X教学单元

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## Examples and Intuitions II

The  $\Theta^{(1)}$  matrices for AND, NOR, and OR are:

$$AND$$
:  $\Theta^{(1)} = [-30 \quad 20 \quad 20]$   $NOR$ :  $\Theta^{(1)} = [10 \quad -20 \quad -20]$   $OR$ :  $\Theta^{(1)} = [-10 \quad 20 \quad 20]$ 

We can combine these to get the XNOR logical operator (which gives 1 if  $x_1$  and  $x_2$  are both 0 or both 1).

$$egin{bmatrix} x_0 \ x_1 \ x_2 \end{bmatrix} 
ightarrow egin{bmatrix} a_1^{(2)} \ a_2^{(2)} \end{bmatrix} 
ightarrow egin{bmatrix} a^{(3)} \ a^{(3)} \end{bmatrix} 
ightarrow h_{\Theta}(x)$$

For the transition between the first and second layer, we'll use a  $\Theta^{(1)}$  matrix that combines the values for AND and NOR:

$$\Theta^{(1)} = egin{bmatrix} -30 & 20 & 20 \ 10 & -20 & -20 \end{bmatrix}$$

For the transition between the second and third layer, we'll use a  $\Theta^{(2)}\,$  matrix that uses the value for OR:

$$\Theta^{(2)} = \begin{bmatrix} -10 & 20 & 20 \end{bmatrix}$$

Let's write out the values for all our nodes:

$$egin{aligned} a^{(2)} &= g(\Theta^{(1)} \cdot x) \ a^{(3)} &= g(\Theta^{(2)} \cdot a^{(2)}) \ h_{\Theta}\left(x
ight) &= a^{(3)} \end{aligned}$$

And there we have the XNOR operator using two hidden layers! The following summarizes the above algorithm:





