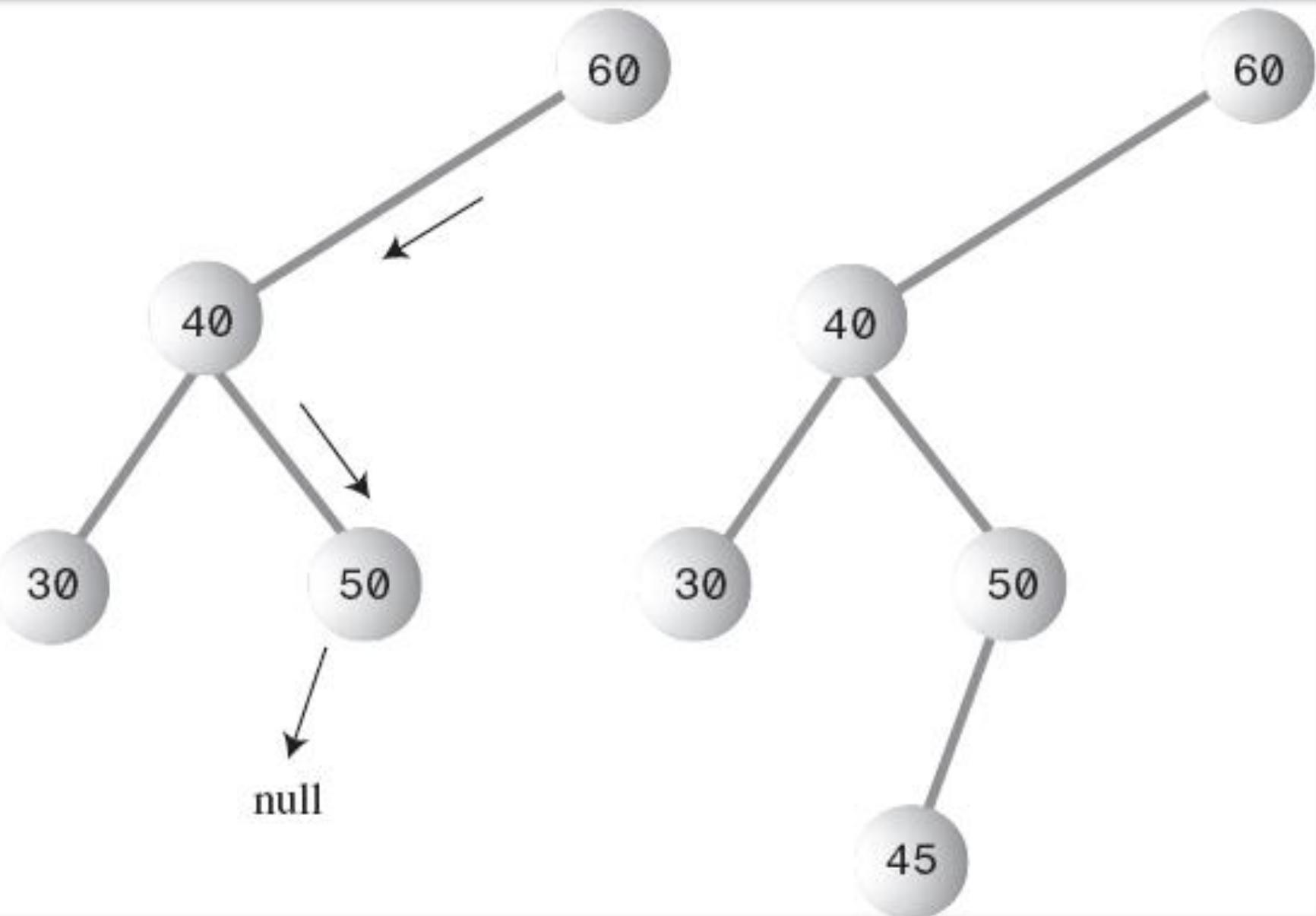
- Is when nodes are mostly in one side
- Is the result of the way they are created
- Prefer balanced tree

Operations on BST

Conceptual algorithms



Finding



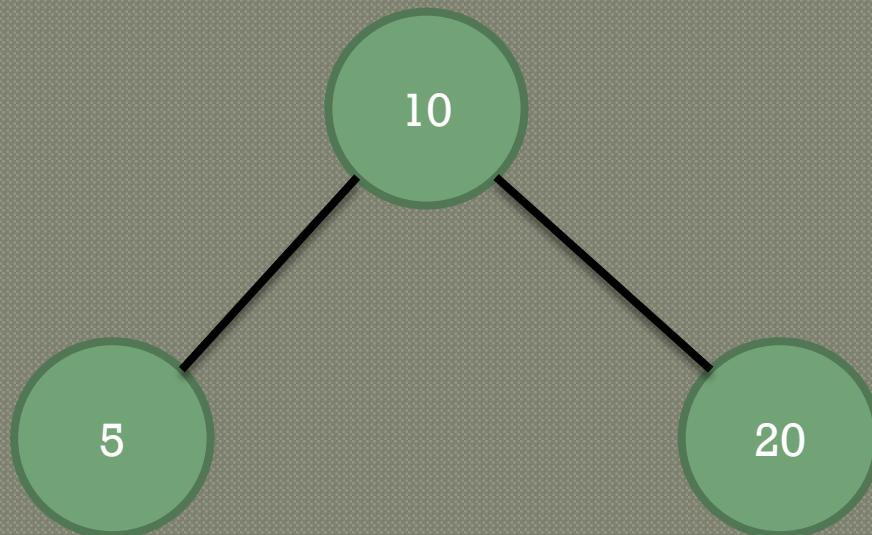
Insert 45 into the tree

Insertion

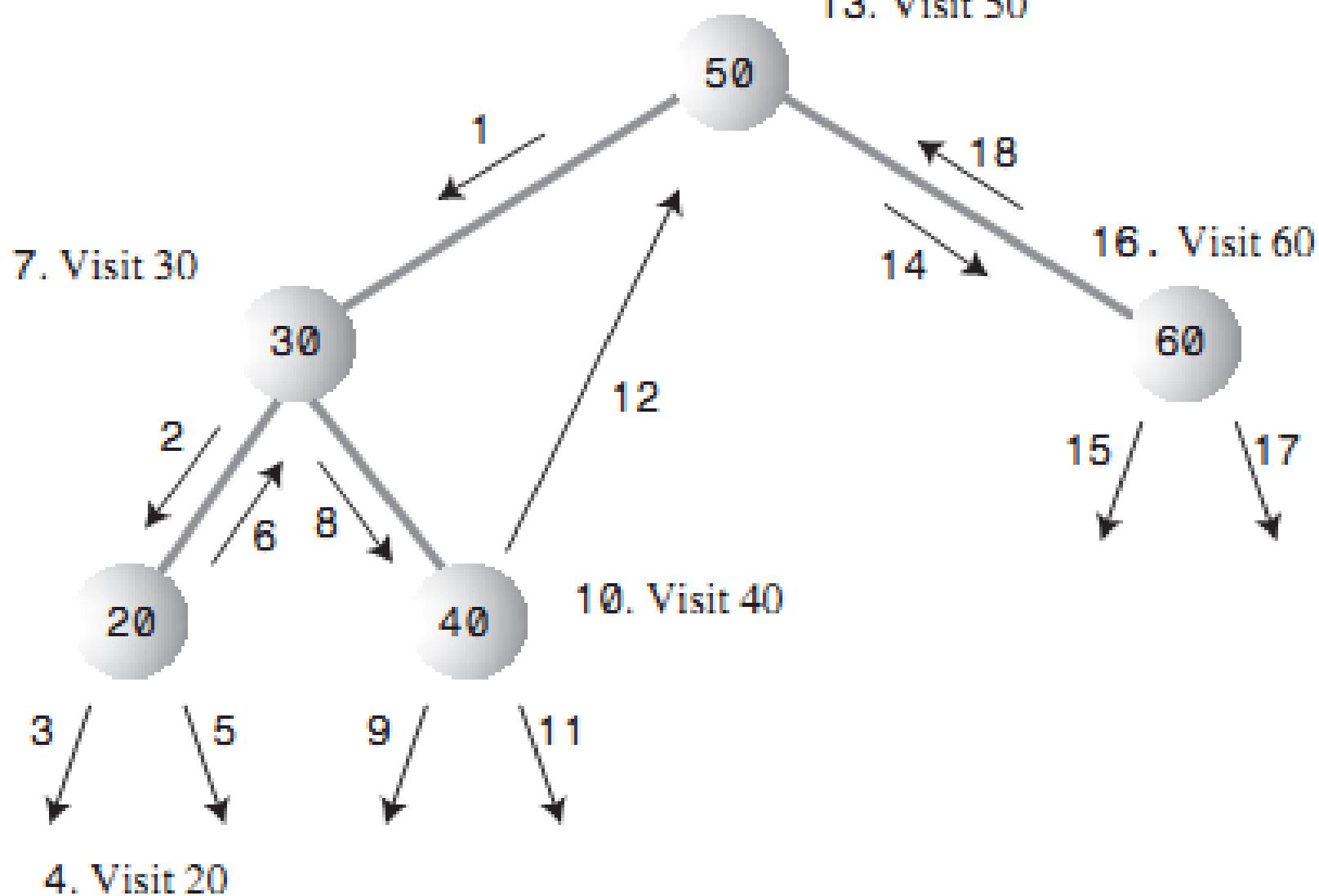
- Unless we run out of memory, we always found the place to insert
- Can handle duplication by modifying the search condition.

Traversing

- Visit all nodes of the tree
- 3 ways to traverse a tree
 - Preorder
 - Inorder
 - Postorder
- Inorder traversing
 - Traverse the node's left subtree
 - Visit the node
 - Traverse the node's right subtree

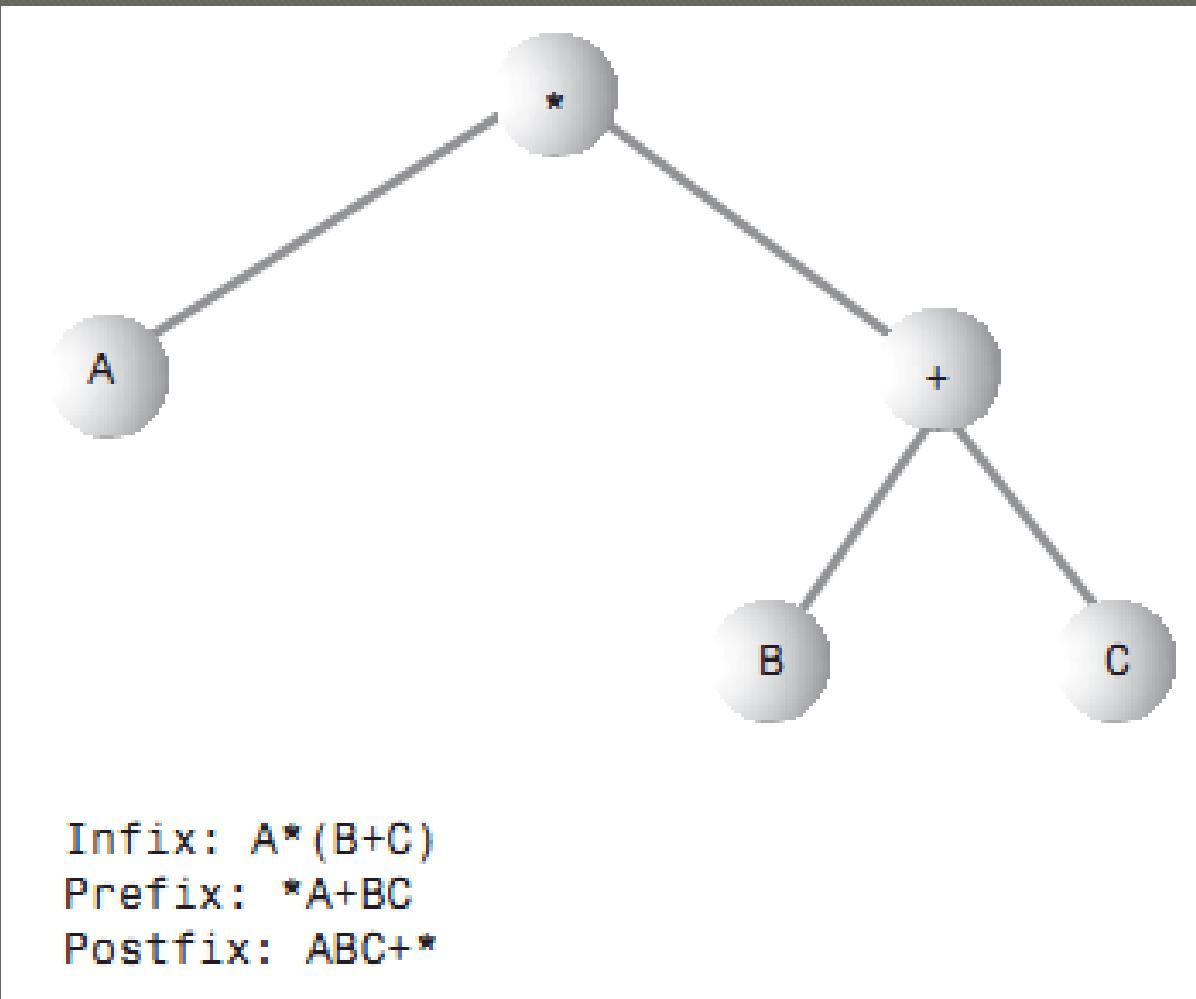


Traverse the tree

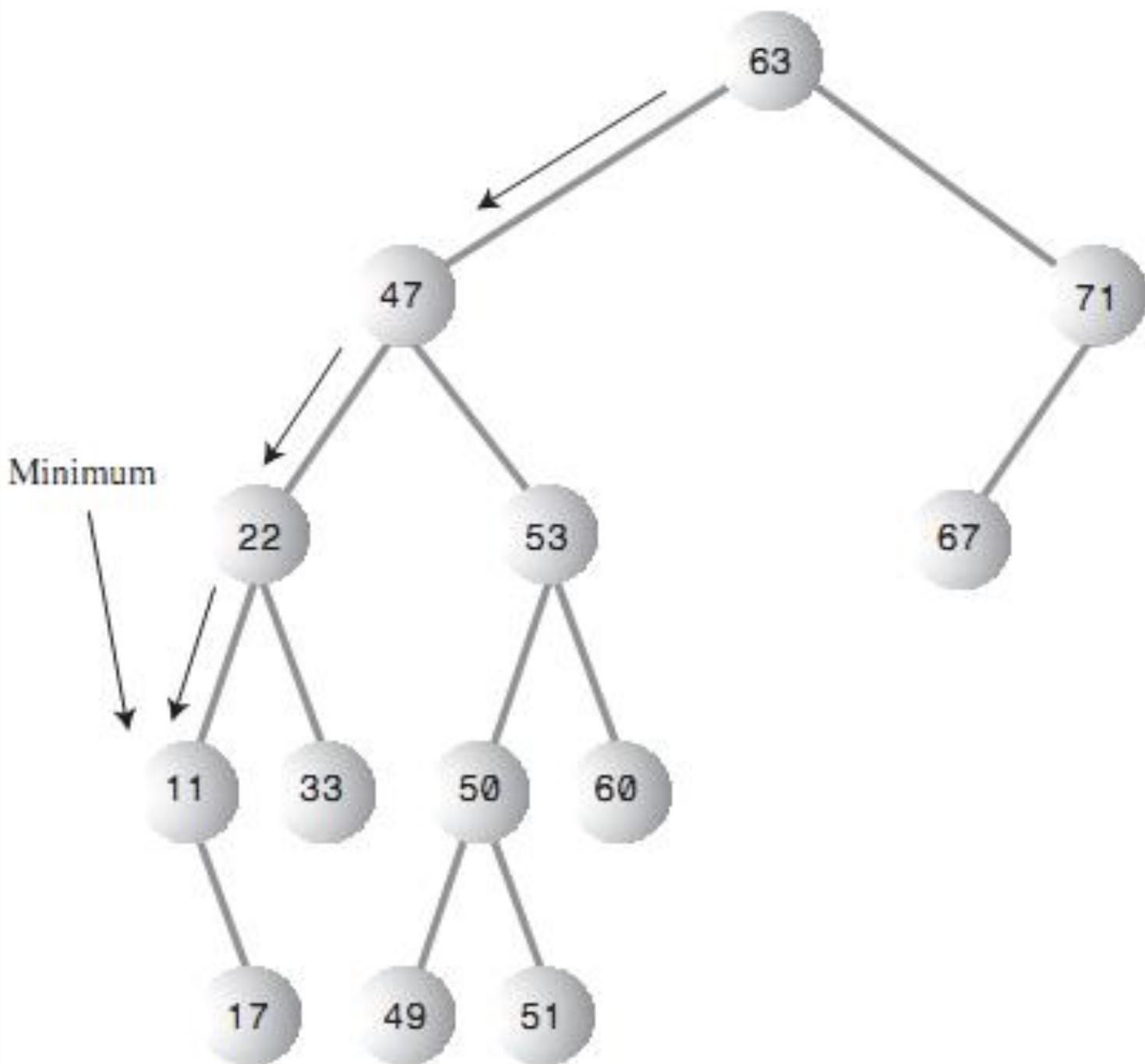


Traverse the tree

Algebraic expression



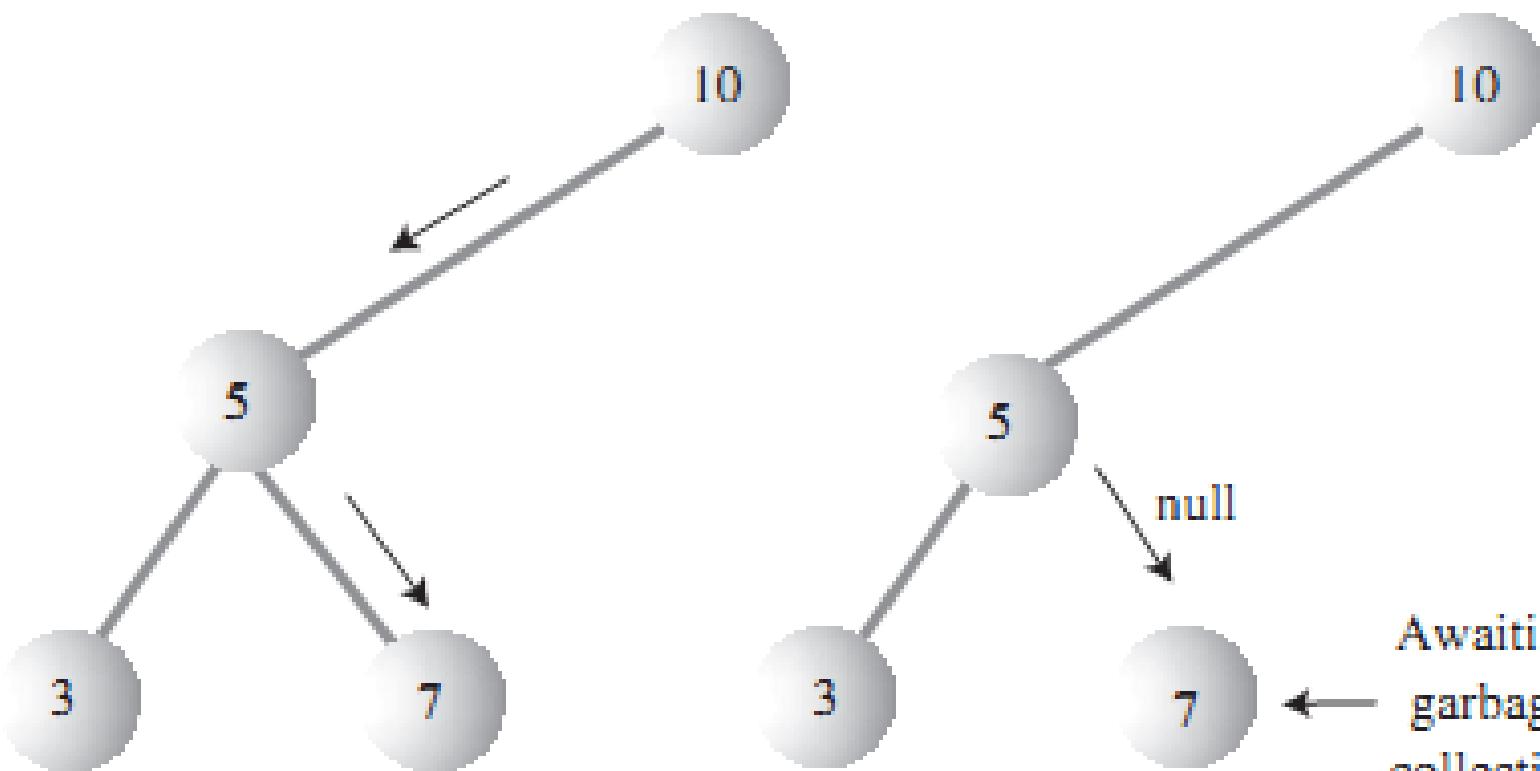
Find
max &
min



Deleting a Node

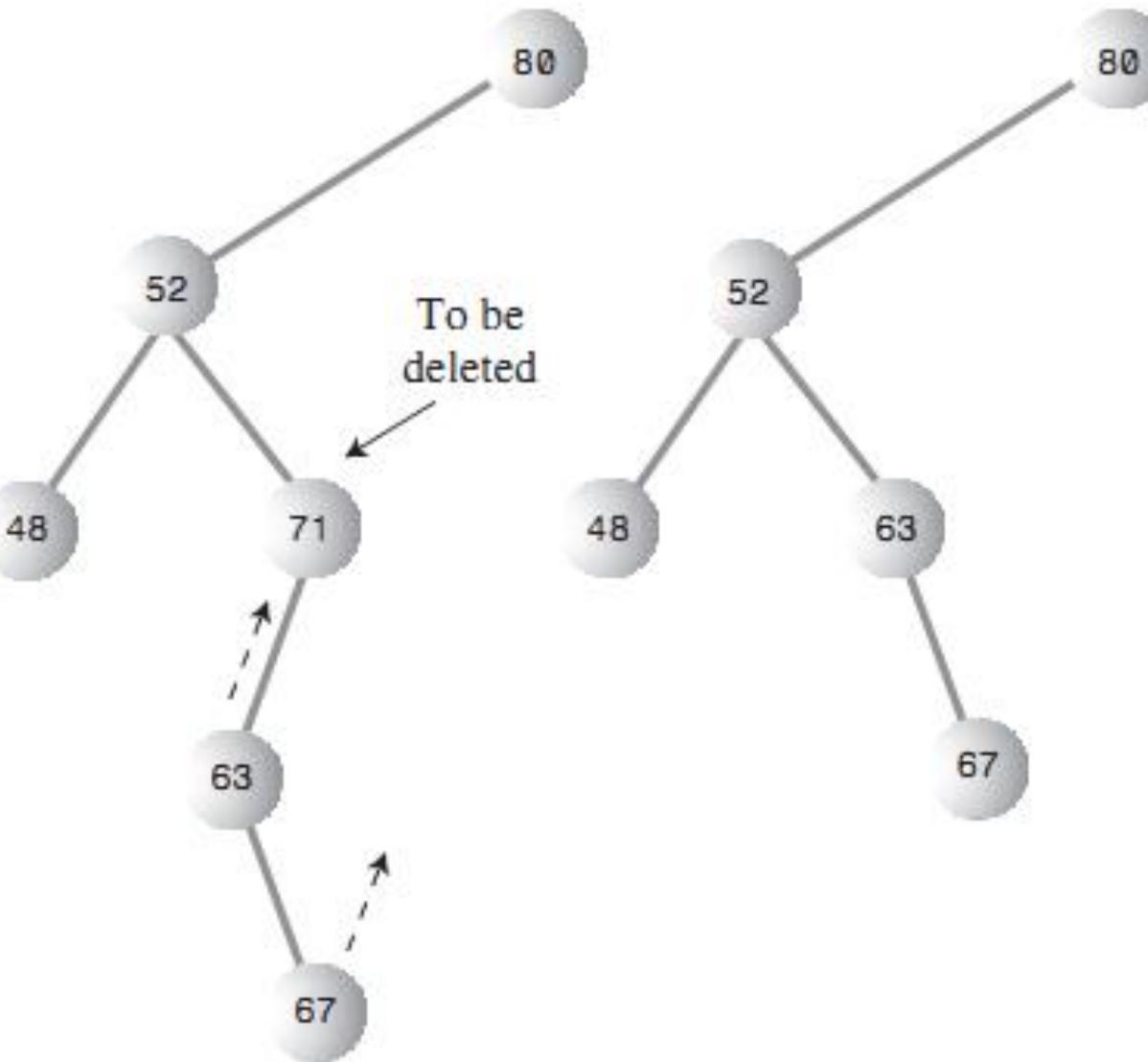
- ➊ Most complicated operation
- ➋ 3 main cases
 - Node to be deleted is a leaf
 - Node to be deleted has one child
 - Node to be deleted has two children

Case 1: Node has no children



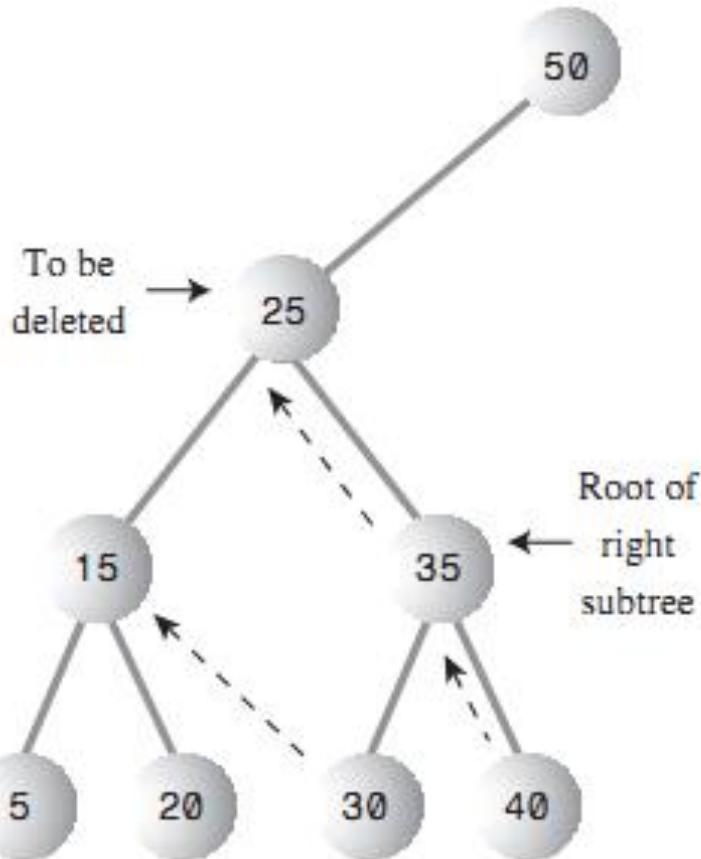
a) Before deletion

b) After deletion

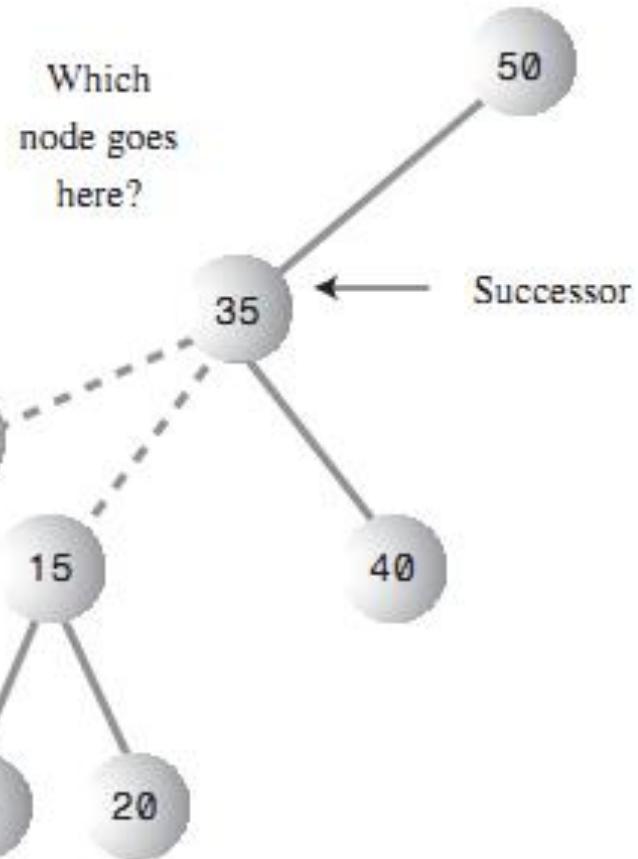


Case2: Node has one child

Case 3: Node has two children

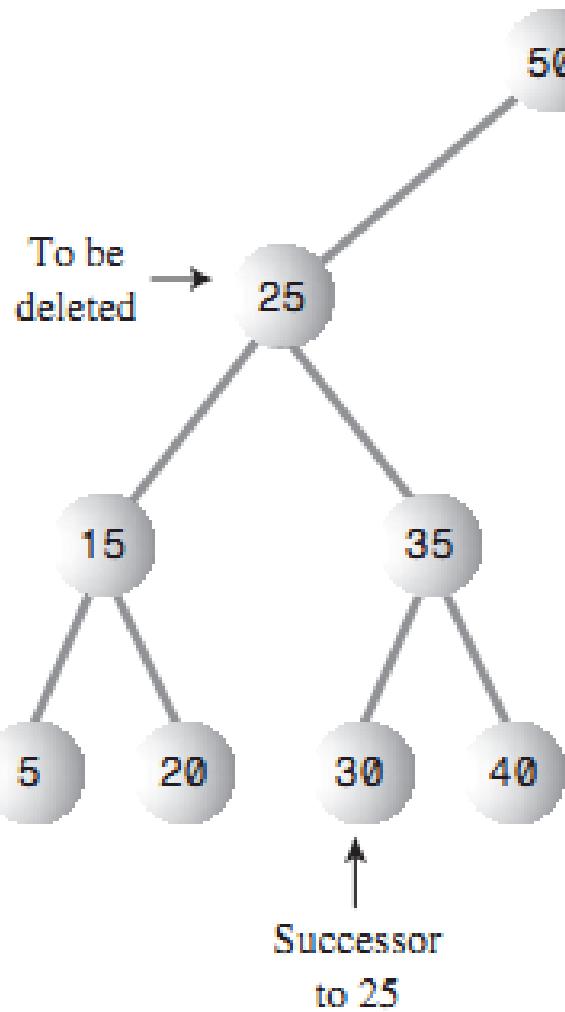


a) Before deletion

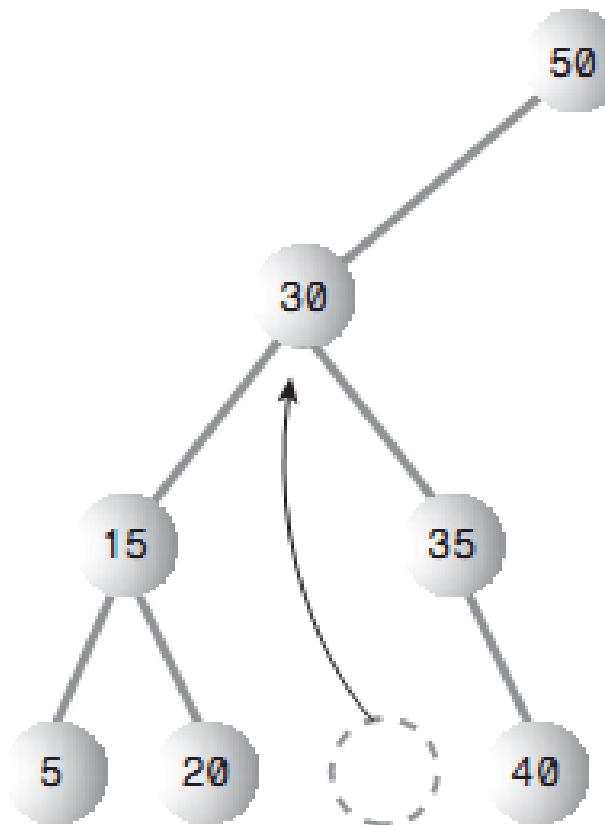


b) After deletion

Case 3: Node has two children



a) Before deletion



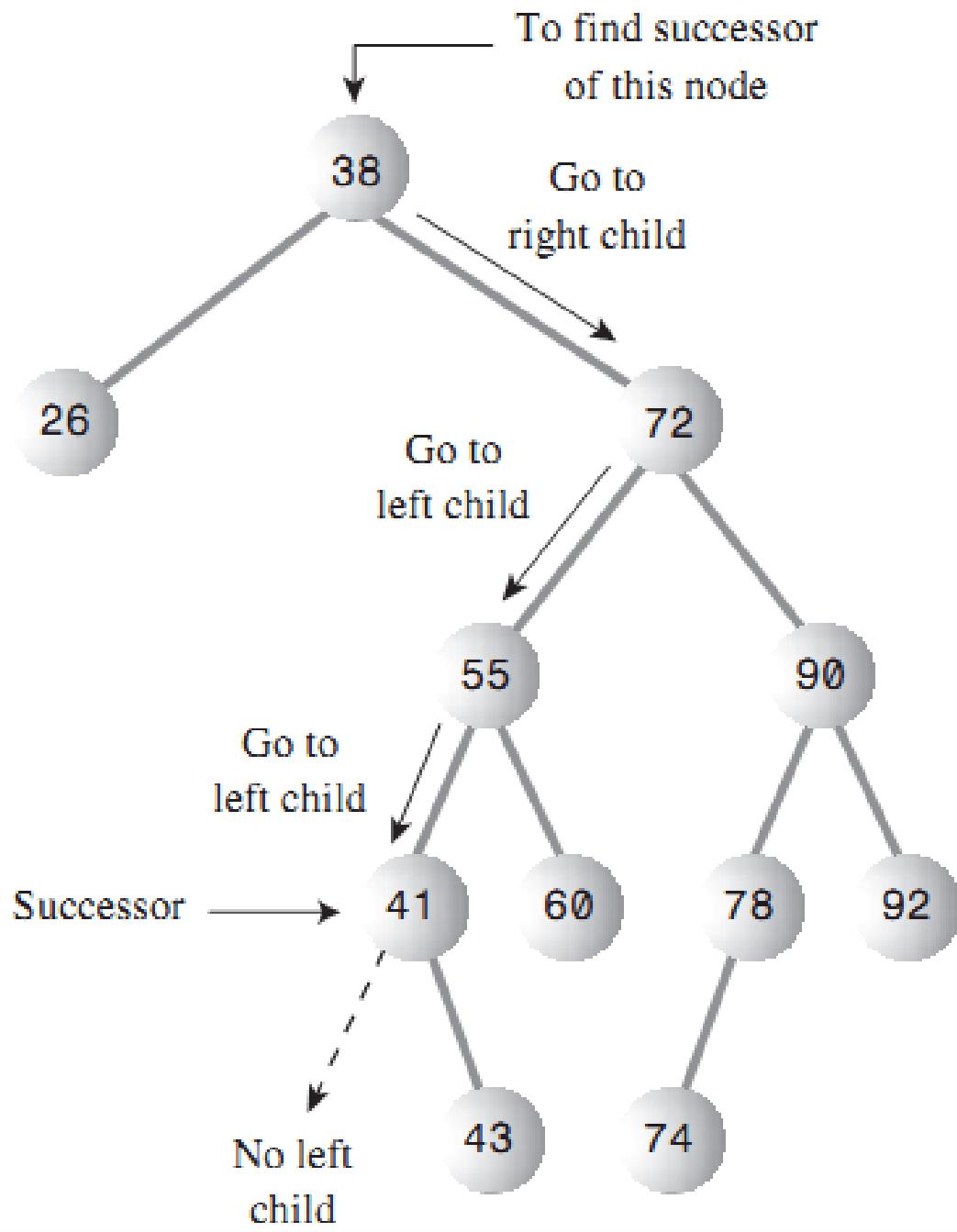
b) After deletion

Find the successor

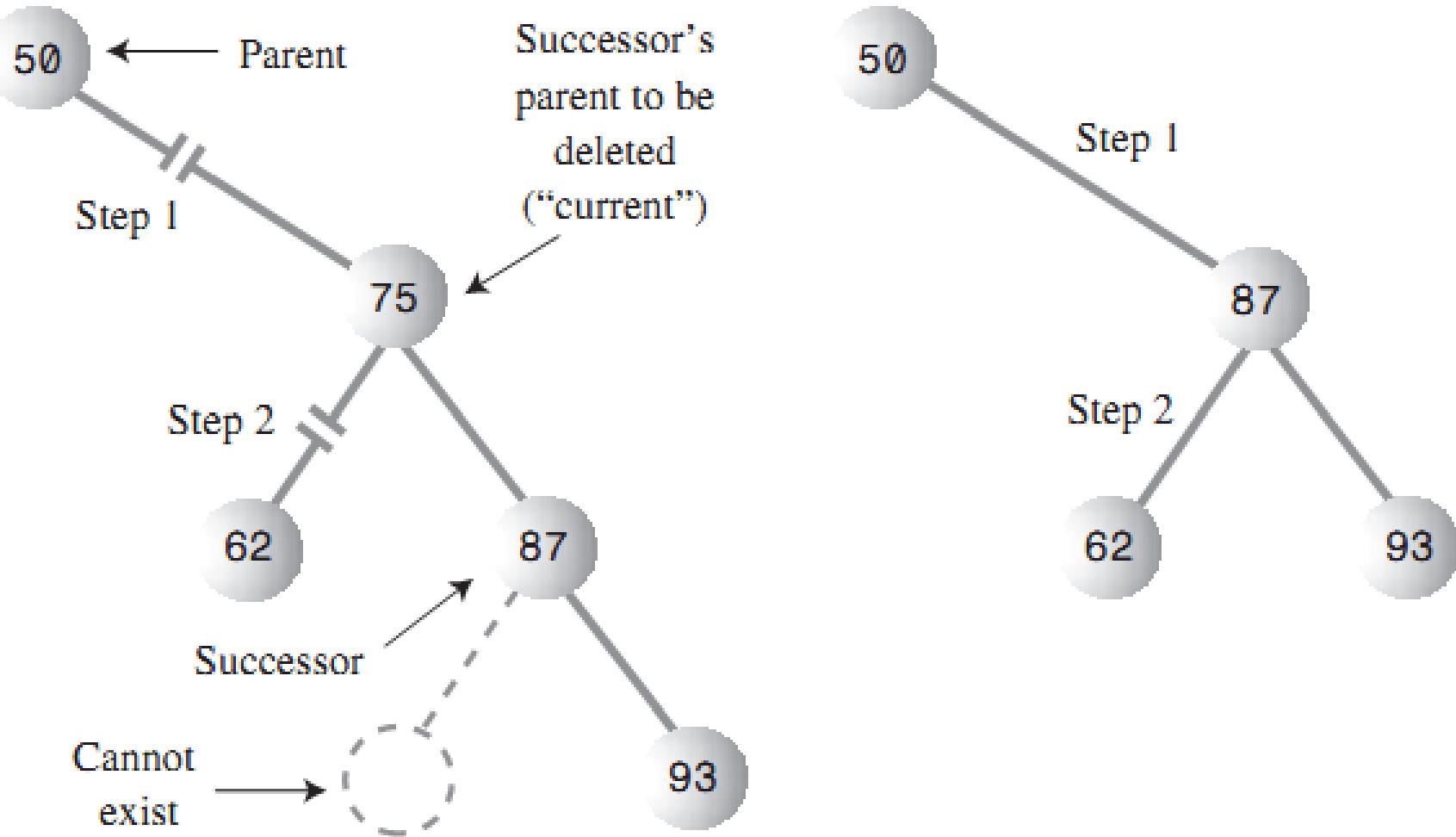
- Successor:

The smallest of the set of nodes that are larger than the given node

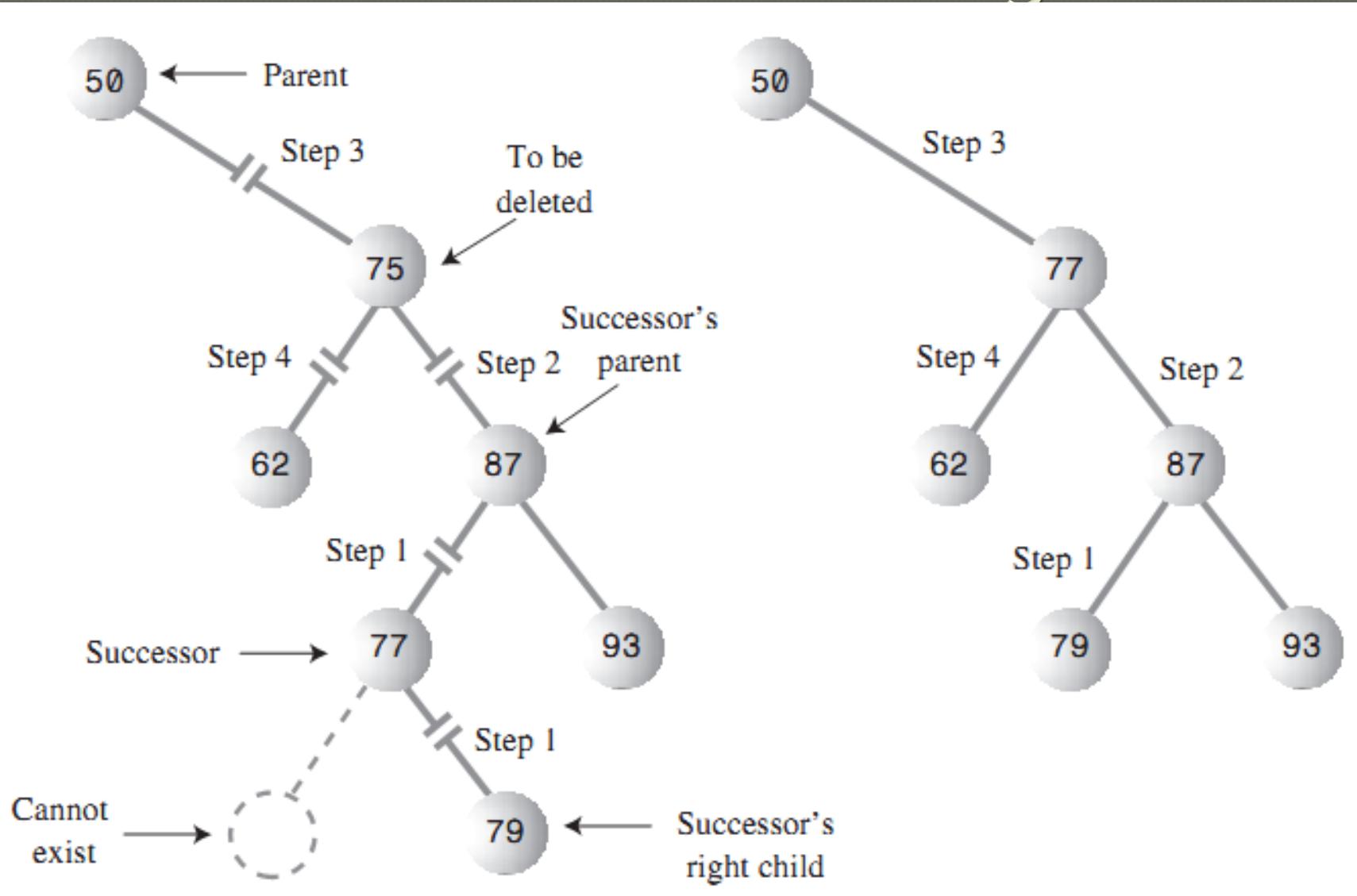
Find successor



Case 3.1: Successor is the right child of delNode



Case 3.2: Successor is left descendant of right child



Implementation of BST

Find a node

```
Node current = root;                      // start at root

while(current.iData != key)                // while no match,
{
    if(key < current.iData)              // go left?
        current = current.leftChild;
    else
        current = current.rightChild;   // or go right?
    if(current == null)                  // if no child,
        return null;                   // didn't find it
}
return current;                           // found it
```

Insert a node

```
Node newNode = new Node();      // make new node
newNode.iData = id;            // insert data
newNode.dData = dd;
if(root==null)                // no node in root
    root = newNode;
else                          // root occupied
{
    Node current = root;      // start at root
    Node parent;
```

Insert a node (cont.)

```
while(true)          // (exits internally)
{
    parent = current;
    if(id < current.iData) // go left?
    {
        current = current.leftChild;
        if(current == null) // if end of the line,
        {
            // insert on left
            parent.leftChild = newNode;
            return;
        }
    } // end if go left
    else          // or go right?
```

Insert a node (cont.)

```
current = current.rightChild;  
if(current == null) // if end of the line  
{  
    // insert on right  
    parent.rightChild = newNode;  
    return;  
}  
}
```

Homework:

Handle the duplication when insert a new node
See page 380-381 for full code of insertion.

Traverse

```
private void inOrder(node localRoot)
{
    if(localRoot != null)
    {
        inOrder(localRoot.leftChild);

        System.out.print(localRoot.iData + " ");

        inOrder(localRoot.rightChild);
    }
}
```

Find min

```
public Node minimum()      // returns node with minimum key value
{
    Node current, last;
    current = root;           // start at root
    while(current != null)    // until the bottom,
    {
        last = current;       // remember node
        current = current.leftChild; // go to left child
    }
    return last;
}
```

Homework: Write the find max function

Deletion

- Homework:
Read code from 406-415

Huffman Code

Homework:
Read &
Implement Huffman Code (if possible)

Red-Black tree, 2-3-4 tree

Read yourself